

Math Camp

Module #0 Introduction

Why are we here?

Who are we?

What is economics?

What is math?

Why is there math in economics?

There's not.

Definition. A *theory* is a set of assumptions together with the necessary implications.

Two approaches to forming theories

1. Construct a narrative to explain behavior witnessed in data

- Pro: language allows for nuance and therefore realistic modeling assumptions
- Con: language is imprecise so assumptions and their implications can be unclear

About math in economics (continued)

2. Use math to lay out precise assumptions and deduce necessary implications

- Pro: meaning of assumptions and what implications follow cannot be debated; debate is limited to appropriateness of assumptions
- Con: tractable assumptions are necessarily restrictive, limiting reach of theory

About this course

Four important points

- New concepts in mathematics are completely mysterious until they are trivial
- Simply reading the lecture slides/text may not be enough to understand the concepts
- Your ability to apply course concepts only comes through self practice
- Don't skip the exercises

Prereqs: Logic

Let P and Q be statements

- “A declarative sentence that is either true or false but not both”
- We can use logical operators to create new compound statements that are either true or false.

Logical Operators

- **Conjunction:** the conjunction of P and Q is the statement “ P and Q ”, denoted $P \wedge Q$. Is only true if **both** P and Q are true.
- **Disjunction:** the disjunction of P and Q is the statement “ P or Q ”, denoted $P \vee Q$, and is only true if **either** P or Q are true.

Prereqs: Logic

Logical Operators cont.

- **Negation:** the negation of a statement P is the statement “*not P*”, denoted $\neg P$, and is only true if P is false, and is only false if P is true.
- **Conditional:** the conditional statement is the statement “*If P then Q*”, denoted $P \rightarrow Q$, means that Q must be true whenever P is true, and is only false when P is true and Q is false.

Prereqs: Numbers

- What about \mathbb{R} ?
 - \mathbb{R} is the completion of the rational numbers
 - Let $A \subset \mathbb{R}$. The *supremum* of A , denoted $\sup A$ is the least upper bound of A (may be infinite).
 - If $A \subset \mathbb{R}$ is bounded above then $\sup A \in \mathbb{R}$. (!!!!)
- What about \mathbb{C} ?
 - \mathbb{C} is algebraically closed: every non-constant polynomial has a root in \mathbb{C}
 - Every polynomial equation has a solution in \mathbb{C}

~

Definition. A *relation* on a set X is a subset R of $X \times X$

- if $(x, y) \in R$ then we write $x \sim y$
- R is an equivalence relation if it has the following properties
 - reflexivity $x \sim x$
 - symmetry $x \sim y \Rightarrow y \sim x$
 - transitivity $x \sim y$ and $y \sim z$ implies $x \sim z$
- the collection of all elements related to a given element is called an equivalence class

partition

Definition. A *partition* of a set X is a collection of non-intersecting subsets whose union is X .

More formally, $\{X_\lambda\}_{\lambda \in \Lambda}$ is a partition of X provided

- $X_\lambda \subset X$ for all $\lambda \in \Lambda$
- $X = \cup_{\lambda \in \Lambda} X_\lambda$
- $\lambda_1 \neq \lambda_2 \Rightarrow X_{\lambda_1} \cap X_{\lambda_2} = \emptyset$