DS-6030 Homework Module 1

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1. Flexible vs Inflexible Methods

For each of parts (a) through (d), indicate whether we would generally expect the performance of a flexible statistical learning method to be better or worse than an inflexible method. Justify your answer.

- (a) The sample size n is extremely large, and the number of predictors p is small.
 - We would expect generally the performance of a flexible statistical learning method to be better than the performance of an inflexible method as a flexible statistical learning method would fit the extremely large set of data more closely.
- (b) The number of predictors p is extremely large, and the number of observations n is small.
 - We would expect generally the performance of a flexible statistical learning method to be worse than the performance of an inflexible method as a flexible statistical learning method would overfit the small set of data.
- (c) The relationship between the predictors and response is highly non-linear.
 - We would expect generally the performance of a flexible statistical method to be better than the performance of an inflexible method as a flexible statistical method has more degrees of freedom.
- (d) The variance of the error terms, i.e. $\sigma^2 = Var(\epsilon)$, is extremely high.
 - We would expect generally the performance of a flexible statistical method to be worse than the performance of an inflexible method as a flexible statistical method would fit the variance, error, and noise of the set of data.
- 2. Explain whether each scenario is a classification or regression problem, and indicate whether we are most interested in inference or prediction. Finally, provide n and p.
 - (a) We collect a set of data on the top 500 firms in the US. For each firm we record profit, number of employees, industry and the CEO salary. We are interested in understanding which factors affect CEO salary.
 - This scenario is an inference regression problem as we are interested in understanding which predictors affect continuous response CEO salary. The number of samples and top firms n = 500. The number of predictors, including profit, number of employees, and industry, p = 3.
 - (b) We are considering launching a new product and wish to know whether it will be a success or a failure. We collect data on 20 similar products that were previously launched. For each product we have recorded whether it was a success or failure, price charged for the product, marketing budget, competition price, and ten other variables.
 - This scenario is a prediction classification problem as we wish to know whether a new product will be a success or a failure. The number of samples and similar products that were previously launched n = 20. The number of predictors, including price charged for the product, marketing budget, competition price, and ten other variables, p = 13.

(c) We are interested in predicting the % change in the USD/Euro exchange rate in relation to the weekly changes in the world stock markets. Hence we collect weekly data for all of 2012. For each week we record the % change in the USD/Euro, the % change in the US market, the % change in the British market, and the % change in the German market.

This scenario is a prediction regression problem as we are interested in predicting the percent change in the US Dollar / Euro exchange rate in relation to the weekly changes in the world stock markets in 2012. The number of samples and weekly records n = 52. The number of predictors, including the percent change in the US market, the percent change in the British market, and the percent change in the German market, p = 3.

3. Describe the differences between a parametric and a non-parametric statistical learning approach.

What are the advantages of a parametric approach to regression or classification (as opposed to a non-parametric approach)? What are its disadvantages?

A parametric approach to regression and classification has the advantages of involving a explicit, understandable formula with generally a relatively small number of parameters with values that are trained based on a modest set of data. A parametric approach generally is simple, may be used for prediction and inference, is inflexible, and may have low variance among predicted values given different training data sets. A parametric approach may be too simple, inflexible, and have a high bias. Variance

$$v = E\left(\left\{\hat{f}(x) - E\left[\hat{f}(x)\right]\right\}^2\right)$$

where $\hat{f}(x)$ is the predicted value of a statistical learning model at x and $E\left[\hat{f}(x)\right]$ is the expected predicted value of a statistical learning model at x given different training data sets. Bias

$$b = \left\{ E\left[\hat{f}(x)\right] - y(x) \right\}^2$$

where y(x) is the ground-truth value at x corresponding to the predicted value.

A non-parametric approach to regression and classification has the advantage of modeling generally nonlinear relationships using a relatively large number of parameters with values that are trained based on a large set of data. A non-parametric approach is flexible and has a low bias. A non-parametric approach may be used for prediction. A non-parametric approach generally is a complex black box that may not be used for inference. A non-parametric approach may have high variance among predicted values given different training data sets and may overfit the set of data.

4. This exercise relates to the College data set, which can be found in the file College.csv on the book website.

It contains a number of variables for 777 different universities and colleges in the US. The variables are

- Private : Public/private indicator
- Apps: Number of applications received
- Accept: Number of applicants accepted
- Enroll: Number of new students enrolled
- Top10perc: New students from top 10 % of high school class
- Top25perc : New students from top 25 % of high school class
- F. Undergrad: Number of full-time undergraduates
- P.Undergrad: Number of part-time undergraduates
- Outstate : Out-of-state tuition
- Room.Board: Room and board costs
- Books: Estimated book costs
- Personal : Estimated personal spending
- PhD: Percent of faculty with Ph.D.'s

- Terminal: Percent of faculty with terminal degree S.F.Ratio: Student/faculty ratio
- perc.alumni : Percent of alumni who donate
- Expend: Instructional expenditure per student
- Grad.Rate: Graduation rate

Before reading the data into R, it can be viewed in Excel or a text editor.

(a) Use the read.csv() function to read the data into R. Call the loaded data college. Make sure that you have the directory set to the correct location for the data.

```
college = read.csv("Colleges.csv")
```

(b) Look at the data using the View() function. You should notice that the first column is just the name of each university. We don't really want R to treat this as data. However, it may be handy to have these names for later. Try the following commands:

```
rownames(college) <- college[, 1]</pre>
View(college)
```

Now you should see that the first data column is Indicator_Of_Whether_College_Is_Private.

Note that another column labeled row names now appears before the Indicator_Of_Whether_College_Is_Private column. However, this is not a data column but rather the name that R is giving to each row.

```
college <- college[, -1]
View(college)</pre>
```

Now you should see that the first data column with name Name_Of_College has been removed from the data frame. Note that another column labeled row names now appears. However, this is not a data column but rather a column of the names that R is giving to each row.

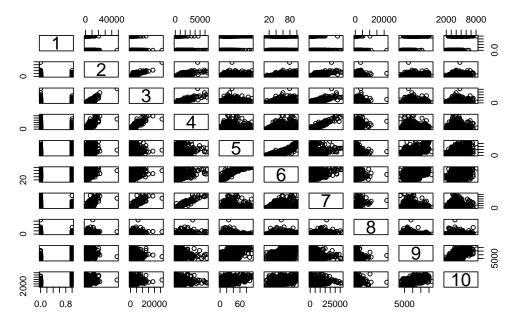
- (c) See below.
 - i. Use the summary() function to produce a numerical summary of the variables in the data set.
 summary(college)

```
Indicator_Of_Whether_College_Is_Private Number_Of_Applications
   Length:777
                                             Min.
  Class : character
                                                      776
                                             1st Qu.:
   Mode : character
                                            Median: 1558
#
                                            Mean
                                                   : 3002
#
                                             3rd Qu.: 3624
#
                                                    :48094
                                            Max.
#
   Number_Of_Acceptances Number_Of_Enrollments
#
                               : 35
  \mathtt{Min}.
              72
                          Min.
#
   1st Qu.: 604
                          1st Qu.: 242
  Median: 1110
                          Median: 434
#
  Mean
         : 2019
                          Mean
                                 : 780
#
   3rd Qu.: 2424
                          3rd Qu.: 902
#
                                 :6392
  Max.
          :26330
                          Max.
  Percent_Of_New_Students_Who_Were_In_Top_10_Percent_Of_High_School_Class
#
  Min.
          : 1.00
#
   1st Qu.:15.00
  Median :23.00
  Mean
          :27.56
   3rd Qu.:35.00
  Max.
          :96.00
```

```
Percent_Of_New_Students_Who_Were_In_Top_25_Percent_Of_High_School_Class
  #
            : 9.0
     Min.
  #
     1st Qu.: 41.0
    Median: 54.0
  #
  #
     Mean
           : 55.8
     3rd Qu.: 69.0
  #
             :100.0
  #
     Number_Of_Full_Time_Undergraduates Number_Of_Part_Time_Undergraduates
  #
  #
            : 139
                                          Min.
                                                      1.0
  #
     1st Qu.: 992
                                                     95.0
                                          1st Qu.:
    Median: 1707
                                          Median :
                                                    353.0
           : 3700
  #
    Mean
                                                    855.3
                                          Mean
     3rd Qu.: 4005
  #
                                          3rd Qu.:
                                                    967.0
  #
    Max.
             :31643
                                          Max.
                                                 :21836.0
  #
     Out_Of_State_Tuition Cost_Of_Room_And_Board Cost_Of_Books
                                                                     Personal_Spending
  #
     Min.
            : 2340
                           Min.
                                  :1780
                                                   Min. : 96.0
                                                                     Min.
                                                                            : 250
  #
     1st Qu.: 7320
                           1st Qu.:3597
                                                   1st Qu.: 470.0
                                                                     1st Qu.: 850
     Median: 9990
                           Median:4200
                                                   Median : 500.0
                                                                     Median:1200
           :10441
  #
     Mean
                           Mean
                                  :4358
                                                   Mean
                                                         : 549.4
                                                                     Mean
                                                                           :1341
     3rd Qu.:12925
  #
                           3rd Qu.:5050
                                                   3rd Qu.: 600.0
                                                                     3rd Qu.:1700
  #
     Max.
             :21700
                           Max.
                                   :8124
                                                   Max.
                                                           :2340.0
                                                                     Max.
                                                                            :6800
     Percent Of Faculty With PhDs Percent Of Faculty With Terminal Degrees
                                           : 24.0
  #
     Min.
           : 8.00
                                   Min.
     1st Qu.: 62.00
                                    1st Qu.: 71.0
  #
    Median : 75.00
                                   Median: 82.0
  #
    Mean
           : 72.66
                                   Mean
                                          : 79.7
  #
     3rd Qu.: 85.00
                                    3rd Qu.: 92.0
  #
             :103.00
                                    Max.
                                           :100.0
    Student_Faculty_Ratio Percent_Of_Alumni_Who_Donate
  #
     Min.
            : 2.50
                            Min.
                                   : 0.00
  #
     1st Qu.:11.50
                            1st Qu.:13.00
     Median :13.60
                            Median :21.00
    Mean
           :14.09
                            Mean :22.74
  #
     3rd Qu.:16.50
                            3rd Qu.:31.00
  #
             :39.80
                            Max.
                                    :64.00
  #
     Instructional Expenditure Per Student Graduation Rate
  #
    Min.
            : 3186
                                             Min.
                                                    : 10.00
  #
     1st Qu.: 6751
                                             1st Qu.: 53.00
  #
     Median : 8377
                                             Median: 65.00
    Mean
           : 9660
                                             Mean : 65.46
     3rd Qu.:10830
                                             3rd Qu.: 78.00
  #
     Max.
             :56233
                                             Max.
                                                    :118.00
ii. Use the pairs () function to produce a scatterplot matrix of the first ten columns or variables
  of the data. Recall that you can reference the first ten columns of a matrix A using A[,1:10].
  number of rows in college <- nrow(college)</pre>
  column_of_numerical_representations <- rep(0, number_of_rows_in_college)</pre>
  condition <- college$Indicator_Of_Whether_College_Is_Private == "Yes"</pre>
  column_of_numerical_representations[condition] <- 1</pre>
  data_frame_of_second_through_tenth_columns <- college[, 2:10]</pre>
  data_frame_representing_first_ten_columns_of_college <- data.frame(</pre>
       column_of_numerical_representations,
       data_frame_of_second_through_tenth_columns
  )
```

```
pairs(
    data_frame_representing_first_ten_columns_of_college,
    main = "Scatterplot Matrix Of The First Ten Columns Of College",
    labels = seq(1, 10)
)
```

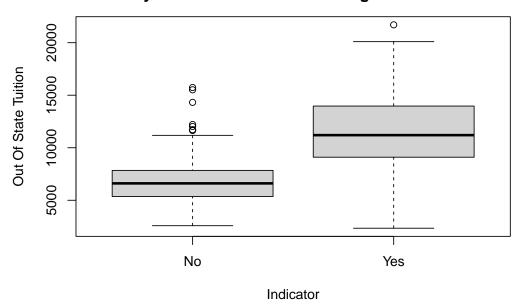
Scatterplot Matrix Of The First Ten Columns Of College



iii. Use the plot() function to produce side-by-side boxplots of Outstate versus Private.

```
factor_Indicator_Of_Whether_College_Is_Private <- as.factor(
    college$Indicator_Of_Whether_College_Is_Private
)
plot(
    x = factor_Indicator_Of_Whether_College_Is_Private,
    y = college$Out_Of_State_Tuition,
    main = "Distributions Of Out Of State Tuition\nBy Indicator Of Whether College Is Private
    xlab = "Indicator",
    ylab = "Out Of State Tuition"
)</pre>
```

Distributions Of Out Of State Tuition By Indicator Of Whether College Is Private



iv. Create a new qualitative variable, called Elite, by binning the Top10perc variable. We are going to divide universities into two groups based on whether or not the proportion of students coming from the top 10% of their high school classes exceeds 50%.

```
number_of_rows_in_college <- nrow(college)
Elite <- rep("No", number_of_rows_in_college)
column_of_percents <- college$
    Percent_Of_New_Students_Who_Were_In_Top_10_Percent_Of_High_School_Class
condition <- column_of_percents > 50
Elite[condition] <- "Yes"
Elite <- as.factor(Elite)
college <- data.frame(college, Elite)</pre>
```

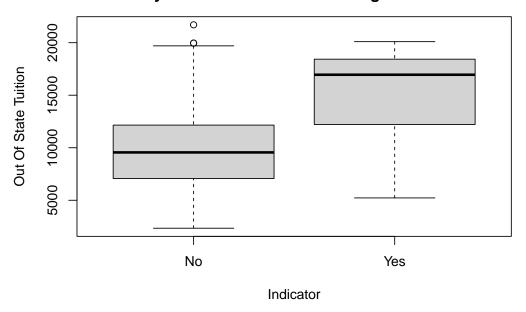
Use the summary() function to see how many elite universities there are. Now use the plot() function to produce side-by-side boxplots of Outstate versus Elite.

```
summary(college$Elite)
```

```
# No Yes
# 699 78

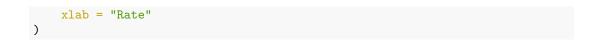
plot(
    x = Elite,
    y = college$Out_Of_State_Tuition,
    main = "Distributions Of Out Of State Tuition\nBy Indicator Of Whether College Is Elite
    xlab = "Indicator",
    ylab = "Out Of State Tuition"
)
```

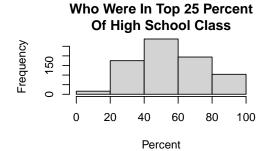
Distributions Of Out Of State Tuition By Indicator Of Whether College Is Elite



v. Use the hist() function to produce some histograms with differing numbers of bins for a few of the quantitative variables. You may find the command par(mfrow = c(2, 2)) useful: it will divide the print window into four regions so that four plots can be made simultaneously. Modifying the arguments to this function will divide the screen in other ways.

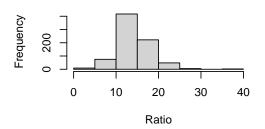
```
par(mfrow = c(2, 2))
column_of_percents <- college$</pre>
    Percent_Of_New_Students_Who_Were_In_Top_25_Percent_Of_High_School_Class
hist(
    x = column_of_percents,
    breaks = 6,
    main = "Percent Of New Students\nWho Were In Top 25 Percent\nOf High School Class",
    xlab = "Percent"
)
hist(
    x = college$Student_Faculty_Ratio,
    breaks = 7,
    main = "Student Faculty Ratio",
    xlab = "Ratio"
)
hist(
    x = college$Instructional_Expenditure_Per_Student,
    breaks = 8,
    main = "Instructional Expenditure\nPer Student",
    xlab = "Expenditure"
)
    x = college$Graduation_Rate,
    breaks = 9,
    main = "Graduation Rate",
```

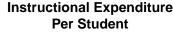


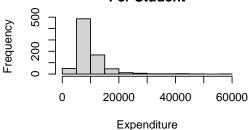


Percent Of New Students

Student Faculty Ratio

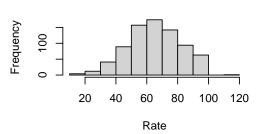






Texas A&M University at Galveston

Graduation Rate



vi. Continue exploring the data, and provide a brief summary of what you discover.

column_Percent_Of_Faculty_With_PhDs <- college\$Percent_Of_Faculty_With_PhDs
summary(column_Percent_Of_Faculty_With_PhDs)</pre>

```
#
     Min. 1st Qu.
                   Median
                              Mean 3rd Qu.
                                               Max.
#
            62.00
                     75.00
                             72.66
                                     85.00
                                             103.00
college_has_percent_of_faculty_with_PhDs_equal_to_103 <-</pre>
    column_Percent_Of_Faculty_With_PhDs == 103
index_of_college_with_percent_of_faculty_with_PhDs_equal_to_103 <-</pre>
    which(college_has_percent_of_faculty_with_PhDs_equal_to_103)
college[index_of_college_with_percent_of_faculty_with_PhDs_equal_to_103, ]
```

Indicator_Of_Whether_College_Is_Private # Texas A&M University at Galveston # Number_Of_Applications Number_Of_Acceptances Texas A&M University at Galveston 481 # Number_Of_Enrollments # Texas A&M University at Galveston # Percent_Of_New_Students_Who_Were_In_Top_10_Percent_Of_F # Texas A&M University at Galveston # Percent_Of_New_Students_Who_Were_In_Top_25_Percent_Of_F Texas A&M University at Galveston # Number_Of_Full_Time_Undergraduates # Texas A&M University at Galveston 1206

Number_Of_Part_Time_Undergraduates

134

```
Out_Of_State_Tuition Cost_Of_Room_And_Board
                                                                            3122
# Texas A&M University at Galveston
                                                     4860
                                    Cost Of Books Personal Spending
#
 Texas A&M University at Galveston
                                               600
#
                                    Percent_Of_Faculty_With_PhDs
#
 Texas A&M University at Galveston
                                    Percent Of Faculty With Terminal Degrees
 Texas A&M University at Galveston
                                    Student_Faculty_Ratio
 Texas A&M University at Galveston
                                    Percent_Of_Alumni_Who_Donate
#
 Texas A&M University at Galveston
                                     Instructional_Expenditure_Per_Student
 Texas A&M University at Galveston
                                                                      6415
                                    Graduation_Rate Elite
# Texas A&M University at Galveston
                                                  43
                                                        No
```

In the College data set, Texas A&M University at Galveston has a percent of faculty with PhD's equal to 103. This value could either be an error or a code for a missing value.

- 5. This exercise involves the Boston housing data set.
 - (a) To begin, load in the Boston data set. The Boston data set is part of the ISLR2 library.

library(ISLR2)

Now the data set is contained in the object Boston.

head(Boston)

```
crim zn indus chas
                                              dis rad tax ptratio 1stat medv
                            nox
                                   rm
                                      age
# 1 0.00632 18
               2.31
                        0 0.538 6.575 65.2 4.0900
                                                    1 296
                                                             15.3
                                                                   4.98 24.0
# 2 0.02731 0
              7.07
                        0 0.469 6.421 78.9 4.9671
                                                    2 242
                                                             17.8 9.14 21.6
# 3 0.02729 0
               7.07
                        0 0.469 7.185 61.1 4.9671
                                                    2 242
                                                             17.8
                                                                   4.03 34.7
# 4 0.03237
            0
               2.18
                        0 0.458 6.998 45.8 6.0622
                                                    3 222
                                                             18.7
                                                                   2.94 33.4
# 5 0.06905 0 2.18
                        0 0.458 7.147 54.2 6.0622
                                                    3 222
                                                             18.7
                                                                   5.33 36.2
# 6 0.02985
            0 2.18
                        0 0.458 6.430 58.7 6.0622
                                                    3 222
                                                             18.7 5.21 28.7
```

Read about the data set:

?Boston

How many rows are in this data set? How many columns? What do the rows and columns represent?

nrow(Boston)

[1] 506

ncol(Boston)

[1] 13

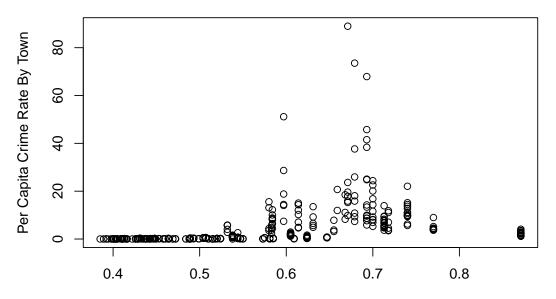
Rows are records containing "housing values in 506 suburbs of Boston" (chrome-extension://efai dnbmnnnibpcajpcglclefindmkaj/https://cran.r-project.org/web/packages/ISLR2/ISLR2.pdf). Columns represent features of suburbs of Boston and include:

- crim: per capita crime rate by town
- zn: proportion of residential land zoned for lots over 25,000 square feet
- indus: proportion of non-retail business acres per town
- chas: Charles River dummy variable that is 1 if tract bounds river and 0 otherwise

- nox: nitrogen oxides concentration in parts per 10 million
- rm: average number of rooms per dwelling
- age: proportion of owner-occupied units built prior to 1940
- dis: weighted mean of distances to five Boston employment centers
- rad: index of accessibility to radial highways
- tax: full-value property-tax rate per 10,000 dollars
- ptratio: pupil-teacher ratio by town
- 1stat: lower status of the population in percent
- medv: median value of owner-occupied homes in thousands of dollars
- (b) Make some pairwise scatterplots of the predictors (columns) in this data set. Describe your findings.

```
plot(
    x = Boston$nox,
    y = Boston$crim,
    main = "Per Capita Crime Rate By Town vs. Nitrogen Oxides Concentration",
    xlab = "Nitrogen Oxides Concentration (Parts Per 10 Million)",
    ylab = "Per Capita Crime Rate By Town"
)
```

Per Capita Crime Rate By Town vs. Nitrogen Oxides Concentration



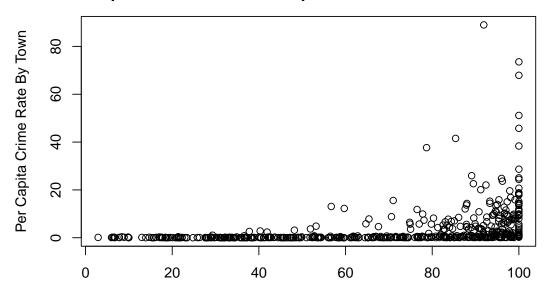
Nitrogen Oxides Concentration (Parts Per 10 Million)

Generally, as nitrogen oxides concentration increases, per capita crime rate by town and its variance increase exponentially. Nitrogen oxides concentration may be a proxy for reduction in quiet green space allowing an individual to be themselves, industrialization, people being on top of each other, and reduction in health.

```
plot(
    x = Boston$age,
    y = Boston$crim,
    main = "Per Capita Crime Rate By Town vs.\nProportion Of Owner-Occupied Units Built Prior '
    xlab = "Proportion of Owner-Occupied Units Built Prior To 1940",
```



Per Capita Crime Rate By Town vs. Proportion Of Owner-Occupied Units Built Prior To 1940

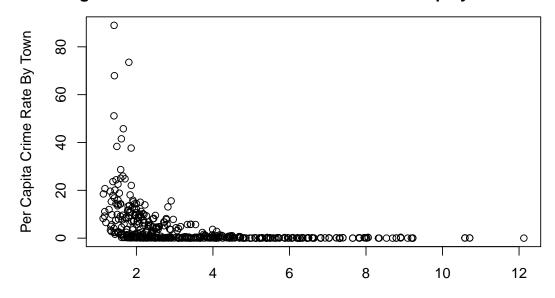


Proportion of Owner-Occupied Units Built Prior To 1940

Generally, as the proportion of owner-occupied units built prior to 1940 increases, per capita crime rate by town and its variance increase exponentially. Proportion of owner-occupied units built prior to 1940 may be a proxy for proportion of substandard housing and urban decay.

```
plot(
    x = Boston$dis,
    y = Boston$crim,
    main = "Per Capita Crime Rate By Town vs.\nWeighted Mean Of Distances To Five Boston Employed Nean Of Distances To Five Boston Employment Centers",
    ylab = "Per Capita Crime Rate By Town"
)
```

Per Capita Crime Rate By Town vs. Weighted Mean Of Distances To Five Boston Employment Centers

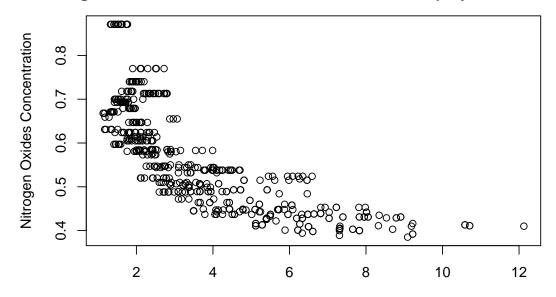


Weighted Mean Of Distances To Five Boston Employment Centers

Generally, as the weighted mean of distances to five Boston employment centers increases, per capita crime rate by town and its variance decrease exponentially. Weighted mean of distances to five Boston employment centers may be a proxy for white flight or reduction in people being on top of each other.

```
plot(
    x = Boston$dis,
    y = Boston$nox,
    main = "Nitrogen Oxides Concentration vs.\nWeighted Mean Of Distances To Five Boston Employ
    xlab = "Weighted Mean Of Distances To Five Boston Employment Centers",
    ylab = "Nitrogen Oxides Concentration"
)
```

Nitrogen Oxides Concentration vs. Weighted Mean Of Distances To Five Boston Employment Centers

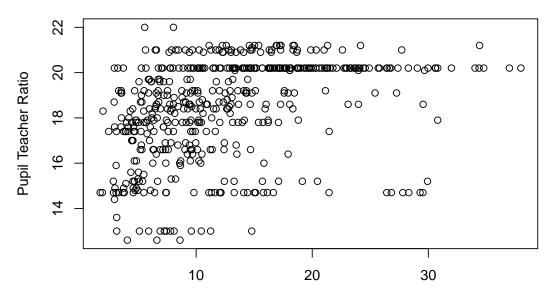


Weighted Mean Of Distances To Five Boston Employment Centers

Generally, as the weighted mean of distances to five Boston employment centers increases, nitrogen oxides concentration decreases. Boston employment centers may be relatively industrialized and distant suburbs may be relatively green.

```
plot(
    x = Boston$lstat,
    y = Boston$ptratio,
    main = "Pupil Teacher Ratio vs. Proportion Of Population With Lower Status",
    xlab = "Proportion Of Population With Lower Status",
    ylab = "Pupil Teacher Ratio"
)
```

Pupil Teacher Ratio vs. Proportion Of Population With Lower Status



Proportion Of Population With Lower Status

Generally, as proportion of population with lower status increases, pupil teacher ratio increases. Pupil teacher ratio may be a proxy for lack of individualized education.

(c) Are any of the predictors associated with per capita crime rate? If so, explain the relationship.

```
correlation_matrix <- cor(Boston)
library(TomLeversRPackage)
analyze_correlation_matrix(correlation_matrix)</pre>
```

```
#
 crim
      V+:
           crim
      V-:
      H+:
      H-:
      M+:
           rad, tax
      M-:
           indus, nox, age, 1stat
      I.+:
           dis, medv
      N:
          zn, chas, rm, ptratio
#
      V+:
           zn
      V-:
      H+:
      H-:
           dis
      M+:
           indus, nox, age
           rm, medv
           rad, tax, ptratio, lstat
      N:
          crim, chas
# indus
```

```
V+: indus
     V-:
     H+: nox, tax
     H-: dis
     M+: age, rad, 1stat
#
     M-: zn
     L+: crim, ptratio
     L-: rm, medv
#
     N: chas
# chas
     V+: chas
#
     V-:
     H+:
     H-:
     M+:
#
     M-:
     L+:
     L-:
#
     N: crim, zn, indus, nox, rm, age, dis, rad, tax, ptratio, lstat, medv
# nox
     V+: nox
     V-:
#
     H+: indus, age
     H-: dis
     M+: rad, tax, lstat
     M-: zn
     L+: crim
     L-: rm, medv
     N: chas, ptratio
# rm
     V+: rm
#
#
     V-:
#
     H+:
#
     H-:
     M+: medv
#
#
     M-: lstat
     L+: zn
     L-: indus, nox, ptratio
     N: crim, chas, age, dis, rad, tax
# age
     V+: age
#
     V-:
#
     H+: nox
     H-: dis
     M+: indus, tax, 1stat
     M-: zn
     L+: crim, rad
     L-: medv
     N: chas, rm, ptratio
# dis
     V+: dis
#
     V-:
#
     H+:
#
     H-: indus, nox, age
```

```
M+: zn
     M-: tax
     L+:
     L-: crim, rad, 1stat
#
     N: chas, rm, ptratio, medv
# rad
     V+: rad, tax
     V-:
#
     H+:
     H-:
     M+: crim, indus, nox
     M-:
     L+: age, ptratio, lstat
     L-: zn, dis, medv
     N: chas, rm
# tax
#
     V+: rad, tax
     V-:
#
     H+: indus
#
     H-:
     M+: crim, nox, age, lstat
     M-: dis
     L+: ptratio
     L-: zn, medv
     N: chas, rm
# ptratio
     V+: ptratio
     V-:
     H+:
     H-:
     M+:
     M-: medv
     L+: indus, rad, tax, lstat
     L-: zn, rm
     N: crim, chas, nox, age, dis
# lstat
     V+: lstat
     V-:
#
     H+:
     H-: medv
     M+: indus, nox, age, tax
     M-: rm
     L+: crim, rad, ptratio
     L-: zn, dis
     N: chas
# medv
     V+: medv
     V-:
     H+:
#
     H-: lstat
     M+: rm
     M-: ptratio
     L+: zn
     L-: crim, indus, nox, age, rad, tax
```

N: chas, dis

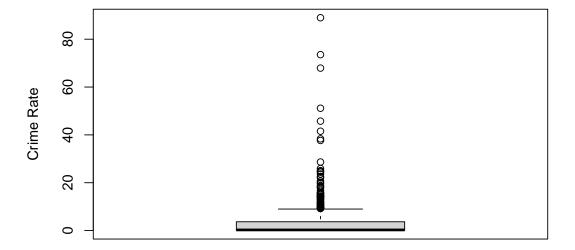
Per capita crime rate is very highly positively associated with itself; highly correlated with no predictors; moderately positively correlated with index of accessibility of radial highways and full-value property-tax rate per 10,000 dollars; lowly positively correlated with proportion of non-retail business acres per town, nitrogen oxides concentration in parts per 10 million, proportion of owner-occupied units built prior to 1940, and lower status of the population in percent; and lowly negatively correlated with weighted mean of distances to five Boston employment centers and median value of owner-occupied homes in thousands of dollars.

(d) Do any of the census tracts of Boston appear to have particularly high crime rates? Tax rates? Pupil-teacher ratios? Comment on the range of each predictor.

Many of the census tracts of Boston appear to have particularly high crime rates. These particularly high crime rates are represented below as outliers in "Distribution Of Crime Rates". According to "Distribution Of Tax Rates" and "Distribution Of Pupil Teacher Ratios", none of the census tracts of Boston appear to have particularly high tax rates or pupil teacher ratios. However, according to "Histogram Of Tax Rates", many of the census tracts of Boston appear to have particularly high tax rates and particularly high pupil teacher ratios. The minimum crime rate for a census tract of Boston is 0.006; the maximum crime rate for a census tract of Boston is 89.0. The minimum tax rate for a census tract of Boston is 711. The minimum pupil teacher ratio for a census tract of Boston is 12.6; the maximum pupil teacher ratio for a census tract of Boston is 22.

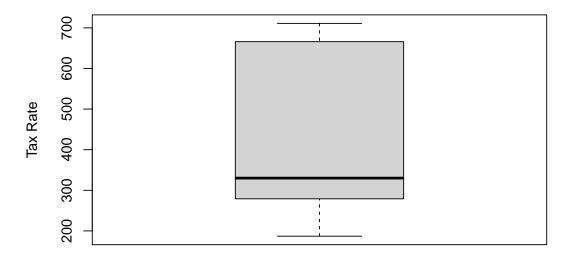
```
boxplot(
   Boston$crim,
   main = "Distribution Of Crime Rates",
   ylab = "Crime Rate"
)
```

Distribution Of Crime Rates



```
min(Boston$crim)
# [1] 0.00632
max(Boston$crim)
# [1] 88.9762
boxplot(
    Boston$tax,
    main = "Distribution Of Tax Rates",
    ylab = "Tax Rate"
)
```

Distribution Of Tax Rates



```
min(Boston$tax)

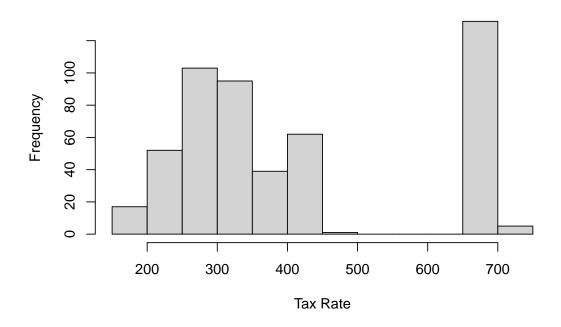
# [1] 187

max(Boston$tax)

# [1] 711

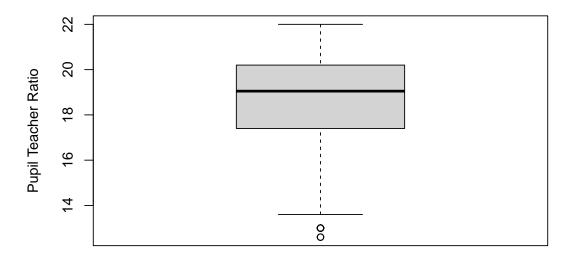
hist(
    x = Boston$tax,
    main = "Histogram Of Tax Rates",
    xlab = "Tax Rate",
    ylab = "Frequency"
)
```

Histogram Of Tax Rates



```
boxplot(
    Boston$ptratio,
    main = "Distribution Of Pupil Teacher Ratios",
    ylab = "Pupil Teacher Ratio"
)
```

Distribution Of Pupil Teacher Ratios



```
min(Boston$ptratio)

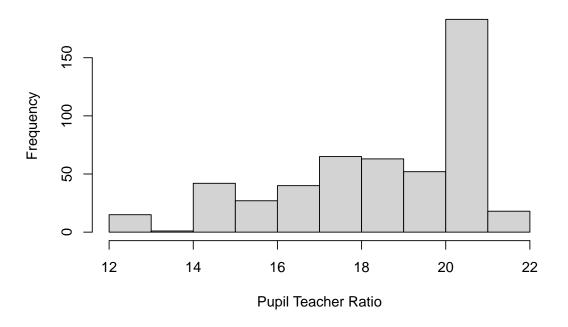
# [1] 12.6

max(Boston$ptratio)

# [1] 22

hist(
    x = Boston$ptratio,
    main = "Histogram Of Pupil Teacher Ratios",
    xlab = "Pupil Teacher Ratio",
    ylab = "Frequency"
)
```

Histogram Of Pupil Teacher Ratios



(e) How many of the census tracts in this data set bound the Charles river?

```
census_tracts_bound_Charles_River <- Boston$chas == 1
vector_of_indices_of_census_tracts_that_bound_Charles_River <-
    which(census_tracts_bound_Charles_River)
length(vector_of_indices_of_census_tracts_that_bound_Charles_River)</pre>
```

- # [1] 35
- (f) What is the median pupil-teacher ratio among the towns in this data set? median(Boston\$ptratio)
 - # [1] 19.05
- (g) Which census tract of Boston has lowest median value of owner-occupied homes? What are the values of the other predictors for that census tract, and how do those values compare to the overall ranges for those predictors? Comment on your findings.

```
index_of_lowest_median_home_value <- which.min(Boston$medv)
index_of_lowest_median_home_value</pre>
```

```
# [1] 399
```

```
record_with_lowest_median_home_value <-
   Boston[index_of_lowest_median_home_value, ]
record_with_lowest_median_home_value</pre>
```

```
# crim zn indus chas nox rm age dis rad tax ptratio lstat medv
# 399 38.3518 0 18.1 0 0.693 5.453 100 1.4896 24 666 20.2 30.59 5
calculate_percentile_of_value_of_record_in_column <-
    function(record, name_of_column) {</pre>
```

```
index <- get_column_index(record, name_of_column)</pre>
    value <- record[1, index]</pre>
    percentile <- calculate_percentile(Boston[, index], value)</pre>
    return(percentile)
}
calculate_percentile_of_value_of_record_in_column(
    record with lowest median home value,
    "crim"
# [1] 99
calculate_percentile_of_value_of_record_in_column(
    record_with_lowest_median_home_value,
    "zn"
)
# [1] 37
calculate_percentile_of_value_of_record_in_column(
    record_with_lowest_median_home_value,
    "indus"
)
# [1] 76
calculate_percentile_of_value_of_record_in_column(
    record_with_lowest_median_home_value,
    "chas"
)
# [1] 47
calculate_percentile_of_value_of_record_in_column(
    record_with_lowest_median_home_value,
    "nox"
)
# [1] 84
calculate_percentile_of_value_of_record_in_column(
    record_with_lowest_median_home_value,
    "rm"
)
# [1] 8
calculate_percentile_of_value_of_record_in_column(
    record with lowest median home value,
    "age"
)
# [1] 96
calculate_percentile_of_value_of_record_in_column(
    record_with_lowest_median_home_value,
    "dis"
)
```

```
# [1] 6
   calculate_percentile_of_value_of_record_in_column(
       record_with_lowest_median_home_value,
   )
   # [1] 87
   calculate_percentile_of_value_of_record_in_column(
       record_with_lowest_median_home_value,
       "tax"
   )
   # [1] 86
   calculate_percentile_of_value_of_record_in_column(
       record_with_lowest_median_home_value,
       "ptratio"
   )
   # [1] 75
   calculate_percentile_of_value_of_record_in_column(
       record_with_lowest_median_home_value,
       "lstat"
   )
   # [1] 98
   calculate_percentile_of_value_of_record_in_column(
       record_with_lowest_median_home_value,
        "medv"
   )
   # [1] 0
(h) In this data set, how many of the census tracts average more than seven rooms per dwelling? More
   than eight rooms per dwelling? Comment on the census tracts that average more than eight rooms
   per dwelling.
   census_tracts_average_more_than_seven_rooms_per_dwelling <- Boston$rm > 7
   census_tracts_average_more_than_eight_rooms_per_dwelling <- Boston$rm > 8
   vector_of_indices_of_tracts_averaging_more_than_seven_rooms_per_dwelling <-
       which(census_tracts_average_more_than_seven_rooms_per_dwelling)
   vector of indices of tracts averaging more than eight rooms per dwelling <-
       which(census_tracts_average_more_than_eight_rooms_per_dwelling)
   length(vector_of_indices_of_tracts_averaging_more_than_seven_rooms_per_dwelling)
   # [1] 64
   number_of_tracts_average_more_than_eight_rooms_per_dwelling <- length(</pre>
       vector_of_indices_of_tracts_averaging_more_than_eight_rooms_per_dwelling
   number_of_tracts_average_more_than_eight_rooms_per_dwelling
   # [1] 13
   data_frame_of_tracts_averaging_more_than_eight_rooms_per_dwelling <-
       Boston[FALSE, ]
   for (i in 1:number_of_tracts_average_more_than_eight_rooms_per_dwelling) {
```

```
index_of_tract_averaging_more_than_eight_rooms_per_dwelling <-</pre>
       vector_of_indices_of_tracts_averaging_more_than_eight_rooms_per_dwelling[
       ٦
   number of rows <-
       nrow(data_frame_of_tracts_averaging_more_than_eight_rooms_per_dwelling)
   data_frame_of_tracts_averaging_more_than_eight_rooms_per_dwelling[
       number_of_rows + 1,
   ] <- Boston[i, ]</pre>
}
data_frame_of_tracts_averaging_more_than_eight_rooms_per_dwelling
        crim
              zn indus chas
                              nox
                                          age
                                                 dis rad tax ptratio lstat medv
                                     rm
# 1 0.00632 18.0 2.31
                                                       1 296
                          0 0.538 6.575
                                         65.2 4.0900
                                                                15.3 4.98 24.0
    0.02731 0.0 7.07
                                                       2 242
                                                                17.8 9.14 21.6
# 2
                          0 0.469 6.421
                                         78.9 4.9671
# 3 0.02729 0.0 7.07
                          0 0.469 7.185
                                         61.1 4.9671
                                                       2 242
                                                                17.8 4.03 34.7
# 4 0.03237 0.0 2.18
                          0 0.458 6.998 45.8 6.0622
                                                       3 222
                                                                18.7 2.94 33.4
# 5 0.06905 0.0 2.18
                          0 0.458 7.147
                                         54.2 6.0622
                                                       3 222
                                                                18.7 5.33 36.2
# 6 0.02985 0.0 2.18
                          0 0.458 6.430 58.7 6.0622
                                                       3 222
                                                                18.7 5.21 28.7
# 7 0.08829 12.5 7.87
                          0 0.524 6.012 66.6 5.5605
                                                       5 311
                                                                15.2 12.43 22.9
# 8 0.14455 12.5 7.87
                          0 0.524 6.172 96.1 5.9505
                                                       5 311
                                                                15.2 19.15 27.1
# 9 0.21124 12.5 7.87
                          0 0.524 5.631 100.0 6.0821
                                                       5 311
                                                                15.2 29.93 16.5
# 10 0.17004 12.5 7.87
                          0 0.524 6.004 85.9 6.5921
                                                       5 311
                                                                15.2 17.10 18.9
# 11 0.22489 12.5 7.87
                          0 0.524 6.377 94.3 6.3467
                                                       5 311
                                                                15.2 20.45 15.0
# 12 0.11747 12.5 7.87
                          0 0.524 6.009 82.9 6.2267
                                                                15.2 13.27 18.9
                                                       5 311
# 13 0.09378 12.5 7.87
                          0 0.524 5.889
                                                                15.2 15.71 21.7
                                         39.0 5.4509
                                                       5 311
summary(Boston$crim)
     Min. 1st Qu.
                     Median
                                Mean 3rd Qu.
                                                  Max.
  0.00632 0.08204 0.25651 3.61352 3.67708 88.97620
summary(data_frame_of_tracts_averaging_more_than_eight_rooms_per_dwelling$crim)
     Min. 1st Qu. Median
                            Mean 3rd Qu.
# 0.00632 0.02985 0.08829 0.09557 0.14455 0.22489
summary(Boston$zn)
    Min. 1st Qu. Median
                            Mean 3rd Qu.
                                            Max.
     0.00
            0.00
                    0.00
                           11.36
                                   12.50 100.00
summary(data_frame_of_tracts_averaging_more_than_eight_rooms_per_dwelling$zn)
    Min. 1st Qu. Median
                            Mean 3rd Qu.
                                            Max.
   0.000
           0.000 12.500
                           8.115 12.500 18.000
summary(Boston$indus)
    Min. 1st Qu. Median
                            Mean 3rd Qu.
                                            Max.
     0.46
            5.19
                    9.69
                           11.14
                                   18.10
                                           27.74
summary(data_frame_of_tracts_averaging_more_than_eight_rooms_per_dwelling$indus)
    Min. 1st Qu. Median
                            Mean 3rd Qu.
                                            Max.
   2.180
           2.310
                   7.870
                           6.006
                                   7.870
                                           7.870
summary(Boston$nox)
```

- # Min. 1st Qu. Median Mean 3rd Qu. Max.
- # 0.3850 0.4490 0.5380 0.5547 0.6240 0.8710

summary(data_frame_of_tracts_averaging_more_than_eight_rooms_per_dwelling\$nox)

- # Min. 1st Qu. Median Mean 3rd Qu. Max.
- # 0.4580 0.4690 0.5240 0.5014 0.5240 0.5380

summary(Boston\$age)

- # Min. 1st Qu. Median Mean 3rd Qu. Max.
- # 2.90 45.02 77.50 68.57 94.08 100.00

summary(data_frame_of_tracts_averaging_more_than_eight_rooms_per_dwelling\$age)

- # Min. 1st Qu. Median Mean 3rd Qu. Max.
- # 39.00 58.70 66.60 71.44 85.90 100.00

summary(Boston\$dis)

- # Min. 1st Qu. Median Mean 3rd Qu. Max.
- # 1.130 2.100 3.207 3.795 5.188 12.127

summary(data_frame_of_tracts_averaging_more_than_eight_rooms_per_dwelling\$dis)

- # Min. 1st Qu. Median Mean 3rd Qu. Max.
- # 4.090 5.451 6.062 5.725 6.082 6.592

summary(Boston\$rad)

- # Min. 1st Qu. Median Mean 3rd Qu. Max.
- # 1.000 4.000 5.000 9.549 24.000 24.000

summary(data_frame_of_tracts_averaging_more_than_eight_rooms_per_dwelling\$rad)

- # Min. 1st Qu. Median Mean 3rd Qu. Max.
- # 1.000 3.000 5.000 3.769 5.000 5.000

summary(Boston\$tax)

- # Min. 1st Qu. Median Mean 3rd Qu. Max.
- # 187.0 279.0 330.0 408.2 666.0 711.0

summary(data_frame_of_tracts_averaging_more_than_eight_rooms_per_dwelling\$tax)

- # Min. 1st Qu. Median Mean 3rd Qu. Max.
- # 222.0 242.0 311.0 278.7 311.0 311.0

summary(Boston\$ptratio)

- # Min. 1st Qu. Median Mean 3rd Qu. Max.
- # 12.60 17.40 19.05 18.46 20.20 22.00

summary(data_frame_of_tracts_averaging_more_than_eight_rooms_per_dwelling\$ptratio)

- # Min. 1st Qu. Median Mean 3rd Qu. Max.
- # 15.20 15.20 15.20 16.42 17.80 18.70

summary(Boston\$1stat)

- # Min. 1st Qu. Median Mean 3rd Qu. Max.
- # 1.73 6.95 11.36 12.65 16.95 37.97

summary(data_frame_of_tracts_averaging_more_than_eight_rooms_per_dwelling\$lstat)

- # Min. 1st Qu. Median Mean 3rd Qu. Max.
- # 2.94 5.21 12.43 12.28 17.10 29.93

summary(Boston\$medv)

- # Min. 1st Qu. Median Mean 3rd Qu. Max.
- # 5.00 17.02 21.20 22.53 25.00 50.00

summary(data_frame_of_tracts_averaging_more_than_eight_rooms_per_dwelling\$medv)

- # Min. 1st Qu. Median Mean 3rd Qu. Max.
- # 15.00 18.90 22.90 24.58 28.70 36.20

The census tracts averaging more than eight rooms per dwelling generally have low crime rates, proportion of residential land zoned for lots over 25,000 square feet, proportion of non-retail business acres per town, nitrogen oxides concentration in parts per 10 million, index of accessibility to radial highways, full-value property-tax rates per 10,000 dollars, and pupil teacher ratio by town. These census tracts generally have average proportion of owner-occupied units built prior to 1940 and percent of population with lower status. These census tracts have high average number of rooms per dwelling, weighted mean of distances to five Boston employment centers, and median value of owner-occupied homes in thousands of dollars. These census tracts do not bound the Charles River.