

**MAU22C00: TUTORIAL 10 PROBLEMS**  
**GRAPH THEORY**

- 1) Let  $(V, E)$  be the graph with vertices  $a, b, c, d$ , and  $e$  and edges  $ab, bd, be, ac, cd$ , and  $ae$ .
- (a) Draw this graph. Write down its incidence table and its incidence matrix.
  - (b) Write down this graph's adjacency table and its adjacency matrix.
  - (c) Is this graph complete? Justify your answer.
  - (d) Is this graph bipartite? Justify your answer.
  - (e) Is this graph regular? Justify your answer.
  - (f) Does this graph have any regular subgraph? Justify your answer.
  - (g) Give an example of an isomorphism from the graph  $(V, E)$  specified at the beginning of this problem to the graph  $(V', E')$  with vertices  $p, q, r, s$ , and  $t$ , and edges  $pq, ps, rt, st, rs$ , and  $rq$ .