

# Macroscopic Geometric Resonance: The Case of the Water Molecule ( $H_2O$ )

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## Abstract

Previous applications of the geometric mass scaling law  $m(n) = m_e(n/2)^2$  have focused on fundamental particles. This brief note extends the theory to composite molecular structures. We demonstrate that the water molecule ( $H_2O$ ) behaves as a coherent geometric resonance, corresponding to the integer quantum number  $n = 362$  with an accuracy of **99.8%**.

## 1 Methodology

To test if composite matter adheres to the harmonic scaling law, we calculate the integer  $n$  required to reproduce the rest mass of a single water molecule.

### 1.1 Experimental Target Mass

The molar mass of water ( $H_2O$ ) is approximately 18.015 unified atomic mass units (u). We convert this to the energy scale (MeV) used in our quantum geometric formula.

- Mass of  $H_2O$ : 18.015 u
- Conversion Factor: 1 u  $\approx$  931.494 MeV

$$M_{exp} = 18.015 \times 931.494 \approx \mathbf{16,781} \text{ MeV} \quad (1)$$

### 1.2 Geometric Calculation

We solve the fundamental scaling equation for  $n$ :

$$m(n) = m_e \times \left(\frac{n}{2}\right)^2 \implies n = 2 \times \sqrt{\frac{M_{exp}}{m_e}} \quad (2)$$

Substituting the values ( $m_e = 0.511 \text{ MeV}$ ):

$$n = 2 \times \sqrt{\frac{16,781}{0.511}}$$

$$n = 2 \times \sqrt{32,839.5}$$

$$n = 2 \times 181.21$$

$$n \approx 362.43$$

The geometry constrains the system to the nearest integer resonance:  $n = 362$ .

## 2 Verification

We calculate the theoretical mass of a pure  $n = 362$  resonance to compare with the experimental value.

$$m(362) = 0.511 \times \left(\frac{362}{2}\right)^2 = 0.511 \times (181)^2 \quad (3)$$

$$m(362) = 0.511 \times 32,761$$

$$M_{theo} = \mathbf{16,741} \text{ MeV} \quad (4)$$

## 3 Conclusion

- **Experimental Mass:** 16,781 MeV
- **Predicted Mass ( $n = 362$ ):** 16,741 MeV
- **Accuracy:** 99.8%

This result suggests that the geometric quantization of spacetime is not limited to subatomic particles but scales upward to stabilize molecular structures. The water molecule represents a coherent  $n = 362$  standing wave on the metric.