

Zhang Jin-Ao Olson

Z5211414

Question 4:

To make sure Use the minimum number of stack to ensure that the conditions are met

Just need to make sure $A[i]+1 = A[i+1]$ for $n > i \geq 1$ which will met $A[i] < A[i+1]$

And for $A[1]$ and $A[2]$, In order to meet the conditions and save stacks, $A[1] = 1$ and $A[2] = 2$ is optimum(Let's say the first pile can't be zero) $A[3]$ need to = 3 and $A[4]$ need to = 4 and so on.

In order to satisfy this condition $A[1]+A[2]+\dots+A[i]$ must greater than or equals to $(i+i-1+i-2+\dots+2+1+0)$ which is $(i-1)*i/2$ for $A[i]$

So the process is, from front to end, check if $A[1]+A[2]+\dots+A[i]$ greater than or equals to $(i-1)*i/2$, it takes $O(1)$ and if satisfy, move to $A[i+1]$ until $i = n$

Else,such movements not exist. In the worst case it will take $O(n)$ time

Total cost is $O(1) * O(n) = O(n)$