

**BIL105E - INTRODUCTION TO SCIENTIFIC AND ENGINEERING COMPUTING****KEYS to MIDTERM EXAM**

(There are 4 Questions. 2-Hour Exam)

**Q.1) (30)** Monte Carlo methods can be thought of as statistical simulation methods that utilize a sequence of random numbers to perform the simulation. The name "Monte Carlo" was coined by Nicholas Constantine Metropolis (1915-1999) and inspired by Stanislaw Ulam (1909-1986), because of the similarity of statistical simulation to games of chance, and because Monte Carlo is a center for gambling and games of chance. In this question you will write a simple Monte Carlo simulation to approximate the value of  $\pi$ . It involves randomly

selecting points  $\{(x_i, y_i)\}_{i=1}^n$  in the unit square and determining the ratio  $\rho = \frac{m}{n}$ , where  $m$  is number of points

that satisfy  $x_i^2 + y_i^2 \leq 1$ . You will read  $n$  from the keyboard, perform the simulation as explained above and print the ratio  $\rho$  to the screen.

```
#include <iostream>
#include <cstdlib>
#include <ctime>
using namespace std;

int main(){
    int n,m=0;
    cin >> n;
    srand(time(NULL));
    for (int i=0;i<n;++i){
        double x,y;
        x = 2.0*((double)rand()/RAND_MAX)-1;
        y = 2.0*((double)rand()/RAND_MAX)-1;
        if ((x*x+y*y)<=1.0) ++m;
    }
    cout << "pi is " << ((4.0*m)/n) ;
    return 0;
}
```

**Q.2) (20)** Write a function (**getSumOfOddDigits**) which takes an **unsigned long integer** and returns the sum of **only its odd valued digits**. Example: for n=23456798, the function should return 3+5+7+9=**24**.

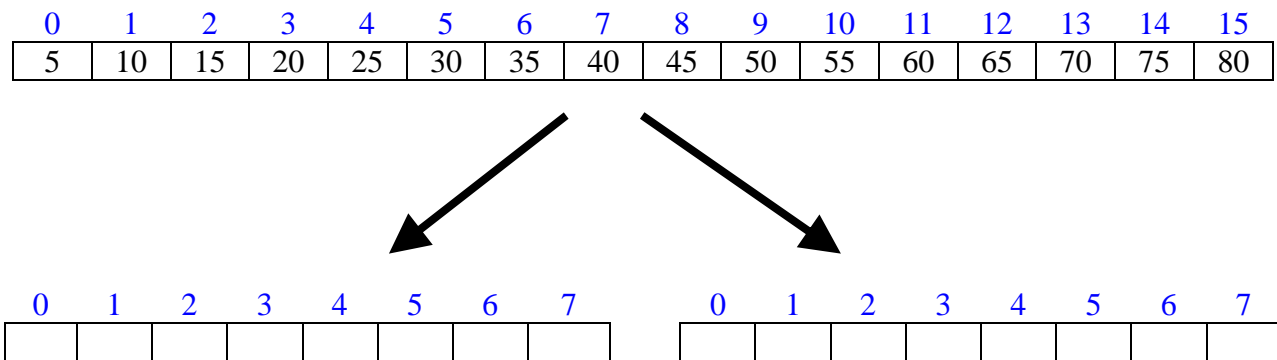
```
#include <iostream>
using namespace std;
```

```
int getSumOfOddDigits(unsigned long int n){
    int sum=0,dig;
    for (;n>0;n/=10)
        if ((dig=(n%10))%2) sum+=dig;
    return sum;
}
```

```
int main(){
    unsigned long int n=123456789;
    cout << getSumOfOddDigits(n) ;
    return 0;
}
```

**Q.3) (30)** Draw a flowchart and write a complete program which performs the following tasks:

- Initialize the original array as shown above.
- **Split** the original array **randomly** into **two other arrays** (the two new arrays should have almost equal lengths.) Then, display the contents of two new arrays.



```
#include <iostream>
#include <cstdlib>
#include <ctime>
using namespace std;

void printArray(int array[], int length){
    for (int i=0;i<length-1;++i)
        cout << array[i] << ", " ;
    cout << array[length-1] << endl ;
}

int main(){
    int array[16]={5};
    for (int i=1;i<16;++i)
        array[i]=array[i-1]+5;
    printArray(array,sizeof(array)/sizeof(int));
    srand(time(0L));
    int k= rand()%16;
    int leftArray[8]={0},rightArray[8]={0};
    for (int i=k,j=0;i<(k+8);++i,++j)
        leftArray[j]=array[i%16];
    printArray(leftArray,sizeof(leftArray)/sizeof(int));
    for (int i=k+8,j=0;i<(k+16);++i,++j)
        rightArray[j]=array[i%16];
    printArray(rightArray,sizeof(rightArray)/sizeof(int));

    return 0;
}
```

## Another solution

```
#include <iostream>
#include <cstdlib>
#include <ctime>
using namespace std;

void printArray(int array[], int length){
    for (int i=0;i<length-1;++i)
        cout << array[i] << ", " ;
    cout << array[length-1] << endl ;
}

int main(){
    int array[16]={5};
    for (int i=1;i<sizeof(array)/sizeof(int);++i)
        array[i]=array[i-1]+5;
    printArray(array,sizeof(array)/sizeof(int));
    srand(time(0L));
    int leftArray[8]={0},rightArray[8]={0};
    int left=0,right=0;
    for (int i=0;i<sizeof(array)/sizeof(int);++i){
        int k= (int)((double)rand()/RAND_MAX+0.5);
        if (left==sizeof(leftArray)/sizeof(int)) k=1;
        if (right==sizeof(rightArray)/sizeof(int)) k=0;
        switch(k){
            case 0:
                leftArray[left++]= array[i];
                break;
            case 1:
                rightArray[right++]= array[i];
                break;
        }
    }
    printArray(leftArray,sizeof(leftArray)/sizeof(int));
    printArray(rightArray,sizeof(rightArray)/sizeof(int));

    return 0;
}
```

## Yet another solution

```
#include <iostream>
#include <cstdlib>
#include <ctime>
using namespace std;

void printArray(int array[], int length){
    for (int i=0;i<length-1;++i)
        cout << array[i] << "," ;
    cout << array[length-1] << endl ;
}

int main(){
    int array[16]={5};
    for (int i=1;i<sizeof(array)/sizeof(int);++i)
        array[i]=array[i-1]+5;
    printArray(array,sizeof(array)/sizeof(int));
    srand(time(0L));
    int leftArray[8]={0},rightArray[8]={0};
    int left=0,right=0;
    for (int i=0;i<sizeof(array)/sizeof(int);++i){
        int k= (int)((double)rand()/RAND_MAX+0.5);
        if (left==sizeof(leftArray)/sizeof(int)) k=1;
        if (right==sizeof(rightArray)/sizeof(int)) k=0;
        switch(k){
            case 0:
                do {
                    int j=rand()%8;
                    if (leftArray[j]==0){
                        leftArray[j]= array[i];
                        ++left;
                        break;
                    }
                } while(true);
                break;
            case 1:
                do {
                    int j=rand()%8;
                    if (rightArray[j]==0){
                        rightArray[j]= array[i];
                        ++right;
                        break;
                    }
                } while(true);
                break;
        }
    }
    printArray(leftArray,sizeof(leftArray)/sizeof(int));
    printArray(rightArray,sizeof(rightArray)/sizeof(int));

    return 0;
}
```

All other solutions are welcome.

**Q.4) (20)** Draw a flowchart and write a complete program which performs the following tasks:

- Read values from keyboard for the coefficients  $A, B, C, D, E, F$  of the equations of two straight lines.  
 $Ax + By = C$   
 $Dx + Ey = F$
- Then determine whether the lines are parallel (their slopes are equal) or the lines intersect.
- If they intersect, determine whether the lines are perpendicular (the multiplication of their slopes is equal to -1).

```
#include <iostream>
using namespace std;

int main(){
    double A,B,C;
    double D,E,F;

    cin >> A >> B >> C ;
    cin >> D >> E >> F ;
    double slope1= -A/B;
    double slope2= -D/E;

    if (slope1==slope2)
        cout << "Two lines are parallel." << endl ;
    else
        if ((slope1*slope2)==-1.)
            cout << "Two lines are perpendicular." << endl ;

    return 0;
}
```