



NUMERICAL ANALYSIS LAB MENUAL



Upoma Das

Lecturer,
Department of EEE, BSMRSTU

MATLAB Program No: 01

Program Name: An M-File to implement the Bisection Method.

Problem: Find a real root of the equation $f(x)=x^3-x-1=0$ by using bisection method.

Main File:

```
function [root,fx,ea,iter]=bisect(func,xl,xu,es,maxit,varargin)
% bisect: root location zeroes
% [root,fx,ea,iter]=bisect(func,xl,xu,es,maxit,p1,p2,...):
% uses bisection method to find the root of func
% input:
% func = name of function
% xl, xu = lower and upper guesses
% es = desired relative error (default = 0.0001%)
% maxit = maximum allowable iterations (default = 50)
% p1,p2,... = additional parameters used by func
% output:
% root = real root
% fx = function value at root
% ea = approximate relative error (%)
% iter = number of iterations
if nargin<3,error('at least 3 input arguments required'),end test =
func(xl,varargin{:})*func(xu,varargin{:});
if test>0,error('no sign change'),end if
nargin<4|isempty(es), es=0.0001;end if
nargin<5|isempty(maxit), maxit=50;end iter = 0; xr
= xl; ea = 100;
while (1)
xrold = xr;
xr = (xl + xu)/2;
iter = iter + 1;
if xr ~= 0,ea = abs((xr - xrold)/xr) * 100;end
test = func(xl,varargin{:})*func(xr,varargin{:});
if test < 0
xu = xr;
elseif test > 0
xl = xr;
else
ea = 0;
end
if ea <= es | iter >= maxit,break,end
end
root = xr; fx = func(xr, varargin{:});
```

Input File:

```
fx=@(x)x^3-x-1;
[root fx ea iter]=bisect(fx,1,2)
```

OUTPUT

On Command Window

```
Command Window
New to MATLAB? See resources for Getting Started.

>> runbisection

root =

    1.3247

fx =

-1.8576e-06

ea =

    7.1991e-05

iter =

    20
```

On Workspace

Workspace	
Name ▲	Value
ea	7.1991e-05
fx	-1.8576e-06
iter	20
root	1.3247

Related Questions:

1. What is Bisection method?
2. Verify this program by solving at least three problems.
3. Make an m-file to implement False Position Method.

MATLAB Program No: 02

Program Name: An M-File to implement the Newton Raphson Method.

Problem: Use the Newton-Raphson method to find a root of the equation $x^3-2x-5=0$.

Main File:

```
function
[root,ea,iter]=newtraph(func,dfunc,xr,es,maxit,varargin)
% newtraph: Newton-Raphson root location zeroes
% [root,ea,iter]=newtraph(func,dfunc,xr,es,maxit,p1,p2,...):
% uses Newton-Raphson method to find the root of func
% input:
% func = name of function
% dfunc = name of derivative of function
% xr = initial guess
% es = desired relative error (default = 0.0001%)
% maxit = maximum allowable iterations (default = 50)
% p1,p2,... = additional parameters used by function
% output:
% root = real root
% ea = approximate relative error (%)
% iter = number of iterations
if nargin<3,error('at least 3 input arguments required'),end if
nargin<4|isempty(es),es=0.0001;end
if nargin<5|isempty(maxit),maxit=50;end iter = 0;

while (1)
xrold = xr;
xr = xr - func(xr)/dfunc(xr);
iter = iter + 1;
if xr ~= 0, ea = abs((xr - xrold)/xr) * 100; end if ea <= es | iter
>= maxit, break, end end

root = xr;
```

Input File:

```
y=@(x)x^3-2*x-5;
dy=@(x)3*x^2-2;
[root ea iter]=newtraph(y,dy,2,0.00001)
```

OUTPUT

On Command Window

```
Command Window
New to MATLAB? See resources for Getting Started.

>> runnewtraph

root =

    2.0946

ea =

    7.4418e-09

iter =

    4
```

On Workspace

Name	Value
dy	@(x)3*x^2-2
ea	7.4418e-09
fx	-1.8576e-06
iter	4
root	2.0946
y	@(x)x^3-2*x-5

Related Questions:

1. What is the difference between bracketing method and open method?
2. As an engineer which method will you prefer?
3. Use the above m-file to estimate the root of $f(x) = e^{-x} - x$ employing an initial guess of $x_0 = 0$.
4. $f(x) = x^3 - 6x^2 + 11x - 6.1$. Determine the root with MATLAB.
5. Write a new matlab program to implement Newton Raphson method which doesn't need the derivative of a function.

MATLAB Program No: 03

Program Name: An M-File to implement Linear regression.

Problem: An experiment gave the following table of values for the dependent variable y for a set of known values of x. Obtain an appropriate least squares fit for the data and plot y vs x with MATLAB.

x	1	2	3	4	5	6	7	8	9
y	5.5	7.0	9.6	11.5	12.6	14.4	17.6	19.5	20.5

Main File:

```
function [a, r2] = linregr(x,y)
% linregr: linear regression curve fitting
% [a, r2] = linregr(x,y): Least squares fit of straight
% line to data by solving the normal equations
% input:
% x = independent variable
% y = dependent variable
% output:
% a = vector of slope, a(1), and intercept, a(2)
% r2 = coefficient of determination
n = length(x);
if length(y)~=n, error('x and y must be same length'); end x = x(:); y = y(:);
% convert to column vectors sx = sum(x); sy = sum(y);

sx2 = sum(x.*x); sxy = sum(x.*y); sy2 = sum(y.*y);
a(1) = (n*sxy-sx*sy)/(n*sx2-sx^2);
a(2) = sy/n-a(1)*sx/n;
r2 = ((n*sxy-sx*sy)/sqrt(n*sx2-sx^2)/sqrt(n*sy2-sy^2))^2;
% create plot of data and best fit line xp =
linspace(min(x),max(x),2);
yp = a(1)*xp+a(2);
plot(x,y,'o',xp,yp) grid
on
```

Input File:

```
x=[1 2 3 4 5 6 7 8 9];
y=[5.5 7 9.6 11.5 12.6 14.4 17.6 19.5 20.5]; linregr(x,y)
```

OUTPUT

On Command Window

```
Command Window

>> runlinegr

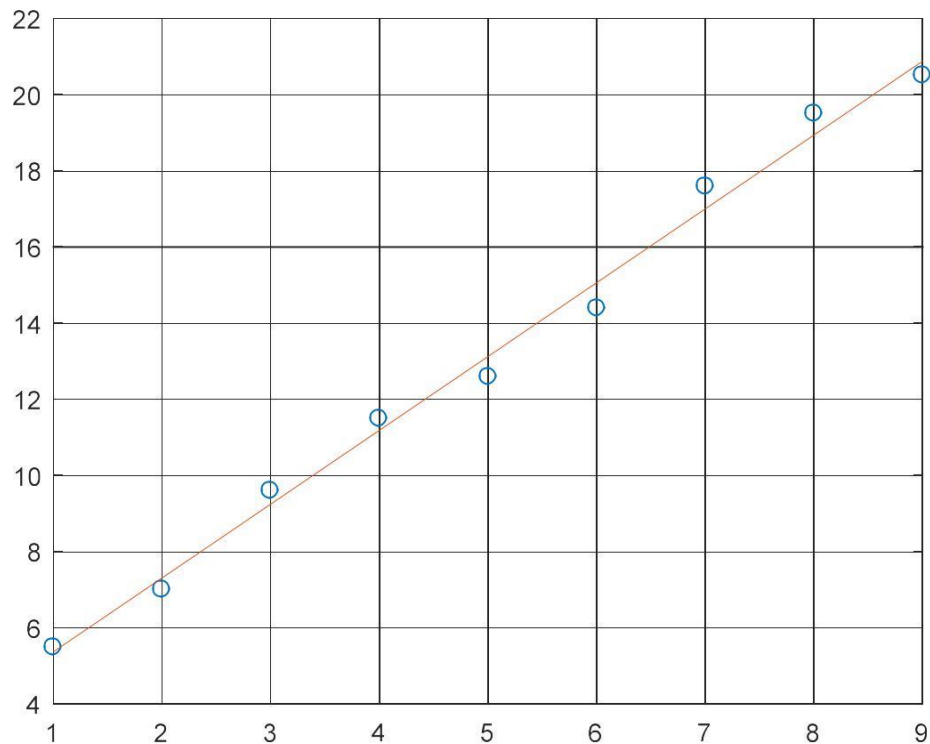
ans =

    1.9400    3.4333
```

On Workspace

Name	Value
ans	[1.9400,3.4333]
x	[1,2,3,4,5,6,7,8,9]
y	[5.5000,7,9,6000,11.50...

Plot y vs x:



Related Questions:

1. What is least squares approximation of functions? Explain it.
2. Why it is important for an engineer?

MATLAB Program No: 04

Program Name: An M-File to implement Lagrange Interpolation.

Problem: Given the following tables of values

x	0.4	0.5	0.7	0.8
y	-0.916	-0.693	-0.357	-0.223

Find the value of $f(0.6)$.

Main File:

```
function yint = Lagrange(x,y,xx)
% Lagrange: Lagrange interpolating polynomial
% yint = Lagrange(x,y,xx): Uses an (n - 1)-order
% Lagrange interpolating polynomial based on n data points
% to determine a value of the dependent variable (yint) at
% a given value of the independent variable, xx.
% input:
% x = independent variable
% y = dependent variable
% xx = value of independent variable at which the
% interpolation is calculated
% output:
% yint = interpolated value of dependent variable
n = length(x);
if length(y)~=n, error('x and y must be same length'); end s = 0;

for i = 1:n
    product = y(i);
    for j = 1:n
        if i ~= j
            product = product*(xx-x(j))/(x(i)-x(j));
        end
    end
    s = s+product;
end
yint = s;
```

Input program :

```
x=[.4 .5 .7 .8]; y=[-.916 -.693 -.357 -
.223]; fx=Lagrange(x,y,0.6)
```


OUTPUT

On Command Window

```
Command Window

>> runlag

fx =

    -0.5102
```

On Workspace

Workspace	
Name ▲	Value
fx	-0.5102
x	[0.4000,0.5000,0.7000,...
y	[-0.9160,-0.6930,-0.35...

Related Questions:

1. What is the main difference between interpolation & least squares approximation?
2. Make a m-file to implement Inverse Lagrange Interpolation.
3. Is it possible to find the value of $f(0.9)$ using the above m-file?
Justify your answer.

MATLAB Program No: 05

Program Name: An M-File to implement Newton interpolation.

Problem: Values of x (in degrees) and sin x are given in the following table:

x (in degrees)	15	20	25	30	35	40
sin x	0.258819	0.3420201	0.4226183	0.5	0.5735764	0.6427876

Determine the value of $\sin 38^\circ$.

Main File:

```
function yint = Newtint(x,y,xx)
% Newtint: Newton interpolating polynomial
% yint = Newtint(x,y,xx): Uses an (n - 1)-order Newton
% interpolating polynomial based on n data points (x, y)
% to determine a value of the dependent variable (yint)
% at a given value of the independent variable, xx.
% input:
% x = independent variable
% y = dependent variable
% xx = value of independent variable at which
% interpolation is calculated
% output:
% yint = interpolated value of dependent variable
% compute the finite divided differences in the form of a
% difference table
n = length(x);
if length(y)~=n, error('x and y must be same length'); end b = zeros(n,n);

% assign dependent variables to the first column of b. b(:,1) = y(:); % the
(:) ensures that y is a column vector. for j = 2:n

for i = 1:n-j+1
b(i,j) = (b(i+1,j-1)-b(i,j-1))/(x(i+j-1)-x(i)); end

end
% use the finite divided differences to interpolate
xt = 1;
yint = b(1,1);
for j = 1:n-1
xt = xt*(xx-x(j));
yint = yint+b(1,j+1)*xt;
end
```

Input File:

```
x=[15 20 25 30 35 40];
y=[.2588190 .3420201 .4226183 .5 .5735764 .6427876];
Newtint(x,y,38)
```

OUTPUT

On Command Window

```
Command Window

>> runnewtint

ans =

    0.6157
```

On Workspace

Workspace	
Name	Value
ans	0.6157
x	[15,20,25,30,35,40]
y	[0.2588,0.3420,0.4226,...]

Related Questions:

1. Make a m-file to implement Bessel's Formulae.
2. Make a m-file to solve the above problem by using central difference table.

MATLAB Program No: 06

Program Name: An M-File to implement the Trapezoidal Rule.

Problem: Evaluate $I = \int_0^1 \frac{1}{1+x} dx$ correct to three decimal places with $h=0.125$.

Main File:

```
function I = trap(func,a,b,n,varargin)
% trap: composite trapezoidal rule quadrature
% I = trap(func,a,b,n,pl,p2,...):
% composite trapezoidal rule
% input:
% func = name of function to be integrated
% a, b = integration limits
% n = number of segments (default = 100)
% pl,p2,... = additional parameters used by func
% output:
% I = integral estimate
if nargin<3,error('at least 3 input arguments required'),end if
~(b>a),error('upper bound must be greater than lower'),end if
nargin<4||isempty(n),n=100;end
x = a; h = (b - a)/n;
s=func(a,varargin{:});
for i = 1 : n-1
x = x + h;
s = s + 2*func(x,varargin{:});
end
s = s + func(b,varargin{:});
I = (b - a) * s/(2*n);
```

Input File:

```
y=@(x)1/(1+x);
trap(y,0,1,8)
```

OUTPUT

On Command Window

```
Command Window
>> runtrap
|
ans =

    0.6941
```

On Workspace

Workspace	
Name ▲	Value
 ans	0.6941
 y	@(x)1/(1+x)

Related Questions:

1. Write a program to implement Simpson's 1/3 rule.
2. Write a program to implement Boole's and Weddle's Rule.

MATLAB Program No: 07

Program Name: An M-File to implement the Trapezoidal Rule for unequally spaced data.

Problem: Use the information in the following Table to integrate the function $f(x) = 0.2 + 25x - 200x^2 + 675x^3 - 900x^4 + 400x^5$.

x	00	0.12	0.22	0.32	0.36	0.40
f(x)	0.200000	1.309729	1.305241	1.743393	2.074903	2.456000

x	0.44	0.54	0.64	0.70	0.80
f(x)	2.842985	3.507297	3.181929	2.363000	0.232000

Main File:

```
function I = trapuneq(x,y)
% trapuneq: unequal spaced trapezoidal rule quadrature
% I = trapuneq(x,y):
% Applies the trapezoidal rule to determine the integral
% for n data points (x, y) where x and y must be of the
% same length and x must be monotonically ascending
% input:
% x = vector of independent variables
% y = vector of dependent variables
% output:
% I = integral estimate
if nargin<2,error('at least 2 input arguments required'),end if
any(diff(x)<0),error('x not monotonically ascending'),end n = length(x);

if length(y)~=n,error('x and y must be same length'); end s = 0;

for k = 1:n-1
s = s + (x(k+1)-x(k))*(y(k)+y(k+1))/2; end

I = s;
```

Input File:

```
x = [0 .12 .22 .32 .36 .4 .44 .54 .64 .7 .8];
y = 0.2+25*x-200*x.^2+675*x.^3-900*x.^4+400*x.^5; trapz(x,y)
```

OUTPUT

On Command Window

```
Command Window
>> Untitled

ans =

    1.5948
```

On Workspace

Workspace	
Name ▲	Value
ans	1.5948
x	1x11 double
y	1x11 double

Related Questions:

1. Compare the above program with previous program (Matlab Program No:06)
2. Is it possible to implement Trapezoidal rule for equally spaced data by the above program?

MATLAB Program No: 08

Program Name: An M-File to implement the Gauss Elimination method.

Problem: Solve the following system of equations by Gauss Elimination method.

$$2x_1 + 3x_2 - x_3 + 2x_4 = 7$$

$$x_1 + x_2 + x_3 + x_4 = 2$$

$$x_1 + x_2 + 3x_3 - 2x_4 = -6$$

$$x_1 + 2x_2 + x_3 - x_4 = -2$$

Main File:

```
function x = GaussNaive(A,b)
% GaussNaive: naive Gauss elimination
% x = GaussNaive(A,b): Gauss elimination without pivoting.
% input:
% A = coefficient matrix
% b = right hand side vector
% output:
% x = solution vector
[m,n] = size(A);
if m~=n, error('Matrix A must be square'); end
nb = n+1;
Aug = [A b];
% forward elimination for
k = 1:n-1
for i = k+1:n
factor = Aug(i,k)/Aug(k,k);
Aug(i,k:nb) = Aug(i,k:nb)-factor*Aug(k,k:nb); end
end
% back substitution
x = zeros(n,1);
x(n) = Aug(n,nb)/Aug(n,n);
for i = n-1:-1:1
x(i) = (Aug(i,nb)-Aug(i,i+1:n)*x(i+1:n))/Aug(i,i); end
```

Input File:

```
A=[2 3 -1 2
    1 1 1 1
    1 1 3 -2
    1 2 1 -1];
b=[ 7 2 -6 -2]';
GaussNaive(A,b)
```


OUTPUT

On Command Window

```
Command Window
ans =
     1
     0
    -1
     2
fx >> |
```

On Workspace

Workspace	
Name ▼	Value
b	[7;2;-6;-2]
ans	[1;0;-1;2]
A	4x4 double

Related Questions:

1. Write a program to implement Gauss-Jordan Method.
2. Write a program to implement LU Decomposition Method.

MATLAB Program No: 09

Program Name: An M-File to implement the GaussSeidel iterative method.

Problem: Solve the following system of equations

$$\begin{aligned}10x+2y+z &= 9 \\ 2x+20y-2z &= -44 \\ -2x+3y+10z &= 22\end{aligned}$$

By GaussSeidel iterative method.

Main File:

```
function x = GaussSeidel(A,b,es,maxit)
% GaussSeidel: Gauss Seidel method
% x = GaussSeidel(A,b): Gauss Seidel without relaxation
% input:
% A = coefficient matrix
% b = right hand side vector
% es = stop criterion (default = 0.00001%)
% maxit = max iterations (default = 50)
% output:
% x = solution vector
if nargin<2,error('at least 2 input arguments required'),end if
nargin<4|isempty(maxit),maxit=50;end if
nargin<3|isempty(es),es=0.00001;end
[m,n] = size(A);
if m~=n, error('Matrix A must be square'); end C = A;

for i = 1:n
C(i,i) = 0;
x(i) = 0;
end
x = x';
for i = 1:n
C(i,1:n) = C(i,1:n)/A(i,i);
end
for i = 1:n
d(i) = b(i)/A(i,i);
end
iter = 0;
while (1)
xold = x;
for i = 1:n
x(i) = d(i)-C(i,:)*x;
if x(i) ~= 0
ea(i) = abs((x(i) - xold(i))/x(i)) * 100;
end
end
iter = iter+1;
if max(ea)<=es | iter >= maxit, break, end end
```

Input File:

```
A=[10 2 1  
    2 20-2  
    -2 3 10];  
b=[9 -44 22]';  
GaussSeidel(A,b)
```

OUTPUT

On Command Window

```
Command Window  
>> rungaussseidel  
  
ans =  
  
    1.0000  
   -2.0000  
    3.0000
```

On Workspace

Workspace	
Name	Value
b	[9;-44;22]
ans	[1.0000;-2.0000;3.0000]
A	[10,2,1;2,20,-2;-2,3,10]

Related Questions:

1. Write a program to implement Jacobi's Method.
2. Solve the following system of equations

$$\begin{aligned}x_1 + 2x_2 &= 9 \\ 2x_1 + 2x_3 &= -44 \\ -3x_2 + 10x_3 &= 22\end{aligned}$$

By GaussSeidel iterative method.