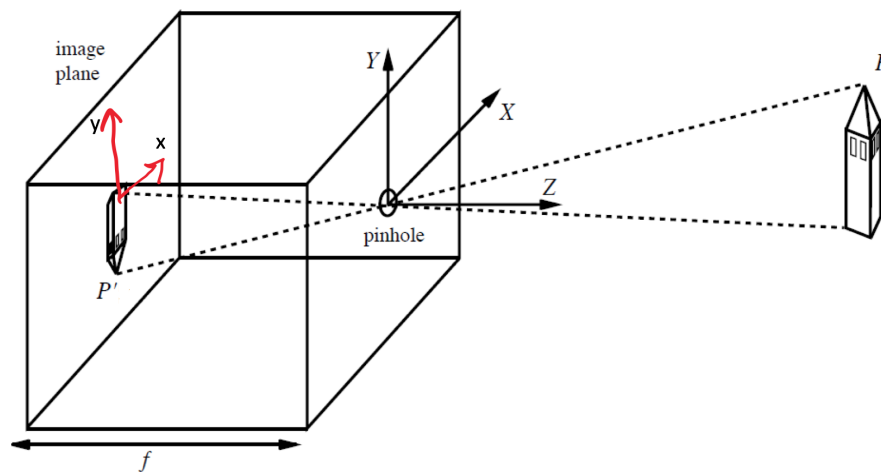


GEOMETRIC IMAGE FORMATION 2

CSE 152: INTRO TO COMPUTER VISION

April 08, 2019

1 Perspective Projection



1. Let $\mathbf{P} = (X, Y, Z)$ be a point in the camera frame shown above, and let $\mathbf{P}' = (x, y)$ be its perspective projection in the real image plane. Using similar triangles, derive the associated perspective projection equation(s), i.e. the equation(s) for \mathbf{P}' in terms of \mathbf{P} .

2. If the Z -axis were pointing in the opposite direction, what would the perspective projection equations become? (Assume that the X - and Y -axes remain unchanged.)
3. If we place a virtual image plane in front of the camera (i.e. in the world) at a distance f' along the Z -axis, what are the projection equations for a point $\mathbf{Q}' = (x_v, y_v)$ on that virtual plane? Use the original coordinate system (the one depicted in the diagram).

2 Vanishing Points

1. We can express a line in 3D as

$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \begin{bmatrix} O_x \\ O_y \\ O_z \end{bmatrix} + \lambda \begin{bmatrix} D_x \\ D_y \\ D_z \end{bmatrix}$$

where O is a point on the line and D is the direction of the line.

As we've learned, perspective projection can take 3D points at infinity (which are at the "ends" of 3D lines) to finite 2D **vanishing points**. What is the vanishing point (x, y) associated with the form of the line given above? *Hint: compute the perspective projection of the line and take the limit as λ goes to infinity.*

2. Based on your answer to the previous question, how can you tell if two lines have the same vanishing point if you are only given the O and D vectors for each line?