

Anthony Ventresque

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Data Structures and Algorithms

COMP20230

# Project 2: Towards an Optimisation Tool

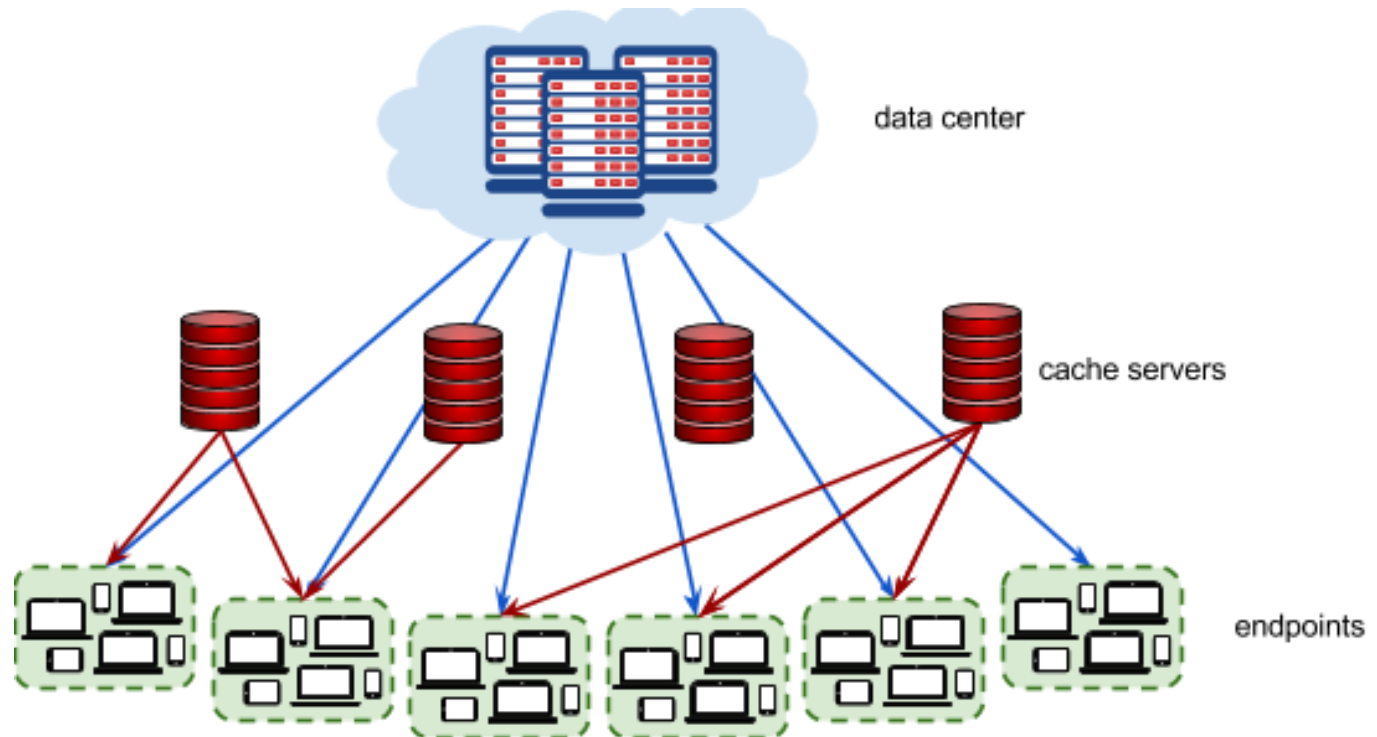


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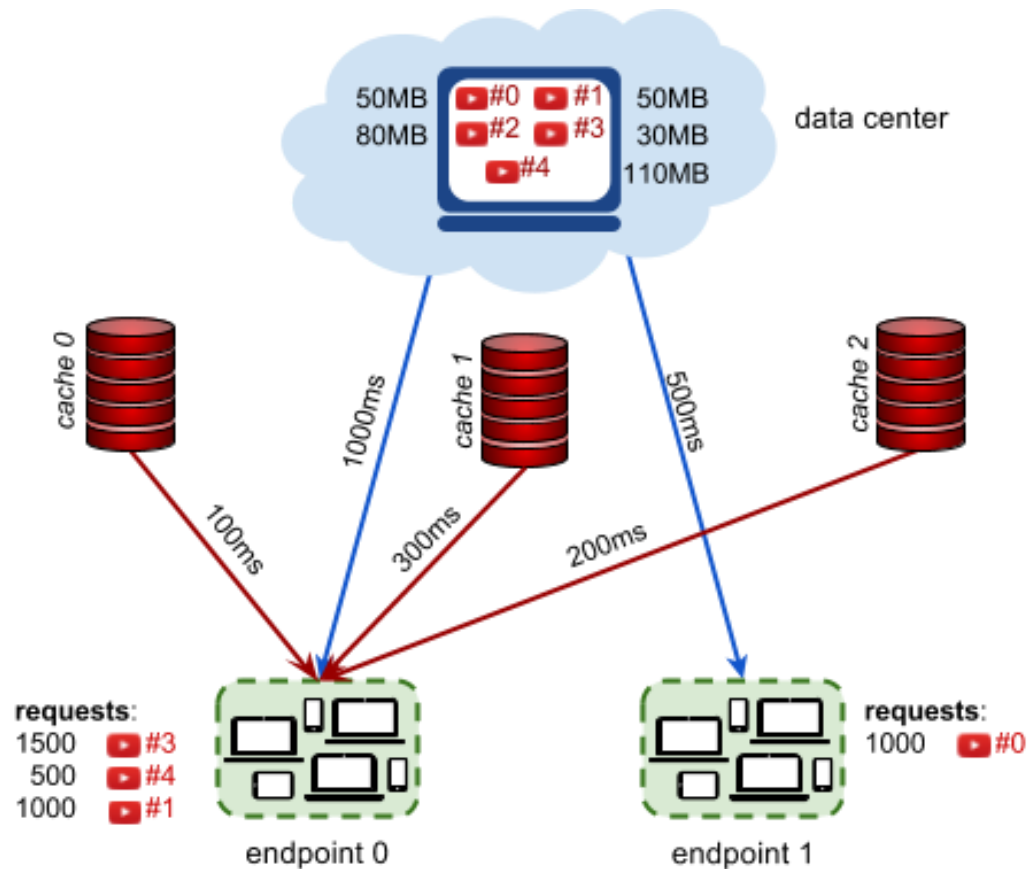
# GOOGLE HASH CODE 2017



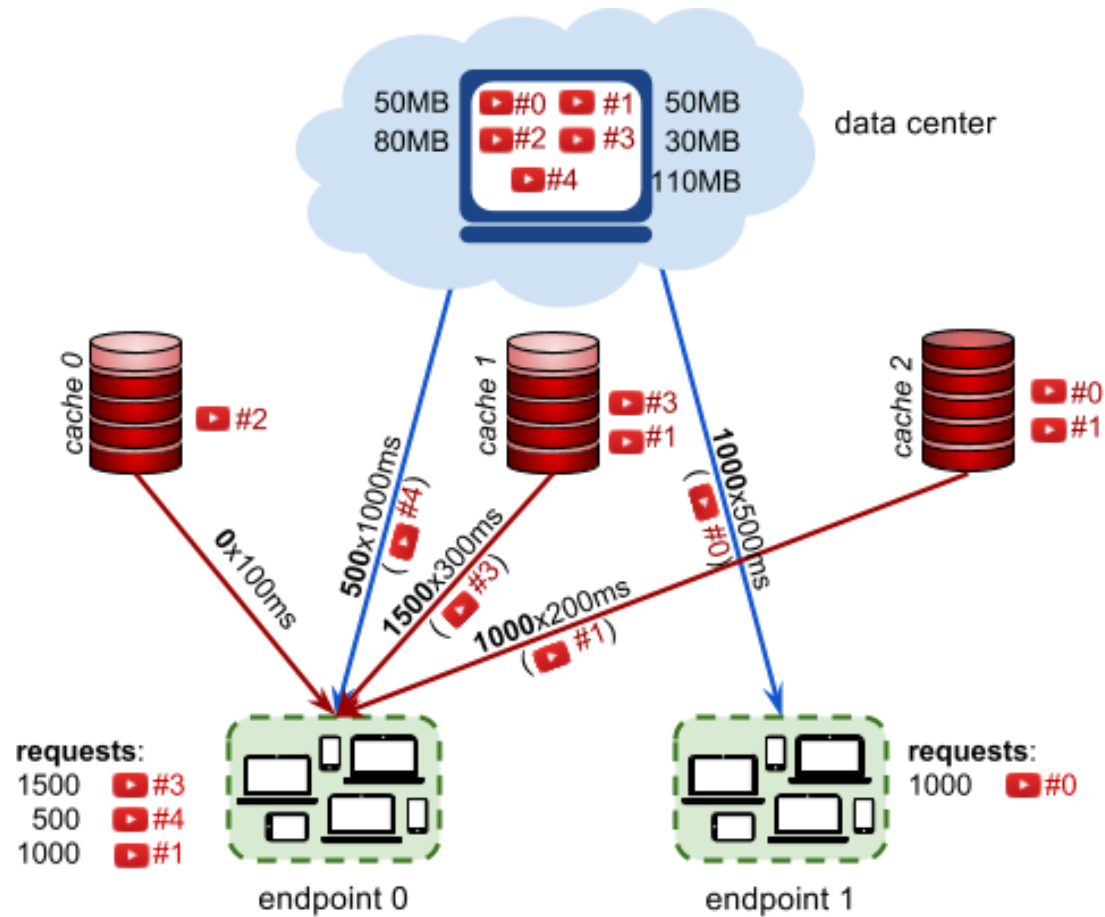
# Problem Description



## Problem Description (2)



# Solutions



# Constraints

- Sum of all videos stored in a cache server  $\leq$  capacity of the cache server



# Scoring Solutions

- Scoring function
  - = "cost function"
  - = "utility function"
  - = "fitness function"

score = 0

for each request q for a file f at an endpoint e

    score += number of videos in the request \*  
        (latency from data centre – best latency  
        from a cache server serving e and hosting f)

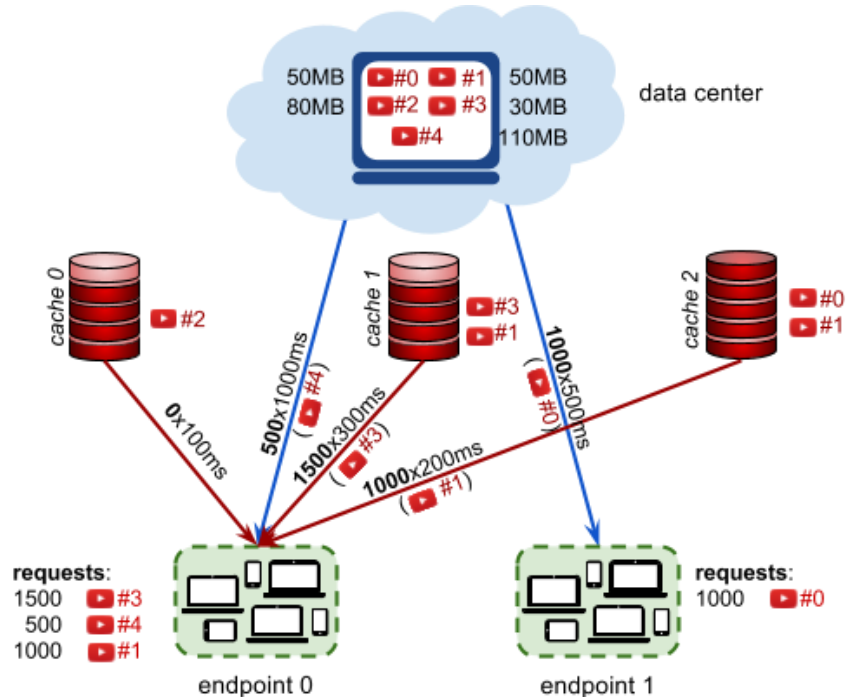
endfor

score = score/number of requests

score \*= 1000



# Scoring Solutions



$1500 \times \text{video 3 from cache 1} =$   
 $1500 \times (1000 - 300)$   
 $500 \times \text{video 4 from data centre} =$   
 $500 \times (1000 - 0)$   
 $1000 \times \text{video 1 from cache 2} =$   
 $1000 \times (1000 - 200)$   
 $1000 \times \text{video 0 from data centre} =$   
 $1000 \times (500 - 0)$   
 $\frac{\%(1500 + 500 + 1000 + 1000)}{462.5 \text{ ms on average}}$   
 $462500 \text{ points}$



# TOWARDS AN OPTIMISATION TOOL



# Components of an Optimisation Tool

Search Algorithm

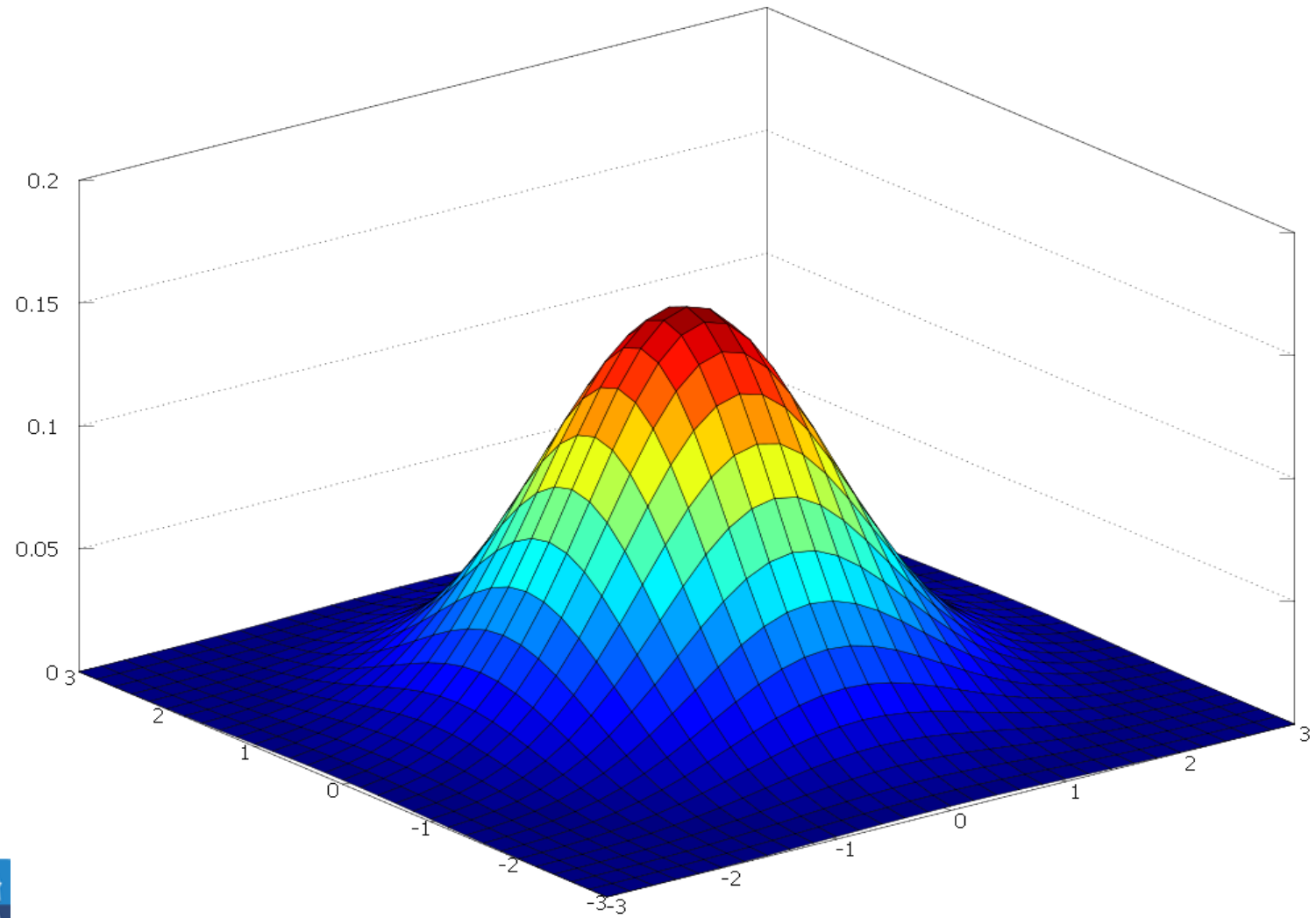
Representation

Search Operators

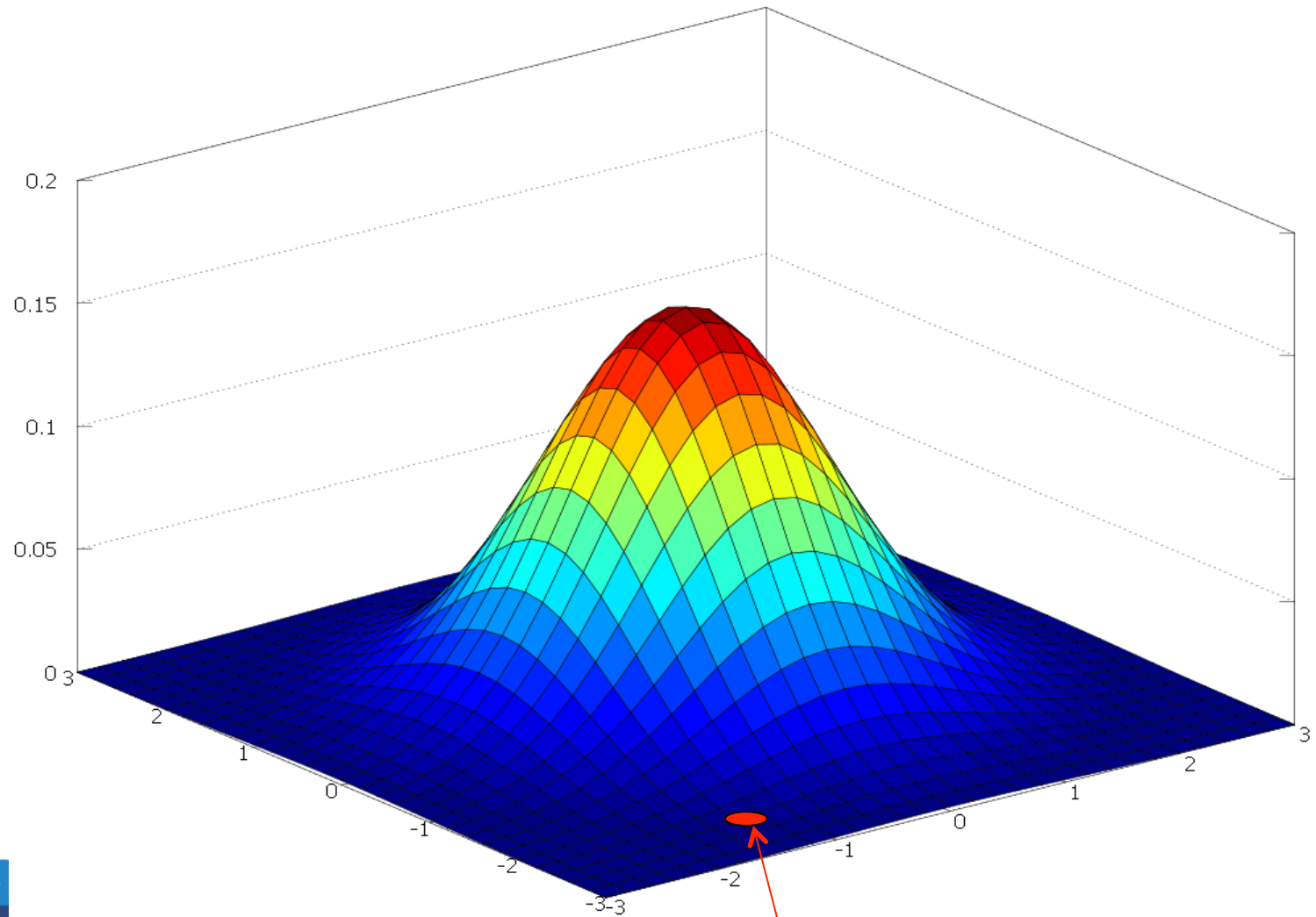
Fitness Function



# Hill Climbing

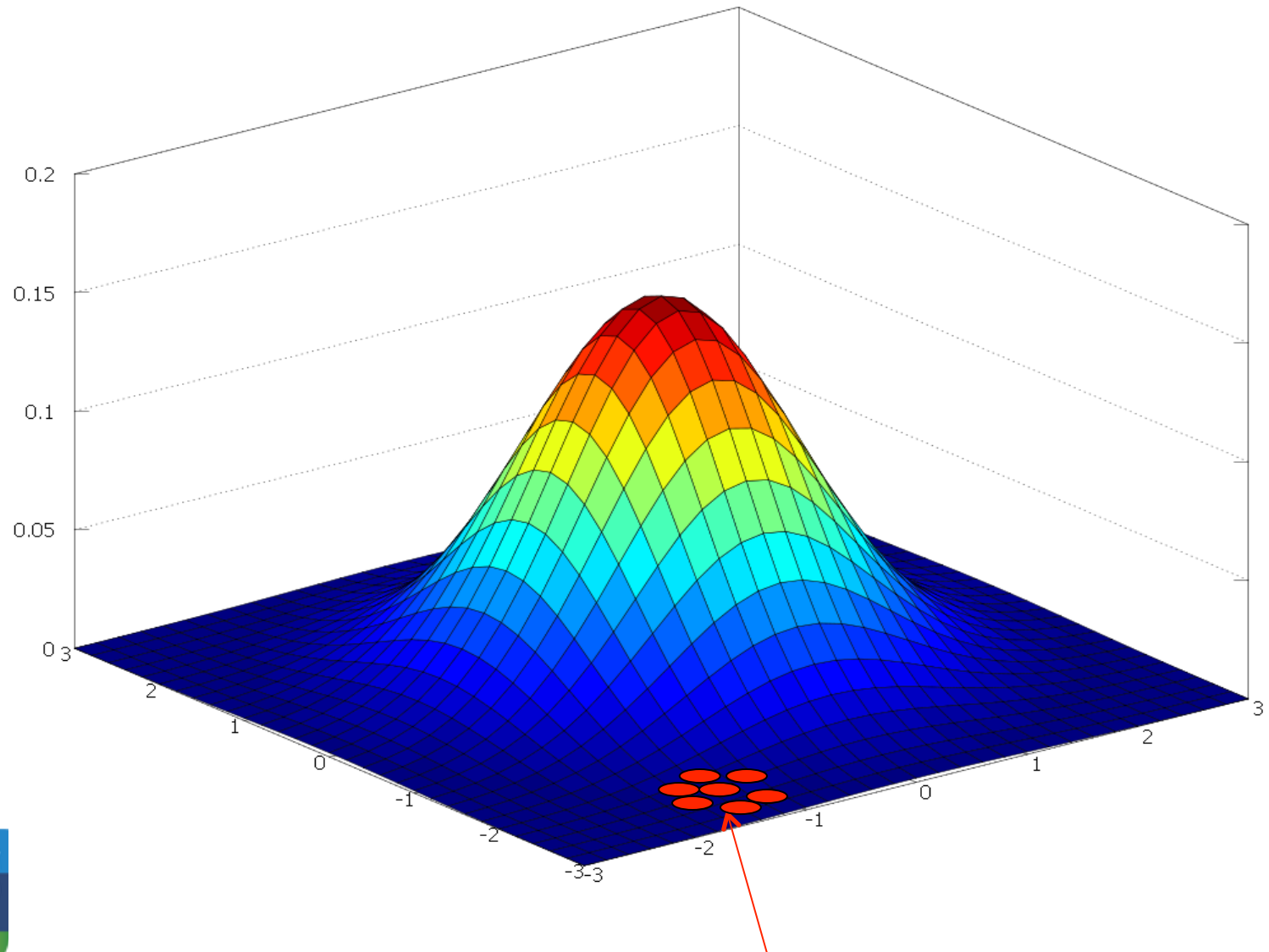


# Hill Climbing



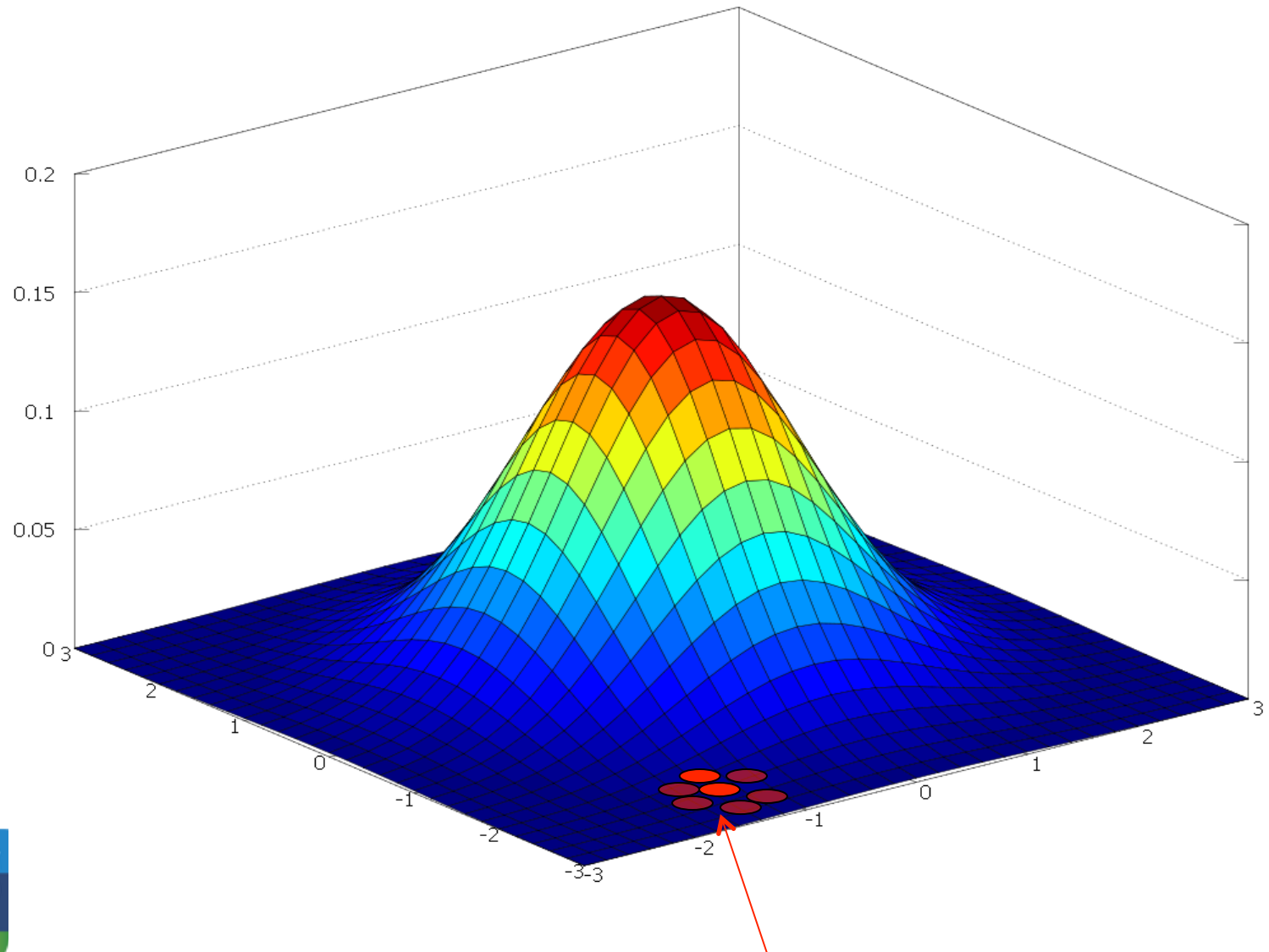
Select random value

# Hill Climbing



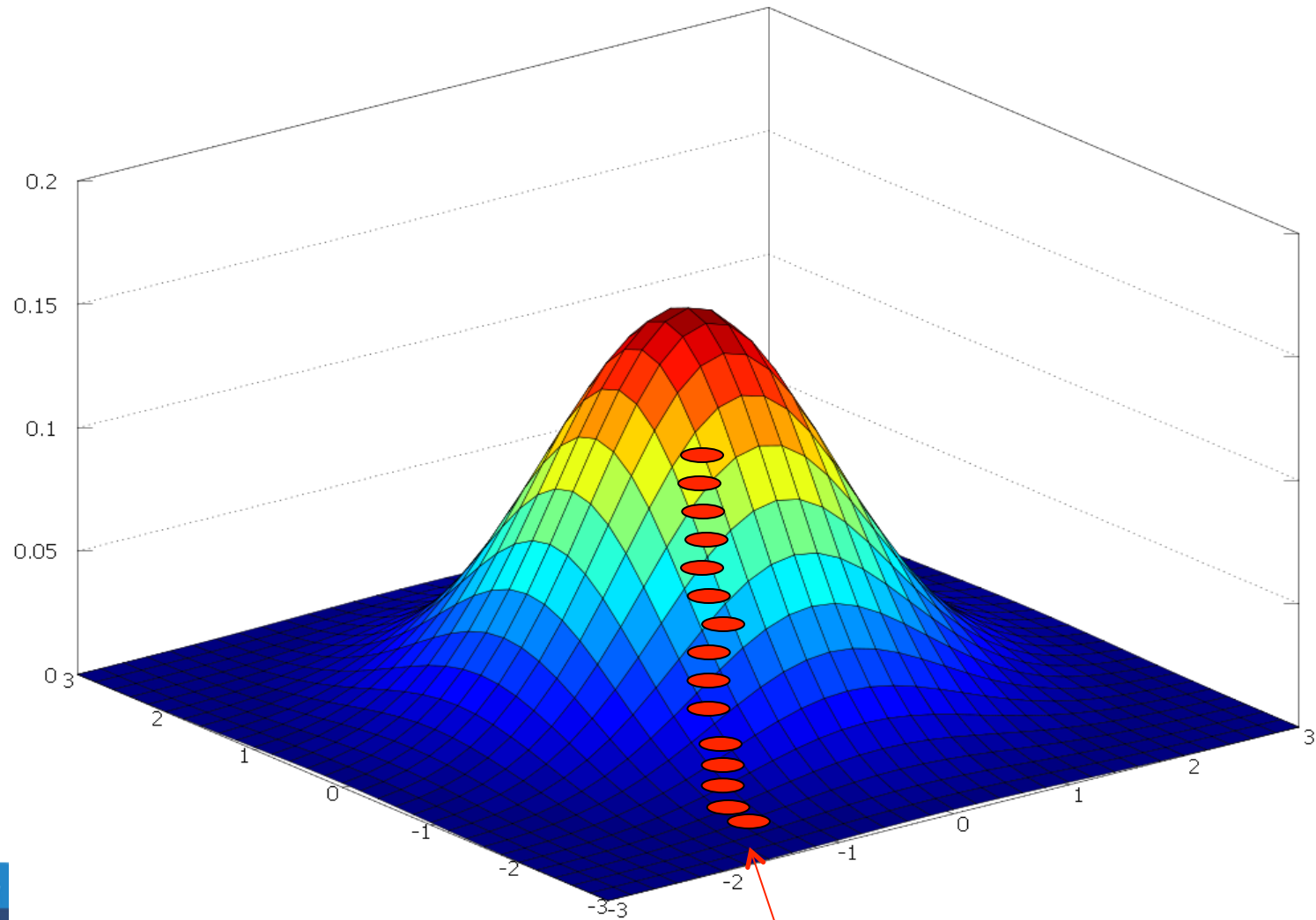
Explore neighbourhood

# Hill Climbing



Choose better neighbour

# Hill Climbing



# Components of an Optimisation Tool

Search Algorithm

Hill climbing

Representation

Search Operators

Fitness Function

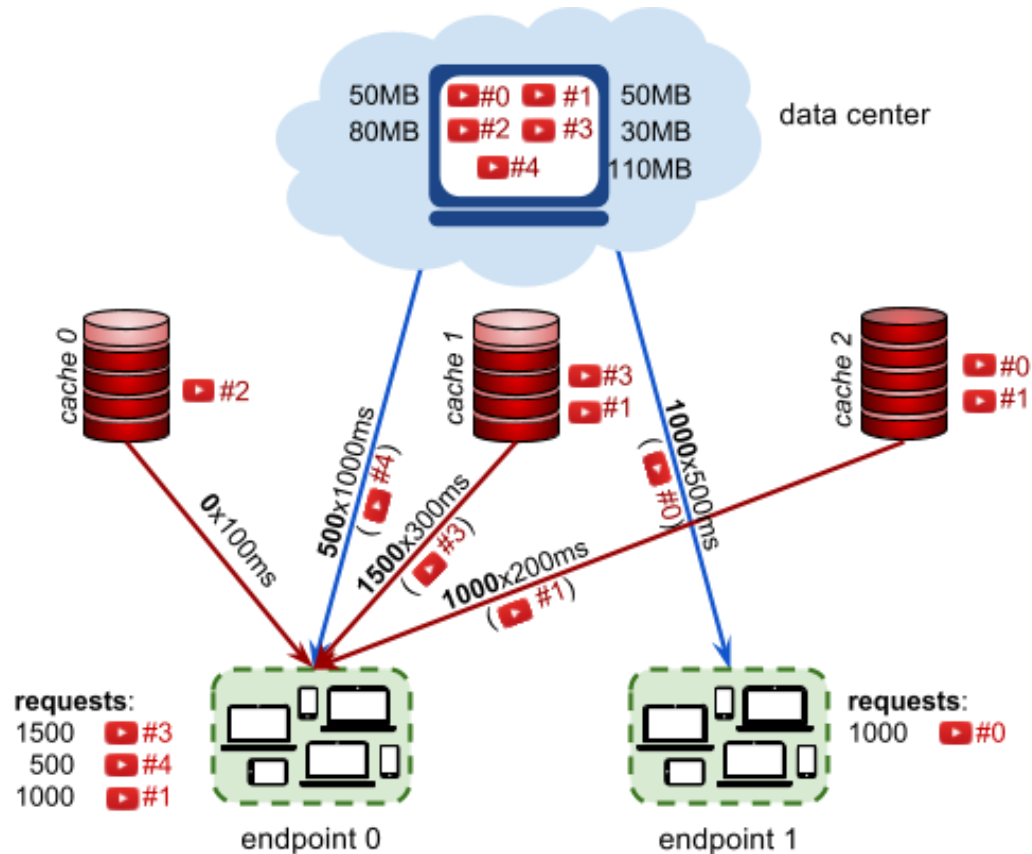




# Representation

cache0 - 2  
cache1 - 1,3  
cache2 - 0,1

$((2), (1, 3), (0, 1))$



# A Solution

cache0 - 2  
cache1 - 1,3  
cache2 - 0,1

↓  
 $((2), (1, 3), (0, 1))$

or

**$((0, 0, 1, 0, 0), (0, 1, 0, 1, 0), (1, 1, 0, 0, 0))$**



# Components of an Optimisation Tool

Search Algorithm

Hill climbing

Representation

2D list

Search Operators

Fitness Function



# Search

$((0,0,1,0,0),(0,1,0,1,0),(1,1,0,0,0))$

+1

-1



$((\mathbf{1},0,1,0,0),(0,1,0,1,0),(1,1,0,0,0))$

$((0,0,\mathbf{0},0,0),(0,1,0,1,0),(1,1,0,0,0))$

$((0,\mathbf{1},1,0,0),(0,1,0,1,0),(1,1,0,0,0))$

$((0,0,1,0,0),(0,\mathbf{0},0,1,0),(1,1,0,0,0))$

$((0,0,1,\mathbf{1},0),(0,1,0,1,0),(1,1,0,0,0))$

$((0,0,1,0,0),(0,1,0,\mathbf{0},0),(1,1,0,0,0))$

$((0,0,1,0,\mathbf{1}),(0,1,0,1,0),(1,1,0,0,0))$

$((0,0,1,0,0),(0,1,0,1,0),(\mathbf{0},1,0,0,0))$

$((0,0,1,0,0),(\mathbf{1},1,0,1,0),(1,1,0,0,0))$

$((0,0,1,0,0),(0,1,0,1,0),(1,\mathbf{0},0,0,0))$

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$((0,0,1,0,0),(0,1,0,1,0),(1,1,\mathbf{1},0,0))$

$((0,0,1,0,0),(0,1,0,1,0),(1,1,0,\mathbf{1},0))$

$((0,0,1,0,0),(0,1,0,1,0),(1,1,0,0,\mathbf{1}))$



# Search

$((0,0,1,0,0),(0,1,0,1,0),(1,1,0,0,0))$

+1

-1



$((\mathbf{1},0,1,0,0),(0,1,0,1,0),(1,1,0,0,0))$

$((0,0,\mathbf{0},0,0),(0,1,0,1,0),(1,1,0,0,0))$

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$((0,0,1,0,\mathbf{1}),(0,1,0,1,0),(1,1,0,0,0))$

$((0,0,1,0,0),(0,1,0,1,0),(\mathbf{0},1,0,0,0))$

$((0,0,1,0,0),(\mathbf{1},1,0,1,0),(1,1,0,0,0))$

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$((0,0,1,0,0),(0,1,0,1,0),(1,1,0,\mathbf{1},0))$

$((0,0,1,0,0),(0,1,0,1,0),(1,1,0,0,\mathbf{1}))$



# Components of an Optimisation Tool

Search Algorithm

Hill climbing

Representation

2D list

Search Operators

Neighbourhood of 2D list

Fitness Function



# Components of an Optimisation Tool

Search Algorithm

Hill climbing

Representation

2D list

Search Operators

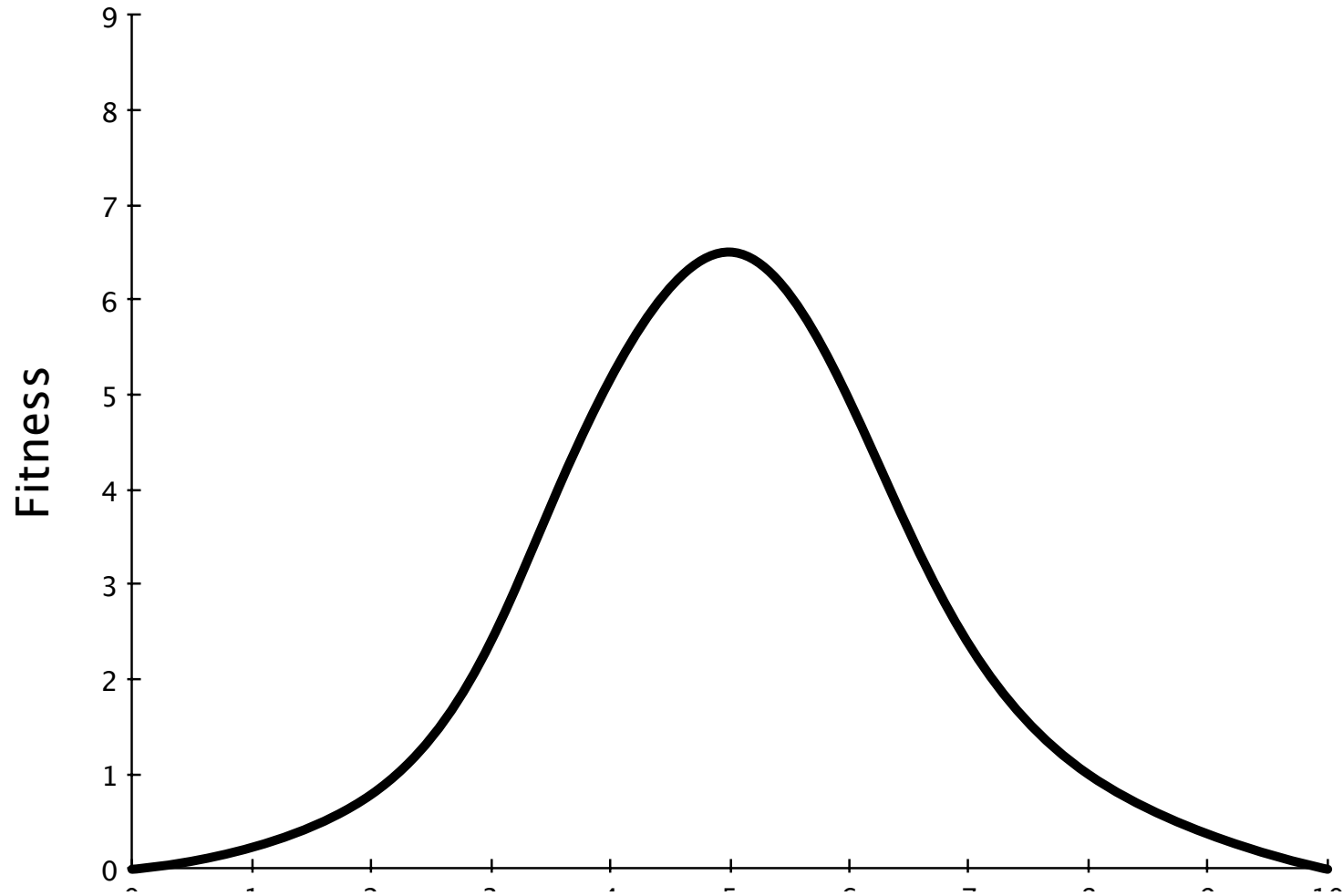
Neighbourhood of 2D list

Fitness Function

as given by Google

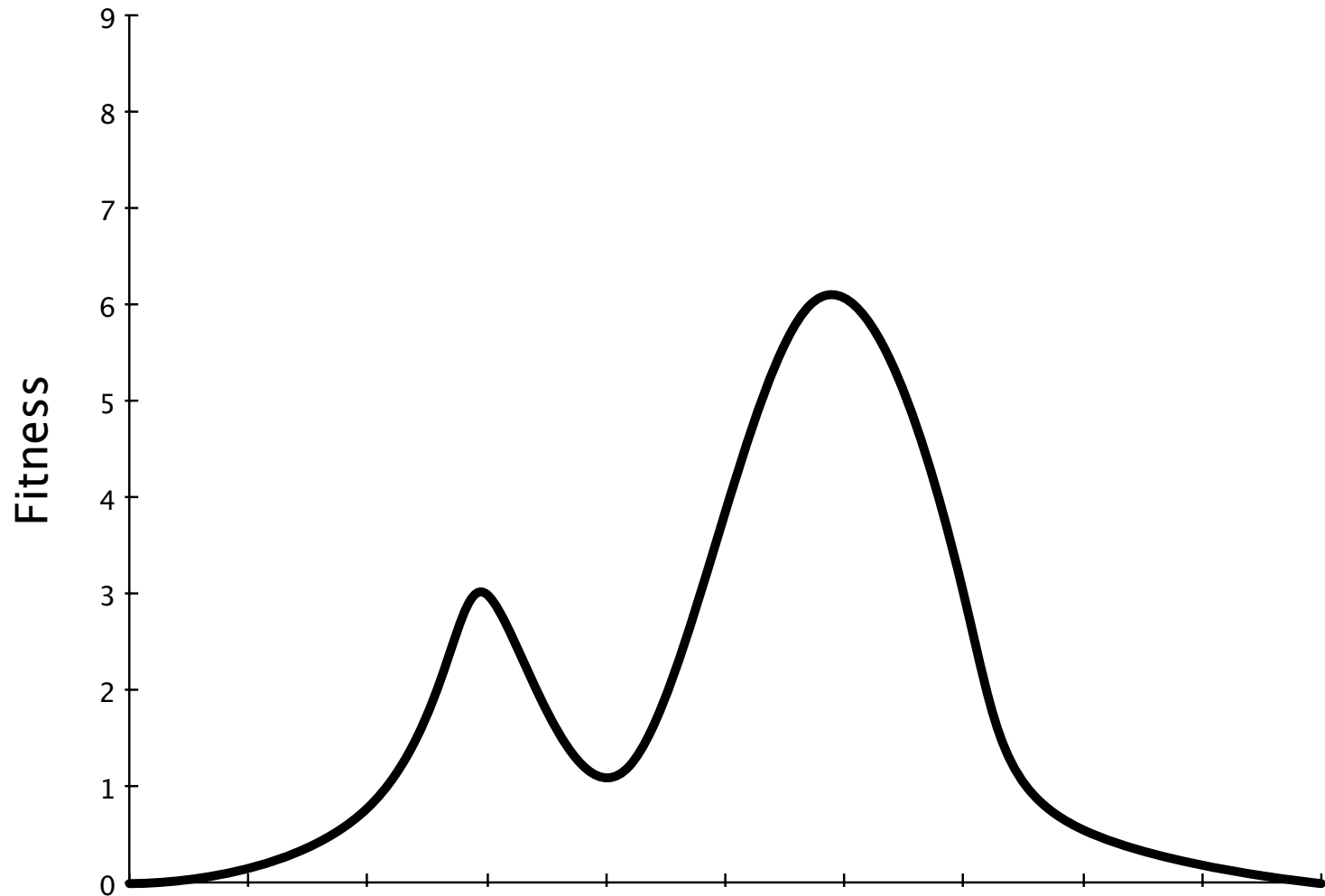


# Problem with Hill-climbing





# Problem with Hill-climbing



# Evolutionary (Genetic) Algorithms

- Two basic operations:

- **Mutation**

$((0,0,1,0,0),(0,1,0,1,0),(1,1,0,0,0))$        $((0,0,1,0,0),(0,1,\mathbf{1},1,0),(1,1,0,0,0))$   
before mutation       $\longrightarrow$  after mutation

- **Crossover**

$((0,0,1,0,0),(0,1,0,1,0),(1,1,0,0,0))$        $((\mathbf{0},\mathbf{1},\mathbf{1},\mathbf{0},\mathbf{0}),(0,1,0,1,0),(1,1,0,0,0))$   
 $((0,1,1,0,0),(0,1,1,1,0),(1,0,0,0,0))$        $((\mathbf{0},\mathbf{0},\mathbf{1},\mathbf{0},\mathbf{0}),(0,1,1,1,0),(1,0,0,0,0))$   
before CO       $\longrightarrow$  after CO



# Selection

- keep only the fittest individuals?
- or keep some “diversity”?
- how many individual solutions do we keep in a population?
- how often do we do crossover?
- how often do we mutate?

