



Radar Recognition of Multi-Propeller Drones using Micro-Doppler Line Spectra

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Outline

- Introduction
- Simulation model for drone micro-Doppler spectrum
- Drone micro-Doppler features analysis and selection
- Application of features to simulated data
- Conclusion

Introduction

- Drones are popular
 - Environmental monitoring, delivery, emergency services



Drone revealing fire damage to Notre Dame

- They pose threats
 - Collision hazards, privacy violation, illegal reconnaissance, smuggling, terrorism

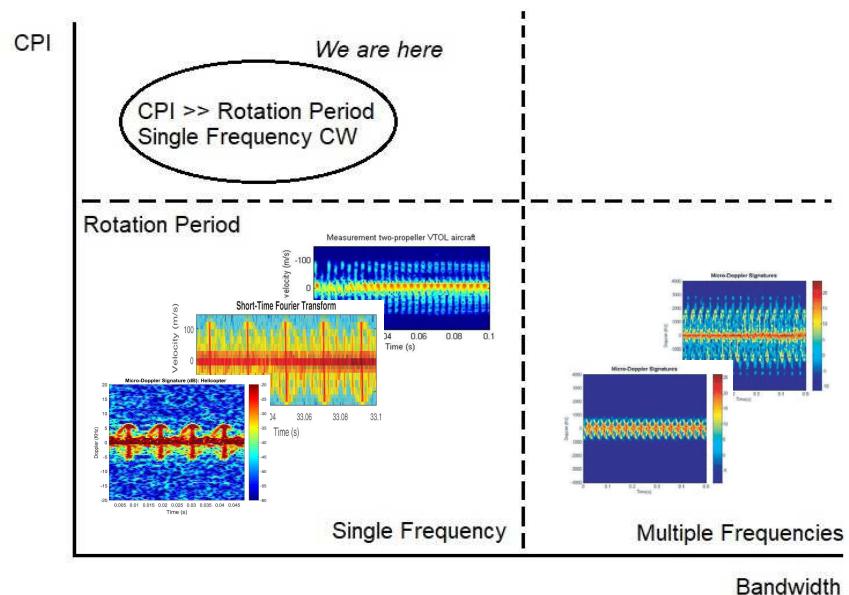
Introduction

- Response to these threats
 - Detection, Tracking, Characterization, Classification
 - then – acting (interception / destruction / jamming)
- All these tasks can be done based on radar micro-Doppler patterns
 - Long range sensing, stable in most weather and light conditions, provides range and velocity information
- What do we need to know for about drones?
 - It is necessary to understand the relations between the observed micro-Doppler pattern, radar parameters and properties of specific drone's rotating parts:
 - Algorithms for aforementioned sensing tasks...

Objectives of the study

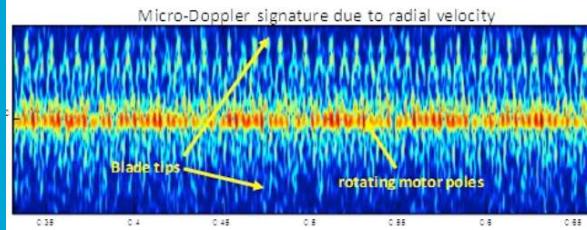
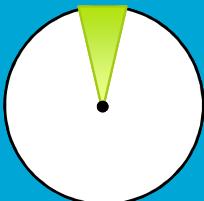
To study the drone's micro-Doppler pattern that are observed by a radar and to select the features that are most informative/useful for drone's type identification/recognition

- Use previously developed and presented general approach for drone's simulation and simplified EM model of scattered on drone signal
- Concentrate on the case of long Coherent Processing Interval (CPI)

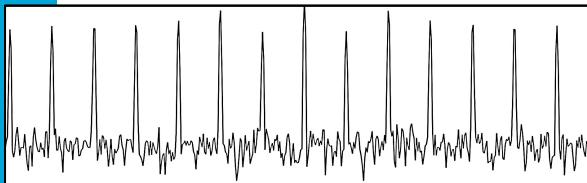


Short and Long Coherent Processing Intervals

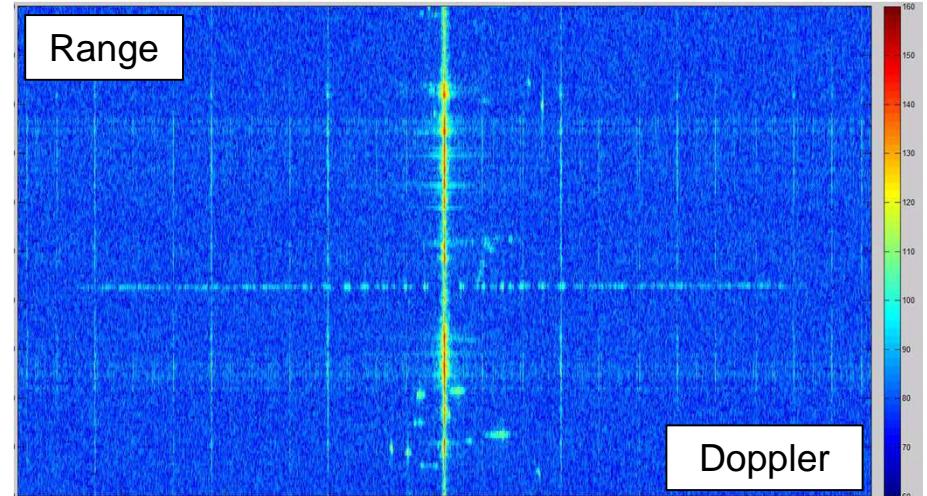
Short CPI << Rotation Period



Long CPI ~ Rotation Period



Line spectrum



DJI Matrix-600, PARSAK radar, HH polarisation,
Range 9 km, 3.315 GHz, PRI = 240us, B=16.8MHz,
PRF = 4.17 kHz, CPI = 0.98 s, SNR ~ 20 dB

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Our proposed simulation approach

Models

Precise EM
(FEKO)

Simple
(thin-wires)

Measurements

Anechoic
Chamber

Angular
dependence of
blade/propeller
scattering
coefficient

One rotor/propeller

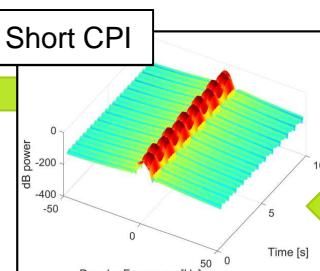
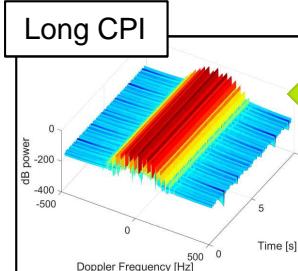
Rotation
Frequency

Radar:
PRF, CPI

Time
dependence

Sampling

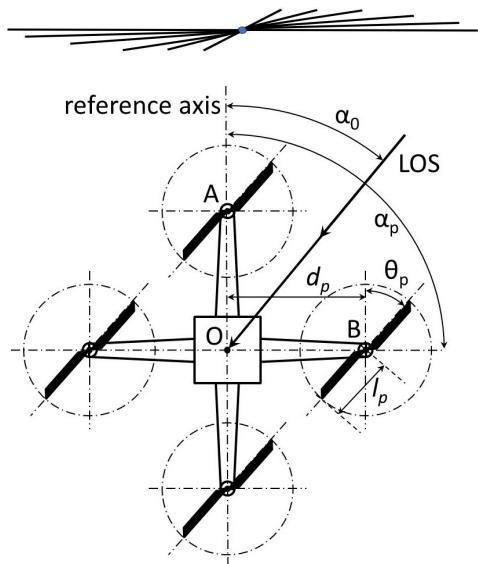
Drone's
Geometry,
LOS
Orientation



Doppler FFT as
Function of Time

Simulation model for drone micro-Doppler spectrum

- Simulation model of drone's EM reflection (HH)



Thin-wire model of multi-propeller drone and each single propeller

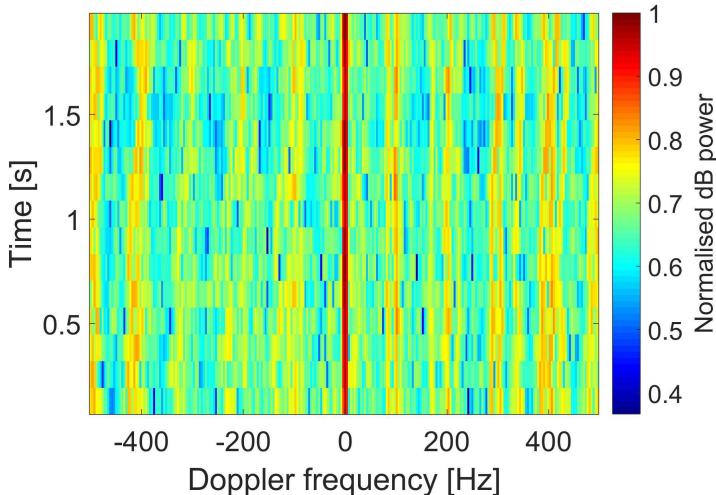
$$\begin{aligned} E^{drone}(t, r_0) &\sim \sum_{p=1}^P E_p^{prop}(t, r_p, \theta_{p,b,w}, l_{p,b,w}) \\ &= \sum_{p=1}^P \sum_{b=1}^B \sum_{w=1}^W E_{p,b,w}^{wire}(t, r_p, \theta_{p,b,w}, l_{p,b,w}) \\ &= \sum_{p=1}^P \sum_{b=1}^B \sum_{w=1}^W \int_0^{l_{p,b,w}} j\eta \frac{ke^{-jk r_p}}{4\pi r_p} \\ &\quad \times E_{r_0}^{in}(t) \sin^2(\theta_{p,b,w} + \Omega_p t) \\ &\quad \times e^{j2ky'_{p,b,w} \cos(\theta_{p,b,w} + \Omega_p t)} dy'_{p,b,w} \\ &= \sum_{p=1}^P j\eta \frac{ke^{-jk r_p}}{4\pi r_p} \cdot E^{propeller} \end{aligned}$$

$$\text{where } r_p = r_0 - d_p \cdot \cos(\alpha_p - \alpha_0)$$

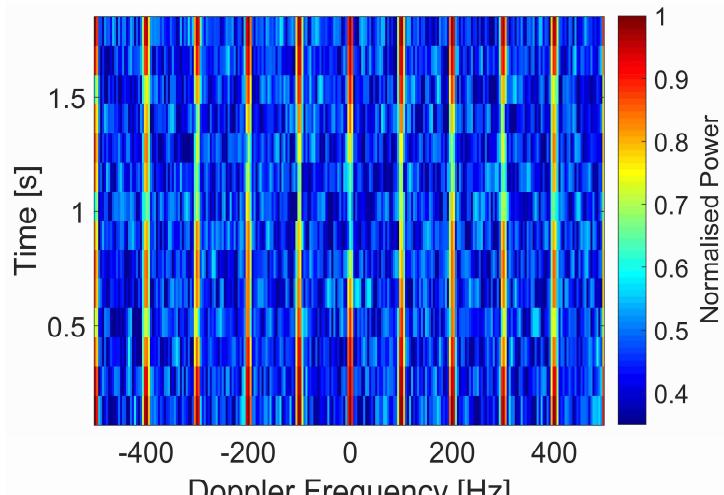
* Synthesis and synchronisation of propellers

Simulation model for drone micro-Doppler spectrum

- Drone micro-Doppler pattern from simulation model
 - Doppler processing to EM reflection signal
 - Linear pattern in long CPI circumstance: S-band, DJI M600 drone, radar CPI much longer than propeller rotation period



Micro-Doppler pattern of hexa-copter
(PARSAX radar measurement)



Micro-Doppler pattern of hexa-copter
(Thin-wire model simulation)

Simulation model for drone micro-Doppler spectrum

- Thin-wire model proposed for the simulation of drone micro-Doppler spectrum
 - Validated in S-band
 - Taking radar setup parameters and drone's properties as input variables
 - Generating line spectral micro-Doppler pattern within long CPI circumstance

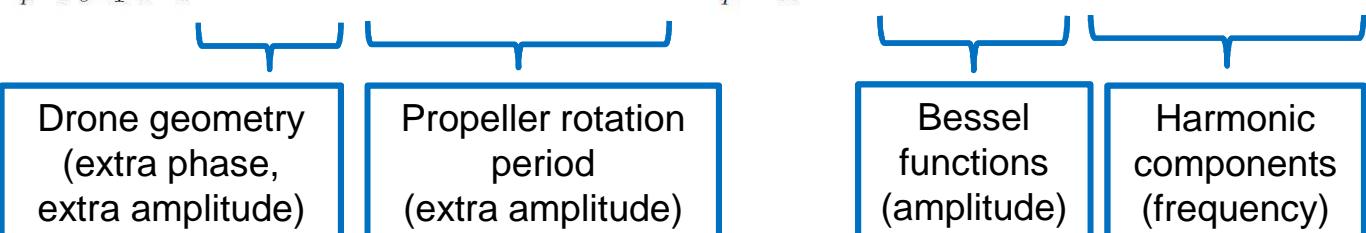
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Drone micro-Doppler features analysis

- Simulation model rewritten in Bessel functions

$$\begin{aligned} E^{drone}[n] &\sim \sum_{p=1}^P \sum_{b=1}^B \sum_{w=1}^W s_{p,b,w}^{wire}[n] \quad \boxed{\text{Sums over wires, blades, propellers}} \\ &= \sum_{p=1}^P \sum_{b=1}^B \sum_{w=1}^W \frac{\eta e^{-j\frac{2\pi}{\lambda}r_p}}{8\pi r_p} \cdot \frac{\sin^2(\theta_{p,b,w} + \Omega_p t_s n)}{\cos(\theta_{p,b,w} + \Omega_p t_s n)} \cdot \left(\sum_{q=-\infty}^{\infty} e^{j\frac{\pi q}{2}} J_q(2\frac{2\pi}{\lambda}l_{p,b,w}) e^{j(\theta_{p,b,w} + \Omega_p t_s n)q} - 1 \right) \end{aligned}$$



Drone geometry
(extra phase,
extra amplitude)

Propeller rotation
period
(extra amplitude)

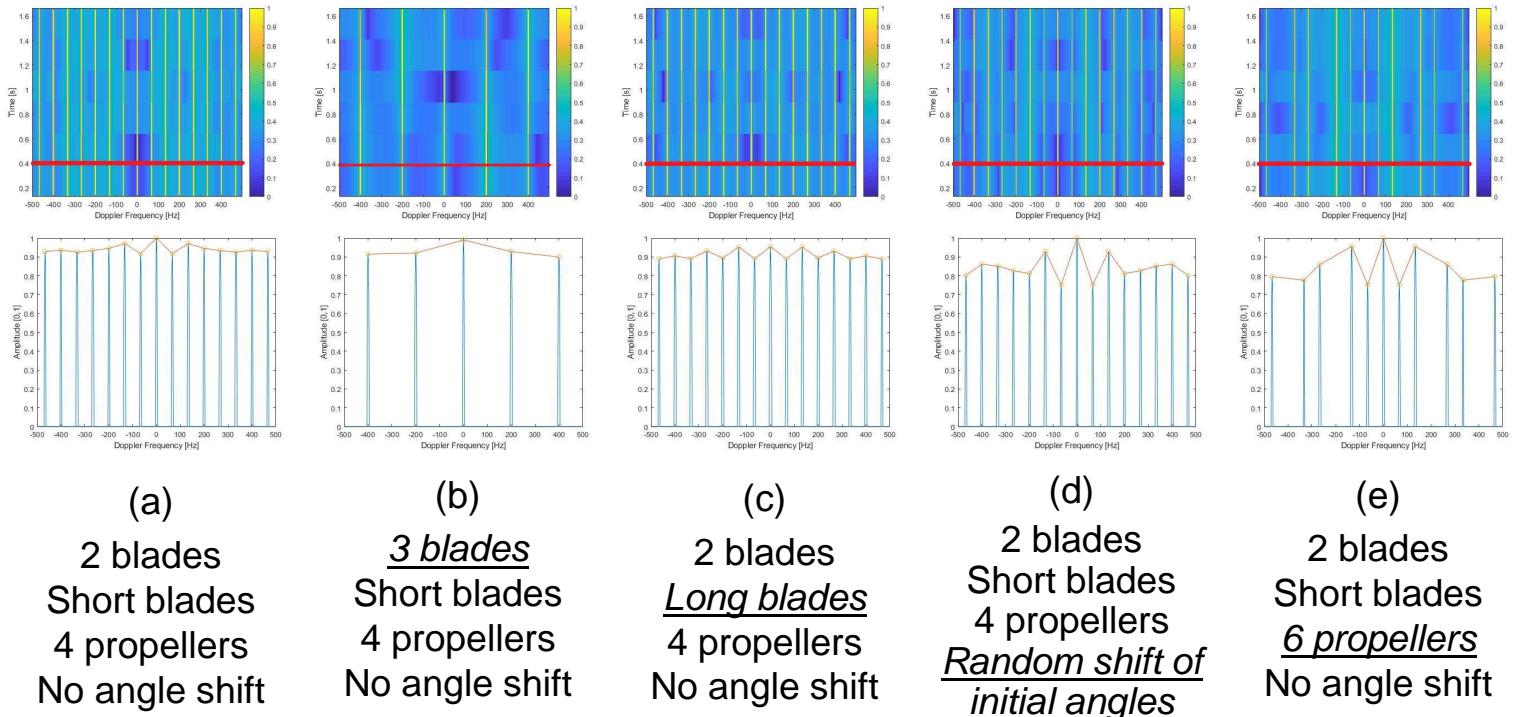
Bessel
functions
(amplitude)

Harmonic
components
(frequency)

- Influence factors: PRF, carrier frequency, drone's geometry, propeller's radius and rotation period
- Influence on the micro-Doppler spectrum: **Amplitude and frequency gap** of harmonic components

Micro-Doppler pattern vs Drone's Properties

- Influence of drones' properties on spectral lines' amplitudes, locations, the total bandwidth of non-folded Doppler spectra



Micro-Doppler patterns of drones and their cuts at some time moment ₁₄

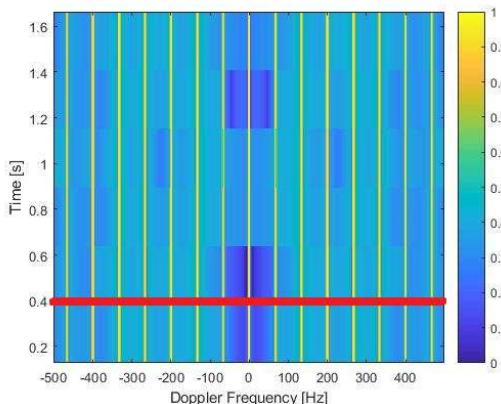
Micro-Doppler pattern vs Propellers Velocities

Hovering

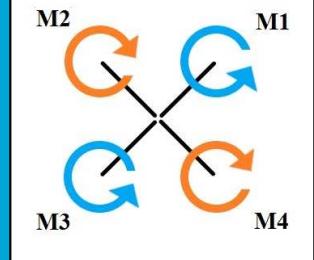
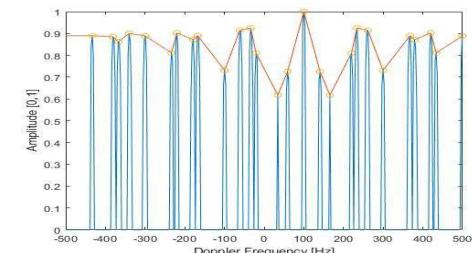
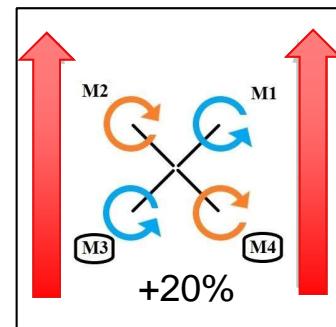
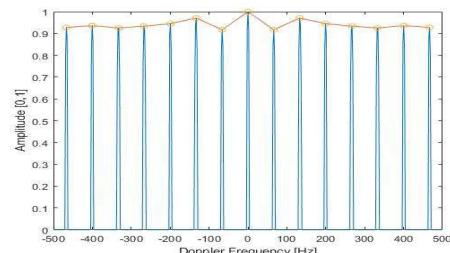
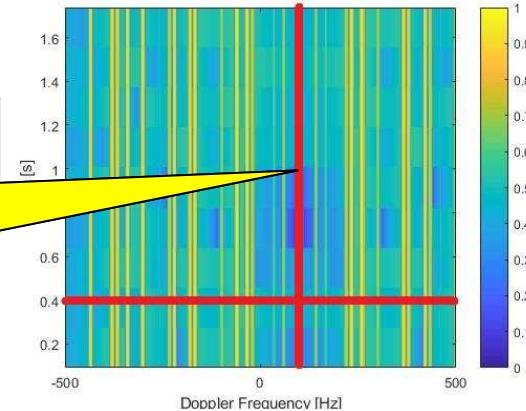
(propellers rotation is synchronous)

Maneuvering

(propellers rotate with different velocities)

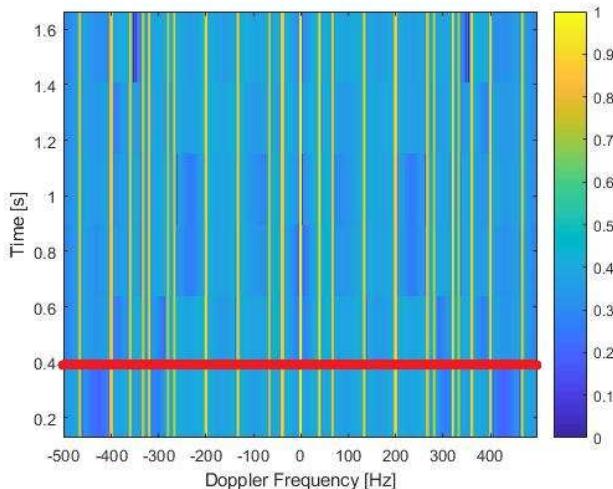


Patterns centres shift away from zero Doppler frequency



Micro-Doppler patterns of drones and their cuts at some time moment ₁₅

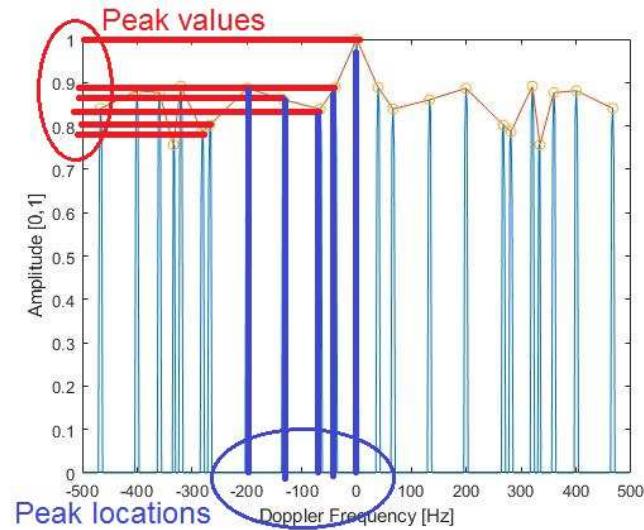
Features for drones recognitions



An example of micro-Doppler pattern

Location = $[0,0,1,0,0,\dots]$

Amplitudes = $[0.84,0.89,0.88,\dots,1,\dots]$



Characteristics of line spectrum

$[1 \times N_{CPI}]$ vector, "1" if a peak appears

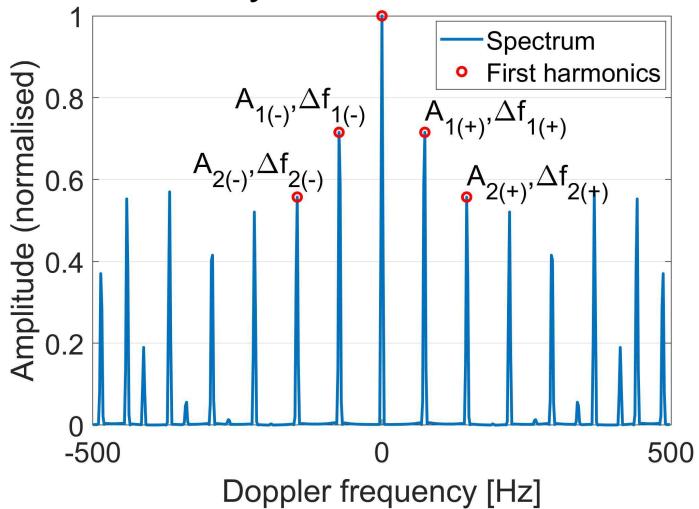
$[1 \times N_{\text{peaks}}]$ vector, peak values

Mean (Amplitudes), Standard Deviation (Amplitudes), Entropy (Amplitudes)

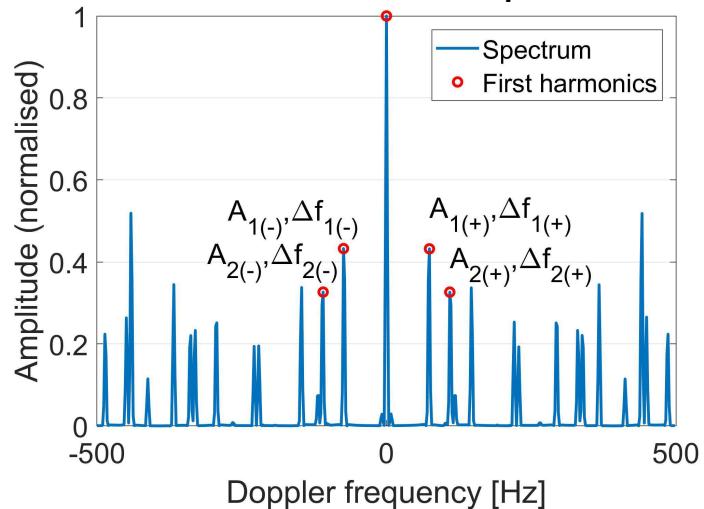
Features = [Location, Mean, Standard Deviation, Entropy]

Drone micro-Doppler features selection

- Features that characterize the micro-Doppler spectrum
 - **Amplitudes** and **frequencies** of harmonic components
 - Only first 4 harmonic components shown in this example



Micro-Doppler spectrum of
hovering quad-copter



Micro-Doppler spectrum of
maneuvering quad-copter

* 2 amplitude modulation,
** Non-uniform frequency gap

Drone micro-Doppler features selection

- Features selection for drone micro-Doppler spectrum in long CPI circumstance
 - Influential factors:
 - radar setup parameters
 - drone properties
 - Proposed features to characterize the spectrum:
 - Set of linear harmonics' amplitudes
 - Set of frequency gaps between them
 - Sub-sets
 - Their statistical moments

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Application of features to simulated data

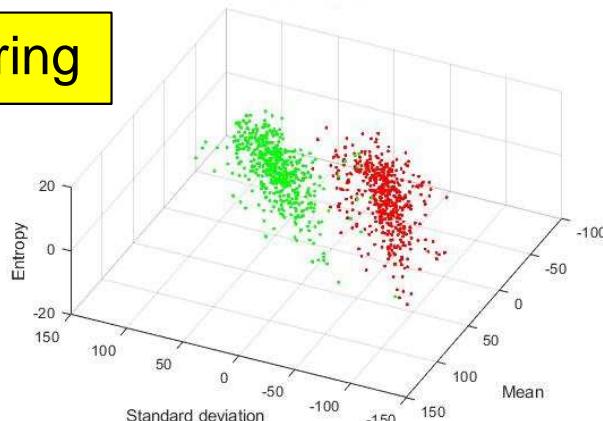
- Simulation data sets
 - Drones: Quad-, hexa-, octo-copter
 - Flight motion modes: Hovering, maneuvering

Combination of Input Variables	Drones & Flight Attitudes	Blade Length l [m]	Arm Length d_p [m]	Propeller Angular Velocity Ω [rpm]
	quadcopter hover	0.114	0.175	$2200 * [1, -1, 1, -1]$
	quadcopter cross range			$2200 * [1, -v_{asyn}, v_{asyn}, -1]$ $v_{asyn} = 1.5$
	hexacopter hover	0.267	0.567	$1800 * [1, -1, 1, -1]$
	hexacopter cross range			$1800 * [1, -v_{asyn}, v_{asyn}, -1]$ $v_{asyn} = 1.5$
	octocopter hover	0.267	0.567	$1500 * [1, -1, 1, -1]$
	octocopter cross range			$1500 * [1, -v_{asyn}, v_{asyn}, -1]$ $v_{asyn} = 1.5$

Two classes recognition

3D – only
amplitudes'
features

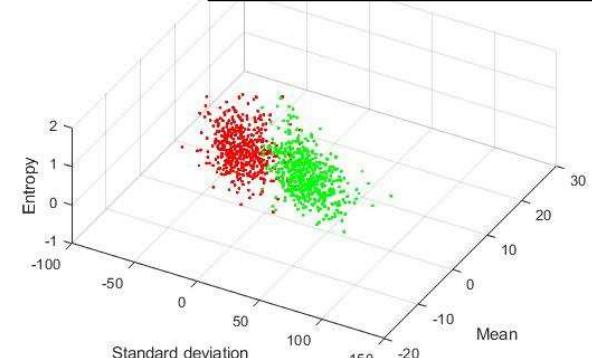
Hovering



4-copter 6-copter
464 obs. 520 obs.
Truth

Decision			
6-copter	4-copter	4-copter	6-copter
462 observations (99.57%)	6 observations (1.15%)		
2 observations (0.43%)	514 observations (98.85%)		

Maneuvering



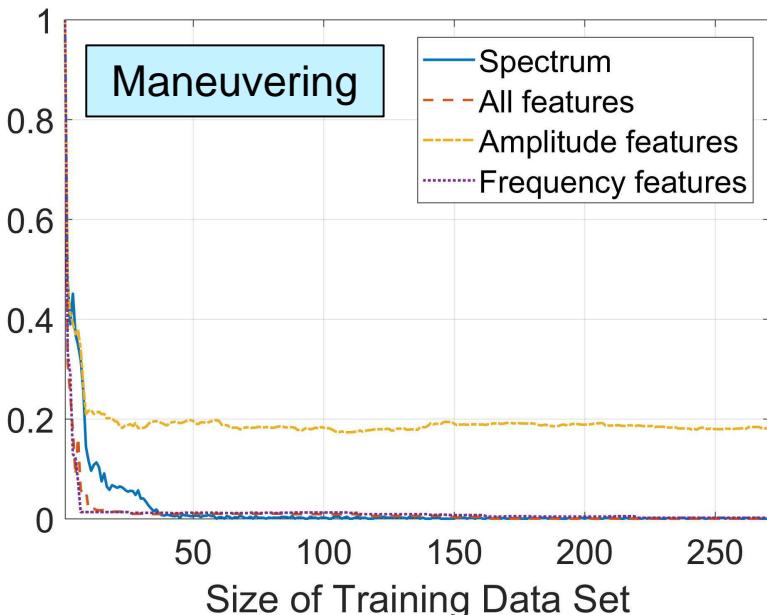
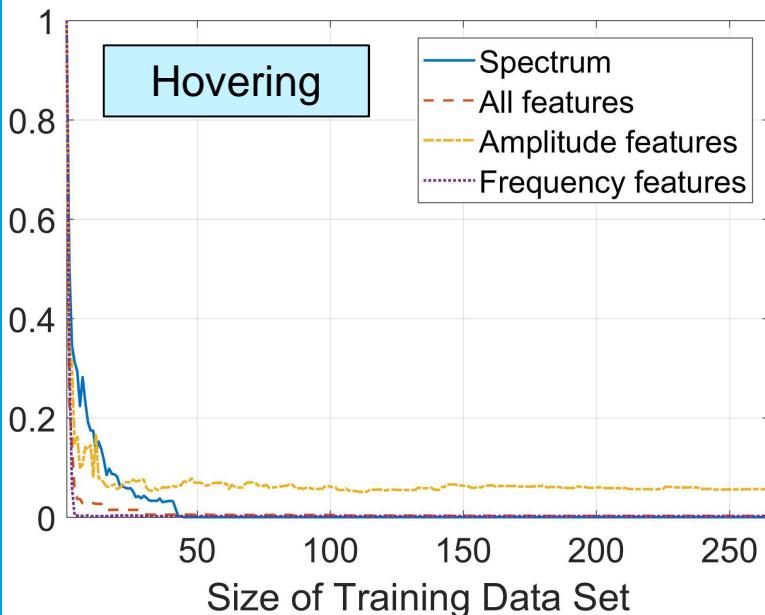
4-copter 6-copter
488 obs. 486 obs.
Truth

Decision			
6-copter	4-copter	4-copter	6-copter
454 observations (93.03%)	33 observations (6.79%)		
34 observations (6.97 %)	453 observations (93.2%)		

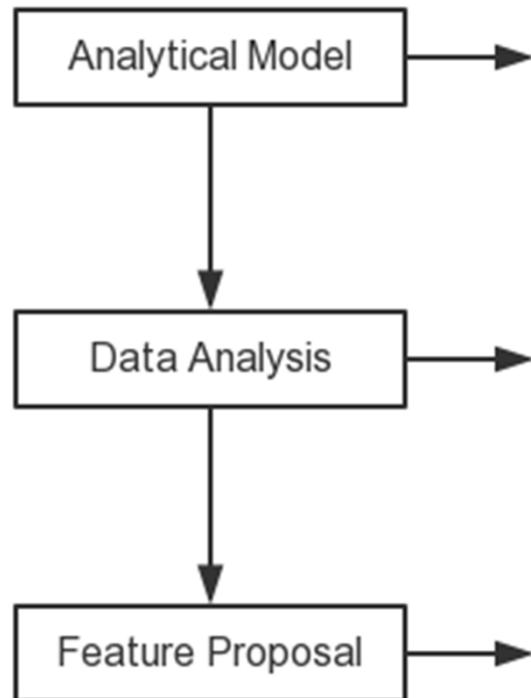
Application of features to simulated data

- Classification results on simulated m-D data
 - SVM classifier, 5-fold cross validation
 - Amplitude and frequency gap of first 4 harmonic components

Probability of classification error



Conclusion



- The simple model efficiently generates micro-Doppler patterns for any selected propeller, drone and radar setup parameters
- The parameters of micro-Doppler pattern are strongly influenced with propeller, drone and radar setup parameters
- The measured during long CPI line spectral micro-Doppler patterns of different drones are precisely characterized with set (and sub-sets) of peaks' amplitudes and frequencies

Questions?

