Stat 6021: Guided Question Set 7

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Car drivers like to adjust the seat position for their own comfort. Car designers find it helpful to know where different drivers will position the seat. Researchers at HuMoSim laboratory at the University of Michigan collected data on 38 drivers. The response variable is hipcenter, the horizontal distance of the midpoint of the hips from a fixed location in the car in mm. They measured the following eight predictors:

- x_1 : Age: Age in years
- x_2 : Weight: Weight in pounds
- x_3 : HtShoes: Height with shoes in cm.
- x_4 : Ht: Height without shoes in cm.
- x_5 : Seated: Seated height in cm.
- x_6 : Arm: Arm length in cm.
- x_7 : Thigh: Thigh length in cm.
- x_8 : Leg: Lower leg length in cm.

The data are from the faraway package in R. After installing the faraway package, load the seatpos data set.

```
library(faraway)
head(seatpos, n = 3)
```

```
Age Weight HtShoes
                            Ht Seated Arm Thigh Leg hipcenter
## 1
      46
            180
                  187.2 184.9
                                 95.2 36.1
                                            45.3 41.3
                                                        -206.300
## 2
      31
            175
                  167.5 165.5
                                 83.8 32.9
                                            36.5 35.9
                                                        -178.210
## 3
            100
                  153.6 152.2
                                 82.9 26.0
                                            36.6 31.0
                                                         -71.673
```

1. Fit the full model with all the predictors. Using the summary function, comment on the results of the t tests and ANOVA F test from the output.

```
library(TomLeversRPackage)
linear_model <- lm(hipcenter ~ ., data = seatpos)
summarize_linear_model(linear_model)</pre>
```

```
##
## Call:
## lm(formula = hipcenter ~ ., data = seatpos)
## Residuals:
##
       Min
                1Q Median
                                 3Q
                                        Max
## -73.827 -22.833 -3.678
                            25.017
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 436.43213 166.57162
                                       2.620
                                               0.0138 *
## Age
                 0.77572
                             0.57033
                                       1.360
                                               0.1843
## Weight
                 0.02631
                             0.33097
                                       0.080
                                               0.9372
```

```
## HtShoes
                -2.69241
                            9.75304
                                      -0.276
                                               0.7845
## Ht
                           10.12987
                                       0.059
                 0.60134
                                               0.9531
                                               0.8882
## Seated
                 0.53375
                            3.76189
                                       0.142
## Arm
                -1.32807
                            3.90020
                                      -0.341
                                               0.7359
## Thigh
                -1.14312
                            2.66002
                                      -0.430
                                               0.6706
                -6.43905
                            4.71386
## Leg
                                      -1.366
                                               0.1824
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 37.72 on 29 degrees of freedom
## Multiple R-squared: 0.6866, Adjusted R-squared: 0.6001
## F-statistic: 7.94 on 8 and 29 DF, p-value: 1.306e-05
##
## E(y \mid x) =
##
       B_0 +
##
       B_Age * Age +
##
       B_Weight * Weight +
##
       B HtShoes * HtShoes +
##
       B Ht * Ht +
##
       B Seated * Seated +
##
       B_Arm * Arm +
##
       B Thigh * Thigh +
       B_Leg * Leg
##
## E(y \mid x) =
##
       436.43212822533 +
##
       0.775716195411176 * Age +
##
       0.0263130815934825 * Weight +
##
       -2.69240773927674 * HtShoes +
##
       0.601344580352112 * Ht +
##
       0.533751697568726 * Seated +
##
       -1.32806863757197 * Arm +
##
       -1.14311887823954 * Thigh +
##
       -6.43904626562725 * Leg
## Number of observations: 38
## Estimated variance of errors: 1422.82012070282
## Multiple R: 0.828585225565444
                                    Adjusted R: 0.774651837544867
## Critical value t(alpha/2 = 0.05/2, DFRes = 29): 2.0452296421327
## Critical value F(alpha = 0.05, DFR = 8, DFRes = 29): 2.27825084905155
```

Since the above F statistic is greater than the above critical value F / the above p-value for an ANOVA F test is less than a significance level $\alpha=0.05$, we reject a null hypothesis that all regression coefficients in our linear model are 0 / insignificant. We have sufficient evidence to support an alternate hypothesis that at least one regression coefficient in our linear model is not 0 / significant.

Since the magnitudes of the above t statistics for all predictors are less than the above critical value t, we have insufficient evidence to reject a null hypothesis that each regression coefficient is 0 / insignificant in the context of the multiple linear model and the other predictors. We have insufficient evidence to support an alternate hypothesis that each regression coefficient is not 0 / significant in the context of the multiple linear model and the other predictors.

2. Briefly explain why, based on your output from part 1, you suspect the model shows signs of multi-collinearity.

Per section 9.4.4: Multicollinearity: Multicollinearity Diagnostics: Other Diagnostics in *Introduction* to Linear Regression Analysis (Sixth Edition) by Douglas C. Montgomery et al., "if the overall F statistic is significant but the individual t statistics are all nonsignificant, multicollinearity is present".

Multicollinearity is present.

3. Provide the output of all the pairwise correlations among the predictors. Comment briefly on the pairwise correlations.

```
library(dplyr)
data_frame_of_predictor_values <- seatpos %>% select(-hipcenter)
correlation_matrix <- round(cor(data_frame_of_predictor_values), 3)</pre>
correlation_matrix
##
              Age Weight HtShoes
                                     Ht Seated
                                                  Arm Thigh
                                                               Leg
                         -0.079 -0.090 -0.170 0.360 0.091 -0.042
## Age
            1.000 0.081
## Weight
            0.081
                  1.000
                           0.828 0.829 0.776 0.698 0.573
                                                             0.784
## HtShoes -0.079
                   0.828
                           1.000 0.998 0.930 0.752 0.725
           -0.090 0.829
                           0.998 1.000 0.928 0.752 0.735
## Ht
                                                            0.910
## Seated -0.170 0.776
                           0.930 0.928
                                         1.000 0.625 0.607
                                                             0.812
## Arm
            0.360 0.698
                           0.752 0.752 0.625 1.000 0.671 0.754
## Thigh
            0.091 0.573
                           0.725 0.735 0.607 0.671 1.000
                                                             0.650
## Leg
           -0.042 0.784
                           0.908 0.910 0.812 0.754 0.650
                                                             1.000
analyze_correlation_matrix(correlation_matrix)
## Age
##
       ۷:
           Age
##
       Η:
##
       M:
##
       L:
           Arm
##
       N:
           Weight, HtShoes, Ht, Seated, Thigh, Leg
## Weight
##
           Weight
       ۷:
##
       Η:
           HtShoes, Ht, Seated, Leg
##
       M:
           Arm, Thigh
##
       L:
##
       N:
           Age
## HtShoes
##
       V: HtShoes, Ht, Seated, Leg
##
       Η:
           Weight, Arm, Thigh
##
       M:
##
       L:
##
       N:
           Age
## Ht
##
       V:
           HtShoes, Ht, Seated, Leg
##
           Weight, Arm, Thigh
##
       M:
##
       L:
##
       N:
           Age
## Seated
##
           HtShoes, Ht, Seated
       V:
##
       Η:
           Weight, Leg
##
           Arm, Thigh
       M:
##
       L:
##
       N:
           Age
## Arm
##
       V: Arm
##
       H: HtShoes, Ht, Leg
```

M: Weight, Seated, Thigh

##

```
L: Age
##
##
      N:
## Thigh
##
      V: Thigh
      H: HtShoes, Ht
##
      M: Weight, Seated, Arm, Leg
##
##
      L:
##
      N: Age
## Leg
##
      V: HtShoes, Ht, Leg
      H: Weight, Seated, Arm
##
      M: Thigh
##
##
      L:
##
      N: Age
```