

12x20 w x-220 w x+1=0

X=0 w x-2 w x=-1

So- He (nticl points are
-1,0,2

properts

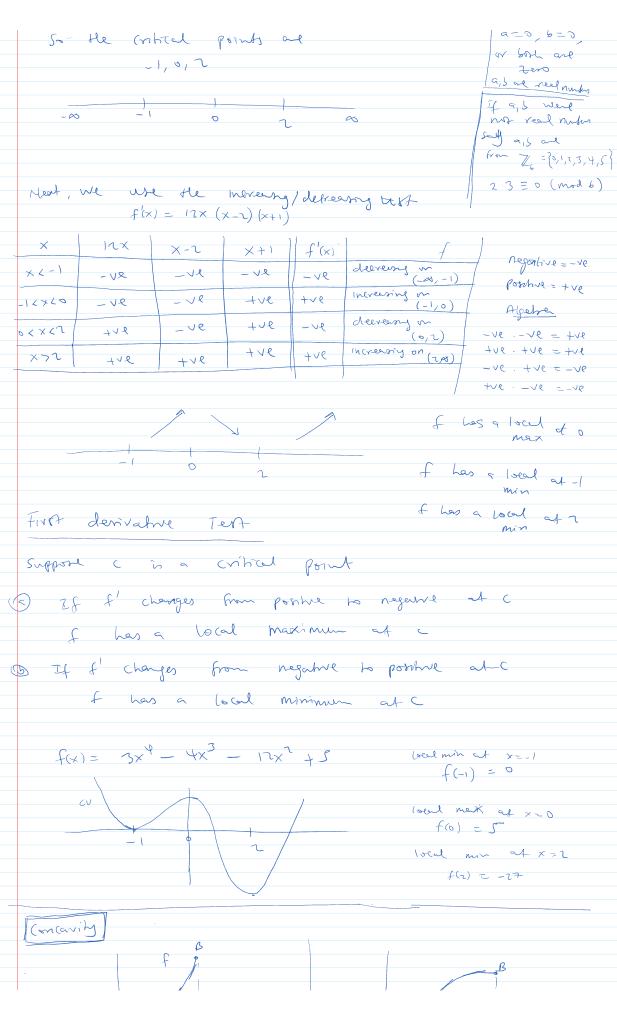
If a.b = 0

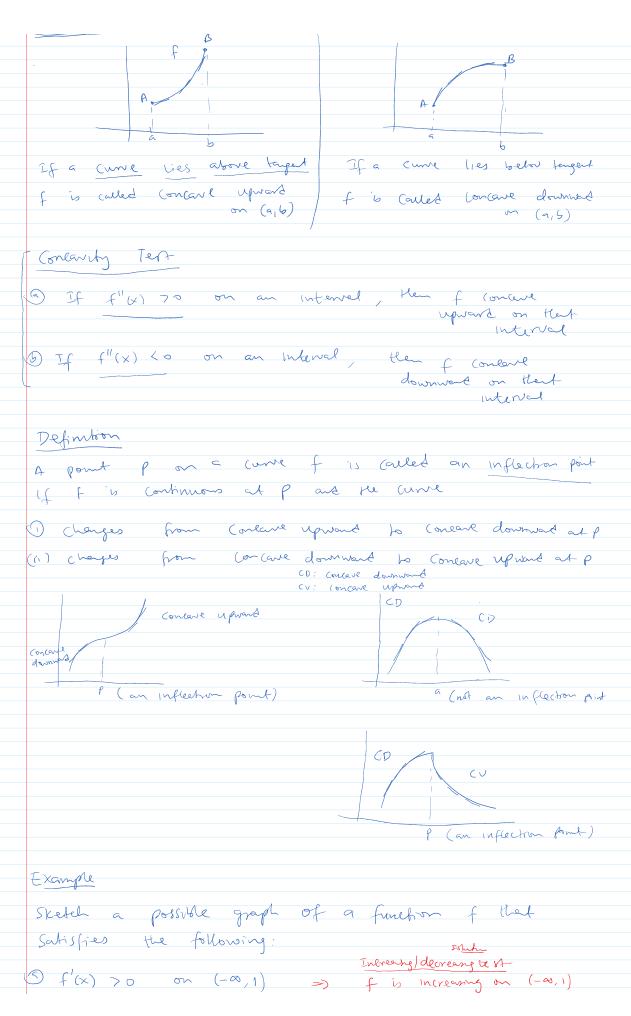
then even

a=0, b=0

or both are

zero





f'(x) < 0 or $(1, \infty)$ f is decreasing on (1,0) Concarry test (5) f''(x) > 0 on $(-\infty, -1)$, $(1, \infty)$ f is concare upward on $f''(x) \langle 0 \rangle$ on (-2,2)(-0,-1), (1,0) f is concave downward on (-1,7) Kayode Olumovin at 11/3/2020 8 14 AM O lim f(x) = -2 and lim f(x) = 0f has Horizontal asymptote live: y = -2 of has Horizontal asymptote line: y=0 - he; y=-2 Second derivative Ten Recall Fenant's Themen (convert of the Fernat's theorem) If f her a local mon/max + an additional condition) at c then c is a critical point () If f(c) = 0, f(c) > 0 Her (f(cc) = 0) f her a local min at C labour of Jenet Thans (b) If f'(c)=0, f"(c)<0 then If f'(1)=0, then f has f has a local max at C f does not have The Second derivative test is inconclusive when f"(c) = 0 Example DISCUSS the Curve $y = x^{4} - 4x^{3}$ With respect to concernty, point of inflection, local max/min Solution $\frac{\text{Solution}}{f(x)} = x^4 - 4x^3$ $f(x) = x - 4x^3$ f(x) = -

 $f'(x) = 4x^3 - 12x^2 = 4x^2(x-3)$

$$f''(x) = 12x^{2} - 24x = 12x (x-2)$$
Next find the central points
$$54t \quad f'(x) = 0 , \text{ sowe for } x$$

$$f'(x) = 4x^{2} (x-3) = 0$$

$$4x^{2} = 0 \text{ or } x-3 = 0$$

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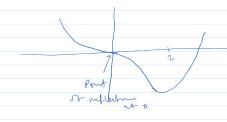
 $f'(x) = \frac{4x^{2}(x-3)}{x}$ $\frac{x}{x} = \frac{4x^{2}(x-3)}{x} = \frac{4x^{2}(x-3)}{x}$ $\frac{x}{x} = \frac{4x^{2}(x-3)}{x} = \frac{4x^{2}(x-3)}{x} = \frac{4x^{2}(x-3)}{x}$ $\frac{x}{x} = \frac{4x^{2}(x-3)}{x} = \frac{4x^{$

fil(x) = 11x(x-2) = 0 x=0 or 2

Interval	12×	X-1	f"(x)	
(-00,0)	-12	- 12	1-16	
(0,2)	+12	-18	-12	
(γ, ∞)	+12	tue 1	416	

(areanty tent $f''(x) 70 \text{ on } (-\alpha, 0), \text{ (solarly on } (-\alpha, 0), \text{ upword on } (-\alpha, 0), \text{ upword on } (-\alpha, 0), \text{ on }$

on (2,00)



Exercial

Sketch the graph $f(x) = x^{1/3} (6-x)^{1/3}$

Solution

$$f'(x) = \frac{4-x}{x''^3(6-x)^{3/3}}$$
 $f''(x) = \frac{-8}{x^{4/3}(6-x)^{5/3}}$

Set
$$f(x) = \frac{4-x}{x^{1/3}(6-x)^{4/3}} = 0$$

We get X = Y (control point) If f'(c) = 0

Sme f'(6) DNE, X=0 is also a control f'(1) DNE

$$f'(x) = \frac{4-x}{x^{1/3}(6-x)^{3/3}}$$

$$f'(6) = \frac{4-6}{6^{13} \cdot (6-6)^3} = -\frac{7}{0}$$
 DNE

		14	-,		
×	4-x	× V3	((-x) ⁴³	f (x)	T T
× <o< th=""><th>tve</th><th>- 12</th><th>+46</th><th>-12</th><th>deer on (-00,0)</th></o<>	tve	- 12	+46	-12	deer on (-00,0)
OCXCA	tve	+18	476	+40	Iner on (0,4)
4 L X L L	-VR	+16	+ve	-16	deer on (4,6)
X76	-72	+76	+76	-16	decr on (6,00)
			1	1	

decr = decreasing

Incr = Increasing

c ba entical

$$f(x) = x^{1/3} (6-x)^{1/3}$$

using the first derivative test

@ of changes from -ve to the near o , f(0) = 0 is a

Of does not charge 81gm at 6 so there is no min (mex of 6

$$f''(x) = \frac{x^{4/3} (6-x)^{5/3}}{-8}$$

we observe that that × 4/3 7 0

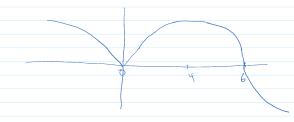
(Cure lies below target)

If counder X(0, f"(x) (0 [(mrail down a d

If counder $\times \langle 0 \rangle$, $f''(x) \langle 0 \rangle$, f (on case downward on $(-\infty,0)$)

If counder $0 \langle \times \langle 6 \rangle$, $f''(x) \langle 0 \rangle$, f (one are downward on (0,6))

If counder $\times \times b$, $f''(x) \wedge b$, f (one are target) (0,6)



 $f(x) = x^{1/3} (6-x)^{1/3}$

(L'HOSPITAL)
4.4 Indeterminate forms an L'Hôpital's rule

L'Hôpital Rule

Suppose f, g are differentiable, g'(x) to on an open interval I that contains a

Support lin fox) = 0 and lin g(x) = 0

xig

or that

or that $\lim_{x \to a} f(x) = \pm \infty$ and $\lim_{x \to a} g(x) = \pm \infty$

then $\frac{f(x)}{(x-)a} = \frac{f(x)}{f(x)} = \frac{f'(x)}{(x-)a}$ $\frac{f(x)}{f(x)} = \frac{f'(x)}{(x-)a}$

Explanation

G
$$\lim_{x \to 1} \frac{x^2 - x}{x^2 - 1} = \lim_{x \to 1} \frac{x(x)}{(x+1)(x)} = \lim_{x \to 1} \frac{x}{x} = \frac{1}{2}$$

$$(9)$$
 $(in \frac{\sin(x)}{x})$ (since we get an indeterminent here)

we use (145 pool rule

$$\lim_{x\to\infty} \frac{\sin(x)}{x} = \lim_{x\to\infty} \frac{4}{4}(\operatorname{sm}(x)) = \lim_{x\to\infty} \frac{(\operatorname{od}(x))}{1} = (\operatorname{od}(x))$$