

Virtual Memory (3)

Dr. Jun Zheng
CSE325 Principles of Operating
Systems
11/8/2019



Least Recently Used (LRU) Algorithm

- ❑ Use past knowledge rather than future
- ❑ Replace page that has not been used in the most amount of time
- ❑ Associate time of last use with each page

reference string

7 0 1 2 0 3 0 4 2 3 0 3 2 1 2 0 1 7 0 1

7	7	7	2		2		4	4	4	0			1		1		1		
	0	0	0		0		0	0	3	3			3		0		0		
		1	1		3		3	2	2	2			2		2		7		

page frames

12 faults – better than FIFO but worse than OPT

Generally good algorithm and frequently used

But how to implement?

LRU Algorithm (Cont.)

- ❑ Counter implementation
 - ❑ Every page-table entry has a time-of-use field and the CPU has a logic clock or counter;
 - ❑ The clock is incremented for every time a page is referenced and the content of the clock register is copied to the time-of-use field in the page-table entry
 - ❑ When a page needs to be replaced, look at the counters to find smallest value
 - ❑ Search through table needed
 - ❑ Overflow of the clock must be considered

LRU Algorithm (Cont.)

❑ Stack implementation

- ❑ Keep a stack of page numbers (use a doubly linked list)
- ❑ Page referenced, move it to the top
 - ❑ The LRU page is always at the bottom of the stack
- ❑ Update is more expensive (at worst changing six pointers) but no search for replacement

❑ LRU and OPT are cases of **stack algorithms** that **don't have Belady's anomaly**

- ❑ A stack algorithm is an algorithm for which it can be shown that the set of pages in memory for n frames is always a *subset* of the set of pages that would be in memory with $n + 1$ frames.

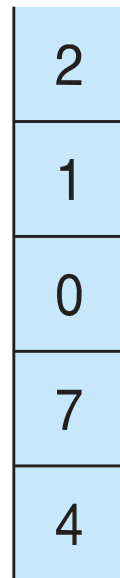
Use Of A Stack to Record Most Recent Page References

reference string

4 7 0 7 1 0 1 2 1 2 7 1 2

↑
a

↑
b



stack
before
a



stack
after
b

In-Class Work 6

Consider the following page reference string:

1, 2, 3, 4, 2, 1, 5, 6, 2, 1, 2, 3, 7, 6, 3, 2, 1, 2, 3, 6

How many page faults would occur for the following replacement algorithms, assuming **three frames**?

Remember that all frames are initially empty, so your first unique pages will cost one fault each.

- ☐ LRU replacement
- ☐ FIFO replacement
- ☐ Optimal replacement