

## Command *fsolve* in Matlab and Octave

*fsolve* solves a system of non-linear equations:

$$\mathbf{F}(\mathbf{x}) = \mathbf{0}$$

⇒ vector  $\mathbf{F}(\mathbf{x})$  of non-linear equations

⇒ vector  $\mathbf{x}$  of arguments

e. g.: 2a) vector of 2 functions  $\mathbf{F}(\mathbf{x})$  and 2 variables  $\mathbf{x}=[x, y]$

2b) vector of 3 functions  $\mathbf{F}(\mathbf{x})$  and 3 variables  $\mathbf{x}=[x_1, x_2, x_3]$

**! number of equations = number of variables**

### How the command works

*fsolve* is an iterative method and solves for roots of functions, starting at a given initial point  $\mathbf{x}_0$ : solves for  $\mathbf{x}$  that fulfills  $\mathbf{F}(\mathbf{x}) = \mathbf{0}$  in several iteration steps

It could be that the (existing) solution is not found: change starting values

Syntax of *fsolve*:

$\mathbf{x} = \text{fsolve}(\text{fcn}, \mathbf{x}_0)$

$\mathbf{x} = \text{fsolve}(\text{fcn}, \mathbf{x}_0, \text{options})$

$[\mathbf{x}, \text{fval}] = \text{fsolve}(\text{fcn}, \mathbf{x}_0)$

...

Elements of *fsolve*:

output      input (must be supplied)

$[x, fval] = \text{fsolve}(\text{fcn}, x_0, \text{options})$

**x**: vector with solution

**fval**: vector with function values at solution

⇒ fcn evaluated at x

⇒  $fval = \text{fcn}(x)$

**fsolve**: command for solving system of non-linear equations

**fcn**: vector with functions to solve

**x0**: vector of initial guess/ starting values for the arguments, used for iterating for the solution

**options**: to set optionally (more information follows)

e. g.: 2b)  $[x, fx] = \text{fsolve}(@(\text{x}) \text{nonlinequB}(\text{x}), \text{x}_0)$

varying elements we want to solve for       $x_0 = [1, 1, 1]$

Command *options*:

define options before command `fsolve`

`options = optimset( )`

different parameters possible, e. g.:

`display`: default = off

choose iter, e. g.:

displays intermediate results for each loop iteration

`MaxFunEvals`: maximal number of function evaluations

`MaxIter`: maximal number of algorithm iterations

in `Example_4_5.m`, e. g.:

`options = optimset('MaxIter', 10000, 'MaxFunEvals', 90000);`

(9 functions for 9 variables)

positive integer

`TolFun`: termination criterion for function output

Difference between calculated function in iteration  $n+1$  and  
calculated function in iteration  $n < \text{TolFun}$

⇒ stop optimization

`TolX`: termination criterion for function input

Difference between  $x$  in iteration  $n+1$  and  
 $x$  in iteration  $n < \text{TolX}$

⇒ stop optimization

positive scalar

... (see links on problem set)