

Assignment 1

1 Question 1

1.1 Part a

- Input:

```
#include<stdio.h>
#include<math.h>

double f(double x)
{
    return 1 / (1+x);
}

int main()
{
    double x, a, b, h, exact, ans, trap();
    int i, n, iter, ITERMAX;

    exact = log((double) 2);
    ITERMAX= 8;
    b = 1.0;
    a = 0;

    printf ("          h          ans          (exact - ans)/h^2 \n");
    n=1;

    for (iter = 0; iter < ITERMAX; iter++) {
        h = (b - a) / n;
        ans = trap (f, a, b, n);
        n *= 2;
        printf ("%12.5f %12.5f%12.5f \n", h, ans, (ans-exact)/(h*h));
    }
}
```

- Output:

h	ans	(exact - ans)/h^2
1.00000	0.75000	0.05685
0.50000	0.70833	0.06074
0.25000	0.69702	0.06203
0.12500	0.69412	0.06238
0.06250	0.69339	0.06247
0.03125	0.69321	0.06249
0.01562	0.69316	0.06250
0.00781	0.69315	0.06250

1.2 Part b

$$-\frac{1}{12}[f'(b) - f'(a)] = -\frac{1}{12}[-.25 + 1] = .06245 = \frac{I - T}{h^2}$$

Therefore, the constant that h approached in part (a) corresponds to the coefficient of the leading error in the trapezium rule.

2 Question 2