

$$1 + 1 + \sum_{i=0}^{n-1} (1 + 2 + 1 + \sum_{j=i}^{n-1} (1 + 2 + 1 + 1 + \sum_{k=i}^j (1 + 2 + 2) + 1 + 4) + 1) + 1 =$$

$$k_1 + \sum_{i=0}^{n-1} k_2 + \sum_{i=0}^{n-1} \sum_{j=i}^{n-1} k_3 + \sum_{i=0}^{n-1} \sum_{j=i}^{n-1} \sum_{k=i}^j 5 = k_1 + k_2 \sum_{i=0}^{n-1} 1 + k_3 \sum_{i=0}^{n-1} \sum_{j=i}^{n-1} 1 + 5 \sum_{i=0}^{n-1} \sum_{j=i}^{n-1} \sum_{k=i}^j 1$$

$$= k_1 + k_2 \sum_{i=1}^n 1 + k_3 \sum_{i=1}^n \sum_{j=1}^{n-i} 1 + 5 \sum_{i=0}^{n-1} \sum_{j=i}^{n-1} \sum_{k=1}^{j-i+1} 1 = k_1 + k_2 n + k_3 \sum_{i=0}^{n-1} (n-i) + 5 \sum_{i=0}^{n-1} \sum_{j=i}^{n-1} (j-i+1)$$

$$= k_1 + k_2 n + k_3 \sum_{i=1}^n (n-i-1) + 5 \sum_{i=0}^{n-1} \sum_{j=1}^{n-i} (j-i+1+i-1) =$$

$$= k_1 + k_2 n + k_3 n \sum_{i=1}^n 1 - k_3 \sum_{i=1}^n i - k_3 \sum_{i=1}^n 1 + 5 \sum_{i=0}^{n-1} \sum_{j=1}^{n-i} j =$$

$$k_1 + k_2 n + k_3 n^2 - k_3 \frac{n(n+1)}{2} - k_3 n + 5 \sum_{i=0}^{n-1} \frac{(n-i)(n-i-1)}{2}$$

$$= k_1 + k_5 n + k_6 n^2 + \frac{5}{2} \sum_{i=0}^{n-1} (n^2 - n - 2ni + i^2 + i) = k_1 + k_5 n + k_6 n^2 + \frac{5}{2} \sum_{i=1}^n (n^2 - n - 2n(i-1) + (i-1)^2 + (i-1))$$

$$= k_1 + k_8 n + k_7 n^2 + \frac{5}{2} n^3 - 5n \sum_{i=1}^n i + \frac{5}{2} \sum_{i=1}^n i^2$$

$$= k_1 + k_{10} n + k_9 n^2 + \frac{5}{2} n^3 - 5n \frac{n(n+1)}{2} + \frac{5}{2} \cdot \frac{1}{3} n^3$$

$$= k_1 + k_{10} n + k_{11} n^2 + \frac{5}{2} n^3 - \frac{5}{2} n^3 + \frac{5}{6} n^3$$

$$= \frac{5}{6} n^3 + k_{11} n^2 + k_{10} n + k_1$$

$$\Rightarrow T(n) \in O(n^3)$$

$$k_1 = 3$$

$$k_2 = 5$$

$$k_3 = 10$$

$$k_4 = NA$$

$$k_5 = k_2 - \frac{k_3}{2} = 5 - \frac{10}{2} = 0$$

$$k_6 = k_3 - \frac{k_3}{2} = 10 - \frac{10}{2} = 5$$

$$k_7 = k_6 - \frac{5}{2} = \frac{15}{2} = -\frac{5}{4}$$

$$k_8 = k_5 = 0$$

$$k_9 = k_7 + \frac{5}{2} \cdot \frac{1}{2} = -\frac{5}{4} + \frac{5}{4} = 0$$

$$k_{10} = k_8 + \frac{1}{6} \cdot \frac{5}{2} = \frac{5}{12}$$

$$k_{11} = k_9 - \frac{5}{2} = -\frac{5}{2}$$

$$\Rightarrow T(n) = \frac{5}{6} n^3 - \frac{5}{2} n^2 + \frac{5}{12} n + 3$$

// Summorna för värden som ej kommer ge n^3 -termer räknas ej ut, men k -värdena uppdateras istället.