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# Simulation of Radar Micro-Doppler Patterns for Multi-Propeller Drones

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*RADAR-2019, Toulon, France*

# Outline

- **Introduction**
- **General Approach**
- **Single propeller characterization**
  - models and measurements
- **Multi-propeller drone simulations**
- **Conclusion**

# Introduction

- Drones are popular
  - Environmental monitoring, delivery, emergency services



Drone revealing fire damage to Notre Dame

- They pose threats
  - Collision hazards, privacy violation, illegal reconnaissance, smuggling, terrorism

# Introduction

- Response to these threats
  - Detection, Tracking, Characterization, Classification
  - then – acting (interception / destruction / jamming)
- All these tasks can be done based on **radar micro-Doppler patterns**
  - Long range sensing, stable in most weather and light conditions, provides range and velocity information
- What do we need to know for about drones?
  - It is necessary to understand the relations between the observed micro-Doppler pattern, radar parameters and properties of specific drone's rotating parts:
  - Algorithms for aforementioned sensing tasks...

# Objectives of the study

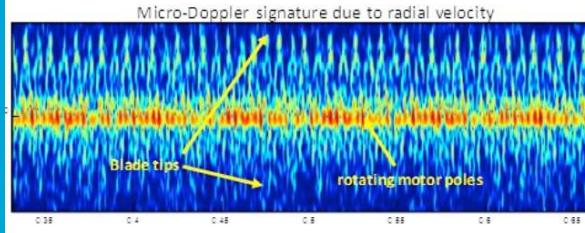
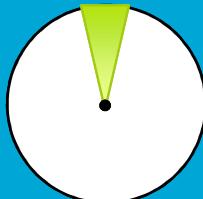
- To develop an approach that will give a possibility to study the relation between the micro-Doppler pattern, radar parameters
    - Operational frequency
    - Pulse Repetition Frequency (PRF)
    - Coherent Processing Interval (CPI)
- properties of specific drone's rotating parts:
- number and length of blades in propeller,
  - number of propellers/rotors,
  - rotors rotation speed and synchronization
- and observed scene
- Drone's motion (hovering or moving) and orientation

# State of the art

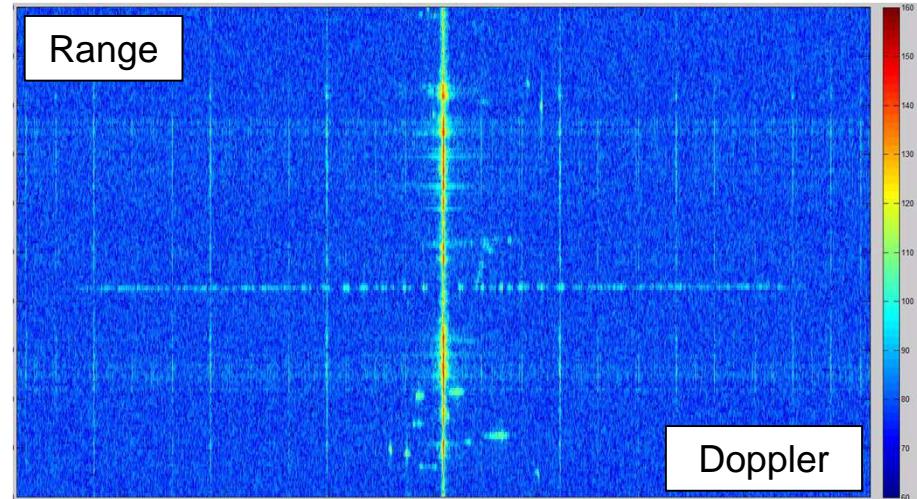
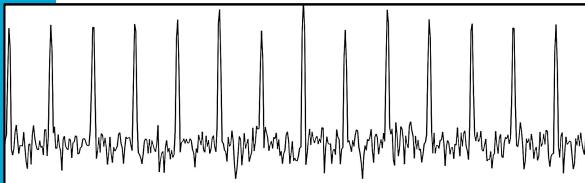
- Data collection methods in previous researches
  - Simulated data
  - Indoor measurements
  - Outdoor measurements
- Problems
  - Time consuming
  - Constant synchronization of propellers (hovering only)
  - Only for a particular drone (drones collection?)
  - Mostly studied for the short CPI, when the propeller's rotation period is much longer this CPI

# Short and Long Coherent Processing Intervals

Short CPI << Rotation Period



Long CPI ~ Rotation Period



DJI Matrix-600, PARSAK radar, HH polarisation,  
Range 9 km, 3.315 GHz, PRI = 240us, B=16.8MHz,  
PRF = 4.17 kHz, CPI = 0.98 s, SNR ~ 20 dB

# Our proposed simulation approach

## Models

Precise EM  
(FEKO)

Simple  
(thin-wires)

Measurements  
Anechoic  
Chamber

Angular  
dependence of  
blade/propeller  
scattering  
coefficient

One rotor/propeller

Rotation  
Frequency

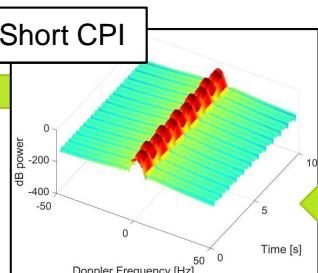
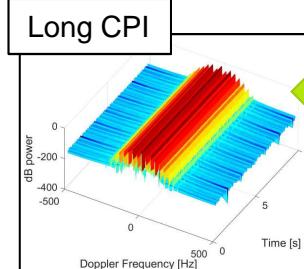
Radar:  
PRF, CPI

Time  
dependence

Sampling

Drone's  
Geometry,  
LOS  
Orientation

Coherent  
Sum  
at Drone's  
Phase  
Center



Doppler FFT as  
Function of Time

# Our proposed simulation approach

## Models

Precise EM  
(FEKO)

Simple  
(thin-wires)

## Measurements

Anechoic  
Chamber

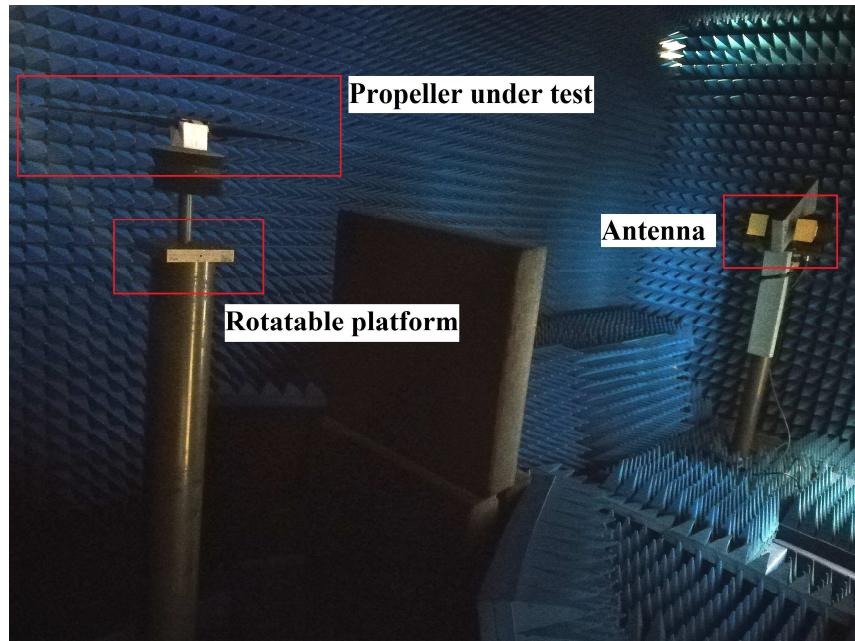
- Study the importance of input data quality (the choice of model source) on final micro-Doppler pattern
- To adapt simple thin-wires model for drone geometry and to study:
  - Efficiency of simplified mathematical model
  - Flexibility of simulation results as function of drone's geometry, propellers number and synchronization in rotation frequencies and initial positions, radar settings (operational frequency, PRF, CPI)
  - New scenarios: low SNR => long CPI

# Outline

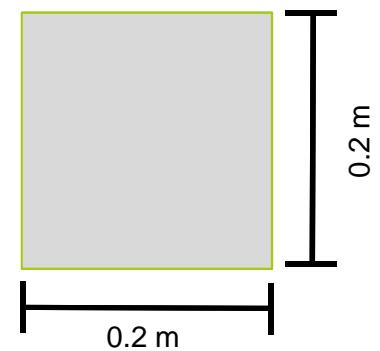
- Introduction
- General Approach
- **Single propeller characterization**  
– models and measurements
- Multi-propeller drone simulations
- Conclusion

# Radar signal scattering on single propeller

- Anechoic chamber measurements
  - HH polarization



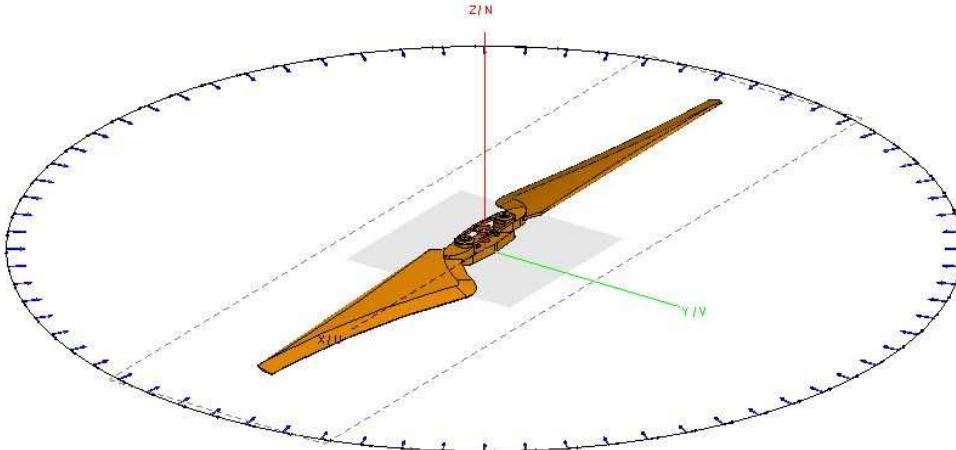
Anechoic chamber setup



Aluminium plate has been used as a reference

# Radar signal scattering on single propeller

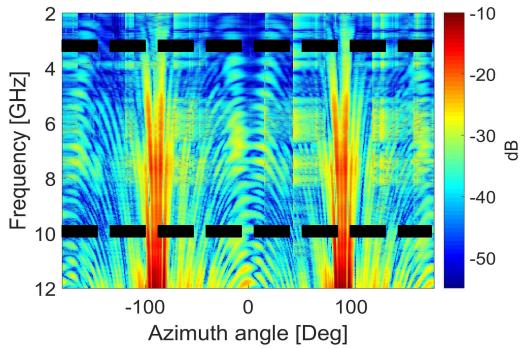
- FEKO software simulations
  - Far field, plane wave, HH polarization
  - Carbon fiber material



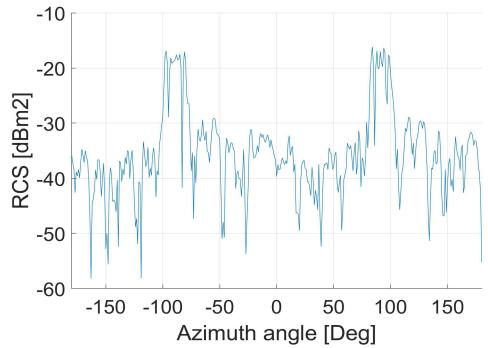
3D propeller model under simulation

# Radar signal scattering on single propeller

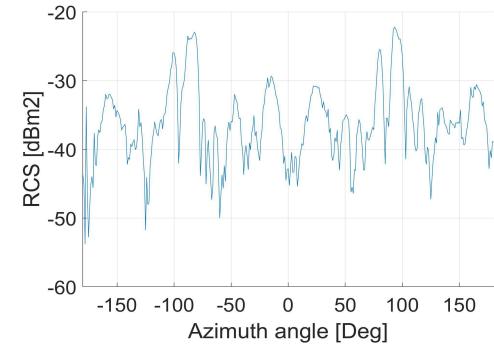
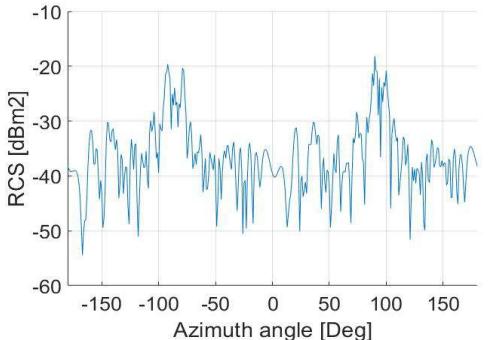
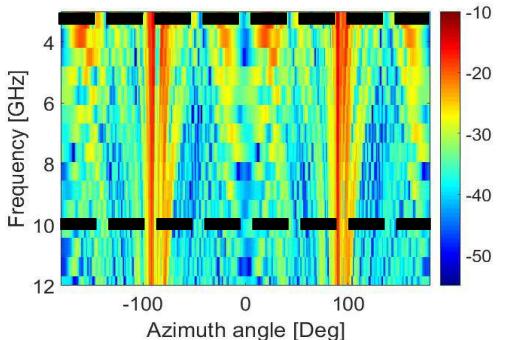
- RCS of single propeller – results from DUCAT and FEKO



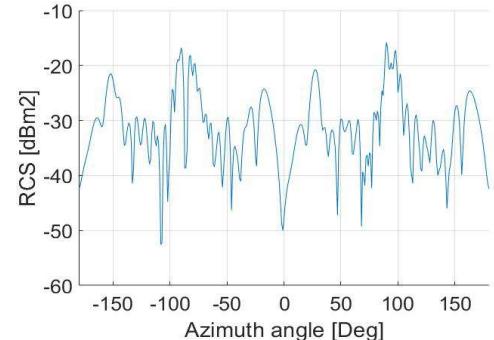
**Propeller RCS**



**Propeller RCS at 10 GHz**



**Propeller RCS at 3 GHz**

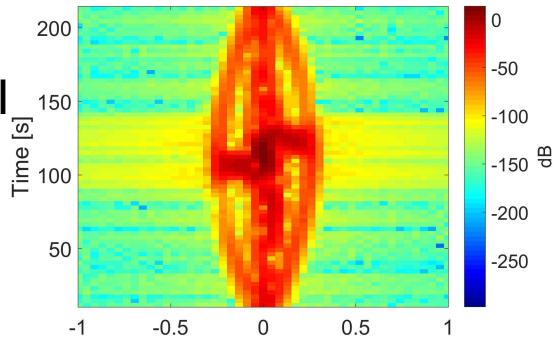


# Radar signal scattering on single propeller

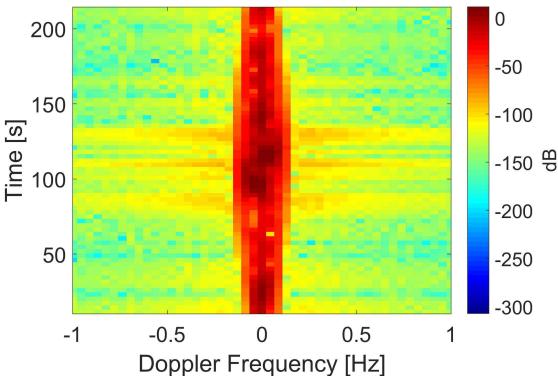
- Micro-Doppler pattern of a rotating propeller

Doppler processing of the rotating propeller scattering coefficient

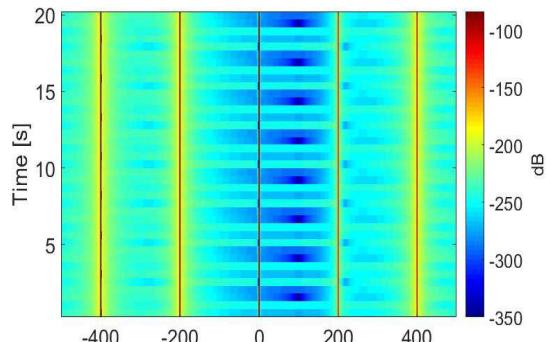
10 GHz,  
short CPI



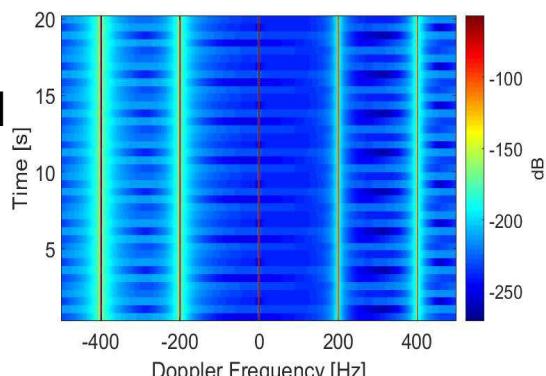
3 GHz,  
short CPI



10 GHz,  
long CPI



3 GHz,  
long CPI

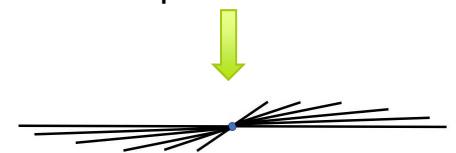


# Radar signal scattering on single propeller

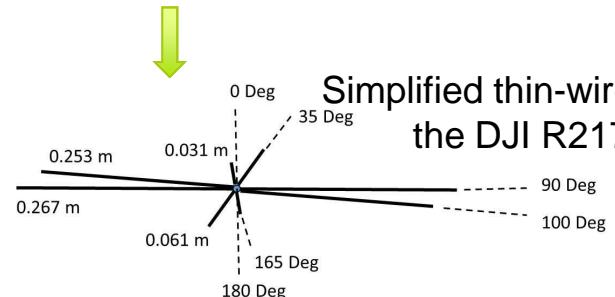
- Adaptation for drone's propeller at thin-wire simplified EM model  
Describe propeller's geometry structure in horizontal plane



Propeller R2170



Thin-wire model of the propeller



EM reflection from thin-wire model of propeller

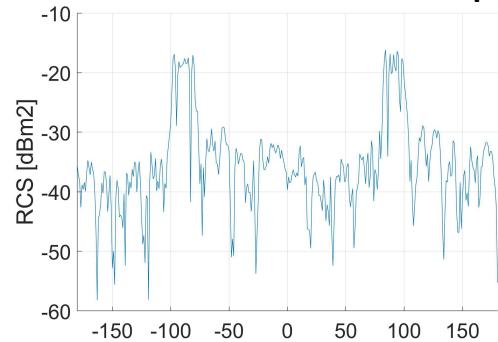
$$\begin{aligned} E^{prop}(t, r_p, \theta_{b,w}, l_{b,w}) &\sim \sum_{b=1}^B E_b^{blade}(t, r_p, \theta_{b,w}, l_{b,w}) \\ &= \sum_{b=1}^B \sum_{w=1}^W E_{b,w}^{wire}(t, r_p, \theta_{b,w}, l_{b,w}) \\ &= \sum_{b=1}^B \sum_{w=1}^W \int_0^{l_{b,w}} j\eta \frac{ke^{-jkr_p}}{4\pi r_p} \\ &\quad \times E_{r_p}^{in}(t) \sin^2(\theta_{b,w} + \Omega t) \\ &\quad \times e^{j2ky'_{b,w} \cos(\theta_{b,w} + \Omega t)} dy'_{b,w} \end{aligned}$$

**10 GHz**

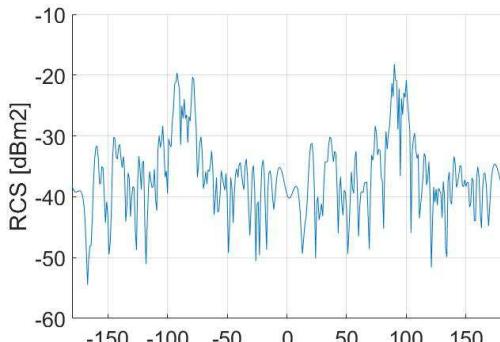
# Radar signal scattering on single propeller

- RCS of a single propeller – from thin-wire model

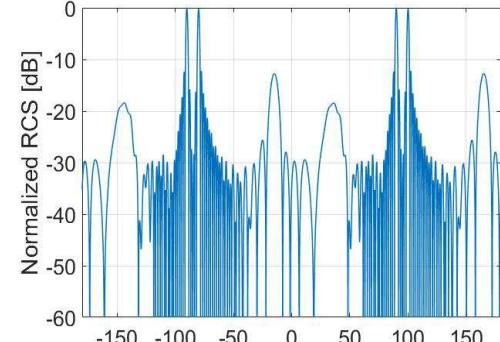
Thin-wire model comparison with the measurements and FEKO sim



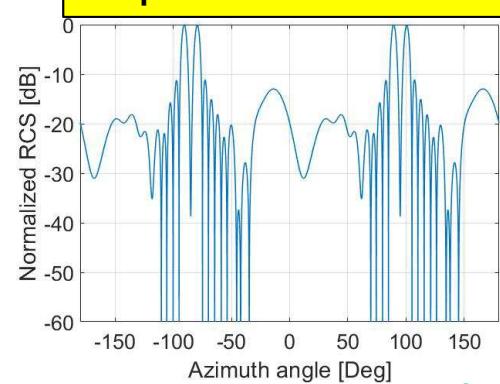
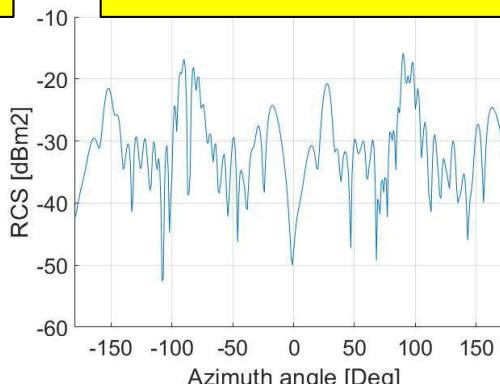
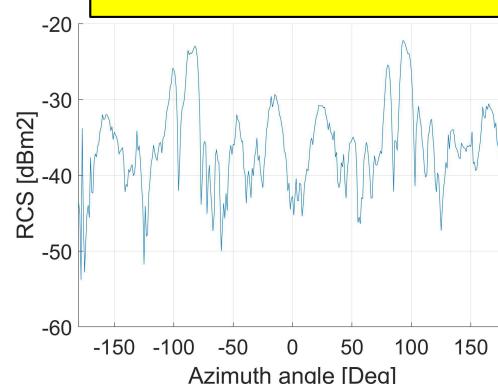
**Chamber measurement**



**FEKO simulation**

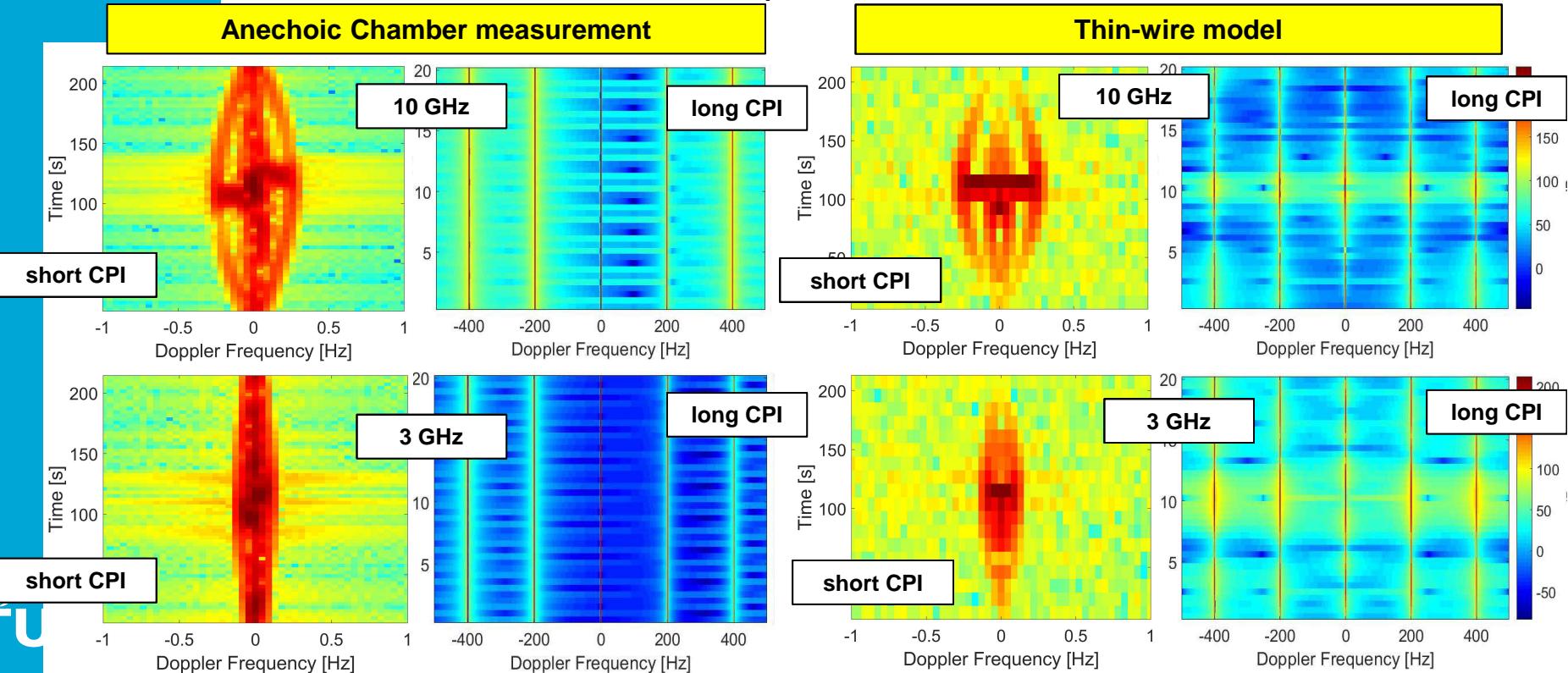


**Proposed thin-wire model**



# Radar signal scattering on single propeller

- micro-Doppler patterns of a single propeller
  - Thin-wire model comparison with the measurements



# Radar signal scattering on single propeller

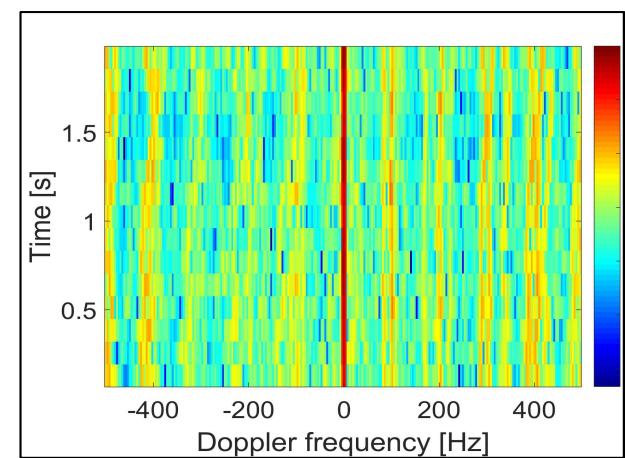
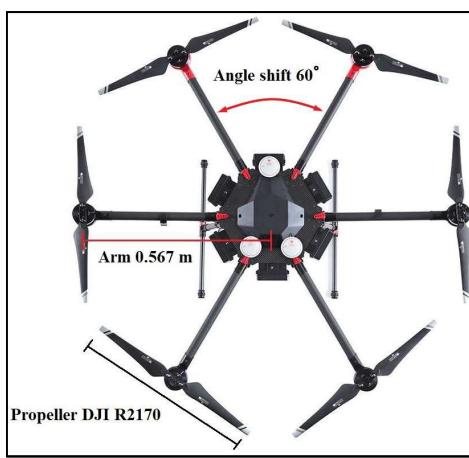
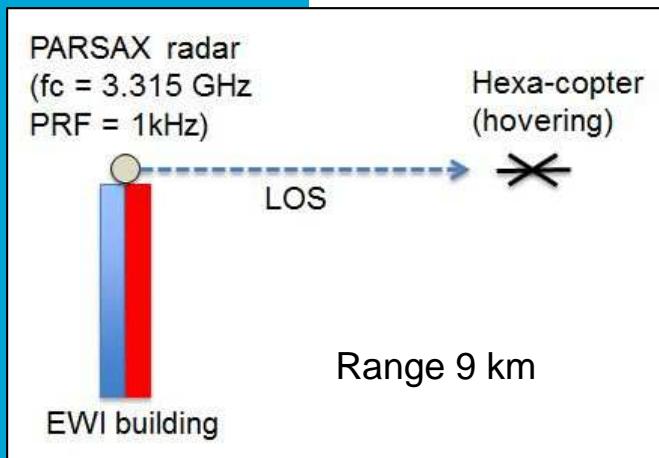
- Developed simplified representation of the propeller geometry as a bunch of thin wires with very low computational complexity of electromagnetic simulations
- The comparison with measurements in X-band and S-band show
  - in case of short CPI there are visible differences in micro-Doppler patterns – better to use for analysis pre-simulated or measured look-up tables
  - For the case of the long CPI only line spectrum frequency components are visible and their relative amplitudes are well reproduced by simple thin-wires model

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# Radar signal scattering on multi-propeller drone

- m-D pattern of a multi-propeller drone
  - Open air measurements by the PARSAAX radar



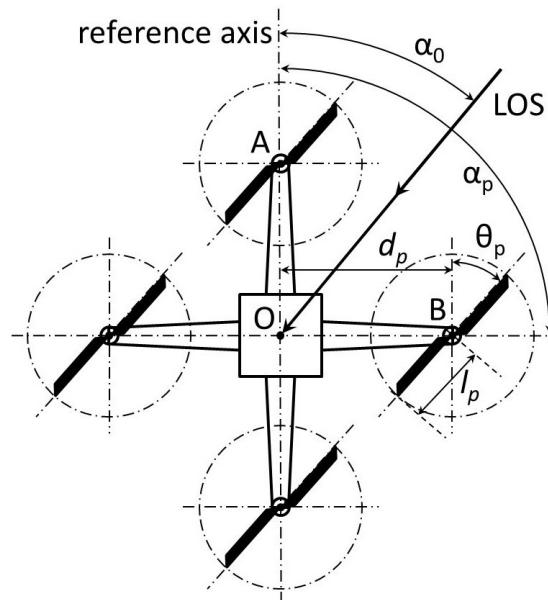
Real measurements

DJI Matrix 600  
Hexa-copter under test

micro-Doppler pattern  
of hexa-copter (long CPI)

# Radar signal scattering on multi-propeller drone

- Thin-wire model - describes the multi-propeller drone's geometry structure in horizontal plane via coherent summation of individual propellers, phase shifted to the drone's phase center:



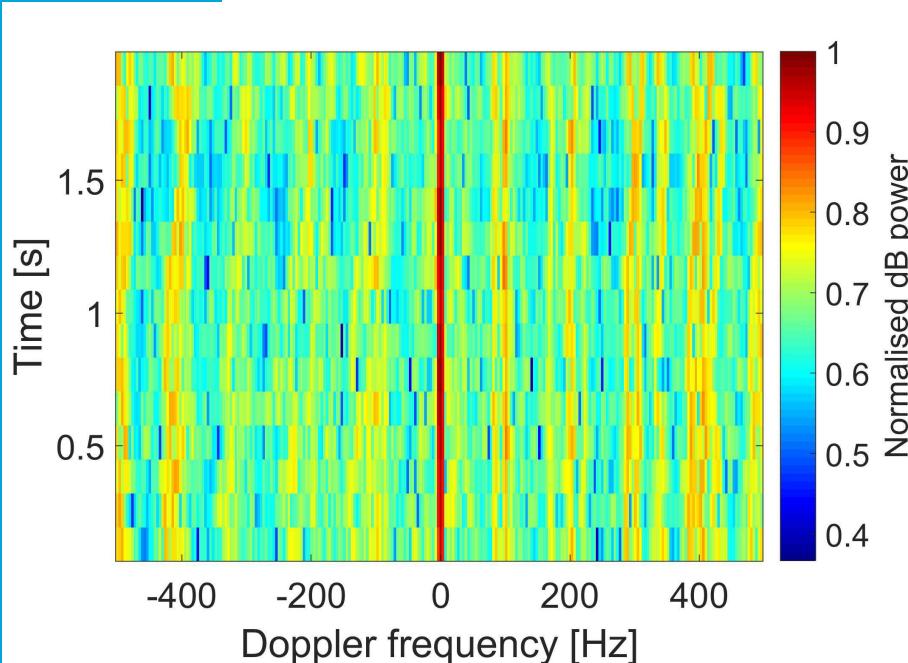
Geometry of multi-propeller drone  
(quad-copter for example)

$$\begin{aligned} E^{drone}(t, r_0) &\sim \sum_{p=1}^P E_p^{prop}(t, r_p, \theta_{p,b,w}, l_{p,b,w}) \\ &= \sum_{p=1}^P \sum_{b=1}^B \sum_{w=1}^W E_{p,b,w}^{wire}(t, r_p, \theta_{p,b,w}, l_{p,b,w}) \\ &= \sum_{p=1}^P \sum_{b=1}^B \sum_{w=1}^W \int_0^{l_{p,b,w}} j\eta \frac{ke^{-jkr_p}}{4\pi r_p} \\ &\quad \times E_{r_0}^{in}(t) \sin^2(\theta_{p,b,w} + \Omega_p t) \\ &\quad \times e^{j2ky'_{p,b,w} \cos(\theta_{p,b,w} + \Omega_p t)} dy'_{p,b,w} \\ &= \sum_{p=1}^P j\eta \frac{ke^{-jkr_p}}{4\pi r_p} \cdot E^{propeller} \end{aligned}$$

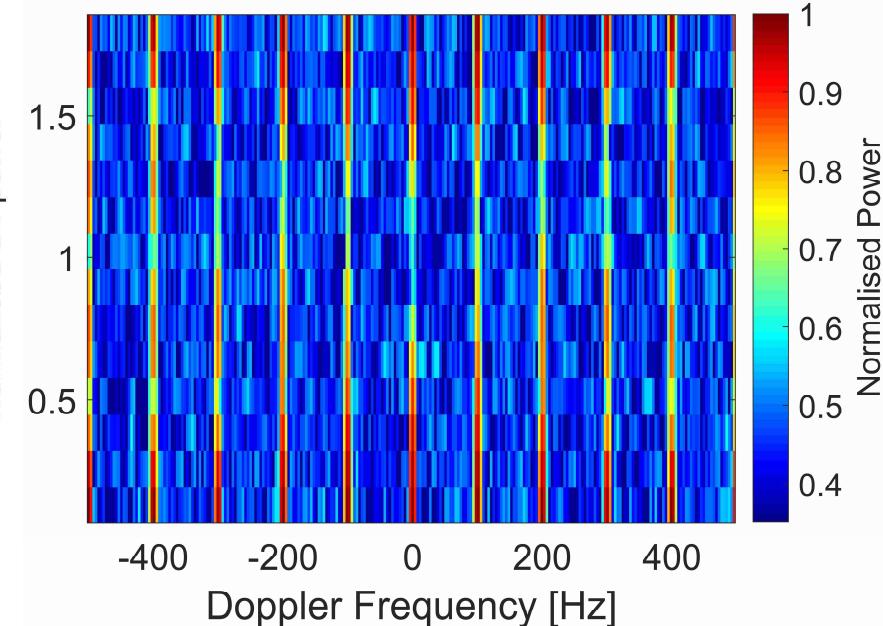
where  $r_p = r_0 - d_p \cdot \cos(\alpha_p - \alpha_0)$ .

# Radar signal scattering on multi-propeller drone

- The comparison of the M600 hexa-copter's micro-Doppler patterns measured with real radar and simulated with thin-wire model



PARSAX measurement



Thin-wire model

# Radar signal scattering on multi-propeller drone

- The proposed model of a multi-propeller drone gives a possibility
  - To synthesis and analyze micro-Doppler patterns of drones with different numbers and configurations of multiple propellers
  - To simulate and analyze the influence of observation angles and propeller synchronization on resulting micro-Doppler pattern
  - The simulation results show good agreement with experimental measurements in long distance (low SNR and, as result, requested long CPI) circumstances

# Conclusion

- Has been presented and illustrated a general approach for multi-propeller drones micro-Doppler patterns simulation based on modelled or experimentally measured angular dependencies of a single propeller scattering coefficients
- Low computational complexity simplified thin-wire model has been proposed to simulate multi-propeller drones micro-Doppler patterns as a function of radar parameters, drone's geometry and rotating propellers variables.
- Its validation by the comparison with real radar measurements at S-band shows good agreement in observed and simulated micro-Doppler patterns in case of radar observations with long CPI in terms of propeller rotation period.
- For more general cases can be used the proposed simulations approach that uses pre-defined (measured or precisely EM modelled) look-up tables of single propeller angular dependencies of scattering coefficient. It can be done for different polarizations and frequencies...

# Questions?

The usage of this model for the recognition of drones with different number of rotors will be illustrated within our presentation on the EuRAD-2019 conference in Paris