

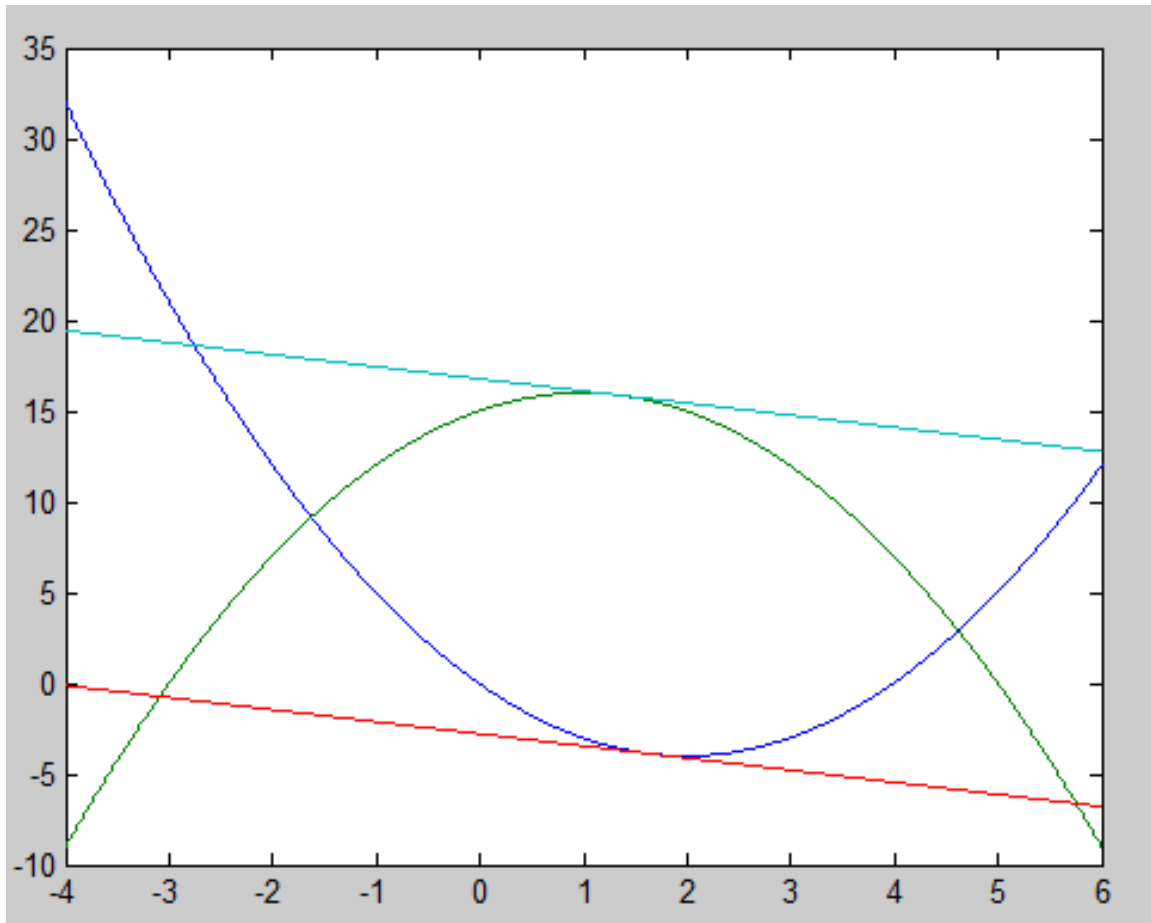
Homework Q2-50 points)

This question is a little bit different from generic linear programming model.

Find maximum and minimum value of $(2x_1+3x_2)$

$$\begin{aligned} \text{Constraints} \quad x_2 &\leq -(x_1)^2+2x_1+15 \\ x_2 &\geq (x_1)^2-4x_1 \end{aligned}$$

(HINT: You can use geometric illustration.)



Maximize:

Slope of $(2x_1+3x_2)$ is $-2/3$. Maximum value looks like top of the green line. Find tangent line that is parallel to $-2/3$.

Derivative of green line is $-2x_1+2=-2/3$ ----> $x_1=4/3$, x_2 is easily found using green curve equation. When both are plugged into $(2x_1+3x_2)$, $151/3$ is obtained.

Minimize:

Slope of $(2x_1+3x_2)$ is $-2/3$. Minimum value looks like bottom of the blue line. Find tangent line that is parallel to $-2/3$.

Derivative of green line is $2x_1-4=-2/3$ ----> $x_1=5/3$, x_2 is easily found using green curve equation. When both are plugged into $(2x_1+3x_2)$, $-25/3$ is obtained.