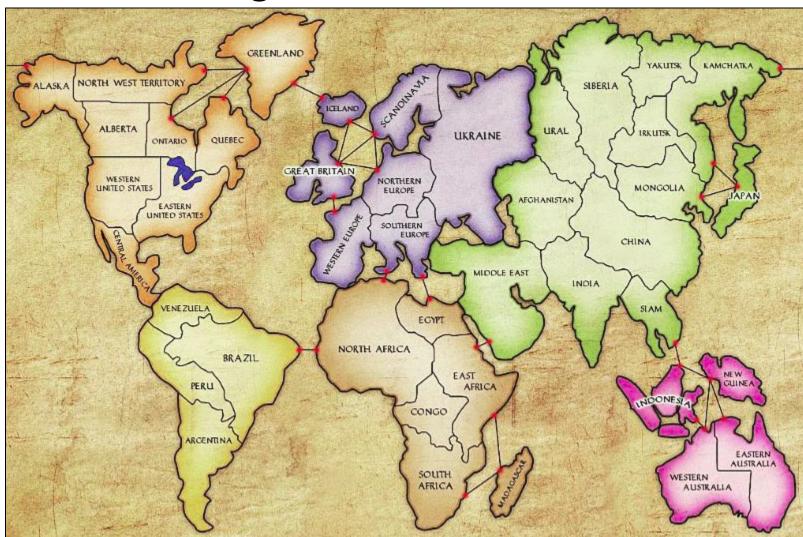
AI For World Domination

Oliver Krengel, Edward Terry, Henry Chen April 23, 2018



Risk: The board game

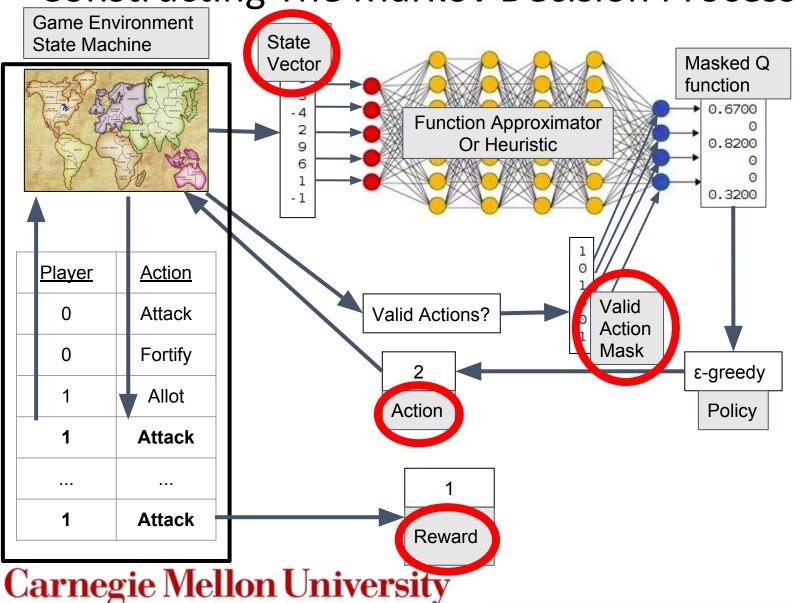


Challenges

- Environment Construction
 - Asynchronous turn order
 - Variable number of players
 - 4 Action types: Allot, Attack, Reinforce, Fortify
- State space
 - 42 territories
 - 7 players
 - Maximum 12 armies per territory
 - True state space: $(12 * 7)^42 = 6.6e80$
 - Simplified state space: (12 * 2)^42 = 9.3e57
 - 42 element vector
- Action space
 - 83 edges + 1 pass action = 84 element vector
 - Small subset are valid
- Highly stochastic dynamics
- State aggregation does not generalize well to valid actions
- But... reward shaping is straightforward!



Constructing The Markov Decision Process





Approach

Key decisions in construction:

- Flatten choices to single dimension game theory
- Game: formulate object as state machine, naive to players
- Environment: translates game state into Markov Decision Process
- Players: objects that hold a policy for each action type
- Policies: common interface
- Built informed heuristics to deploy as adversaries, and for imitation learning

To train: Initialize with imitation learning, then play against itself

Algorithm for imitation learning:

- 1. Repeat for N games:
 - a. Generate episode with heuristics: states (S), valid masks (V), actions (A)
 - b. Add winner's (S,V,A) to dataset
- 2. Repeat for E epochs:
 - a. Feed (S,V) into function approximator
 - b. Compute cross-entropy loss
 - c. Perform batch gradient descent



Hypothesis for Imitation Learning

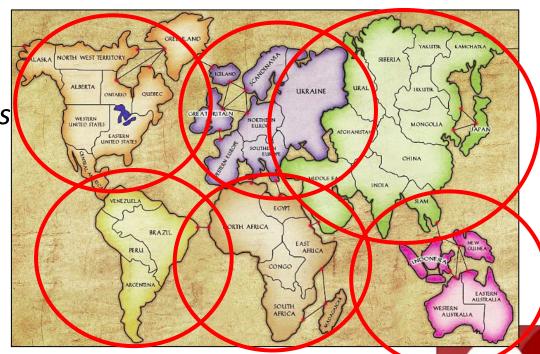
Heuristics:

- conservative is typically better than aggressive, but not always
- Do not make any state-specific decisions
- Don't treat continents any differently

Hypothesis:

By using winner moves, we will encode better policies than the dominant heuristic Reasoning:

Winners have made better state-specific decisions



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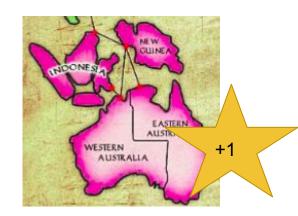
Results: Imitation Learning

Began with simpler environment: Australia!

Owner of Eastern Australia gets a bonus army

Hypothesis: best network will be #3

Network: {16:tanh:16:tanh:mask:sigmoid}



#	Hyperparameters					1000 games versus		
#	Players	Attack Heuristic	α	N	Е	Conservative	Aggressive	Random
1	2	Conservative x 2	1e-4	1000	10000	506 wins	522 wins	733 wins
2	2	Conservative, Aggressive	1e-4	1000	10000	449 wins	451 wins	634 wins
3	2	Conservative, Aggressive	1e-4	1000	20000	518 wins	503 wins	668 wins
4	2	Aggressive x 2	1e-4	1000	1000	465 wins	488 wins	640 wins

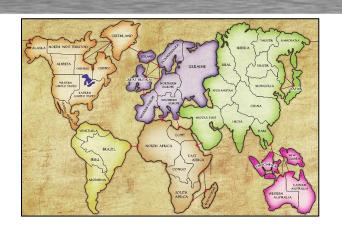
Results were inconclusive, but it took much longer to train the network attempting to learn from both policies



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Full board challenges

- Generalizing human data: autoencoder?
- How to best explore state-space?
- Bad policies can still win
 - Random wins ~5% against 6 conservative opponents
 - Some untrained networks can beat random policies
 - Makes testing very difficult!
- Attack heuristics break down, "gloat"
- For game with 7 conservative players, states visited:
 - Median: 405, μ = 420, σ =102
 - Most of these states are end-game, irrelevant
 - Solution: trim number of states visited, using:
 - $Max_States = \mu \sigma = 318$
- Playing 100 games takes 250s on 4-core Intel i5 @2.5Ghz





Full board results

KEY: Attack policies

F	N	С	A	R
Untrained network	Trained network	Conservative heuristic	Aggressive heuristic	Random policy



Hyperparameters

Architecture	α	N	E	Expert Policy	Max States
512:tanh:256:tanh:128	1e-4	100	2700	Winner of 7x conservative heuristics	318

Results: out of 100 games

	Wins by Player									
Matchup	0	1	2	3	4	5	6			
RAAACCC	7	8	7	13	30	19	16			
FAAACCC	2	7	5	6	29	30	21			
NAAACCC	7	18	25	25	6	10	9			
RC	6	94	-	-	-	-	-			
NC	20	80	-	-	-	-	-			

Lingering questions

- Train on/against human game data
- How to get state space sample
- More accurate n-player state space representation?
 - Separate maps for each player
 - Complex state-space representation
 - Angle corresponds to player
 - Magnitude corresponds to armies
 - Generalizes mid-game
- How to measure best policy?
 - No optimal game-theoretic policy exists
 - How can we manipulate other players??
-an utter lack of diplomacy......

