

### Question5

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(a)  $f'(n) = 1/n \cdot \ln 2 = 0$

$$g'(n) = 1/10 \cdot n^{(9/10)}$$

$$\lim_{n \rightarrow \infty} f'(n)/g'(n) = \lim_{n \rightarrow \infty} (10 \cdot n^{(-1/10)}) / \ln 2 = 0$$

which means after a certain point  $f(n)$  will always be smaller than  $g(n)$

**so  $f(n) = O(g(n))$**

(b)

$$f'(n) = n^n \cdot (\ln(n) + 1)$$

$$g'(n) = 2n^{2n} \cdot (\ln(n) + 1)$$

$$\lim_{n \rightarrow \infty} f'(n)/g'(n) = \lim_{n \rightarrow \infty} 1/2n^n = 0$$

which means after a certain point  $f(n)$  will always be smaller than  $g(n)$

**so  $f(n) = O(g(n))$**

(c)

$$f(n) = n^{(1+\sin(\pi \cdot n))} = n \cdot n^{(\sin(\pi \cdot n))} \text{ since } n \text{ is an integer so } \sin(\pi \cdot n) = 0$$

$$= n \cdot n^0 = n \cdot 1 = n$$

$$f(n) = g(n) = n$$

**so  $f(n) = \Theta(g(n))$**