Jin-Ao Olson Zhang Z5211414 Question2:

Suppose we have M roads from warehouses to shops, lets sort all the roads by their time cost di Complexity O(M log(M))

First create a biparite graph,let n warehouse and n shops be the vertices (all warehouses in the sam side and shops in the other side)

For every road i from warehouse j to shop k, link an edge from warehouse j to shop k, edge cost is di.

Create a super source linked to all the warehouses ,only one truck located at one warehouse, ci = 1.

Create a super sink linked to all the shops ,ci = 1

Let di = dm first

- 1. If their exit a road j has dj < di, cj = 1 else cj = 0
- 2. Use max-flow algorithm to find the max-flow, if max-flow == n,which means time dican send all the trucks to all the shops,but that time may not be the shortest cost.
- 3. Use binary search to get the next di and repeated step 1,2 until find the smallest time
- 4. That time is the shortest time until all shops are supplied

Complexity max-flow algorithm * binary search = $O(n^3)$ * $O(log(M)) = O(n^3 log(M))$

Total time complexity $O(M \log(M)) + O(n^3 \log(M))$