

20240614 λ -Calculus with Typing in C or C++ Topics

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Play ground & Examples:

Resources Link : ① http://youtube/ViPNHMSUog?si=wqa_Ao-qFzUoV8TB
[EyesomorphiC]

Case 1: Boolean

set $TRUE = \lambda x \lambda y. x$

$FALSE = \lambda x. \lambda y. y$

$NOT = \lambda b. b _ FALSE _ TRUE$

① " $\lambda x. \lambda y. x$ " \rightarrow " λx " " λy " " x "

" $\lambda x. \lambda y. x$ " β " K " find all x in the original string THEN Replace all word " x " with " K "

$\lambda "x" . " \lambda y. x "$ $\rightarrow L_1 \Rightarrow L_2 \quad L_1 = "x"$

now set $L_1 = "K"$

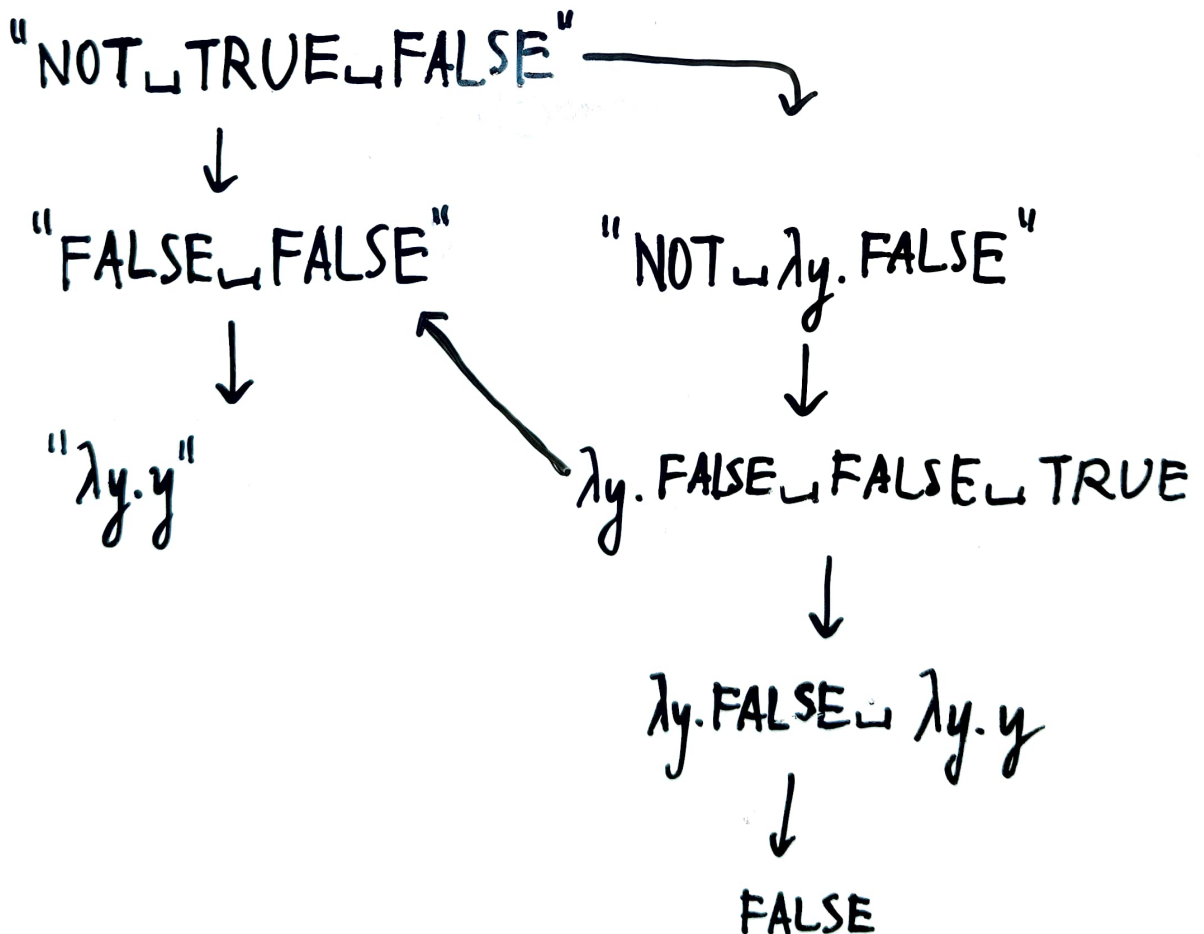
and return " $\lambda y. K$ " As new output

Sidetrail Hulting Problem

set " A " = $\lambda x. \lambda y. A_{x,y}$

$A_{2,3} \rightarrow A_{4,2,3} \rightarrow A_{4,2,3} \rightarrow \dots$

Back continue Case 1



Case 2: Num

$$3 = \lambda f. \lambda x. f(f(f _ x))$$

$$2 = \lambda f. \lambda x. f(f _ x)$$

$$5 = \lambda f. \lambda x. f(f(f(f(f _ x))))$$

$$+ = \lambda x. \lambda y. x$$

$$3 _ f _ (2 _ f _ x)$$

=

$$3 _ f = \lambda x. f(f(f _ x))$$

$$2 _ (3 _ f) = \lambda x. f(f(f _ (f(f(f _ x)))))$$

$$2 _ 3$$

↓

$$* / x : \lambda x. \lambda y. x _ y$$

$$3 _ 2 = \lambda y. 2(2(2 _ y))$$

$$= \lambda y. 2(2(\lambda x. y(y _ x)))$$

$$\lambda x. (\lambda x. y(y _ x)) (\lambda x. y(y _ x) _ x)$$

$$\lambda x. y(y(y _ x))$$

So As Above we found multiplication.