# Core Econometrics III: Problem Set 2

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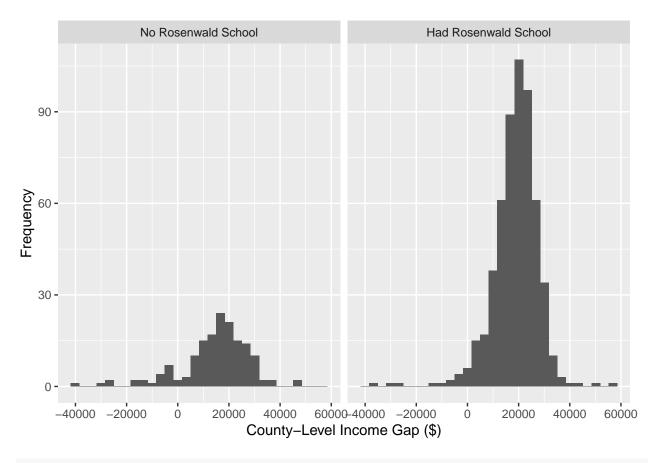
## Question 1

```
library(pacman)
p_load(dplyr, tidyverse, stargazer, fixest, magrittr, kableExtra, scales)
data = read.csv("data-002.csv")
```

## Question 2

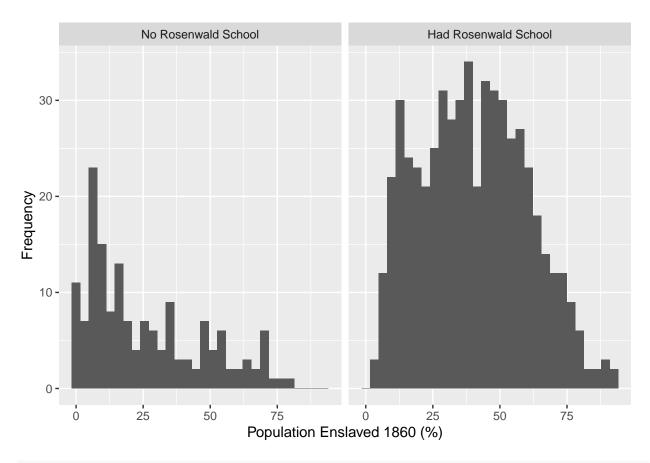
A histogram of the county-level income gap (income\_white\_2010 - income\_black\_2010) split by whether the county had a Rosenwald school (had\_rosenwald\_school)

```
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```

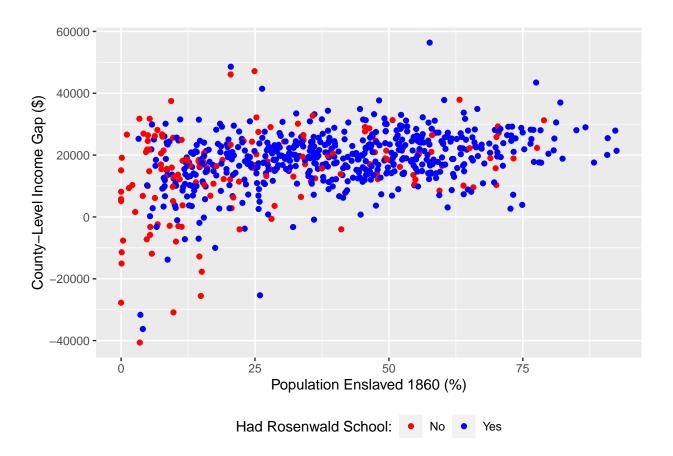


A histogram of the percent of the population in 1860 that was enslaved (pct\_pop\_enslaved\_1860) also split by whether the county had a Rosenwald school (had\_rosenwald\_school)

```
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```



A scatter plot with pct\_pop\_enslaved\_1860 on the x axis and the county income gap on the y axis with the points colored by whether or not the county had a Rosenwald school.



# Question 3

	Race Income Gap (1)	
(Intercept)	14,537.5***	
Had Rosenwald School	(802.8) $4,323.7***$	
Had Rosenward School	(909.7)	
Observations	710	
$\mathbb{R}^2$	0.03092	
Adjusted $R^2$	0.02955	

The identifying assumptions necessary to interpret these results as causal are that we are estimating the true model, that there are no omitted relevant variables, that the exogenous variables are uncorrelated with the disturbances.

## Question 4

Observations 710  $R^2$  0.09778
Within  $R^2$  0.02938

State Fixed Effects

The conditional independence assumption required by this regression for a causal interpretation is that conditional on the state a county is in, potential outcomes of racial income gaps in that county are independent of whether or not that county had a Rosenwald School.

# Question 5

	Race Income Gap	
	(1)	
Had Rosenwald School	2,252.9***	
	(669.1)	
% Population Enslaved 1860	129.1***	
	(20.06)	
Total Population 1860	0.1062**	
	(0.0409)	
Observations	710	
$R^2$	0.16186	
Within R <sup>2</sup>	0.10130	
VV IOIIIII IC	0.03031	
State Fixed Effects	$\checkmark$	

## Question 6

If these new variables (pct\_pop\_enslaved\_1860 & pop\_total\_1860) were causing bias in the regression in question 4, then I would suspect them to be upward biasing factors – since Rosenwald schools were located in

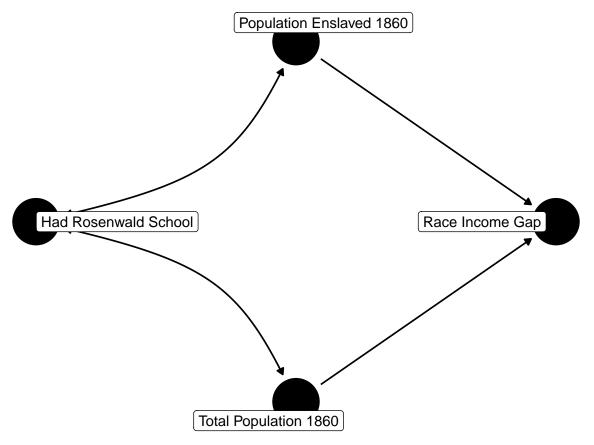
areas with high Black populations (as shown in the histograms above), which will likely also be highly populated areas in general – making both of these new variables positively correlated with had\_rosenwald\_school. Additionally, it makes sense that they would also correlate positively with the race income gap. Since the estimated coefficient on had\_rosenwald\_school dropped dramatically after adding the new variables into the regression, the omitted variables were biasing the estimate positively, which matches my intuition.

## Question 7

The conditional independence assumption required by the regression in question 5 is that conditional on the percent of population of a county that was in enslaved in 1860 and the total population of that county, potential outcomes of racial income gaps are independent of whether or not that county had a Rosenwald school.

I do not believe this is a valid assumption.

```
p_load(ggdag)
coordinates = list(
 x = c(X = 0, Z = 1, W = 1, Y = 2), # Node name = x coordinate for that node
 y = c(X = 1, Z = 0, W = 2, Y = 1) # Node name = y coordinate for that node
dag_7.1 = dagify(W \sim X,
                 Z ~~ X,
                 Y \sim W + Z
                 coords = coordinates,
                 labels = c(Y = "Race Income Gap",
                            X = "Had Rosenwald School",
                            W = "Population Enslaved 1860",
                            Z = "Total Population 1860"))
ggdag(dag_7.1,
      text = FALSE,
      use_labels = "label") +
  theme_void()
```



This dag draws out the conditional independence assumption: Had Rosenwald School  $\perp$  Race Income gap | Population Enslaved 1860, Total Population Enslaved 1860

By selecting these two variables, we open biasing paths. There is selection bias for which counties got the Rosenwald Schools, mainly those with high black populations, which were counties with high enslavement and total populations.

## Question 8

Adding the county's 2010 population (Black, White, and/or total) as a control in the regression is a bad idea because there are numerous unclear causal relationships between these variables and our current controls and treatment. For example, a county with high enslavement in 1860 (therefore a high black population in 1860) is likely to have received a Rosenwald School, and it is likely more black people would have moved to those counties to receive education from those schools, increasing the black population in 2010. Therefore, we have an unclear alternating effect between three variables that will bias our estimates. This hurts our conditional independence assumption.

## Question 9

```
data %<>% mutate(p_score = reg_9.1$fitted.values)
```

#### Estimate propensity scores

# Question 10

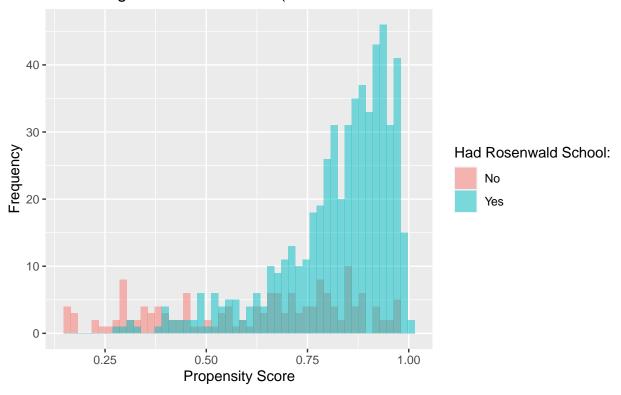
```
# Regression using the p_score instead of the variables
reg_10.1 = feols(
  race_income_gap ~ had_rosenwald_school + p_score + pct_pop_enslaved_1860 + pop_total_1860 | state,
  data = data)
table10.1 = etable(reg_10.1,
                    style.tex = style.tex("aer"),
                    tex = TRUE)
                              Race Income Gap
                                     (1)
                                    1,626.8
 Had Rosenwald School
                                    (928.2)
 Propensity Score
                                    7,464.5
                                   (4,561.5)
                                   95.69***
 % Population Enslaved 1860
                                    (23.67)
 Total Population 1860
                                   0.0619*
                                   (0.0317)
 Observations
                                     710
 \mathbb{R}^2
                                   0.16806
 Within R<sup>2</sup>
                                   0.10498
```

State Fixed Effects  $\checkmark$ 

Using the propensity scores instead of the variables has decreased the estimate on the coefficient on had\_rosenwald\_school by around 600, meaning the effect of a county having Rosenwald schools on that county's race income gap was overestimated in previous regressions. Additionally, the standard errors on the coefficient on had\_rosenwald\_school has increased, and our estimate is no longer statistically significant.

# Question 11

# Frequency of Propensity Scores for Likelihood of Receiving Rosenwald School (50 bins



## Question 12

What percent of observations aren't supported by overlap

```
# Create function to assign p_score to a group
  # Create the groups by finding the min, max, and the steps
p_min = min(data$p_score)
p_max = max(data$p_score)
p_step = (p_max - p_min)/50
  # compile these into a handy dataframe
p_data = data.frame(step_max = seq(from = p_min, to = p_max, by = p_step)) %>%
            mutate(step_min = lag(step_max),
                   group = 0:50) %>%
            filter(group >= 1)
  # creating the function itself
find_p_group = function(X) {
  null_vec = logical(length=nrow(p_data))
  for (j in 0:nrow(p_data)) {
    x2_min = p_data$step_min[j]
    x2_max = p_data$step_max[j]
```

```
if( isTRUE((X >= x2_min) && (X <= x2_max))) {</pre>
      null_vec[j] = as.logical("T")} else {
      null_vec[j] = as.logical("F")}
  }
 return(which(null_vec == T))
}
# Use function to create new variable that groups the p_scores into respective boxes
  # I'm sure there are better ways but they weren't working
  # The function works, but started giving me a warning for some curious reason.
  # The try() function supresses that message
try(for (i in 1:(nrow(data))) {
data$p_group[i] = find_p_group(data$p_score[i])
}, silent = T)
# Find the groups that have both had rosenwald school of 0 & 1
  # meaning the mean of the groups is between 0 and 1
match_groups = data %>%
          select(had_rosenwald_school, p_group) %>%
          group_by(p_group) %>%
          summarize(avg = mean(had_rosenwald_school)) %>%
          filter(avg > 0 & avg < 1) %>%
          select(p_group)
# Calculate the percent in those groups:
numerator = nrow(data %>% filter(p_group %in%match_groups$p_group))
denominator = nrow(data)
(1 - numerator/denominator) * 100
```

#### ## [1] 7.323944

Therefore when using 50 groups, about **7.3**% of data points aren't supported by overlap. (When I used 30 groups, it was only 2.1%, and since I believe in erring on the side of caution, I will use this larger number of groups).

#### Question 13

We care about enforcing overlap because we want there to be a positive probability for a given individual (or county, in this case,) to be placed in either the treatment or control group. This gives us a stronger identification strategy, and rids some selection bias from our sample – as those who would always or never be treated are removed.

## Question 14

```
data_overlap = data %>% filter(p_group %in% match_groups$p_group)
# Regression using the p_score instead of the variables
reg_14.1 = feols(
  race_income_gap ~ had_rosenwald_school + p_score + pct_pop_enslaved_1860 + pop_total_1860 | state,
  data = data_overlap)
table14.1 = etable(reg_14.1,
                   style.tex = style.tex("aer"),
                   tex = TRUE)
                             Race Income Gap
                                   (1)
 Had Rosenwald School
                                 1,667.6*
                                  (908.1)
 Propensity Score
                                 8,296.3
                                 (4,958.1)
 \% Population Enslaved 1860
                                 94.99***
                                  (21.06)
 Total Population 1860
                                  0.0340
                                 (0.0277)
```

 $R^2$  0.16565 Within  $R^2$  0.09757 State Fixed Effects

Compared to the regression in question 10, our standard error for the estimate on had\_rosenwald\_school shrunk, and our estimate increased. The estimate is now statistically significant at the 10% significance level.

658

# Question 15

Observations

```
Race Income Gap
                                        (1)
Had Rosenwald School
                                     2,233.0
                                     (1,349.0)
                                     135.5***
% Population Enslaved 1860
                                     (21.81)
Total Population 1860
                                     0.0835*
                                     (0.0425)
Observations
                                       658
R^2
                                     0.15906
Within \mathbb{R}^2
                                     0.08687
State Fixed Effects
```

Our estimate on had\_rosenwald\_school increased, and its standard error increase. The estimate is once again not statistically significant.

#### Question 16

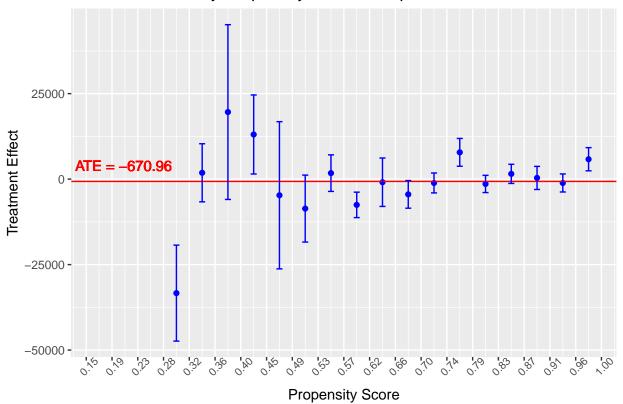
```
# Going to use just 20 bins
  # Create the groups by finding the min, max, and the steps
p_min2 = min(data$p_score)
p_max2 = max(data$p_score)
p_step2 = (p_max - p_min)/20
  # compile these into a handy dataframe
p_data2 = data.frame(step_max = seq(from = p_min2, to = p_max2, by = p_step2)) %>%
            mutate(step_min = lag(step_max),
                   group = 0:20) %>%
            filter(group >= 1)
  # creating the function itself
find_p_group2 = function(X) {
  null_vec = logical(length=nrow(p_data2))
  for (j in 0:nrow(p_data2)) {
    x2_min = p_data2$step_min[j]
    x2_max = p_data2$step_max[j]
    if( isTRUE((X >= x2_min) && (X <= x2_max))) {</pre>
      null_vec[j] = as.logical("T")} else {
      null_vec[j] = as.logical("F")}
  }
  return(which(null_vec == T))
try(for (i in 1:(nrow(data))) {
```

```
# Creating data frame for the graph
data_q16 = match_groups2 %>%
           mutate(treatment effect = NA,
                   standard_error = NA) %>%
            rename(group = p_group2)
# Regressions for each group
for (i in 1:nrow(data_q16)) {
 j = data_q16$group[i]
 data_group = data_overlap2 %>% filter(p_group2 == j)
 reg_16.j = feols(race_income_gap ~ had_rosenwald_school + pct_pop_enslaved_1860 + pop_total_1860 | st
                data = data_group)
 data_q16$treatment_effect[i] = reg_16.j$coefficients[[1]]
 data_q16$standard_error[i] = reg_16.j$se[[1]]
}
# Compiling and refining data fro the graph
data_q16.2 = right_join(data_q16, p_data2, by = "group")
data_q16.2 %<>% mutate(p_score = (data_q16.2$step_max + data_q16.2$step_min)/2) %>%
                mutate(upper = treatment_effect + standard_error,
                       lower = treatment_effect - standard_error)
# Calculating Average Treatment Effect
ATE.16 = data_q16.2 %>% select(treatment_effect) %% summarize(ATE = mean(treatment_effect, na.rm = T))
ATE = ATE.16$ATE[1]
# The graph!
```

#### **Regression Part**

## Warning: Removed 3 rows containing missing values (geom\_point).

# Treatment Effect by Propensity Score Groups



#### $\mathbf{Q}$

I think that were we to employ a 'selection on unobservables' strategy by using pct\_pop\_enslaved\_1860 as an instrument for whether a county received a Rosenwald school (had\_rosenwald\_school), we might run into a few similar issues as seen in this problem set above. We would desire the use of an instrumental variable if the were disturbances affecting both had\_rosenwald\_school and race\_income\_gap were also unassociated with pct\_pop\_enslaved\_1860, as that is a requirement for using instrumental variables. However, I find it difficult to believe that these disturbances between our treatment and outcome would be uncorrelated with this instrument, given how closely tied the history of systemic racism is to all of these variables. Therefore, I do not believe this strategy would be a stronger identification strategy than what has been done here.