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Question2:

First let's sort N P and Q to get

The skill level of worker x_i in increasing order: it takes $N \log N$

The most required skill level p_j in decreasing order: it takes $P \log P$

The least required skill level q_k in increasing order: it takes $Q \log Q$

Now it cost $N \log N + P \log P + Q \log Q$ time

Let $N \geq i \geq 1, P \geq j \geq 1, Q \geq k \geq 1$

First check N and Q from front to end, if x_i greater than q_k , and delete i th worker in N (if necessary also can delete k th job in Q) to record that worker found a job. Then move to x_{i+1} and q_{k+1} .

Once x_i less than or equals to q_k , move to x_{i+1} and compare x_{i+1} with q_k and so on, in the worst case it takes $N+Q$ time

After that check P from front to end and N from end to front,

If x_i less than or equals to p_j , delete i th worker in N (if necessary also can delete j th job in p) to record this worker found a job, Then move to x_{i-1} and p_{j+1} .

Once x_i greater than p_j , move to x_{i-1} and compare x_{i-1} with p_j and so on, in the worst case it takes $N+P$ time

It totally takes $N \log N + P \log P + Q \log Q + N + P + N + Q$ time

Which is equals to $N \log N + P \log P + Q \log Q$

finished