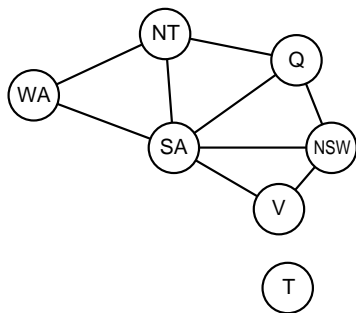


Graph modeling

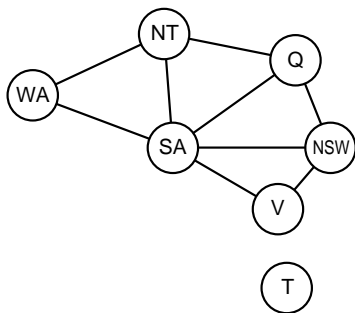


Graph modeling



Russell & Norvig

Graph modeling



Russell & Norvig

```
arc(wa,nt).    arc(nt,q).    arc(q,nsw).  
arc(wa,sa).    arc(nt,sa).    arc(sa,q).  
arc(sa,nsw).   arc(sa,v).     arc(v,nsw).  
  
arc2(X,Y) :- arc(X,Y) ; arc(Y,X).
```

Non-termination (due to poor choices)

i :- p,q. [i]

i :- r.

p :- i.

r.

| ?- i.

prove([],_).

prove([H|T],KB) :- member([H|B],KB), append(B,T,Next),
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| ?- prove([i],[[i,p,q],[i,r],[p,i],[r]]).

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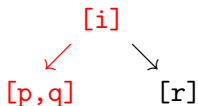
$i :- p, q.$

$i :- r.$

$p :- i.$

$r.$

$| \text{?- } i.$



$\text{prove}([], _).$

$\text{prove}([H|T], KB) :- \text{member}([H|B], KB), \text{append}(B, T, \text{Next}),$
 $\text{prove}(\text{Next}, KB).$

$| \text{?- } \text{prove}([i], [[i, p, q], [i, r], [p, i], [r]]).$

Non-termination (due to poor choices)

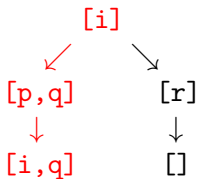
`i :- p,q.`

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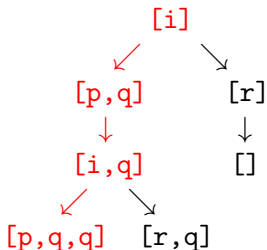
`i :- p,q.`

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`p :- i.`

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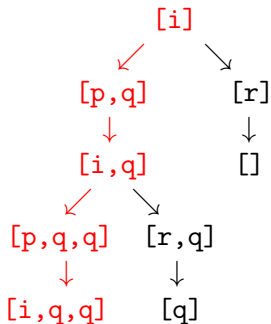
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`i :- r.`

`p :- i.`

`r.`

`| ?- i.`



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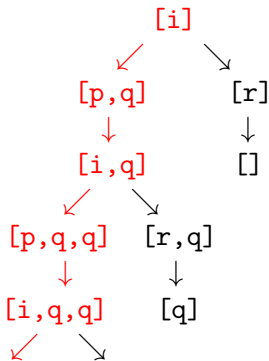
Non-termination (due to poor choices)

$$i \quad :- \quad p, q.$$
$$i \coloneqq r.$$

p :- i.

r.

| ?- i.



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```

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prove([H|T],KB) :- member([H|B],KB), append(B,T,Next),
                    prove(Next,KB).
```

```
| ?- prove([i],[[i,p,q],[i,r],[p,i],[r]]).
```

Determinization (eliminate choice)

A fsm $[Trans, Final, Q_0]$ such that

for all $[Q, X, Q_n]$ and $[Q, X, Q_{n'}]$ in $Trans$, $Q_n = Q_{n'}$

is a *deterministic finite automaton* (DFA).

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Proof: Subset (powerset) construction

Apply to arc, goal, contra Trans, Final:

```
arcD(NodeList, NextList) :-  
    setof(Next, arcLN(NodeList, Next), NextList).  
arcLN(NodeList, Next) :- member(Node, NodeList),  
                           arc(Node, Next).
```

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```

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```

```
    arc(Node, Next).
```

```
goalD(NodeList) :- member(Node, NodeList), goal(Node).
```

```
searchD(NL) :- goalD(NL);
```

```
    (arcD(NL, NL2), searchD(NL2)).
```

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```

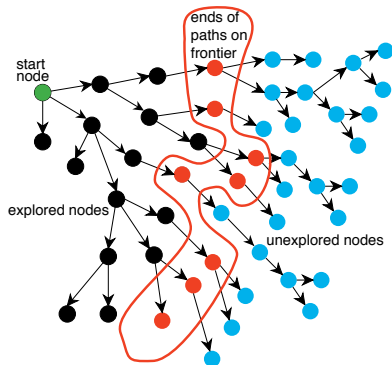
```
arcLN(NodeList, Next) :- member(Node, NodeList),  
                           arc(Node, Next).
```

```
goalD(NodeList) :- member(Node, NodeList), goal(Node).
```

```
searchD(NL) :- goalD(NL);  
               (arcD(NL, NL2), searchD(NL2)).
```

```
search(Node) :- searchD([Node]).
```

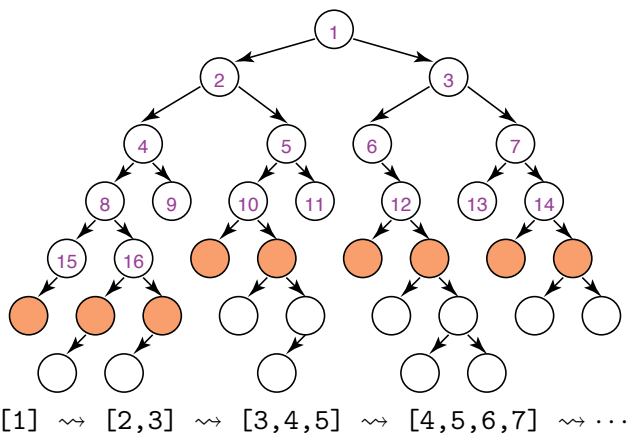
Frontier search



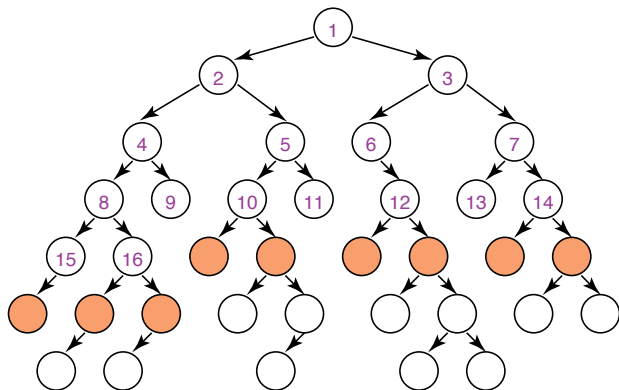
Poole & Mackworth

```
search(Node) :- frontierSearch([Node]).  
frontierSearch([Node|_]) :- goal(Node).  
frontierSearch([Node|Rest]) :-  
    findall(Next, arc(Node,Next), Children),  
    add2frontier(Children,Rest,NewFrontier),  
    frontierSearch(NewFrontier).
```


Breadth-first: queue (FIFO)



Breadth-first: queue (FIFO)

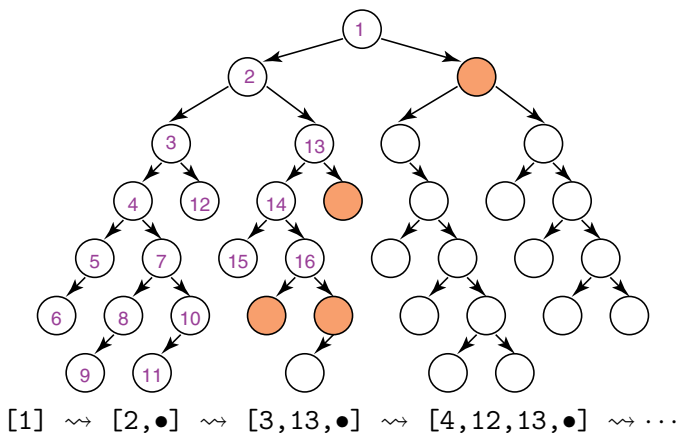


$[1] \rightsquigarrow [2,3] \rightsquigarrow [3,4,5] \rightsquigarrow [4,5,6,7] \rightsquigarrow \dots$

```
add2frontier(Children, [], Children).
```

```
add2frontier(Children, [H|T], [H|More]) :-  
    add2frontier(Children, T, More).
```

Depth-first: stack (LIFO)



If-then-else and cut !

$i :- p, !, q.$

$i :- r.$

$p.$

$r.$

$| \text{ ?- } i.$

If-then-else and cut !

i :- p,!,q. [i]

i :- r.

p.

r.

| ?- i.

If-then-else and cut !

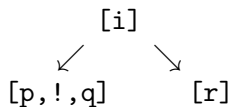
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`i :- r.`

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`r.`

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If-then-else and cut !

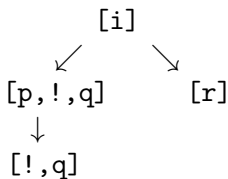
`i :- p,!,q.`

`i :- r.`

`p.`

`r.`

`| ?- i.`



Cut ! is true but destroys backtracking.

If-then-else and cut !

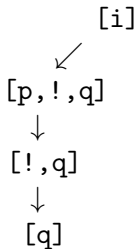
`i :- p,!,q.`

`i :- r.`

`p.`

`r.`

`| ?- i.`



Cut ! is true but destroys backtracking.

If-then-else and cut !

i :- p,!,q.

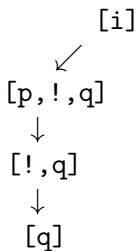
i :- r.

p.

r.

| ?- i.

no



Cut ! is true but destroys backtracking.

Review: Depth-first as frontier search

```
prove([],_).      % goal([]).  
prove(Node,KB) :- arc(Node,Next,KB), prove(Next,KB).
```

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prove([],_).      % goal([]).  
prove(Node,KB) :- arc(Node,Next,KB), prove(Next,KB).
```

```
fs([[]|_],_).
```

```
fs([Node|More],KB) :- findall(X,arc(Node,X,KB),L),  
                      append(L,More,NewFrontier),  
                      fs(NewFrontier,KB).
```

Review: Depth-first as frontier search

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                      fs(NewFrontier,KB).
```

Cut?

Tracking the frontier

[[i]]

i :- p,!,q.

[i]

i :- r.

p.

r.

| ?- i.

Tracking the frontier

$[[i]] \rightsquigarrow [[p,!,q],[r]]$

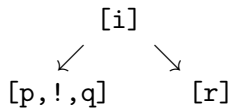
$i :- p,!,q.$

$i :- r.$

$p.$

$r.$

$| \text{?- } i.$



Tracking the frontier

$$[[i]] \rightsquigarrow [[p,!,q],[r]] \rightsquigarrow [[!,q],[r]]$$

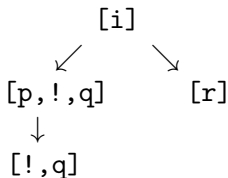
`i :- p,!,q.`

`i :- r.`

`p.`

`r.`

`| ?- i.`



Tracking the frontier

$$[[i]] \rightsquigarrow [[p,!,q],[r]] \rightsquigarrow [[!,q],[r]] \rightsquigarrow [[q]]$$

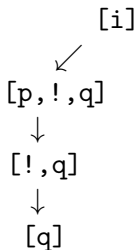
i :- p,!,q.

i :- r.

p.

r.

| ?- i.



Tracking the frontier

$$[[i]] \rightsquigarrow [[p,!,q],[r]] \rightsquigarrow [[!,q],[r]] \rightsquigarrow [[q]] \rightsquigarrow []$$

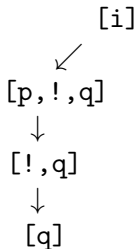
`i :- p,!,q.`

`i :- r.`

`p.`

`r.`

`| ?- i.`



Tracking the frontier

$$[[i]] \rightsquigarrow [[p,!,q],[r]] \rightsquigarrow [[!,q],[r]] \rightsquigarrow [[q]] \rightsquigarrow []$$

`i :- p,!,q.`

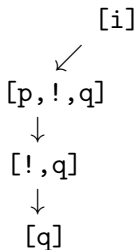
`i :- r.`

`p.`

`r.`

`| ?- i.`

`no`



Cut via frontier depth-first search

```
fs([],_).
```

```
fs([Node|More],KB) :-  
    findall(X,arc(Node,X,KB),L),  
    append(L,More,NewFrontier),  
    fs(NewFrontier,KB).
```

Cut via frontier depth-first search

```
fs([],_).
```

```
fs([[cut|T]|_],KB)) :- fs([T],KB).
```

```
fs([Node|More],KB) :-
```

```
    findall(X,arc(Node,X,KB),L),  
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```

Cut via frontier depth-first search

```
fs([],_).
```

```
fs([[cut|T]|_],KB) :- fs([T],KB).
```

```
fs([Node|More],KB) :- Node = [H|_], H\== cut,  
                        findall(X,arc(Node,X,KB),L),  
                        append(L,More,NewFrontier),  
                        fs(NewFrontier,KB).
```

Cut via frontier depth-first search

```
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```

```
if(p,q,r) :- (p,!,q); r.           % contra (p,q);r
```

Cut via frontier depth-first search

```
fs([],_).
```

```
fs([cut|T|_],KB) :- fs(T,KB).
```

```
fs([Node|More],KB) :- Node = [H|_], H \== cut,  
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                        append(L,More,NewFrontier),  
                        fs(NewFrontier,KB).
```

```
if(p,q,r) :- (p,!,q); r.           % contra (p,q);r
```

```
negation-as-failure(p) :- (p,!,fail); true.
```