



Recommendation ITU-R P.676-11
(09/2016)

Attenuation by atmospheric gases

P Series
Radiowave propagation

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BS	Broadcasting service (sound)
BT	Broadcasting service (television)
F	Fixed service
M	Mobile, radiodetermination, amateur and related satellite services
P	Radiowave propagation
RA	Radio astronomy
RS	Remote sensing systems
S	Fixed-satellite service
SA	Space applications and meteorology
SF	Frequency sharing and coordination between fixed-satellite and fixed service systems
SM	Spectrum management
SNG	Satellite news gathering
TF	Time signals and frequency standards emissions
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Note: This ITU-R Recommendation was approved in English under the procedure detailed in Resolution ITU-R 1.

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RECOMMENDATION ITU-R P.676-11

Attenuation by atmospheric gases

(Question ITU-R 201/3)

(1990-1992-1995-1997-1999-2001-2005-2007-2009-2012-2013-2016)

Scope

This Recommendation provides methods to estimate the attenuation of atmospheric gases on terrestrial and slant paths using:

- a) an estimate of gaseous attenuation computed by a summation of individual absorption lines that is valid for the frequency range 1-1 000 GHz; and
- b) a simplified approximate method to estimate gaseous attenuation that is applicable in the frequency range 1-350 GHz.

Keywords: Gaseous absorption, specific attenuation, slant path attenuation, total attenuation, water vapour, oxygen, dry air

The ITU Radiocommunication Assembly,

considering

- a) the necessity of estimating the attenuation by atmospheric gases on terrestrial and slant paths,
- recommends*

1 that, for general application, the procedure in Annex 1 be used to calculate gaseous attenuation at frequencies up to 1 000 GHz;

2 that, for approximate estimates of gaseous attenuation in the frequency range 1-350 GHz, the computationally less intensive procedure given in Annex 2 is used.

Guide to this Recommendation

This Recommendation provides the following three methods of predicting the specific and path gaseous attenuation due to oxygen and water vapour:

- 1 Calculation of specific and path gaseous attenuation using the line-by-line summation in Annex 1 assuming the atmospheric pressure, temperature, and water vapour density vs. height;
- 2 An approximate estimate of specific and path gaseous attenuation in Annex 2 assuming the water vapour density at the surface of the Earth;
- 3 An approximate estimate of path attenuation in Annex 2 assuming the integrated water vapour content along the path.

These prediction methods can use local meteorological data, or, in the absence of local data, reference atmospheres or meteorological maps corresponding to a desired probability of exceedance that are provided in other ITU-R P-series Recommendations.

Specific attenuation

Annex 1 equation (1), which is applicable to frequencies up to 1 000 GHz, or the sum of Annex 2 equations (22) and (23), which is applicable to frequencies up to 350 GHz, may be used to predict specific attenuation. Both methods require the pressure, temperature, and water vapour density at the applicable location. If local data is not available, a combination of: a) the mean annual global

reference atmosphere given in Recommendation ITU-R P.835, b) the map of mean annual surface temperature in Recommendation ITU-R P.1510 and c) the maps of surface water vapour density vs. exceedance probability given in Recommendation ITU-R P.836 may be used in lieu of the standard ground-level surface water vapour density of 7.5 g/m^3 .

Slant path (Earth-space) attenuation

Annex 1 equation (20), or Annex 2 equations (28) or (29) may be used.

- Annex 1 equation (20) requires knowledge of the temperature, pressure, and water vapour density profiles along the path. If local profile data is not available, the reference atmospheric profiles given in Recommendation ITU-R P.835 may be used. The surface water vapour density vs. exceedance probability given in Recommendation ITU-R P.836 may be used in lieu of the standard ground-level surface water vapour density of 7.5 g/m^3 .
- Annex 2 equation (28) requires knowledge of the surface pressure, surface temperature, and surface water vapour density. Annex 2 equation (28) is an approximation to equation (20) applicable to frequencies up to 350 GHz assuming a mean annual global reference atmosphere and an arbitrary surface water vapour density with a negative exponential water vapour density profile vs. height. Annex 2 equation (28) can be used to predict: a) the instantaneous gaseous attenuation for a specific value of surface pressure, surface temperature, and surface water vapour density or b) the gaseous attenuation corresponding to the surface water vapour density at a desired probability of exceedance. If local surface water vapour density data is not available, the surface water vapour density maps in Recommendation ITU-R P.836 may be used.
- Annex 2 equation (29) requires knowledge of the surface temperature, surface pressure, and integrated water vapour content along the path. Similar to Annex 2 equation (28), Annex 2 equation (29) can be used to predict: a) the instantaneous gaseous attenuation for a specific value of surface pressure, surface temperature, and integrated water vapour content, or b) the gaseous attenuation corresponding to the integrated water vapour content at a desired probability of exceedance. If local surface integrated water vapour content data is not available, the integrated water vapour maps in Recommendation ITU-R P.836 may be used.

If local surface water vapour density and integrated water vapour content data are both available, Annex 2 equation (29) using local integrated water vapour content is considered to be more accurate than Annex 2 equation (28) using local surface water vapour density data. Similarly, if local data is not available, Annex 2 equation (29) using the maps of integrated water vapour content in Recommendation ITU-R P.836 is considered to be more accurate than Annex 2 equation (28) using the maps of surface water vapour density in Recommendation ITU-R P.836.

	Annex 1 Equation (20)	Annex 2 Equation (28)	Annex 2 Equation (29)
Frequency range	$\leq 1\,000 \text{ GHz}$	$\leq 350 \text{ GHz}$	
Accuracy	Best, line-by-line sum	Approximation	
Pressure vs. height	Arbitrary	Mean Annual Global Reference Atmospheric Profile	
Temperature vs. height			
Water vapour density vs. height		Surface value with negative exponential profile vs. height	Integrated water vapour content in lieu of water vapour density vs. height

Annex 1

Line-by-line calculation of gaseous attenuation

1 Specific attenuation

The specific attenuation at frequencies up to 1 000 GHz, due to dry air and water vapour, can be evaluated most accurately at any value of pressure, temperature and humidity by means of a summation of the individual resonance lines from oxygen and water vapour, together with small additional factors for the non-resonant Debye spectrum of oxygen below 10 GHz, pressure-induced nitrogen attenuation above 100 GHz and a wet continuum to account for the excess water vapour-absorption found experimentally. Figure 1 shows the specific attenuation using the prediction method, calculated from 0 to 1 000 GHz at 1 GHz intervals, for a pressure of 1 013.25 hPa, temperature of 15° C for the cases of a water-vapour density of 7.5 g/m³ (Standard) and a dry atmosphere (Dry).

Near 60 GHz, many oxygen absorption lines merge together at sea-level pressures to form a single, broad absorption band, which is shown in more detail in Fig. 2. This figure also shows the oxygen attenuation at higher altitudes, with the individual lines becoming resolved as the pressure decreases with increasing altitude. Some additional molecular species (e.g. oxygen isotopic species, oxygen vibrationally excited species, ozone, ozone isotopic species, and ozone vibrationally excited species, and other minor species) are not included in the line-by-line prediction method. These additional lines are insignificant for typical atmospheres, but may be important for a dry atmosphere.

For quick and approximate estimates of specific attenuation at frequencies up to 350 GHz, in cases where high accuracy is not required, simplified algorithms are given in Annex 2 for restricted ranges of meteorological conditions.

The specific gaseous attenuation is given by:

$$\gamma = \gamma_o + \gamma_w = 0.1820f \left(N''_{Oxygen}(f) + N''_{WaterVapour}(f) \right) \quad (\text{dB/km}) \quad (1)$$

here γ_o and γ_w are the specific attenuations (dB/km) due to dry air (oxygen, pressure-induced nitrogen and non-resonant Debye attenuation) and water vapour, respectively, f is the frequency (GHz), and $N''_{Oxygen}(f)$ and $N''_{Water Vapour}(f)$ are the imaginary parts of the frequency-dependent complex refractivities:

$$N''_{Oxygen}(f) = \sum_i (Oxygen) S_i F_i + N''_D(f) \quad (2a)$$

$$N''_{Water Vapour}(f) = \sum_i (Water Vapour) S_i F_i \quad (2b)$$

S_i is the strength of the i -th oxygen or water vapour line, F_i is the oxygen or water vapour line shape factor, and the summations extend over all the lines in Tables 1 and 2;

$N''_D(f)$ is the dry continuum due to pressure-induced nitrogen absorption and the Debye spectrum as given by equation (8).

The line strength is given by:

$$\begin{aligned} S_i &= a_1 \times 10^{-7} p \theta^3 \exp [a_2 (1 - \theta)] && \text{for oxygen} \\ &= b_1 \times 10^{-1} e \theta^{3.5} \exp [b_2 (1 - \theta)] && \text{for water vapour} \end{aligned} \quad (3)$$

where:

p : dry air pressure (hPa)

e : water vapour partial pressure (hPa) (total barometric pressure, $p_{tot} = p + e$)

$\theta = 300/T$

T : temperature (K).

FIGURE 1

Specific attenuation due to atmospheric gases, calculated at 1 GHz intervals, including line centres

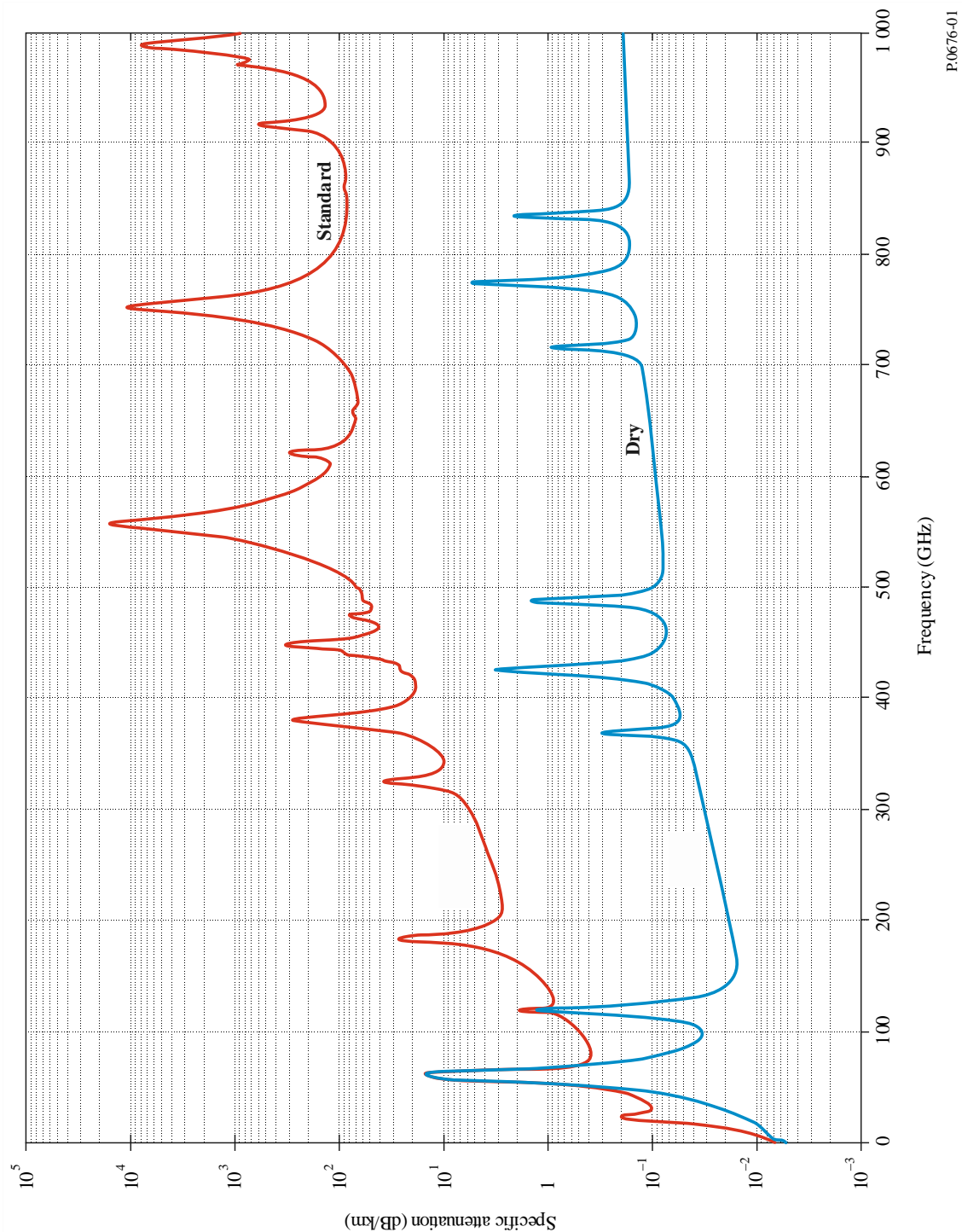
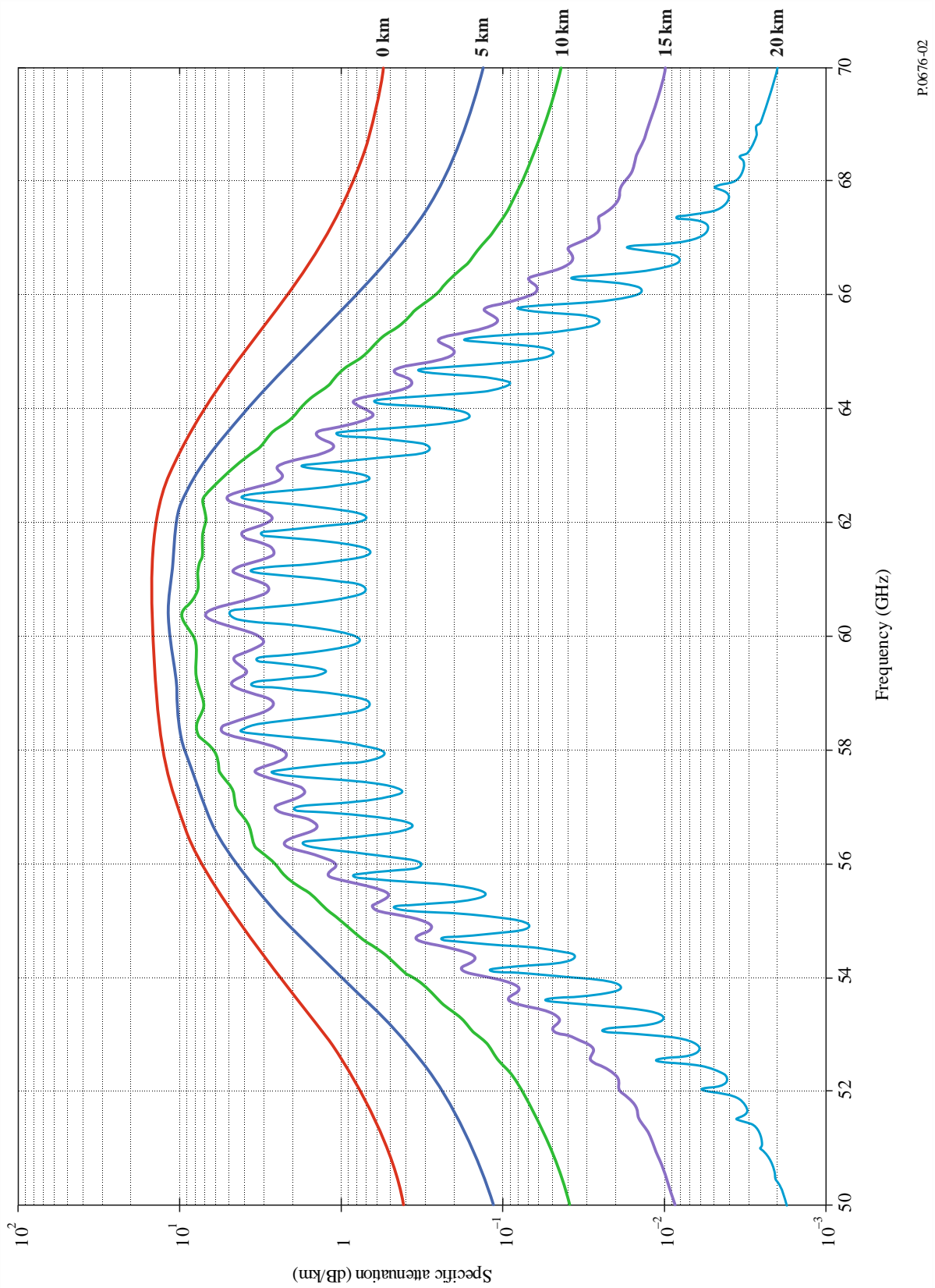


FIGURE 2

Specific attenuation in the range 50-70 GHz at the altitudes indicated, calculated at intervals of 10 MHz, including line centres (0 km, 5 km, 10 km, 15 km and 20 km)



If available, local altitude profiles of p , e and T (e.g. using radiosondes) should be used. In the absence of local information, a reference standard atmosphere given in Recommendation ITU-R P.835 should be used. (Note that where total atmospheric attenuation is being calculated, the same-water vapour partial pressure is used for both dry-air and water-vapour attenuations.)

The water-vapour partial pressure, e , at an altitude may be obtained from the water-vapour density, ρ , and the temperature, T , at that altitude using the expression:

$$e = \frac{\rho T}{216.7} \quad (4)$$

Spectroscopic data for oxygen is given in Table 1, and spectroscopic data for water vapour is given in Table 2. The last entry in Table 2 is a pseudo-line centred at 1 780 GHz whose lower wing represents the combined contribution below 1 000 GHz of water-vapour resonances not included in the line-by-line prediction method (i.e. the wet continuum). The pseudo-line's parameters are adjusted to account for the difference between the measured absorption in the atmospheric windows and the calculated local-line absorption.

The line-shape factor is given by:

$$F_i = \frac{f}{f_i} \left[\frac{\Delta f - \delta(f_i - f)}{(f_i - f)^2 + \Delta f^2} + \frac{\Delta f - \delta(f_i + f)}{(f_i + f)^2 + \Delta f^2} \right] \quad (5)$$

where f_i is the oxygen or water vapour line frequency and Δf is the width of the line:

$$\begin{aligned} \Delta f &= a_3 \times 10^{-4} (p \theta^{(0.8 - a_4)} + 1.1 e \theta) && \text{for oxygen} \\ &= b_3 \times 10^{-4} (p \theta^{b_4} + b_5 e \theta^{b_6}) && \text{for water vapour} \end{aligned} \quad (6a)$$

The line width Δf is modified to account for Zeeman splitting of oxygen lines and Doppler broadening of water vapour lines:

$$\begin{aligned} \Delta f &= \sqrt{\Delta f^2 + 2.25 \times 10^{-6}} && \text{for oxygen} \\ &= 0.535 \Delta f + \sqrt{0.217 \Delta f^2 + \frac{2.1316 \times 10^{-12} f_i^2}{\theta}} && \text{for water vapour} \end{aligned} \quad (6b)$$

δ is a correction factor that arises due to interference effects in oxygen lines:

$$\begin{aligned} \delta &= (a_5 + a_6 \theta) \times 10^{-4} (p + e) \theta^{0.8} && \text{for oxygen} \\ &= 0 && \text{for water vapour} \end{aligned} \quad (7)$$

TABLE 1
Spectroscopic data for oxygen attenuation

f_0	a_1	a_2	a_3	a_4	a_5	a_6
50.474214	0.975	9.651	6.690	0.0	2.566	6.850
50.987745	2.529	8.653	7.170	0.0	2.246	6.800
51.503360	6.193	7.709	7.640	0.0	1.947	6.729
52.021429	14.320	6.819	8.110	0.0	1.667	6.640
52.542418	31.240	5.983	8.580	0.0	1.388	6.526
53.066934	64.290	5.201	9.060	0.0	1.349	6.206
53.595775	124.600	4.474	9.550	0.0	2.227	5.085
54.130025	227.300	3.800	9.960	0.0	3.170	3.750
54.671180	389.700	3.182	10.370	0.0	3.558	2.654
55.221384	627.100	2.618	10.890	0.0	2.560	2.952
55.783815	945.300	2.109	11.340	0.0	-1.172	6.135
56.264774	543.400	0.014	17.030	0.0	3.525	-0.978
56.363399	1331.800	1.654	11.890	0.0	-2.378	6.547
56.968211	1746.600	1.255	12.230	0.0	-3.545	6.451
57.612486	2120.100	0.910	12.620	0.0	-5.416	6.056
58.323877	2363.700	0.621	12.950	0.0	-1.932	0.436
58.446588	1442.100	0.083	14.910	0.0	6.768	-1.273
59.164204	2379.900	0.387	13.530	0.0	-6.561	2.309
59.590983	2090.700	0.207	14.080	0.0	6.957	-0.776
60.306056	2103.400	0.207	14.150	0.0	-6.395	0.699
60.434778	2438.000	0.386	13.390	0.0	6.342	-2.825
61.150562	2479.500	0.621	12.920	0.0	1.014	-0.584
61.800158	2275.900	0.910	12.630	0.0	5.014	-6.619
62.411220	1915.400	1.255	12.170	0.0	3.029	-6.759
62.486253	1503.000	0.083	15.130	0.0	-4.499	0.844
62.997984	1490.200	1.654	11.740	0.0	1.856	-6.675
63.568526	1078.000	2.108	11.340	0.0	0.658	-6.139
64.127775	728.700	2.617	10.880	0.0	-3.036	-2.895
64.678910	461.300	3.181	10.380	0.0	-3.968	-2.590
65.224078	274.000	3.800	9.960	0.0	-3.528	-3.680
65.764779	153.000	4.473	9.550	0.0	-2.548	-5.002
66.302096	80.400	5.200	9.060	0.0	-1.660	-6.091
66.836834	39.800	5.982	8.580	0.0	-1.680	-6.393
67.369601	18.560	6.818	8.110	0.0	-1.956	-6.475
67.900868	8.172	7.708	7.640	0.0	-2.216	-6.545
68.431006	3.397	8.652	7.170	0.0	-2.492	-6.600
68.960312	1.334	9.650	6.690	0.0	-2.773	-6.650
118.750334	940.300	0.010	16.640	0.0	-0.439	0.079

TABLE 1 (*end*)

f_0	a_1	a_2	a_3	a_4	a_5	a_6
368.498246	67.400	0.048	16.400	0.0	0.000	0.000
424.763020	637.700	0.044	16.400	0.0	0.000	0.000
487.249273	237.400	0.049	16.000	0.0	0.000	0.000
715.392902	98.100	0.145	16.000	0.0	0.000	0.000
773.839490	572.300	0.141	16.200	0.0	0.000	0.000
834.145546	183.100	0.145	14.700	0.0	0.000	0.000

TABLE 2

Spectroscopic data for water-vapour attenuation

f_0	b_1	b_2	b_3	b_4	b_5	b_6
*22.235080	.1079	2.144	26.38	.76	5.087	1.00
67.803960	.0011	8.732	28.58	.69	4.930	.82
119.995940	.0007	8.353	29.48	.70	4.780	.79
*183.310087	2.273	.668	29.06	.77	5.022	.85
*321.225630	.0470	6.179	24.04	.67	4.398	.54
*325.152888	1.514	1.541	28.23	.64	4.893	.74
336.227764	.0010	9.825	26.93	.69	4.740	.61
*380.197353	11.67	1.048	28.11	.54	5.063	.89
390.134508	.0045	7.347	21.52	.63	4.810	.55
437.346667	.0632	5.048	18.45	.60	4.230	.48
439.150807	.9098	3.595	20.07	.63	4.483	.52
443.018343	.1920	5.048	15.55	.60	5.083	.50
*448.001085	10.41	1.405	25.64	.66	5.028	.67
470.888999	.3254	3.597	21.34	.66	4.506	.65
474.689092	1.260	2.379	23.20	.65	4.804	.64
488.490108	.2529	2.852	25.86	.69	5.201	.72
503.568532	.0372	6.731	16.12	.61	3.980	.43
504.482692	.0124	6.731	16.12	.61	4.010	.45
547.676440	.9785	.158	26.00	.70	4.500	1.00
552.020960	.1840	.158	26.00	.70	4.500	1.00
*556.935985	497.0	.159	30.86	.69	4.552	1.00

TABLE 2 (*end*)

f_0	b_1	b_2	b_3	b_4	b_5	b_6
620.700807	5.015	2.391	24.38	.71	4.856	.68
645.766085	.0067	8.633	18.00	.60	4.000	.50
658.005280	.2732	7.816	32.10	.69	4.140	1.00
*752.033113	243.4	.396	30.86	.68	4.352	.84
841.051732	.0134	8.177	15.90	.33	5.760	.45
859.965698	.1325	8.055	30.60	.68	4.090	.84
899.303175	.0547	7.914	29.85	.68	4.530	.90
902.611085	.0386	8.429	28.65	.70	5.100	.95
906.205957	.1836	5.110	24.08	.70	4.700	.53
916.171582	8.400	1.441	26.73	.70	5.150	.78
923.112692	.0079	10.293	29.00	.70	5.000	.80
970.315022	9.009	1.919	25.50	.64	4.940	.67
987.926764	134.6	.257	29.85	.68	4.550	.90
*1 780.000000	17506.	.952	196.3	2.00	24.15	5.00

The dry air continuum arises from the non-resonant Debye spectrum of oxygen below 10 GHz and a pressure-induced nitrogen attenuation above 100 GHz.

$$N_D''(f) = f p \theta^2 \left[\frac{6.14 \times 10^{-5}}{d \left[1 + \left(\frac{f}{d} \right)^2 \right]} + \frac{1.4 \times 10^{-12} p \theta^{1.5}}{1 + 1.9 \times 10^{-5} f^{1.5}} \right] \quad (8)$$

where d is the width parameter for the Debye spectrum:

$$d = 5.6 \times 10^{-4} (p + e) \theta^{0.8} \quad (9)$$

2 Path attenuation

2.1 Terrestrial paths

For a terrestrial path, or for slightly inclined paths close to the ground, the path attenuation, A , may be calculated as:

$$A = \gamma r_0 = (\gamma_o + \gamma_w) r_0 \quad \text{dB} \quad (10)$$

where r_0 is the path length (km).

2.2 Slant paths

This section provides a method to integrate the specific attenuation calculated using the line-by-line model given above, at different pressures, temperatures and humidities through the atmosphere. By

this means, the path attenuation for communications systems with any geometrical configuration within and external to the Earth's atmosphere may be accurately determined simply by dividing the atmosphere into horizontal layers, specifying the profile of the meteorological parameters pressure, temperature and humidity along the path. In the absence of local profiles, from radiosonde data, for example, the reference standard atmospheres given in Recommendation ITU-R P.835 may be used, either for global application or for low (annual), mid (summer and winter) and high latitude (summer and winter) sites.

Figure 3 shows the zenith attenuation calculated at 1 GHz intervals with this model for the global reference standard atmosphere given in Recommendation ITU-R P.835, with horizontal layers 1 km thick and summing the attenuations for each layer, for the cases of a moist atmosphere (Standard) and a dry atmosphere (Dry).

The total slant path attenuation, $A(h, \varphi)$, from a station with altitude, h , and elevation angle, φ , can be calculated as follows when $\varphi \geq 0$:

$$A(h, \varphi) = \int_h^\infty \frac{\gamma(H)}{\sin \Phi} dH \quad (11)$$

where the value of Φ can be determined as follows based on Snell's law in polar coordinates:

$$\Phi = \arccos \left(\frac{c}{(r+H) \times n(H)} \right) \quad (12)$$

where:

$$c = (r+h) \times n(h) \times \cos \varphi \quad (13)$$

where $n(h)$ is the atmospheric radio refractive index, calculated from pressure, temperature and water-vapour pressure along the path (see Recommendation ITU-R P.835) using equations (1) and (2) of Recommendation ITU-R P.453.

When $\varphi < 0$, there is a minimum height, h_{min} , at which the radio beam becomes parallel with the Earth's surface. The value of h_{min} can be determined by solving the following transcendental equation:

$$(r+h_{min}) \times n(h_{min}) = c \quad (14)$$

This can be easily solved by repeating the following calculation, using $h_{min} = h$ as an initial value:

$$h'_{min} = \frac{c}{n(h_{min})} - r \quad (15)$$

Therefore, $A(h, \varphi)$ can be calculated as follows:

$$A(h, \varphi) = \int_{h_{min}}^\infty \frac{\gamma(H)}{\sin \Phi} dH + \int_{h_{min}}^h \frac{\gamma(H)}{\sin \Phi} dH \quad (16)$$

In carrying out the integration of equations (11) and (16), care should be exercised since the integrand becomes infinite at $\Phi = 0$. However, this singularity can be eliminated by an appropriate variable conversion, for example, by using $u^4 = H - h$ in equation (11) and $u^4 = H - h_{min}$ in equation (16).

A numerical solution for the attenuation due to atmospheric gases can be implemented with the following algorithm.

To calculate the total attenuation for a satellite link, it is necessary to know not only the specific attenuation at each point of the link but also the length of path that has that specific attenuation. To derive the path length it is also necessary to consider the ray bending that occurs with a spherical Earth.

Using Fig. 4 as a reference, a_n is the path length through layer n with thickness δ_n that has refractive index n_n . α_n and β_n are the entry and exit incidence angles. r_n is the radius from the centre of the Earth to the beginning of layer n . a_n can then be expressed as:

$$a_n = -r_n \cos \beta_n + \frac{1}{2} \sqrt{4 r_n^2 \cos^2 \beta_n + 8 r_n \delta_n + 4 \delta_n^2} \quad (17)$$

The angle α_n can be calculated from:

$$\alpha_n = \pi - \arccos \left(\frac{-a_n^2 - 2 r_n \delta_n - \delta_n^2}{2 a_n r_n + 2 a_n \delta_n} \right) \quad (18)$$

β_1 is the incidence angle at the ground station (the complement of the elevation angle φ). β_{n+1} can be calculated from α_n using Snell's law as follows:

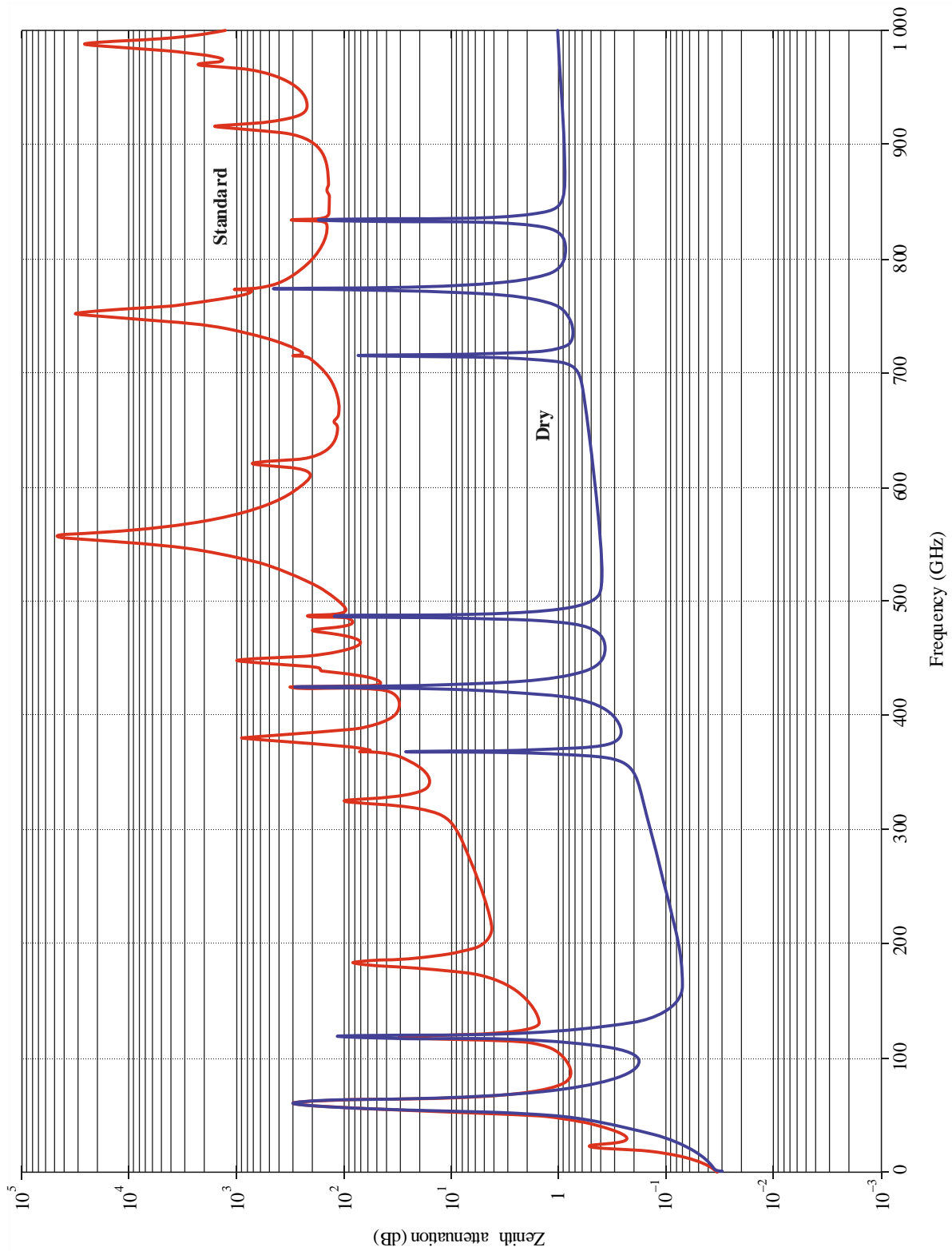
$$\beta_{n+1} = \arcsin \left(\frac{n_n}{n_{n+1}} \sin \alpha_n \right) \quad (19)$$

where n_n and n_{n+1} are the refractive indexes of layers n and $n + 1$.

Equation (19) may become invalid at very low elevation angles ($\varphi < 1^\circ$) when radiosonde data from certain regions of the world susceptible to ducting conditions are used as input. In such cases, air layers with radio refractivity gradients less than -157 N/km are present and the ray-tracing algorithm (equations (17) to (19)), which is based on geometrical optics, is no longer applicable. The arcsine function in equation (19) becomes complex under these anomalous conditions since its argument is then slightly larger than 1. It should be noted that equation (19) is valid for all elevation angles when the reference standard atmospheres given in Recommendation ITU-R P.835 are used as input, since these idealized atmospheres – clearly without strong negative refractivity gradients – do not support such anomalous propagation conditions.

FIGURE 3

Zenith attenuation due to atmospheric gases, calculated at 1 GHz intervals, including line centres



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The total attenuation, A_{gas} , can be derived using:

$$A_{gas} = \sum_{n=1}^k a_n \gamma_n \quad \text{dB}$$

(20)

where γ_n is the specific attenuation of the n^{th} layer per equation (1).

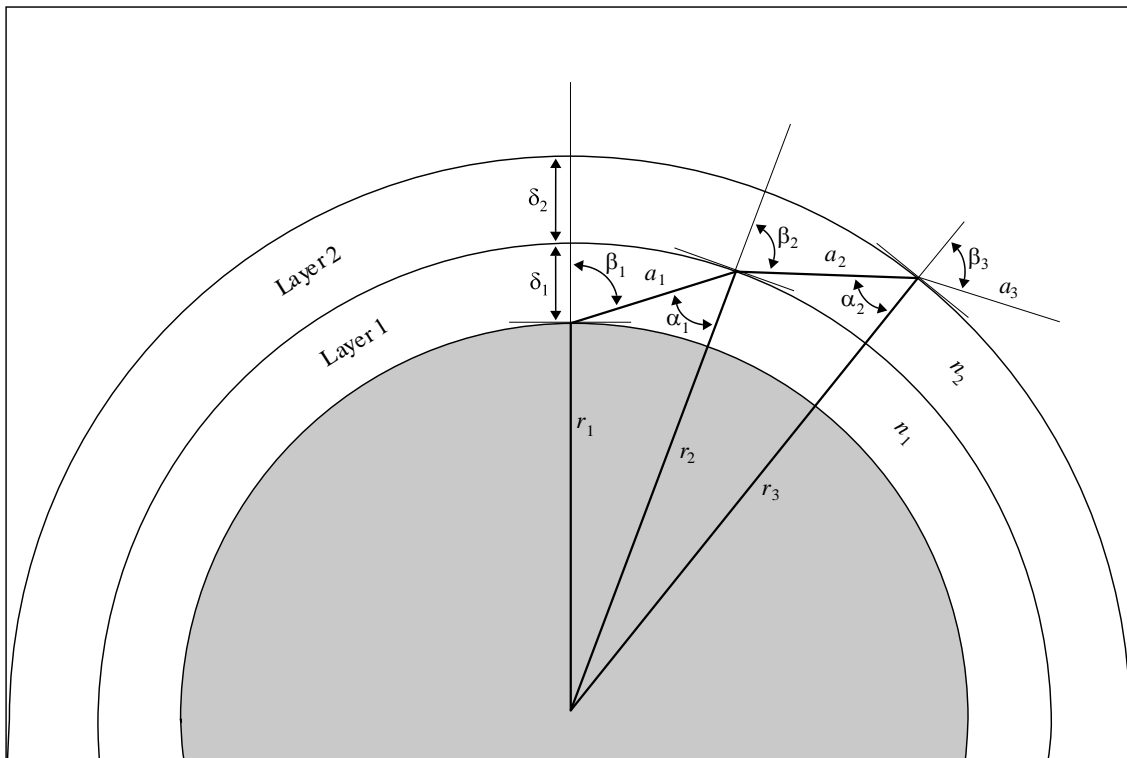
To ensure an accurate estimate of the path attenuation, the thickness of the layers should increase exponentially, from 10 cm at the lowest layer (ground level) to 1 km at an altitude of 100 km, according to the following equation:

$$\delta_i = 0.0001 \exp \left\{ \frac{i - 1}{100} \right\} \quad \text{km} \quad (21)$$

for $i = 1$ to 922, noting that $\delta_{922} \cong 1.0$ km and $\sum_{i=1}^{922} \delta_i \cong 100$ km.

For Earth-to-space applications, the integration should be performed up to at least 30 km, and up to 100 km at the oxygen line-centre frequencies.

FIGURE 4
Path through the atmosphere



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3 Dispersive effects

In addition to the attenuation described in the previous paragraph, which is based on the imaginary part of the frequency-dependent complex refractivity, oxygen and water vapour also introduce dispersion, which is based on the real part of the frequency-dependent complex refractivity. This effect is described in terms of phase vs. frequency (degree/km) or group delay vs. frequency (ps/km); and, similar to attenuation, can be calculated for slant paths. The effects of dispersion are discussed in Chapter 6 of the ITU-R Handbook on Radiometeorology, which contains a model for calculating

dispersion based on the line-by-line prediction method. For practical purposes, dispersive effects should not impose serious limitations on millimetric terrestrial communication systems operating with bandwidths of up to a few hundred MHz over short ranges (for example, less than about 20 km), especially in the window regions of the spectrum, at frequencies removed from the centres of major absorption lines. For satellite communication systems, the longer path lengths through the atmosphere will constrain operating frequencies to be within the window regions, where both the atmospheric attenuation and the corresponding dispersion are low.

Annex 2

Approximate estimation of gaseous attenuation in the frequency range 1-350 GHz

This Annex contains simplified algorithms for approximate estimates of gaseous attenuation for a limited range of meteorological conditions and a limited variety of geometrical configurations.

1 Specific attenuation

The specific attenuation due to dry air and water vapour, from sea level to an altitude of 10 km, can be estimated using the following simplified algorithms, which are based on the oxygen and water vapour specific attenuation from the line-by-line calculation and the effective oxygen and water vapour heights. These approximations have good agreement with the line-by-line calculation. However, for altitudes higher than 10 km, and in cases where higher accuracy is required, the line-by-line calculation should be used.

The specific attenuation for dry air, γ_o (dB/km), and the specific attenuation for moist air, γ_w (dB/km), are given by the following equations:

$$\gamma_o = 0.1820 f (\sum_{i(Oxygen)} S_i F_i + N_D''(f)) \quad (22)$$

$$\gamma_w = 0.1820 f \sum_{i(Water\ Vapour)} S_i F_i \quad (23)$$

where S_i , F_i , and $N_D''(f)$ are defined in equations (3), (5), (6a), (7), (8), and (9) for oxygen, and S_i , and F_i are defined in equations (3), (4), (5), (6a), and (7) for water vapour. Equation (6b) is not included since Zeeman splitting of oxygen lines and Doppler broadening of water vapour lines does not need to be considered at altitudes below 10 km. The summation for oxygen is over all oxygen lines in Table 1, and the summation for water vapour is over the subset of 9 water vapour lines in Table 2 denoted with an asterisk.

The dry pressure, p , and the temperature, T , are the dry pressure and temperature at the surface of the Earth. If local data is not available, the mean annual global reference atmosphere given in Recommendation ITU-R P.835 can be used to determine the dry pressure and temperature at the altitude of the surface of the Earth.

Figure 5 shows the dry air (Dry), water vapour only with a density of 7.5 g/m³ (Water Vapour), and total (Total) specific attenuation from 1 to 350 GHz at sea-level for the mean annual global reference atmosphere given in Recommendation ITU-R P.835.

2 Path attenuation

2.1 Terrestrial paths

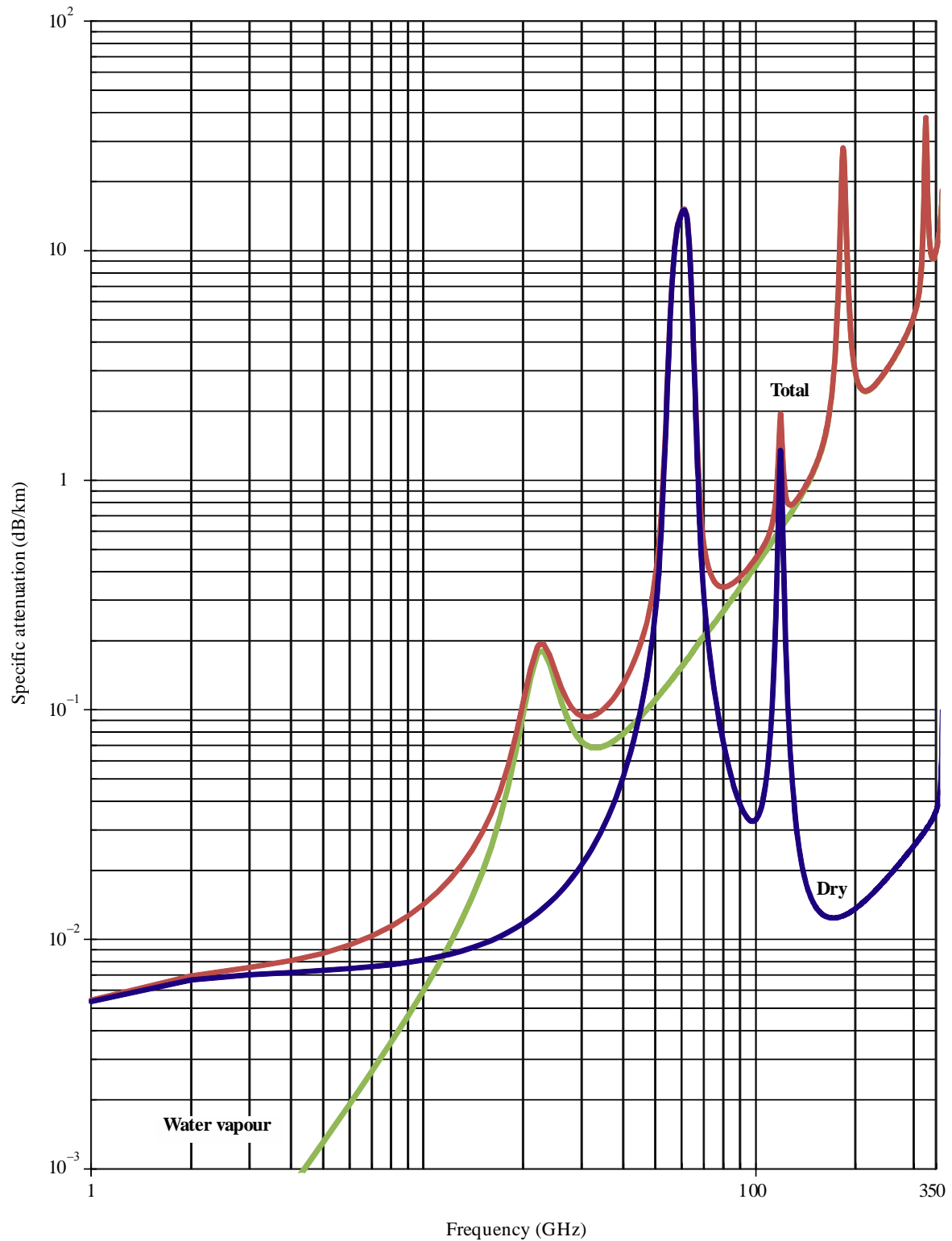
For a horizontal path, or for slightly inclined paths close to the ground, the path attenuation, A , may be calculated as:

$$A = \gamma r_0 = (\gamma_o + \gamma_w) r_0 \quad \text{dB} \quad (24)$$

where r_0 is the path length (km).

FIGURE 5

Specific attenuation due to atmospheric gases

(Pressure = 1 013.25 hPa; Temperature = 15°C; Water Vapour Density = 7.5 g/m³)

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2.2 Slant paths

This section contains reduced complexity algorithms for estimating the gaseous attenuation along slant paths through the Earth's atmosphere, by defining an equivalent height by which the specific

attenuation calculated in paragraph 1 may be multiplied to obtain the zenith attenuation. The equivalent heights are dependent on pressure, and can hence be employed for determining the zenith attenuation from sea level up to an altitude of about 10 km. The resulting zenith attenuations are accurate to within $\pm 10\%$ for dry air and $\pm 5\%$ for water vapour from sea level up to altitudes of about 10 km, using the pressure, temperature and water-vapour density appropriate to the altitude of interest. For altitudes higher than 10 km, and particularly for frequencies within 0.5 GHz of the centres of resonance lines at any altitude, the procedure in Annex 1 should be used. Note that the Gaussian function in equation (25b) describing the oxygen equivalent height in the 60 GHz band can yield errors higher than 10% at certain frequencies, since this procedure is not intended to accurately reproduce the structure shown in Figure 7. The expressions below were derived from zenith attenuations calculated with the procedure in Annex 1, integrating the attenuations numerically over a bandwidth of 500 MHz; the resultant attenuations effectively represent approximate minimum values in the 50-70 GHz band. The path attenuation at elevation angles other than the zenith may then be determined using the procedures described later in this section.

For dry air, the equivalent height is given by:

$$h_o = \frac{6.1}{1 + 0.17 r_p^{-1.1}} (1 + t_1 + t_2 + t_3) \quad (25a)$$

where:

$$t_1 = \frac{4.64}{1 + 0.066 r_p^{-2.3}} \exp \left[- \left(\frac{f - 59.7}{2.87 + 12.4 \exp(-7.9 r_p)} \right)^2 \right] \quad (25b)$$

$$t_2 = \frac{0.14 \exp(2.12 r_p)}{(f - 118.75)^2 + 0.031 \exp(2.2 r_p)} \quad (25c)$$

$$t_3 = \frac{0.0114}{1 + 0.14 r_p^{-2.6}} f \frac{-0.0247 + 0.0001f + 1.61 \times 10^{-6} f^2}{1 - 0.0169f + 4.1 \times 10^{-5} f^2 + 3.2 \times 10^{-7} f^3} \quad (25d)$$

with the constraint that:

$$h_o \leq 10.7 r_p^{0.3} \quad \text{when } f < 70 \text{ GHz} \quad (25e)$$

and, for water vapour, the equivalent height is:

$$h_w = 1.66 \left(1 + \frac{1.39 \sigma_w}{(f - 22.235)^2 + 2.56 \sigma_w} + \frac{3.37 \sigma_w}{(f - 183.31)^2 + 4.69 \sigma_w} + \frac{1.58 \sigma_w}{(f - 325.1)^2 + 2.89 \sigma_w} \right) \quad (26a)$$

for $f \leq 350 \text{ GHz}$

$$\sigma_w = \frac{1.013}{1 + \exp[-8.6 (r_p - 0.57)]} \quad (26b)$$

where:

$$r_p = (p + e)/1013.25$$

The zenith attenuation between 50 to 70 GHz is a complicated function of frequency, as shown in Fig. 7, and the above algorithms for equivalent height can provide only an approximate estimate, in general, of the minimum levels of attenuation likely to be encountered in this frequency range. For greater accuracy, the procedure in Annex 1 should be used.

The concept of equivalent height is based on the assumption of an exponential atmosphere specified by a scale height to describe the decay in density with altitude. Note that scale heights for both dry air and water vapour may vary with latitude, season and/or climate, and that water vapour distributions in the real atmosphere may deviate considerably from the exponential profile, with corresponding changes in equivalent heights. The values given above are applicable up to altitudes of about 10 km.

The total zenith attenuation is then:

$$A = \gamma_o h_o + \gamma_w h_w \quad \text{dB} \quad (27)$$

Figure 6 shows the total zenith attenuation at sea level (Total), as well as the attenuation due to dry air (Dry) and water vapour (Water Vapour), using the mean annual global reference atmosphere given in Recommendation ITU-R P.835. Between 50 and 70 GHz, greater accuracy can be obtained from the 0 km curve in Fig. 7 which was derived using the line-by-line calculation described in Annex 1.

2.2.1 Elevation angles between 5° and 90°

2.2.1.1 Earth-space paths

For an elevation angle, φ , between 5° and 90°, the path attenuation is obtained using the cosecant law, as follows:

For path attenuation based on surface meteorological data:

$$A = \frac{A_o + A_w}{\sin \varphi} \quad \text{dB} \quad (28)$$

where $A_o = h_o \gamma_o$ and $A_w = h_w \gamma_w$

and for path attenuation based on integrated water vapour content:

$$A = \frac{A_o + A_w}{\sin \varphi} \quad \text{dB} \quad (29)$$

where A_w is given in § 2.3.

2.2.1.2 Inclined paths

To determine the attenuation values on an inclined path between a station situated at altitude h_1 and another at a higher altitude h_2 , where both altitudes are less than 10 km above mean sea level, the values h_o and h_w in equation (28) must be replaced by the following h'_o and h'_w values:

$$h'_o = h_o \left[e^{-h_1/h_o} - e^{-h_2/h_o} \right] \quad \text{km} \quad (30)$$

$$h'_w = h_w \left[e^{-h_1/h_w} - e^{-h_2/h_w} \right] \quad \text{km} \quad (31)$$

it being understood that the value ρ of the water-vapour density used in equation (23) is the hypothetical value at sea level calculated as follows:

$$\rho = \rho_1 \times \exp(h_1/2) \quad (32)$$

where ρ_1 is the value corresponding to altitude h_1 of the station in question, and the equivalent height of water vapour density is assumed as 2 km (see Recommendation ITU-R P.835).

Equations (30), (31) and (32) use different normalizations for the dry air and water-vapour equivalent heights. While the mean air pressure referred to sea level can be considered constant around the world

(equal to 1 013.25 hPa), the water-vapour density not only has a wide range of climatic variability but is measured at the surface (i.e. at the height of the ground station). For values of surface water-vapour density, see Recommendation ITU-R P.836.

2.2.2 Elevation angles between 0° and 5°

2.2.2.1 Earth-space paths

In this case, Annex 1 of this Recommendation should be used. Annex 1 should also be used for elevations less than zero.

2.2.2.2 Inclined paths

The attenuation on an inclined path between a station situated at altitude h_1 and a higher altitude h_2 (where both altitudes are less than 10 km above mean sea level), can be determined from the following:

$$A = \gamma_o \sqrt{h_o} \left[\frac{\sqrt{R_e + h_1} \cdot F(x_1) e^{-h_1/h_o}}{\cos \varphi_1} - \frac{\sqrt{R_e + h_2} \cdot F(x_2) e^{-h_2/h_o}}{\cos \varphi_2} \right] + \gamma_w \sqrt{h_w} \left[\frac{\sqrt{R_e + h_1} \cdot F(x'_1) e^{-h_1/h_w}}{\cos \varphi_1} - \frac{\sqrt{R_e + h_2} \cdot F(x'_2) e^{-h_2/h_w}}{\cos \varphi_2} \right] \quad \text{dB} \quad (33)$$

where:

R_e : effective Earth radius including refraction, given in Recommendation ITU-R P.834, expressed in km (a value of 8 500 km is generally acceptable for the immediate vicinity of the Earth's surface)

φ_1 : elevation angle at altitude h_1

F : function defined by:

$$F(x) = \frac{1}{0.661 x + 0.339 \sqrt{x^2 + 5.51}} \quad (34)$$

$$\varphi_2 = \arccos \left(\frac{R_e + h_1}{R_e + h_2} \cos \varphi_1 \right) \quad (35a)$$

$$x_i = \tan \varphi_i \sqrt{\frac{R_e + h_i}{h_o}} \quad \text{for } i = 1, 2 \quad (35b)$$

$$x'_i = \tan \varphi_i \sqrt{\frac{R_e + h_i}{h_w}} \quad \text{for } i = 1, 2 \quad (35c)$$

it being understood that the value ρ of the water vapour density used in equation (23) is the hypothetical value at sea level calculated as follows:

$$\rho = \rho_1 \cdot \exp(h_1/2) \quad (36)$$

where ρ_1 is the value corresponding to altitude h_1 of the station in question, and the equivalent height of water vapour density is assumed as 2 km (see Recommendation ITU-R P.835).

FIGURE 6

Total, dry air and water-vapour zenith attenuation from sea level
 (Pressure = 1 013.25 hPa; Temperature = 15°C; Water Vapour Density = 7.5 g/m³)

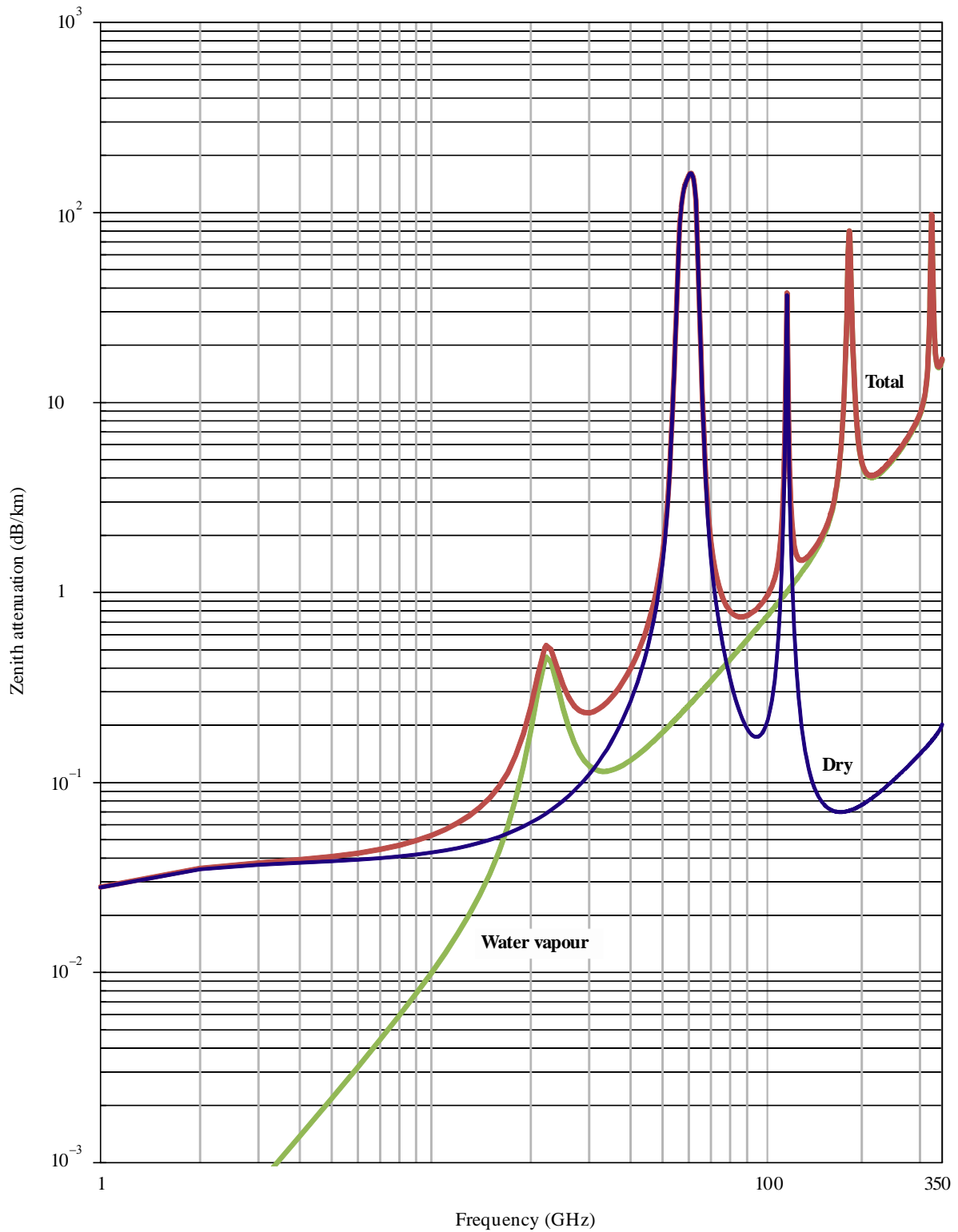
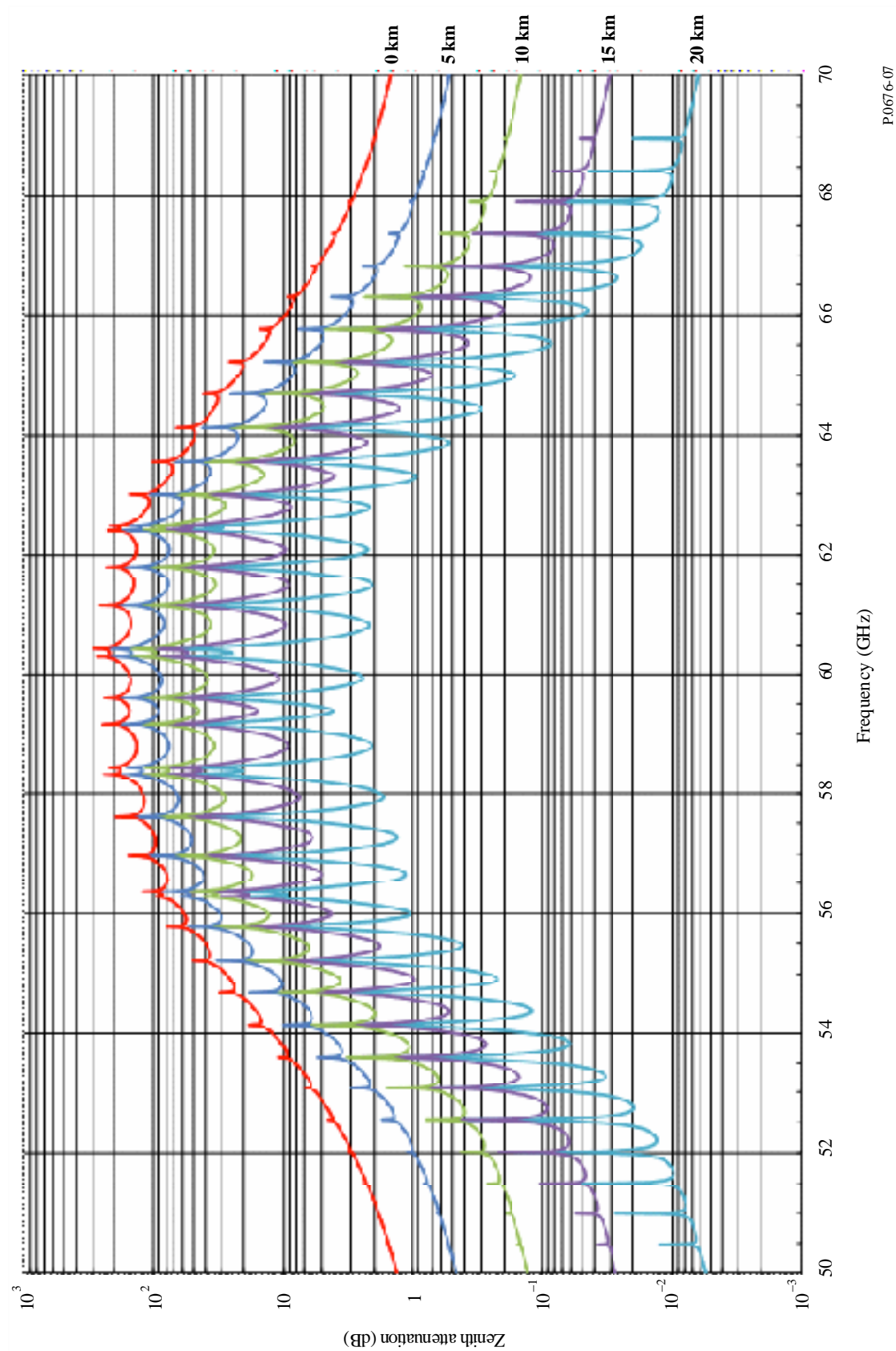


FIGURE 7

Zenith oxygen attenuation from the altitudes indicated, calculated at intervals of 10 MHz, including line centres (0 km, 5 km, 10 km, 15 km and 20 km)



Values for ρ_1 at the surface can be found in Recommendation ITU-R P.836. The different formulation for dry air and water vapour is explained at the end of paragraph 2.2.

2.3 Zenith path water-vapour attenuation

The above method for calculating slant path attenuation relies on knowledge of the surface water-vapour density. If integrated water vapour content, V_t , is known, the total water-vapour attenuation can be estimated as follows:

$$A_w = \begin{cases} \frac{0.0176 V_t \gamma_w(f, p_{ref}, \rho_{v,ref}, t_{ref})}{\gamma_w(f_{ref}, p_{ref}, \rho_{v,ref}, t_{ref})}, & 1 \text{ GHz} \leq f \leq 20 \text{ GHz} \\ \frac{0.0176 V_t \gamma_w(f, p_{ref}, \rho_{v,ref}, t_{ref})}{\gamma_w(f_{ref}, p_{ref}, \rho_{v,ref}, t_{ref})} (ah^b + 1), & 20 \text{ GHz} < f \leq 350 \text{ GHz} \end{cases} \text{ dB} \quad (37)$$

where:

$$\begin{aligned} a &= 0.2048 \exp \left[- \left(\frac{f - 22.43}{3.097} \right)^2 \right] + 0.2326 \exp \left[- \left(\frac{f - 183.5}{4.096} \right)^2 \right] \\ &+ 0.2073 \exp \left[- \left(\frac{f - 325}{3.651} \right)^2 \right] - 0.113 \\ b &= 8.741 \times 10^4 \exp(-0.587f) + 312.2f^{-2.38} + 0.723 \\ h &= \begin{cases} h_o & h_o \leq 4 \text{ km} \\ 4 & h_o > 4 \text{ km} \end{cases} \end{aligned}$$

and

f : frequency (GHz)

f_{ref} : 20.6 (GHz)

p_{ref} = 815 (hPa)

$\rho_{v,ref} = \frac{V_t}{3.67} \text{ (g/m}^3\text{)}$

$t_{ref} = 14 \ln \left(\frac{0.22 V_t}{3.67} \right) + 3 \text{ (}^\circ\text{C)}$

V_t : integrated water vapour content from: a) local radiosonde or radiometric data or b) at the required percentage of time (kg/m^2 or mm) obtained from the digital maps in Recommendation ITU-R P.836 (kg/m^2 or mm)

$\gamma_w(f, p, \rho, t)$: specific attenuation as a function of frequency, pressure, water-vapour density, and temperature calculated from equation (23) (dB/km).

h_o : station height above mean sea level (a.m.s.l) (km)