



1. New Type Definition (Disjoint Union)

```
data Decision = Yes | No | Maybe
data Weekday = Monday | Tuesday | Wednesday | Thursday | Friday
data SpringDate = March Int | April Int | May Int deriving (Show, Eq, Ord)
data SchoolMember = Student [Char] [Char] Int | Teacher [Char] [Char] Int deriving
(Show, Eq, Ord)
```

2. Typeclasses

Deriving members of **Show** class can be presented as strings.

```
Prelude> show 242
```

```
"242"
```

```
Prelude> show [2,4,2]
```

```
"[2,4,2]"
```

Example (Without Show)

```
Prelude> data Decision = Yes | No | Maybe
```

```
Prelude> :t Yes
```

```
Yes :: Decision
```

```
Prelude> Yes
```

```
<interactive>:18:1: error:
```

```
  * No instance for (Show Decision) arising from a use of `print'
```

```
  ...
```

Example (With Show)

```
Prelude> data Decision = Yes | No | Maybe deriving Show
```

```
Prelude> :t Yes
```

```
Yes :: Decision
```

```
Prelude> Yes
```

```
Yes
```

Eq is used to support equality check between deriving types. Types that derive **Eq** can implement `==` and `/=` operators for equality testing.

Example (Without Eq)

```
Prelude> data Decision = Yes | No | Maybe
```

```
Prelude> Yes == No
```

```
<interactive>:28:1: error:
```

```
  * No instance for (Eq Decision) arising from a use of `=='
```

```
  ...
```

Example (With Eq)

```
Prelude> data Decision = Yes | No | Maybe deriving Eq
Prelude> Yes == No
False
Prelude> Yes == Yes
True
Prelude> Yes /= No
True
```

Ord is used to check ordering between deriving types. Types that derive **Ord** can implement `>`, `<`, `>=`, `<=` and compare function. Only the members of **Eq** can be the members of **Ord**.

Example (Without Ord)

```
Prelude> data Decision = Yes | No | Maybe
Prelude> Yes > No
<interactive>:42:1: error:
```

```
* No instance for (Ord Decision) arising from a use of `>'
...
```

Example (With Ord)

```
Prelude> data Decision = Yes | No | Maybe deriving (Eq, Ord)
Prelude> Yes > No
False
```

Example 2 (With Ord)

```
Prelude> data Decision = No | Yes | Maybe deriving (Eq, Ord)
Prelude> Yes > No
True
```

Read typeclass takes a string and returns a type that is a deriving member of itself. It works like the opposite of Show typeclass.

```
Prelude> read "200" + 42
242
Prelude> read "[2,4]" ++ [2]
[2,4,2]
```

Example (Without Read)

```
Prelude> data Decision = Yes | No | Maybe deriving Eq
Prelude> read "Yes" == Yes
```

```
<interactive>:53:1: error:
```

```
* No instance for (Read Decision) arising from a use of `read'
...
```

Example (With Read)

```
Prelude> data Decision = Yes | No | Maybe deriving (Eq, Read)
Prelude> read "Yes" == Yes
True
```

3. Usage of Disjoint Union Types

```
-----disjointExample.hs-----
data Decision = Yes | No | Maybe deriving (Show, Eq, Ord)
data SchoolMember = Student [Char] [Char] Int | Teacher [Char] [Char] [Char] | TA
[Char] [Char] deriving (Show, Eq, Ord)

askQuestion x = if x == "Are you taking CNG 242?" then Yes
                else if x == "Do you want to fail CNG 242?" then No
                else Maybe

react Yes = "Nice!"
react No = "Why?"
react Maybe = "To what?"

accept Yes = "OK!"
accept _ = "You should accept!"

toString (Student name surname id) = "I am a student in METU NCC, my name is " ++
name ++ ", my surname is " ++ surname ++ ", and my student ID is " ++ (show id)
toString (Teacher name surname department) = "My name is " ++ name ++ " " ++
surname ++ ". I am the instructor of CNG 242 in " ++ department ++ " department"
toString (TA name message) = "You have a message from your TA, " ++ name ++ ": "
++ message
-----
```

Sample Run:

```
[1 of 1] Compiling Main (... \disjointExample.hs, interpreted)
Ok, one module loaded.
*Main> askQuestion "Are you ok?"
Maybe
*Main> askQuestion "Are you taking CNG 242?"
Yes
*Main> react No
"Why?"
*Main> react Maybe
"To what?"
*Main> accept No
"You should accept!"
*Main> accept Maybe
"You should accept!"
*Main> :t accept
accept :: Decision -> [Char]
*Main> :react
*Main> :t askQuestion
askQuestion :: [Char] -> Decision
*Main> toString (Teacher "Enver" "Ever" "Computer Engineering")
"My name is Enver Ever. I am the instructor of CNG 242 in Computer Engineering
department"
*Main> toString (TA "Zekican" "Hello World!")
"You have a message from your TA, Zekican: Hello World!"
```

4. Polymorphic Data Types

Example (Non-polymorphic Disjoint Union)

```
data Distance = Kilometres Float | Miles Float deriving Show ← Float only
```

```
Prelude> Kilometres 5.5
```

```
Kilometres 5.5
```

```
Prelude> Miles 8
```

```
Miles 8.0
```

```
Prelude> Kilometres "12"
```

```
<interactive>:45:12: error:
```

```
  * Couldn't match expected type `Float' with actual type `[Char]'
```

```
...
```

Example (Polymorphic Disjoint Union)

```
data Distance a = Kilometres a | Miles a deriving Show
```

```
Prelude> Kilometres 5.5
```

```
Kilometres 5.5
```

```
Prelude> Miles 8
```

```
Miles 8
```

```
Prelude> Kilometres "12"
```

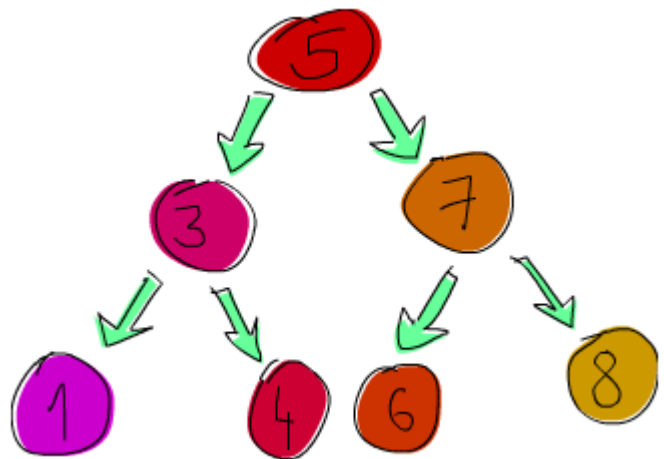
```
Kilometres "12"
```

```
Prelude> Miles "13.5"
```

```
Miles "13.5"
```

5. Recursive Data Types with Tree Example

```
data Tree = EmptyTree | Node Integer Tree Tree deriving (Show, Eq, Ord)
```



- insertElement function inserts a new element to the given binary tree.

¹ <http://learnyouahaskell.com/making-our-own-types-and-typeclasses>

```

-----Tree.hs-----
data Tree = EmptyTree | Node Integer Tree Tree deriving (Show, Eq, Ord)
insertElement x EmptyTree = Node x EmptyTree EmptyTree    -- BASE CASE
insertElement x (Node a left right) = if x == a             -- DO NOTHING
                                     then (Node x left right)
                                     else if x < a            -- INSERT TO LEFT
                                     then (Node a (insertElement x left) right)
                                     else                      -- INSERT TO RIGHT
                                     Node a left (insertElement x right)
-----

[1 of 1] Compiling Main (...\\Tree.hs, interpreted)
Ok, one module loaded.
*Main> insertElement 5 EmptyTree
Node 5 EmptyTree EmptyTree
*Main> x = insertElement 5 EmptyTree
*Main> x
Node 5 EmptyTree EmptyTree
*Main> y = insertElement 10 x
*Main> y
Node 5 EmptyTree (Node 10 EmptyTree EmptyTree)
*Main> x = insertElement 3 y
*Main> x
Node 5 (Node 3 EmptyTree EmptyTree) (Node 10 EmptyTree EmptyTree)

```

6. Lambda Abstractions

```

Prelude> square x = x * x
Prelude> square 2
4
Prelude> (\x -> x * x) 2
4
Prelude> (\x y -> (x + y)/2) 5 7
6.0
Prelude> example q p = (\x y -> ([a | a<-x,a<'o',a/='a'],[ b | b<-y,b>=2])) q p
Prelude> example "congrats" [(-2),2,1,(-3),4,(-4),2,0]
("cng",[2,4,2])

```

Practical Exercises:

1. Write a Haskell function that takes a list and a number and replicate the elements of a list a given number of times [3].

Sample Run:

```

*Main> repli "abc" 3
"aaabbbcccc"
*Main> repli "tb" 2
"ttbb"

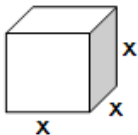

```

- Write a Haskell function that takes a list and eliminate consecutive duplicates of list elements. If a list contains repeated elements they should be replaced with a single copy of the element. The order of the elements should not be changed [3].

Sample Run:

```
*Main> compress "aaaabccaadeeee"
"abcade"
```

- Implement first and second exercise using lambda abstraction.
- Define a new type for `ThreeDShapes`. It should have a data constructor for `Cube` and `Cylinder`. `Cube` should have side length and `Cylinder` should have radius and height. You need to implement two functions related to this type.
 - `volume` function calculates the volume of the 3D shape
 - `surfaceArea` function calculates the surface area of the 3D shape.

Volume and Surface Area Formulas for Cube and Cylinder		
Cube		$\text{Volume} = x^3$ $\text{Surface Area} = 6x^2$
Cylinder		$\text{Volume} = \pi r^2 h$ $\text{Surface Area} = 2 \pi r h + 2 \pi r^2$

- Modify your data type in exercise four so that it works with both integers and floating-point numbers.

For question 6,7,8 and 9 you can use the given `Tree` example and `insertElement` function or you can implement your own `Tree` type and use it.

- Write a Haskell function which takes a list of numbers and generates a binary tree. Hint: You can use the `insertElement` function

Sample Run:

```
*Main> inserter [1,2,3]
Node 3 (Node 2 (Node 1 EmptyTree EmptyTree) EmptyTree) EmptyTree
*Main> inserter [5]
Node 5 EmptyTree EmptyTree
*Main> inserter []
EmptyTree
*Main> inserter [1,2,3,4,5]
Node 5 (Node 4 (Node 3 (Node 2 (Node 1 EmptyTree EmptyTree) EmptyTree) EmptyTree) EmptyTree) EmptyTree
*Main> inserter [12,4,2,6,3,5,7,8]
Node 8 (Node 7 (Node 5 (Node 3 (Node 2 EmptyTree EmptyTree) (Node 4 EmptyTree EmptyTree)) (Node 6 EmptyTree EmptyTree)) EmptyTree) (Node 12 EmptyTree EmptyTree)
```

7. Write a Haskell function which returns the minimum value in the given Tree.

Sample Run:

```
*Main> x = inserter [3,2,4]
*Main> x
Node 4 (Node 2 EmptyTree (Node 3 EmptyTree EmptyTree)) EmptyTree
*Main> minOf x
2
*Main> minOf (Node 5 (Node 3 EmptyTree EmptyTree) EmptyTree)
3
```

8. Write a Haskell function that checks if a given Tree is empty or not.

Sample Run:

```
*Main> t = EmptyTree
*Main> isEmpty t
True
*Main> t = Node 3 EmptyTree (Node 7 EmptyTree EmptyTree)
*Main> isEmpty t
False
```

9. Write a Haskell function that searches a given element inside a given Tree. It should return True if the element is found.

Sample Run:

```
*Main> t = Node 3 EmptyTree (Node 7 EmptyTree EmptyTree)
*Main> searchElement 4 t
False
*Main> searchElement 7 t
True
```

References:

1. Learn You a Haskell <<http://learnyouahaskell.com/chapters>>
2. Types and Typeclasses – Learn You a Haskell <<http://learnyouahaskell.com/types-and-typeclasses>>
3. A Gentle Introduction to Haskell <<http://www.haskell.org/tutorial/index.html>>
4. H-99: Ninety-Nine Haskell Problems <[https://wiki.haskell.org/H-99: Ninety-Nine Haskell Problems](https://wiki.haskell.org/H-99:_Ninety-Nine_Haskell_Problems)>