

# Rotational dynamics of proteins from spin relaxation times and molecular dynamics simulations

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Conformational fluctuations and rotational tumbling of proteins can be experimentally accessed with nuclear spin relaxation experiments. Interpretation of molecular dynamics from the experimental data is, however, often complicated, especially for molecules with anisotropic shape. Here we apply classical molecular dynamics simulations to interpret conformational fluctuations and rotational tumbling of proteins with arbitrarily anisotropic shape. The direct calculation of spin relaxation times from simulation data did not reproduce the experimental data. This was successfully corrected by scaling the overall rotational diffusion constants around protein inertia axes with a constant factor. The achieved good agreement with experiments allowed the interpretation of internal and overall dynamics of proteins with significantly anisotropic shape. The overall rotational diffusion was found to be brownian, having only a short subdiffusive region below 0.12 ns. The presented methodology can be applied to interpret rotational dynamics and conformation fluctuations of proteins with arbitrary anisotropic shape. However, for intrinsically disordered proteins a water model with more realistic dynamical properties is probably required.

## I. INTRODUCTION

Conformational fluctuations and the entropy of proteins play a significant role in their functionality and interactions with other biomolecules. Conformational fluctuations and the overall brownian tumbling of proteins are experimentally accessible through the spin relaxation times of  $^{15}\text{N}$  and  $^{13}\text{C}$  nuclei measured with nuclear magnetic resonance (NMR) techniques [1–7]. The spin relaxation rates have been used to, for example, analyze conformational entropies [1, 8–10], binding entropies [1, 11], resolve sampled structures [3–5, 12] and validate molecular dynamics simulations [13–17]. These analyses are almost exclusively based on the separation of the internal conformational fluctuations and the overall rotational tumbling [18, 19]. Also the isotropic overall diffusion is often assumed, while analysis of anisotropic molecules is significantly more complicated [1, 2, 20–23]. Thus, the new approaches are needed to interpret spin relaxation times measured from anisotropic or intrinsically disordered molecules.

Classical molecular dynamics simulation methods are promising tools to interpret spin relaxation experiments for molecules with significantly anisotropic shape or correlations between internal and overall rotational motions. Practical applications are, however, limited by inaccuracies in the force field descriptions and the available time scales in the simulations [16, 17, 24–26]. The main issues have been the overestimated overall rotational diffusion of proteins due to inaccuracies in water models [25] and insufficient accuracy of correlation functions calculated from single molecules in MD simulations [26, 27].

In this work we overcome these issues by assuming that the overall rotational dynamics of protein follows anisotropic

rigid body diffusion. Diffusion coefficients around inertia axes are directly calculated from angular displacements. The diffusion coefficients are then used to determine the contribution of the overall rotational tumbling to the rotational correlation functions of N-H bonds. This reduces the required simulation length for the accurate determination of rotational correlation functions. Furthermore, the overestimated overall brownian tumbling rates due to the inaccurate water model can be corrected during the correlation function calculation by scaling the diffusion coefficients in all directions with a constant factor. The corrected correlation functions can be used to interpret the spin relaxation experiments for proteins with arbitrarily anisotropic shapes.

The developed approach is demonstrated by interpreting the experimental spin relaxation data for C-terminal domains of TonB proteins from *H. pylori* (HpTonB) [28] and from *Pseudomonas aeruginosa* (PaTonB). Both proteins have significantly anisotropic shape, which would significantly complicate the standard spin relaxation data analysis [1, 2, 20–23].

## II. METHODS

### A. Spin relaxation experiments and rotational dynamics of molecules

Molecular dynamics of the protein backbone residues and spin relaxation experiments can be connected by using the spectral density  $J(\omega)$

$$J(\omega) = 2 \int_0^\infty C(t) \cos(\omega t) dt, \quad (1)$$

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which is the Fourier transformation of the second order rotational correlation function for N-H bond vector

$$C(t) = \left\langle \frac{3}{2} \cos^2 \theta_{t'+t} - \frac{1}{2} \right\rangle_{t'}, \quad (2)$$

where  $\theta_{t'+t}$  is the N-H bond angle between times  $t'$  and  $t' + t$  and angular brackets refer to the ensemble average. Connection to the experimentally measured spin relaxation times  $T_1$ ,  $T_2$  and  $T_{\text{NOE}}$  is given by the Redfield equations [29, 30]

$$\frac{1}{T_1} = \frac{d_{\text{NH}}^2 N_{\text{H}}}{20} \left[ J(\omega_{\text{H}} - \omega_{\text{N}}) + 3J(\omega_{\text{N}}) + 6J(\omega_{\text{N}} + \omega_{\text{H}}) \right] + \frac{(\sigma\omega_{\text{N}})^2}{15} J(\omega_{\text{N}}), \quad (3)$$

$$\frac{1}{T_2} = \frac{1}{2} \frac{d_{\text{NH}}^2 N_{\text{H}}}{20} \left[ 4J(0) + 3J(\omega_{\text{N}}) + J(\omega_{\text{H}} - \omega_{\text{N}}) + 6J(\omega_{\text{H}}) + 6J(\omega_{\text{N}} + \omega_{\text{H}}) \right] + \frac{(\sigma\omega_{\text{N}})^2}{90} [4J(0) + 3J(\omega_{\text{N}})], \quad (4)$$

$$\frac{1}{T_{\text{NOE}}} = 1 + \frac{d_{\text{NH}}^2 N_{\text{H}}}{20} \left[ 6J(\omega_{\text{N}} + \omega_{\text{H}}) + J(\omega_{\text{H}} - \omega_{\text{N}}) \right] \frac{\gamma_{\text{H}} T_1}{\gamma_{\text{N}}}, \quad (5)$$

where  $\omega_{\text{N}}$  and  $\omega_{\text{H}}$  are the Larmor angular frequencies of  $^{15}\text{N}$  and  $^1\text{H}$  respectively, and the number of bound protons  $N_{\text{H}} = 1$  for N-H bonds. The dipolar coupling constant is given by

$$d_{\text{NH}} = -\frac{\mu_0 \hbar \gamma_{\text{H}} \gamma_{\text{N}}}{4\pi \langle r_{\text{CN}}^3 \rangle},$$

where  $\mu_0$  is the magnetic constant or vacuum permeability,  $\hbar$  is the reduced Planck constant,  $\gamma_{\text{N}}$  and  $\gamma_{\text{H}}$  are the gyromagnetic constants of  $^{15}\text{N}$  and  $^1\text{H}$ , respectively. The average cubic length is calculated as  $\langle r_{\text{CN}}^3 \rangle = (0.101\text{nm})^3$  and the value of  $\Delta\sigma = -160$  ppm is used for the chemical shift anisotropy of N-H bonds in proteins [30, 31].

Spin relaxation experiments are typically interpreted for proteins by assuming that the motions related to the overall brownian tumbling and conformational fluctuations are independent. The rotational correlation function for chemical bonds can be then written as [1, 2, 18, 19, 32]

$$C(t) = C_I(t)C_O(t), \quad (6)$$

where  $C_I(t)$  and  $C_O(t)$  are correlation functions for internal and overall rotations, respectively. Conformational fluctuations can be described in this approximation by using the square of the order parameter respect to molecular axes  $S^2$ ,

which is given by the plateau of the internal rotational correlation function. Timescales for the fluctuations can be characterized by using the effective correlation time

$$\tau_{\text{eff}} = \int_0^\infty C_I'(t) dt, \quad (7)$$

where  $C_I'(t) = \frac{C_I - S^2}{1 - S^2}$  is the reduced correlation function [19].

The overall rotational correlation function is often described by approximating the protein as a rigid body. For arbitrarily anisotropic molecules, the correlation functions can be presented as a sum of five exponentials [2, 20]

$$C_O(t) = \sum_{j=1}^5 A_j e^{-t/\tau_j}, \quad (8)$$

where the time constants  $\tau_j$  are related to the diffusion constants around three principal axes of a molecule ( $D_{xx}$ ,  $D_{yy}$  and  $D_{zz}$ ) [33] and the prefactors  $A_j$  depend on the directions of chemical bonds respect to the molecular axes [20, 22].

The simplest approach to extract molecular dynamics from experimental data is the original "model free analysis" [19], where an isotropic diffusion is assumed for the overall rotation of the protein. This reduces Eq. 8 to a monoexponential form and the overall rotational dynamics can be described with a single time constant  $\tau_c$ . Also the internal correlation functions for each residue are assumed to decay exponentially with a single time constant  $\tau_{\text{eff}}$  toward to the square of the order parameter  $S^2$ . The three parameters ( $\tau_c$ ,  $\tau_{\text{eff}}$  and  $S^2$ ) can be successfully resolved from a fit to the experimental data. However, the amount of parameters to be fitted increases if the protein experiences an anisotropic overall diffusion or has several timescales for internal motions, in which case the fitting often becomes ambiguous [1, 22, 34]. The anisotropic rotational diffusion is sometimes described with hydrodynamical calculations, but they are quite sensitive for the assumptions about the hydration shell of the protein [35].

Rough estimate for the timescale of overall rotational dynamics is often given by using the  $T_1/T_2$  ratio [30]. This is based on the assumptions that  $T_1$  and  $T_2$  are essentially independent of internal motions and that the overall dynamics is isotropic. The spectral density then reduces to

$$J'(\omega) = S^2 \frac{\tau_c'}{1 + (\omega\tau_c')^2} \quad (9)$$

and the correlation time describing the overall rotational motion,  $\tau_c'$ , can be then estimated by numerically minimizing the equation

$$\frac{T_1}{T_2} \approx \frac{\frac{1}{2} \frac{d_{\text{NH}}^2 N_{\text{H}}}{20} \left[ 4J'(0) + 3J'(\omega_{\text{N}}) + J'(\omega_{\text{H}} - \omega_{\text{N}}) + 6J'(\omega_{\text{H}}) + 6J'(\omega_{\text{N}} + \omega_{\text{H}}) \right] + \frac{(\sigma\omega_{\text{N}})^2}{90} [4J'(0) + 3J'(\omega_{\text{N}})]}{\frac{d_{\text{NH}}^2 N_{\text{H}}}{20} \left[ J'(\omega_{\text{H}} - \omega_{\text{N}}) + 3J'(\omega_{\text{N}}) + 6J'(\omega_{\text{N}} + \omega_{\text{H}}) \right] + \frac{(\sigma\omega_{\text{N}})^2}{15} J'(\omega_{\text{N}})} \quad (10)$$

with respect to the experimentally measured  $T_1/T_2$  ratio.

## B. Rotational dynamics from molecular dynamics simulations

A classical molecular dynamics simulation gives a trajectory for each atom in the system as a function of time. Rotational correlation functions for each bond can be then directly calculated from the trajectories by using Eq. 2 and used to calculate the spin relaxation times through Eqs. 1-5. The resulting values can be compared to experimental data in order to assess simulation model quality [13–17, 36] or interpret experiments [36].

The direct comparison with experiments is, however, often complicated by insufficient statistics for the calculated correlation functions and the overestimated rotational diffusion due to inaccuracies in water models [25, 26]. Here we show that the statistical accuracy of the contribution of the overall tumbling to the correlation functions,  $C_0(t)$  in Eq. 6, can be increased for rigid proteins by directly calculating the diffusion coefficients for inertia axes. The rotational diffusion coefficients can be related to timescales in the correlation function for anisotropic rigid body rotation in Eq. 8 [20, 33].

The rotational diffusion coefficients are calculated by fitting a linear slope to the square angle deviation of inertia axes (see below). This requires less simulation data for the good statistics than a direct fit of multiexponential sum in Eq. 8 to the rotational correlation function calculated from MD simulation. In addition, the overestimated rotational diffusion due to water model [25] can be corrected by scaling the diffusion coefficients around all inertia axes by a constant factor. This approach takes into account the anisotropic shape of the molecule. This is a significant advancement to the studies, which assume isotropic rotational diffusion with a single exponential rotational correlation function [10, 14–16, 37] or use order parameters to compare simulations with experimental data [13, 16, 17, 37].

The practical analysis can be divided into seven steps:

- 1) The total rotational correlation functions  $C(t)$  for the protein N-H bond vectors are directly calculated from MD simulation trajectory by applying Eq. 2.
- 2) The rotational correlation functions for internal dynamics  $C_I(t)$  are calculated from MD simulation trajectory by removing overall rotation of the protein.
- 3) The overall and internal motions are assumed to be independent and the overall rotational correlation function is calculated from Eq. 6 as  $C_O(t) = C(t)/C_I(t)$ .
- 4) The mean square angle deviations of rotation around protein inertia axes are calculated from MD simulation trajectory.
- 5) Rotational diffusion constants  $D_x$ ,  $D_y$  and  $D_z$  are calculated by fitting a straight line to the mean square angle deviations

$$\begin{aligned}\langle \Delta \alpha_{t'+t}^2 \rangle_{t'} &= 2D_x t \\ \langle \Delta \beta_{t'+t}^2 \rangle_{t'} &= 2D_y t \\ \langle \Delta \gamma_{t'+t}^2 \rangle_{t'} &= 2D_z t,\end{aligned}\quad (11)$$

where  $\langle \Delta \alpha_{t'+t}^2 \rangle_{t'}$ ,  $\langle \Delta \beta_{t'+t}^2 \rangle_{t'}$  and  $\langle \Delta \gamma_{t'+t}^2 \rangle_{t'}$  are the mean square angle deviations from the shortest protein inertia axis to the longest, respectively.

6) Contribution of the overall rotational tumbling to all correlation functions is assumed to follow Eq. 8 with timescales  $\tau_j$  calculated from the rotational diffusion constants [33]. Weighting factors  $A_j$  are determined by fitting the equation with new timescales to the overall rotational correlation functions calculated from MD simulations in step 3.

7) The new correlation functions are calculated by substituting internal correlation functions,  $C_I(t)$ , from step 2 and anisotropic rigid body rotational correlation functions,  $C_O(t)$ , from step 6 to Eq. 6 giving

$$C_N(t) = C_I(t) \sum_{j=1}^5 A_j e^{-t/\tau_j}. \quad (12)$$

These correlation functions are then used to calculate spin relaxation times from Eqs. 1-5. The incorrect overall rotational diffusion due to water model can be corrected at this point by scaling the rotational diffusion coefficients, i.e. timescales  $\tau_j$ , with a constant factor before calculating new correlation functions from Eq. 12.

## C. Simulation and analysis details

All simulations were ran using Gromacs 5 [38] and Amber ff99SB-ILDN [39] force field for proteins. The proteins were solvated to tip3p[40], tip4p [40] or OPC4 [41] water models. Initial structures were taken from NMR structures of *HpTonB* [28] and *PaTonB* [? ]. Temperature was coupled to the desired value with v-rescale thermostat [42] and pressure was isotropically set to 1 bar using Parrinello-Rahman barostat [43]. Timestep was 2 fs, Lennart-Jones interactions were cut-off at 1.0 nm, PME [44, 45] was used for electrostatics and LINCS was used to constraint all bond lengths [46]. Simulation trajectory and related files are available at [? ]. The simulated systems are listed in Table I

Rotational correlation functions are calculated with *gmx rotacf* from Gromacs package [47]. The overall rotation was removed for  $C_I(t)$  calculation by using a fit option of the *gmx trjconv* tool in Gromacs package [47]. The order parameters  $S^2$  were determined by averaging rotational correlation functions from oriented trajectory,  $C_I(t)$ , over lag times above 50 ns. Effective correlation times were then calculated by using Eq. 7. Inertia axes of proteins were calculated with *compute\_inertia\_tensor* function from MDTraj python library [48].

Spectral density was calculated by fitting a sum of 471 exponentials with timescales from 1 ps to 50 ns with logarithmic spacing

$$C_N(t) = \sum_{i=1}^N \alpha_i e^{-t/\tau_i} \quad (13)$$

to the new correlation function from Eq. 12 by using the

TABLE I. Simulated systems and rotational diffusion coefficients ( $\text{rad}^2 \cdot 10^7/\text{s}$ ) calculated from simulations.

Protein	Water model	T (K) <sup>a</sup>	$t_{\text{sim}}$ (ns) <sup>b</sup>	$t_{\text{anal}}$ (ns) <sup>c</sup>	$D_{xx}$	$D_{yy}$	$D_{zz}$	$D_{  }/D_{\perp}$ <sup>d</sup>	$D_{\text{av}}$ <sup>e</sup>	files
<i>Pa</i> TonB	tip4p	298	400	390	$1.81 \pm 0.01$	$2.06 \pm 0.03$	$4.55 \pm 0.03$	$2.35 \pm 0.04$	$2.80 \pm 0.02$	[? ]
<i>Pa</i> TonB	tip4p	310	400	390	$2.60 \pm 0.02$	$2.22 \pm 0.05$	$5.0 \pm 0.1$	$2.07 \pm 0.09$	$3.26 \pm 0.07$	[? ]
<i>Pa</i> TonB	OPC4	310	1200	1190	$2.01 \pm 0.01$	$2.19 \pm 0.01$	$5.01 \pm 0.03$	$2.39 \pm 0.02$	$3.07 \pm 0.01$	[? ]
<i>Hp</i> TonB	tip3p	310	570	370	$8.25 \pm 0.05$	$7.67 \pm 0.06$	$15.9 \pm 0.3$	$1.99 \pm 0.06$	$10.6 \pm 0.2$	[? ]
<i>Hp</i> TonB	tip3p	303	800	790	$6.24 \pm 0.02$	$7.04 \pm 0.03$	$11.9 \pm 0.2$	$1.80 \pm 0.03$	$8.40 \pm 0.07$	[? ]
<i>Hp</i> TonB	tip4p	310	470	370	$3.6 \pm 0.1$	$3.24 \pm 0.01$	$6.3 \pm 0.3$	$1.8 \pm 0.1$	$4.4 \pm 0.2$	[? ]
<i>Hp</i> TonB	tip4p	303	400	200	$2.7 \pm 0.1$	$2.71 \pm 0.02$	$5.6 \pm 0.5$	$2.1 \pm 0.2$	$3.7 \pm 0.2$	[? ]
<i>Hp</i> TonB	OPC4	310	800	790	$2.85 \pm 0.01$	$2.70 \pm 0.01$	$5.56 \pm 0.01$	$2.00 \pm 0.01$	$3.70 \pm 0.01$	[? ]

<sup>a</sup> Simulation temperature<sup>b</sup> Total simulation time<sup>c</sup> Analyzed simulation time<sup>d</sup>  $D_{||} = D_{zz}$ ,  $D_{\perp} = \frac{1}{2}(D_{xx} + D_{yy})$ <sup>e</sup>  $D_{\text{av}} = \frac{1}{3}(D_{xx} + D_{yy} + D_{zz})$ 

*lsqnonneg* routine in MATLAB [49]. The Fourier transform was then calculated by using analytical function for the sum of exponentials

$$J(\omega) = 4 \sum_{i=1}^N \alpha_i \frac{\tau_i}{1 + \omega^2 \tau_i^2}. \quad (14)$$

A similar approach has been previously used for the lamellar lipid and surfactant systems in combination with solid state NMR experiments [50, 51].

#### D. Spin relaxation experiments

TO BE WRITTEN BY HARRI, UNLESS WE WAIT THAT *Pa*TonB and *Hp*TonB PUBLICATIONS ARE READY.

### III. RESULTS

#### A. Global rotational dynamics of protein

The mean square angle deviations for the rotation of *Pa*TonB protein construct around inertia axes in the simulation with OPC4 water model are shown in Fig. 1. This is the longest simulation data set in this work ( $1.2\mu\text{s}$ ) and the linear behaviour of the mean square angle deviations are observed for the lag times up to one hundredth of the total simulation length (12 ns), which is expected to be the maximum lag time for the good statistics for rotational dynamics analyzed from a single molecule in MD simulations [27]. Deviations from the linear behaviour are only seen with the lag times longer than this limit, as also demonstrated for shorter simulations in Figs. 8 and 9 with tip4p water at two different temperatures. The plots with log-log scale in Figs. 1, 8 and 9 B) reveals a weakly subdiffusive region only below very short timescales of approximately 0.12 ns. Thus, we conclude that the protein experiences the brownian rotational tumbling with a good approximation. Diffusion coefficients can be then calculated

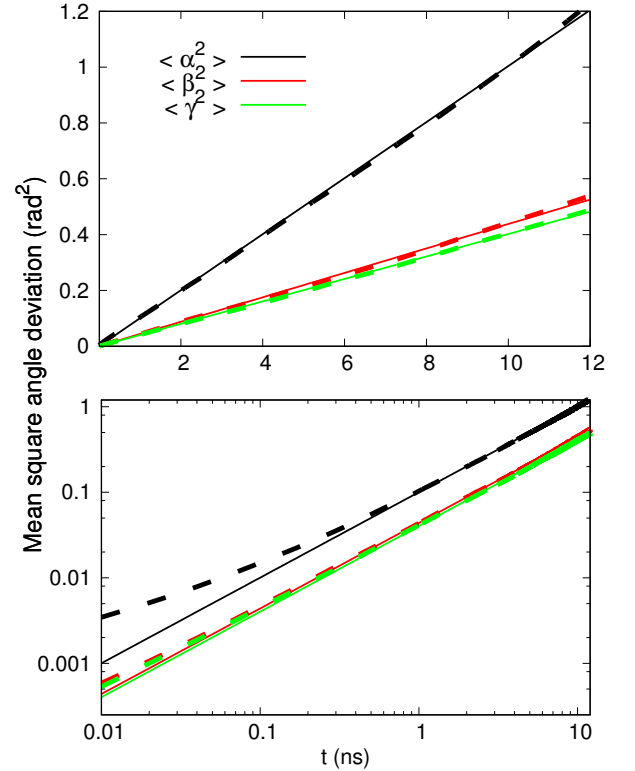


FIG. 1. Mean square angle deviations of inertia tensor axes calculated from *Pa*TonB simulation with OPC water model. The data shown with linear (top) and logarithmic scale (bottom).

from the slope of the mean square angle deviations according to Eq. 11 by using lag times less than one hundredth of the total MD simulation length. The error bars were calculated varying the lag time with 1 ns to both directions. The data from *Hp*TonB protein (not shown) led to similar conclusions.

The resulting rotational diffusion constants from different simulations are shown in Table I. As expected, the rotational diffusion coefficients increase with temperature and decrease

ing size of a protein. The values are, however, larger than would be expected from the experimental  $T_2/T_1$  ratio analysed with Eq. 10 and from the previously reported values for proteins with similar sizes [52], especially when tip3p water model is used. Similar results were previously explained by the overestimated water self-diffusion of tip3p water model [25].

The analysis leading to the new correlation functions in Eq. 12 (see section II B) is exemplified in Fig. 2 for three residues locating in different domains of *PaTonB* protein with different characteristic rotational dynamics. The flexible C-terminus is represented by the residue 341, more rigid  $\beta$ -sheet by the residue 331 and a flexible loop between two sheets by the residue 322. The total correlation functions  $C(t)$  of all the residues in Fig. 2 (top, solid lines) decay toward zero within  $\sim 10$ -50 ns. The internal correlation functions  $C_I(t)$  in Fig. 2 (middle) decay to a plateau value, which defines the square of the order parameter  $S^2$ . As expected, the internal correlation function for the residue 331 in the rigid  $\beta$ -sheet rapidly decays to the largest order parameter value, while the correlation functions of the residues in the loop and C-terminus decay slower to the smaller order parameter values due to the larger conformational ensemble sampled by these regions.

The overall rotational correlation functions,  $C_O(t) = C(t)/C_I(t)$ , are shown in Fig. 2 (bottom, solid lines). Also the correlation functions of anisotropic rigid body rotation from Eq. 8 are shown in Fig. 2 (bottom, dashed lines). The timescales for the latter,  $\tau_i$ , are given by the rotational diffusion coefficients from the simulation and the relation in Ref. 33, and the prefactors,  $A_j$ , are determined by fitting Eq. 8 to the overall rotation correlation functions,  $C_O(t)$ , calculated the MD simulation. The new correlation functions, determined from Eq. 12 and shown in Fig. 2 (top, dashed lines), are indistinguishable from the correlation functions calculated from the original MD simulations with the lag times shorter than one hundredth of total simulation time (approximately 4-12 ns for the studied systems), which is the expected limit for the good statistics in single molecule MD simulations [27]. This suggests that the anisotropic rigid body diffusion model (Eq. 8) and the separation of internal and global motions (Eq. 6) are good approximations for the studied system. The analytical description of the overall rotation with Eq. 8 in the new correlation functions clearly reduces the statistical fluctuations with the long lag times in Fig. 2. The effect is most visible for the flexible C-terminus (residue 341) having the smallest, thus the least detectable, contribution from the overall rotation of the protein due to the small order parameters values.

## B. Global rotational dynamics in simulations and experiments

Spin relaxation times are compared between the experiments and simulations using two different water models in Fig. 3 for the *HpTonB* construct. Simulations with tip3p water model are significantly off from the experimental data and underestimate  $T_1/T_2$  ratio, suggesting too fast overall rota-

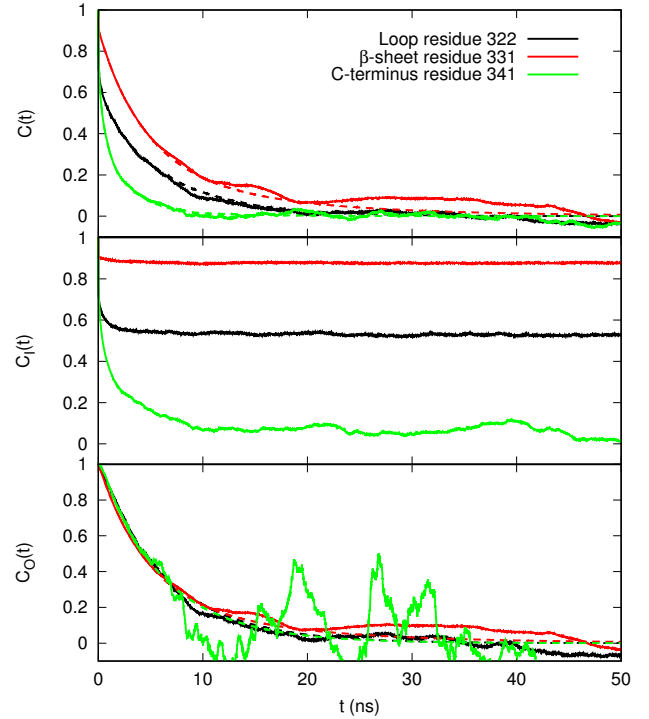


FIG. 2. Rotational correlation functions calculated from MD simulations of *PaTonB* with tip4p water model at 298K for residues at different regions. (top) total correlation functions  $C(t)$  calculated from MD simulation (solid lines) and new correlation functions determined from Eqs. 6 and 8 by using rotational diffusion constants and fitted prefactors (dashed lines), (middle) correlation functions for internal motions calculated from simulation with removed overall protein rotation (bottom) correlation function for overall motions determined as  $C_O(t) = C(t)/C_I(t)$  (solid lines) and by fitting to Eq. 8 with timescales from rotational diffusion coefficients in Table I (dashed lines).

tional diffusion dynamics [53]. This is in agreement with previous study, where overestimation of rotational diffusion was attributed to the overestimated self-diffusion of tip3p [25]. On the other hand, simulation results with tip4p water model show significantly better agreement with the experimental data in Fig. 3.

To see if the discrepancy in spin relaxation times for simulations with tip3p water model could be explained purely by the overestimated protein overall diffusion, we scaled the diffusion constants by a constant factor of 2.9 before applying Eq. 12 to calculate the new correlation functions. The spin relaxation times calculated from the new correlation functions with the scaled rotational diffusion constants are shown in Fig. 4 together with experimental values. Indeed, the reduction of overall diffusion constants with a scaling factor brings the spin relaxation times in good agreement with the experimental data.

Comparison of spin relaxation times between experiments and simulations of *PaTonB* with tip4p and OPC4 water models are shown in Fig. 5. The experimentation of the OPC4 water model was inspired by the recent study reporting sig-

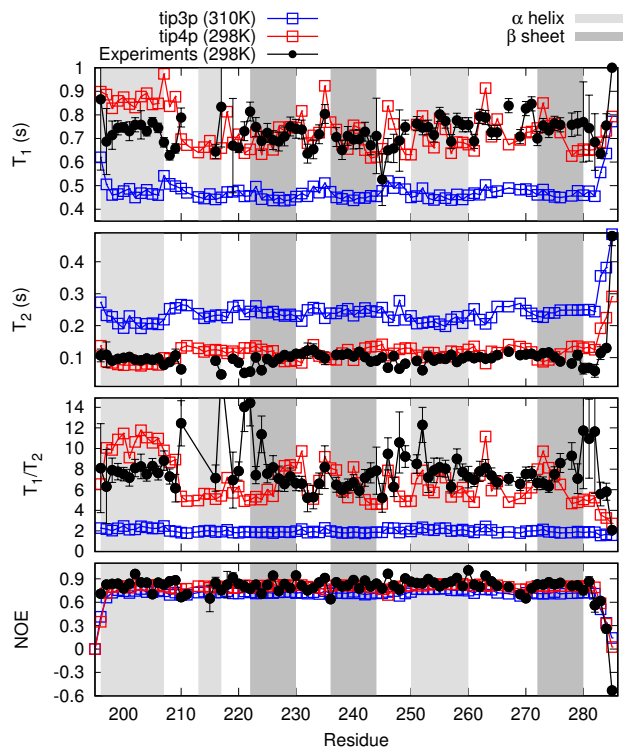


FIG. 3.  $^{15}\text{N}$  Spin relaxation times for *HpTonB* from experimental data (circles) and MD simulations with different water models (squares).

nificant improvements in lipid monolayer simulations when this water model was used [56]. Since tip3p water model was observed to lead the significant overestimation of rotational diffusion of a protein, it was not used in *PaTonB* simulations. Also the simulations of *PaTonB* with tip4p and OPC4 water models systemically underestimate  $T_1$  values and  $T_1/T_2$  ratio when compared with experiments. The discrepancy is, however, less severe than for *HpTonB* simulated with tip3p in Fig. 3, suggesting that also the required correction for the overall rotational diffusion should be smaller. Indeed, the spin relaxation times calculated from *PaTonB* simulation with tip4p water model were in good agreement with experiments in Fig. 6 after the diffusion coefficients were divided with a constant factor of 1.2, which is smaller than 2.9 used for *HpTonB* simulation above. Notably, the effect of temperature difference of 12 degrees on spin relaxation times is significantly smaller than the difference between simulations and experiments or the effect of the diffusion constant scaling.

The correction of the overall rotational diffusion coefficients with a constant factor led to a good agreement with experimental spin relaxation data for both studied proteins simulated with different water models, as seen in Figs. 4 and 6. The good agreement with experiments suggests that the scaled rotational diffusion coefficients from MD simulations can be considered as an interpretation of the anisotropic rotational motion in NMR experiments. The scaled rotational diffusion coefficients from simulations giving the best agreement with the

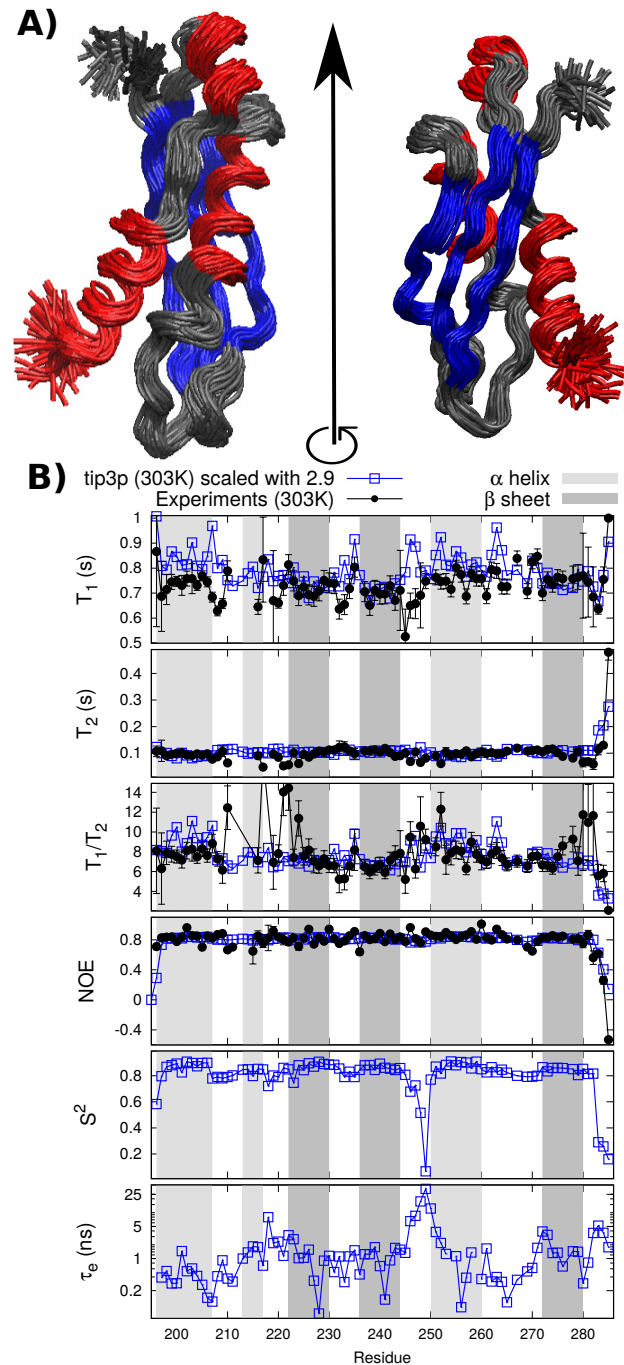


FIG. 4. A) Structures of *HpTonB* from the MD simulations with tip3p at 303 K (100 structures taken from 400ns long trajectory). Secondary structures are colour-labelled with Visual Molecular dynamics [54, 55];  $\alpha$ -helices are red and  $\beta$ -sheets are blue. B) Spin relaxation times from experiments (circles) and tip3p simulations (squares) with rotational diffusion coefficients divided by a constant factor of 2.9 at 303 K. Order parameters and effective internal correlation times calculated from simulations

experimental data are collected in Table II. In contrast to the unscaled diffusion constants in Table I, these results are in



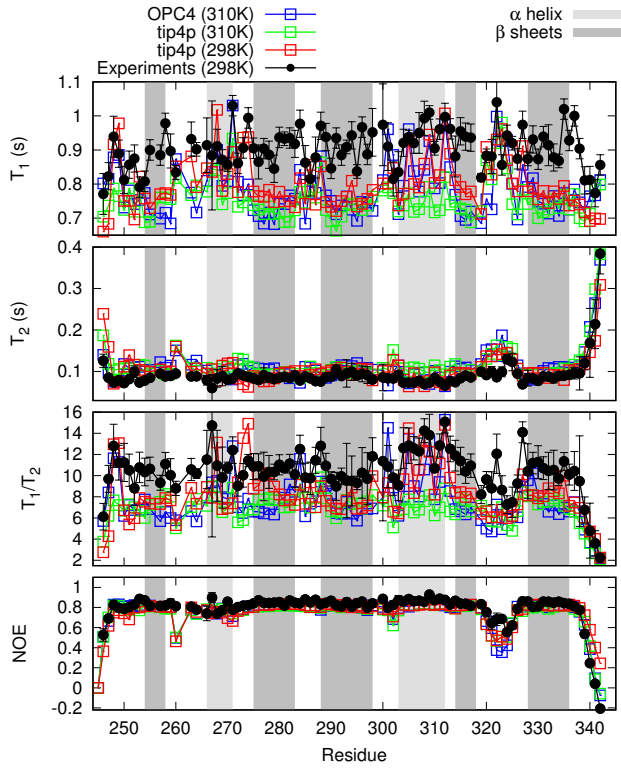


FIG. 5. Plots of experimental (circles) and simulated (squares) spin relaxation times for *PaTonB*.

line with previously reported values for proteins with similar sizes [52]. Also the timescales,  $\tau'_c$ , estimated from Eq. 10 are close to the average diffusion coefficient,  $\tau_c = (6D_{av})^{-1}$ , in Table I.

TABLE II. Rotational diffusion coefficients giving the best agreement with experimental spin relaxation data. For *HpTonB* construct the values calculated from simulation with tip3p were scaled with 2.9 (spin relaxation data in Fig. 4) and for *PaTonB* the values from tip4p simulation at 298K were scaled by 1.2 (spin relaxation data in Fig. 6).

	<i>HpTonB</i>	<i>PaTonB</i>
$D_{xx}$	$2.15 \pm 0.01$	$1.51 \pm 0.01$
$D_{yy}$	$2.43 \pm 0.01$	$1.72 \pm 0.03$
$D_{zz}$	$4.10 \pm 0.01$	$3.79 \pm 0.03$
$D_{av}$	$2.90 \pm 0.03$	$2.3 \pm 0.02$
$\tau_c(\text{ns})^a$	$5.7 \pm 0.1$	$7.2 \pm 0.1$
$\tau'_c(\text{ns})^b$	$5.8 \pm 0.1$	$6.9 \pm 0.1$

<sup>a</sup>  $(6D_{av})^{-1}$

<sup>b</sup> Average over all residues given by Eq. 10

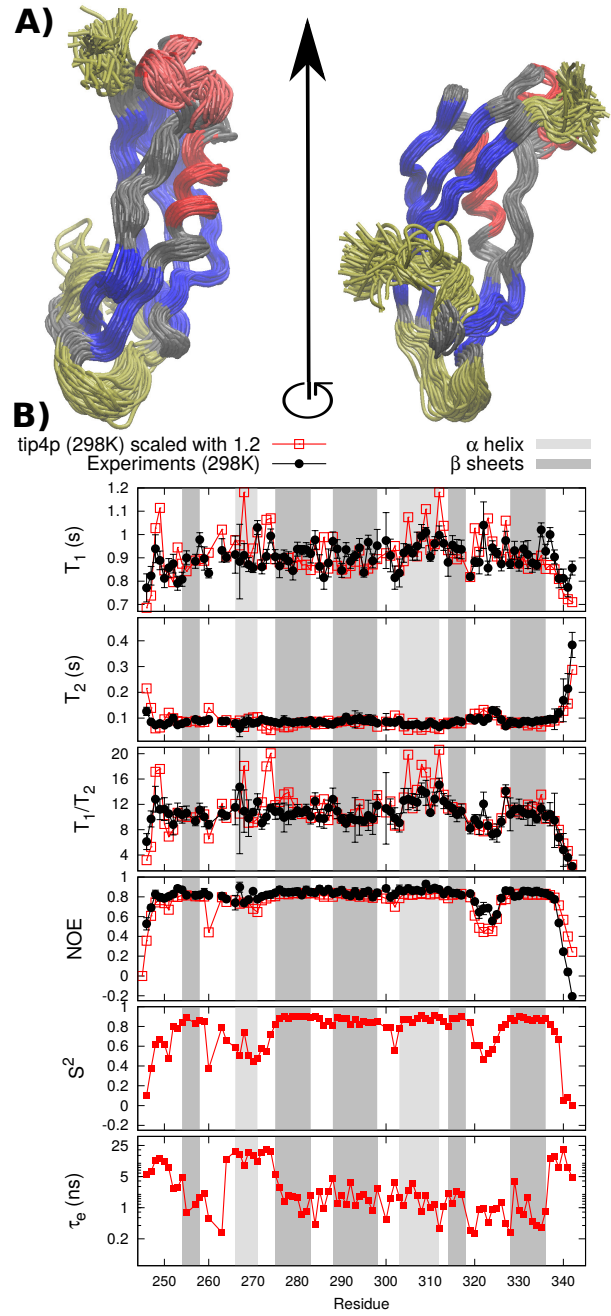


FIG. 6. A) Structures sampled by *PaTonB* from MD simulations with tip4p at 298 K (100 structures from 400ns long trajectory). Secondary structures are colour labelled with Visual Molecular dynamics [54, 55];  $\alpha$ -helices are red and  $\beta$ -sheets are blue. Residues 246-251, 320-326 and 338-342 with increased internal dynamics are yellow and  $\alpha$ -helix fluctuations between two orientations (residues 266-270) is pink in the left column. B) Spin relaxation times from experiments (circles) and tip4p simulations (squares) with rotational diffusion coefficients divided by a constant factor of 1.2 at 298 K. Order parameters and effective internal correlation times calculated from simulations.

### C. Interpretation of protein internal relaxation from MD simulations

Good agreement of spin relaxation times between simulations with scaled overall rotational diffusion constants and experiments in Figs. 4 and 6 suggest that the simulations can be used to interpret the internal dynamics of proteins observed in the experiments.

Only small variations between different residues are observed for spin relaxation times of *HpTonB* construct in Fig. 3. This indicates a rather rigid protein structure, which is also seen in MD simulation snapshots overlayed in Fig. 3 A). Only few residues in the terminal ends show slightly enhanced conformational fluctuations in MD simulations and in spin relaxation data. Deviations from average spin relaxation times are also observed in experiments close to residues 210-222, where also difficulties in peak assignment were observed [28]. Simulations of *HpTonB* construct do not explain this, however, similar region in *PaTonB* simulation shows fluctuations between two orientations of  $\alpha$ -helix (see discussion below). Residues 245-250 in *HpTonB* give exceptionally low order parameters and long effective correlation times in simulations and small  $T_1$  times in experiments. The interpretation of this is, however, not straightforward, because low  $T_1$  values in this region are not reproduced by MD simulations.

More variety in internal dynamics between residues is observed for *PaTonB* protein and segments with enhanced conformational fluctuations are labelled with yellow colour in Fig. 6. Larger number of sampled conformations in both terminal ends are characterized by low order parameters and long effective internal correlation times observed in simulations. Enhanced conformational fluctuations is also observed for residues between 320-326, which is a loop between two  $\beta$ -sheets. MD simulations predict low order parameters and long internal effective correlation times also for residues between 260-274. These can be explained by two different orientations sampled by the  $\alpha$ -helix in this region (colour labelled with pink in Fig. 6 A). The orientational fluctuations of the similar short helix could also explain lower spectral resolution and deviations in spin relaxation times observed for residues close to residue 210-222 in *HpTonB* [28].

MD simulations can be used to suggest how rotational dynamics of N-H bonds builds up from different components. Here we fit a sum of 471 different timescales to the correlation functions according to Eq. 13. Most prefactor values are zero in all correlation functions in this work, thus the remaining timescales with non-zero prefactors are considered as different components of the total relaxation process. The prefactors are shown in Fig. 7 for the same residues of *PaTonB*, which were used to exemplify correlation functions in Fig. 2. As expected for residue 322 in rigid  $\beta$ -sheet with large order parameter value, the rotational relaxation is dominated by timescales of  $\sim 5.5$  ns and  $\sim 8$  ns, matching with protein overall rotation. Also the dynamics of the selected residue 322 in flexible loop is dominated by timescales around  $\sim 8$  ns corresponding protein overall rotation, however, fast motions from internal dynamics are more significant than for the rigid  $\beta$ -sheet residue. This is in agreement with lower order parameter

value in the flexible loop residues. On the other hand, the rotational dynamics of the selected residue 341 in the flexible N-terminus is dominated by timescales below 3 ns, most likely related to the internal protein dynamics. The contribution from timescales close to  $\sim 13$  ns probably arises from slow conformational fluctuations of N-terminus, rather than overall rotational dynamics. This supports the conclusion that fluctuations of large amount of conformations leads to small order parameters and large effective correlation times observed in Fig. 5. While fractionalization of rotational dynamics to different components gives intuitively understandable results, it should be kept in mind that it is based on fitting of multiexponential sum to the simulation data and the solution of such fit is not unique.

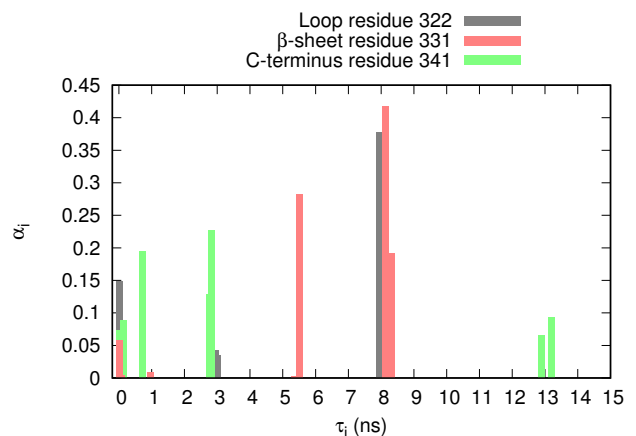


FIG. 7. Prefactors  $\alpha_i$  corresponding different timescales  $\tau_i$  resulting from a fit of Eq.13 to correlation functions from MD simulation of *PaTonB* at 298K. The used correlation functions give a good agreement with experimental spin relaxation times as shown in Fig. 6.

## IV. DISCUSSION AND CONCLUSIONS

Experimental spin relaxation data for protein backbone N-H bonds was successfully reproduced by using classical molecular dynamics simulations for two different proteins with anisotropic molecular shape. Thus, the simulation trajectories give an atomic resolution interpretation for the protein dynamics measured with NMR experiments. Interpretation of overall and internal dynamics was demonstrated for two relatively rigid proteins. The proposed approach is expected to be especially useful in the interpretation of spin relaxation data of proteins containing some interesting flexible domains and having an anisotropic shape. Interpretation of relaxation data measured from such proteins has been very challenging with the previously available methods [57].

Direct analysis of classical molecular dynamics trajectories did not, however, reproduce the experimental data. Comparison of calculated diffusion constants and spin relaxation times with experimental data suggested that the overall brownian tumbling of protein is too rapid in simulations, in agreement



with previous studies suggesting that the discrepancy arises from the inaccuracies in water models [25]. Scaling down the diffusion coefficients in simulation data with the same factor in all directions led to good agreement with experiments and allowed the interpretation. The overall rotation of proteins was found to be brownian having only a small subdiffusive behaviour with short timescales below  $\sim 0.12$  ns. This can be contrasted with crowded environments, where anomalous diffusion is expected to be more significant [58].

Similarity between correlation functions from the original MD trajectory and the new correlation functions from Eq. 12 suggest that the usage of inertia axes and the separation of internal and overall rotational motions (Eq. 6) are good approximations for the investigated proteins. However, rather rigid proteins are studied in this work and in previous publications with similar conclusions [10, 25]. These assumptions become less rigorous for proteins with larger fractions of intrinsically disordered segments. In such cases the option might be to use isotropic reorientational eigenmode dynamics (iRED) [24] or quaternions [26]. However, the correction of the overall rotational diffusion artefact due to the inaccurate water model would be complicated for intrinsically ordered molecules in all the discussed approaches. Thus, a water model giving cor-

rect overall rotational diffusion rates for biomolecules is probably necessary to compare simulations of intrinsically disordered molecules to experimental spin relaxation data.

Overall rotational diffusion coefficients were overestimated by a factor of  $\sim 3$  in *HpTonB* simulations with tip3p water model, in agreement with previous studies [24–26]. Simulations with tip4p and opc4 water models gave spin relaxation times in reasonable agreement with experiments with scaling factors of  $\sim 1$ – $1.2$ , which is significantly less than for tip3p. It should be noted, however, that the correct scaling factor for tip4p seems to slightly differ for *HpTonB* and *PaTonB* suggesting that the correction is not fully determined by bulk water properties. Thus, the role of hydration layer and water-protein interactions in rotational dynamics is also expected to be significant.

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## SUPPLEMENTARY INFORMATION

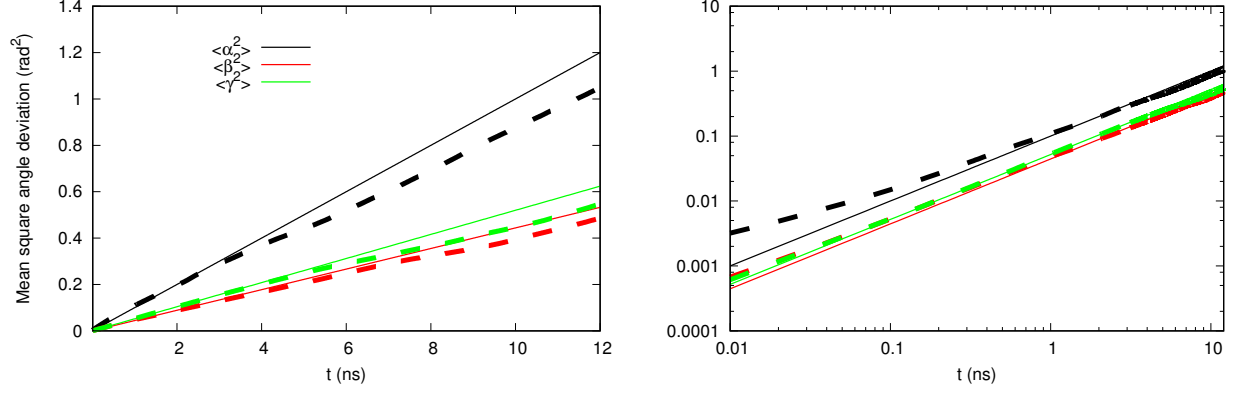


FIG. 8. The inertia tensor angles as a function of time and mean square angular deviations for *PaTonB* simulation with tip4p water model at 310K.

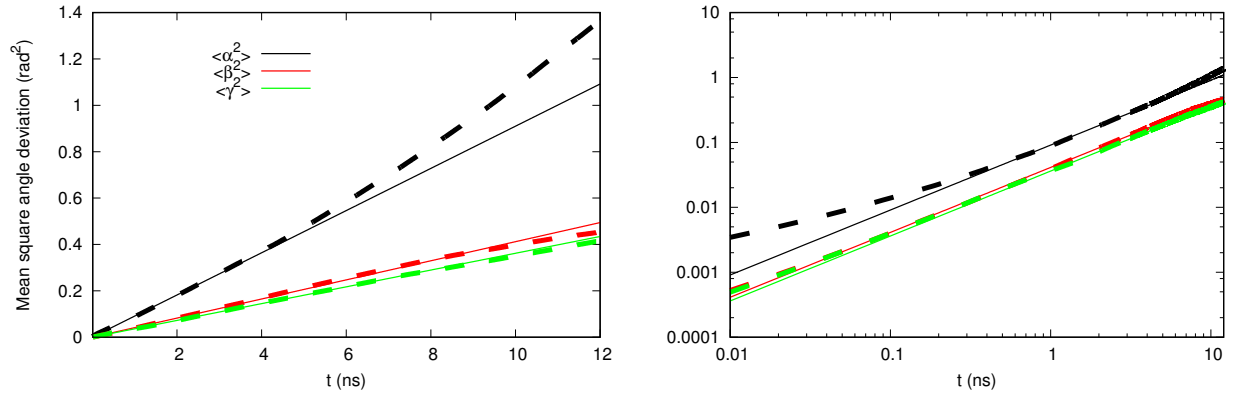


FIG. 9. The inertia tensor angles as a function of time and mean square angular deviations for *PaTonB* simulation with tip4p water model at 298K.