## Problem 1

```
Original Grammar:
                            main { <stmts> }
   cprogram>
    <stmts>
                            <stmt>;
                            <stmt>; <stmts>
    <stmt>
                            <var> = <expr>
    <expr>
                            <term> + <term>
                    \rightarrow
                            <term> - <term>
                            <term>
                            <var> | const
    <term>
                            a | b | c | d
    <var>
a) Augmented Grammar:
    <while>
                    \rightarrow
                            while (<stmt>) { <stmts> }
    <for>
                    \rightarrow
                            for (<stmt>; <stmt>) { <stmts> }
                    \rightarrow
                            <for>
    <stmts>
                    \rightarrow
                            <for> <stmts>
                            <while>
                            <while> <stmts>
                            <var> < <expr>
    <stmt>
b) Program 1:
    main
    {
            a = const;
            b = const;
            while (a < const)
```

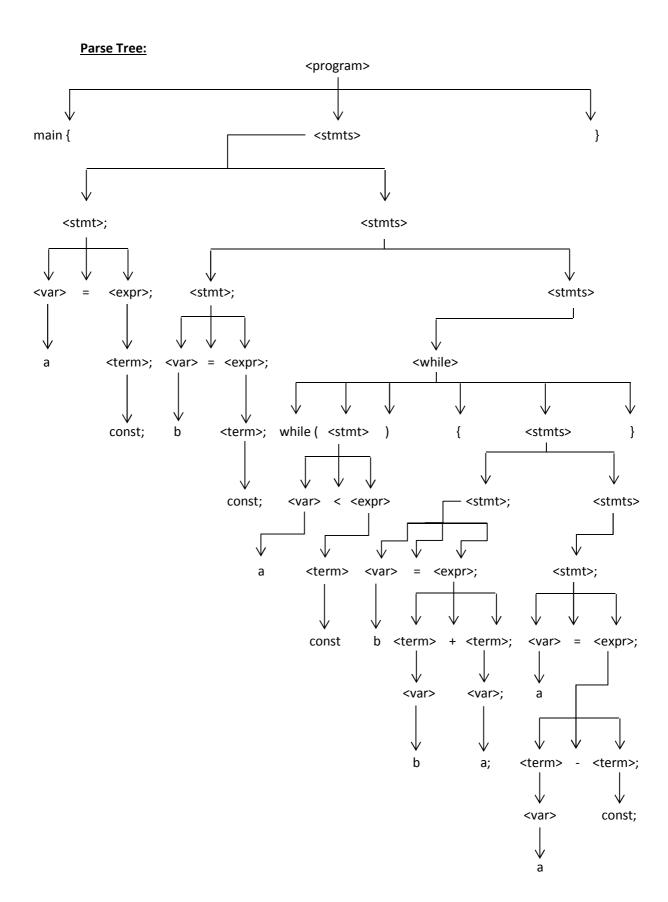
b = b + a; a = a – const;

}

}

## **Leftmost Derivation:**

```
main { <stmt>; <stmts> }
            → main { <var> = <expr>; <stmts> }
            → main { a = <expr>; <stmts> }
            → main { a = <term>; <stmts> }
            → main { a = const; <stmts> }
            → main { a = const; <stmt>; <stmts> }
            → main { a = const; <var> = <expr>; <stmts> }
            → main { a = const; b = <expr>; <stmts> }
            → main { a = const; b = <term>; <stmts> }
            → main { a = const; b = const; <stmts> }
            → main { a = const; b = const; <while> }
            → main { a = const; b = const; while (<stmt>) { <stmts> }}
            → main { a = const; b = const; while (<var> < <expr>) { <stmts> }}
            → main { a = const; b = const; while (a < <expr>) { <stmts> }}
            → main { a = const; b = const; while (a < <term>) { <stmts> }}
            → main { a = const; b = const; while (a < const) { <stmts> }}
            → main { a = const; b = const; while (a < const) { <stmt>; <stmts> }}
            → main { a = const; b = const; while (a < const) { <var> = <expr>; <stmts> }}
            → main { a = const; b = const; while (a < const) { b = <expr>; <stmts> }}
            → main { a = const; b = const; while (a < const) { b = <term> + <term>; <stmts> }}
            → main { a = const; b = const; while (a < const) { b = <var> + <term>; <stmts> }}
            → main { a = const; b = const; while (a < const) { b = b + <term>; <stmts> }}
            → main { a = const; b = const; while (a < const) { b = b + <var>; <stmts> }}
            → main { a = const; b = const; while (a < const) { b = b + a; <stmts> }}
            → main { a = const; b = const; while (a < const) { b = b + a; <stmt>; }}
            \rightarrow main { a = const; b = const; while (a < const) { b = b + a; <var> = <expr>; }}
            \rightarrow main { a = const; b = const; while (a < const) { b = b + a; a = <expr>; }}
            → main { a = const; b = const; while (a < const) { b = b + a; a = <term> + <term>; }}
            → main { a = const; b = const; while (a < const) { b = b + a; a = <term> - <term>; }}
            \rightarrow main { a = const; b = const; while (a < const) { b = b + a; a = <var> - <term>; }}
            \rightarrow main { a = const; b = const; while (a < const) { b = b + a; a = a - <term>; }}
            \rightarrow main
                {
                        a = const;
                        b = const;
                        while (a < const)
                        {
                                b = b + a;
                                a = a - const;
                        }
                }
```



```
Program 2:
main
{
        a = const;
        b = const;
        for (a = const; a < const; a = a - const)
                b = b + a;
        }
}
Leftmost Derivation:
→ main { <stmts> }
            → main { <stmt>; <stmts> }
            → main { <var> = <expr>; <stmts> }
            \rightarrow main { a = <expr>; <stmts> }
            → main { a = <term>; <stmts> }
            → main { a = const; <stmts> }
            → main { a = const; <stmt>; <stmts> }
            → main { a = const; <var> = <expr>; <stmts> }
            → main { a = const; b = <expr>; <stmts> }
            → main { a = const; b = <term>; <stmts> }
            → main { a = const; b = const; <stmts> }
            → main { a = const; b = const; <for> }
            → main { a = const; b = const; for (<stmt>; <stmt>) { <stmt>> } }
            → main { a = const; b = const; for (<var> = <expr>; <stmt>; <stmt>) { <stmts> } }
            → main { a = const; b = const; for (a = <expr>; <stmt>; <stmt>) { <stmts> } }
            → main { a = const; b = const; for (a = <term>; <stmt>; <stmt>) { <stmts> } }
            → main { a = const; b = const; for (a = const; <stmt>; <stmt>) { <stmts> } }
            → main { a = const; b = const; for (a = const; <var> < <expr>; <stmt>) { <stmts> } }
            → main { a = const; b = const; for (a = const; a < <expr>; <stmt>) { <stmts> } }
            → main { a = const; b = const; for (a = const; a < <term>; <stmt>) { <stmts> } }
            → main { a = const; b = const; for (a = const; a < const; <stmt>) { <stmts> }}
            → main { a = const; b = const; for (a = const; a < const; <var> = <expr>) { <stmts> }}
            → main { a = const; b = const; for (a = const; a < const; a = <expr>) { <stmts> } }
            → main {
                        a = const; b = const;
                        for (a = const; a < const; a = <term> - <term>) { <stmts> }
                }
            → main {
                        a = const; b = const;
                        for (a = const; a < const; a = <var> - <term>) { <stmts> }
                }
            → main {
                        a = const; b = const;
                        for (a = const; a < const; a = a - <term>) { <stmts> }
```

}

```
→ main {
             a = const; b = const;
             for (a = const; a < const; a = a - const) { <stmts> }
→ main {
             a = const; b = const;
             for (a = const; a < const; a = a - const) { <stmt>; }
    }
→ main {
             a = const; b = const;
             for (a = const; a < const; a = a - const) { <var> = <expr>; }
    }
→ main {
             a = const; b = const;
             for (a = const; a < const; a = a - const) { b = \langle expr \rangle; }
→ main {
             a = const; b = const;
             for (a = const; a < const; a = a - const) { b = <term> + <term>; }
    }
\rightarrow main {
             a = const; b = const;
             for (a = const; a < const; a = a - const) { b = <var> + <term>; }
    }
→ main {
             a = const; b = const;
             for (a = const; a < const; a = a - const) { b = b + <term>; }
→ main {
             a = const; b = const;
             for (a = const; a < const; a = a - const) { b = b + <var>; }
    }
\rightarrow main
  {
             a = const;
             b = const;
             for (a = const; a < const; a = a - const)
                      b = b + a;
             }
    }
```

