

is given by

$$\hat{b}(n) = \arg \max_i \int_{nT}^{(n+1)T} r(t) s_i(t) dt$$

(6.42)

You may not have seen the

$$\arg \max_i$$

notation before. $\max_i\{i, \cdot\}$ yields the maximum value of its argument with respect to the index

$$i. \arg \max_i$$

equals the value of the index that yields the maximum. Note that the precise numerical value of the integrator's output does not matter; what does matter is its value relative to the other integrator's output.

Let's assume a perfect channel for the moment: The received signal equals the transmitted one. If bit 0 were sent using the baseband BPSK signal set, the integrator outputs would be

$$\begin{aligned} \int_{nT}^{(n+1)T} r(t) s_0(t) dt &= A^2 T \\ \int_{nT}^{(n+1)T} r(t) s_1(t) dt &= (A^2 T) \end{aligned}$$

(6.43)

If bit 1 were sent,

$$\begin{aligned} \int_{nT}^{(n+1)T} r(t) s_0 dt &= -(A^2 T) \\ \int_{nT}^{(n+1)T} r(t) s_1 dt &= A^2 T \end{aligned}$$

(6.44)

Exercise 6.16.1

Can you develop a receiver for BPSK signal sets that requires only one multiplier-integrator combination?

Exercise 6.16.2

What is the corresponding result when the amplitude-modulated BPSK signal set is used? Clearly, this receiver would always choose the bit correctly. Channel attenuation would not affect this correctness; it would only make the values smaller, but all that matters is which is largest.