

Problem Set 5

1. (from Goldberger) Let \bar{X} and S^2 denote the sample mean and sample variance in random sampling, sample size 15, from a $N(10, 100)$ population. Find the probability of each of these events:

$$\begin{aligned} A &= \{\bar{X} \leq 14.9\} & B &= \{5.1 \leq \bar{X} \leq 14.9\} & C &= \{S^2 \leq 92.04\} \\ D &= B \cap C & E &= \{\sqrt{15}(\bar{X} - 10)/S \leq 1.746\} & F &= \{\bar{X} \leq 10 + 0.53S\} \end{aligned}$$

Note: You will need to use tables (or excel) for evaluating the cdf's of the normal distribution, the Student's t distribution and the Chi-squared distribution.

In addition, solve the following problems from Casella and Berger: 5.1, 5.3, 5.5, 5.11 and 5.15.