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In [26]: # ISMET OKAN CELIK CWID:10472265
         # Homework-6
In [41]: import numpy as np
         def matrix_factor(R, P, Q, K, steps, alpha, beta):
             for step in range(steps):
                 for i in range(len(R)):
                     for j in range(len(R[i])):
                         if R[i][j] > 0:
                             error = R[i][j] - np.dot(P[i,:],Q[:,j])
                             for k in range(K):
                                  Gradient1=(2 * error * Q[k][j] - beta * P[i][k])
                                  Gradient2=(2 * error * P[i][k] - beta * Q[k][j])
                                  P[i][k] = P[i][k] + alpha * Gradient1
                                  Q[k][j] = Q[k][j] + alpha * Gradient2
             return P,Q
In [61]: R=np.array([[5,3,0,1],
                     [4,0,0,1],
                     [1,1,0,5],
                     [1,0,0,4],
                     [0,1,5,4]
         nRow, nCol =np.shape(R)
         P=np.random.rand(nRow,K)
         Q=np.random.rand(K,nCol)
         steps=5000
         alpha=0.0002
         beta=0.02
         nP,nQ=matrix_factor(R,P,Q,K,steps,alpha,beta)
In [62]: np.dot(nP,nQ)
Out[62]: array([[5.01251503, 2.88358879, 5.72358085, 0.99841092],
                [3.9491545 , 2.27711736, 4.65029273, 0.99747176],
                [1.09429696, 0.74789197, 4.42288605, 4.96644042],
                [0.95405708, 0.64318265, 3.61845706, 3.97441095],
                [2.17053854, 1.33833387, 4.8824778 , 4.02962678]])
In [63]: R
Out[63]: array([[5, 3, 0, 1],
                [4, 0, 0, 1],
                [1, 1, 0, 5],
                [1, 0, 0, 4],
                [0, 1, 5, 4]])
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In [58]: R=np.array([[4,3,0,1,2],
                      [5,0,0,1,0],
                      [1,2,1,5,4],
                      [1,0,0,4,0],
                      [0,1,5,4,0],
                     [5,5,0,0,1]])
         nRow, nCol =np.shape(R)
         P=np.random.rand(nRow,K)
         Q=np.random.rand(K,nCol)
         steps=10000
         alpha=0.0002
         beta=0.02
         nP,nQ=matrix_factor(R, P, Q, K, steps, alpha, beta)
In [59]: np.dot(nP,nQ)
Out[59]: array([[4.00393279, 2.96801337, 3.3495112 , 1.03261157, 1.96057978],
                 [4.97648818, 3.50768434, 4.27513264, 0.99350213, 2.29336459],
                 [1.00426565, 1.98493593, 1.01274581, 4.96844592, 3.98101392],
                 [0.99672298, 1.43692215, 1.30237308, 3.98485439, 3.44315635],
                 [2.96626042, 1.01373931, 4.97555751, 3.98072785, 5.2177704],
                 [4.97163129, 4.987712 , 2.43726713, 0.70521586, 1.01734922]])
In [60]: R
Out[60]: array([[4, 3, 0, 1, 2],
                 [5, 0, 0, 1, 0],
                 [1, 2, 1, 5, 4],
                 [1, 0, 0, 4, 0],
                 [0, 1, 5, 4, 0],
                [5, 5, 0, 0, 1]])
 In [ ]:
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