

FORMAL LANGUAGES AND AUTOMATA
Homework-3

1. Let α be a relation defined over the set $A = \{a, b, c, d\}$, expressed with the following matrix.

$$\alpha = \begin{bmatrix} 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}$$

- a. Express α as a relation graph.
 - b. Find $rs(\alpha)$ and $sr(\alpha)$ and show that they are equal.
 - c. Find $st(\alpha)$ and $ts(\alpha)$ and show that $st(\alpha) \subseteq ts(\alpha)$.
2. Design context-free grammars for the following languages:
- a. The set $\{0^n 1^n \mid n \geq 1\}$, that is, the set of all strings of one or more 0's followed by an equal number of 1's.
 - b. The set $\{a^i b^j c^k \mid i \neq j \text{ or } j \neq k\}$, that is, the set of strings of a's followed by b's followed by c's, such that there are either a different number of a's and b's or a different number of b's and c's, or both.
3. Consider the following grammar.

$$\begin{aligned} S &\rightarrow AbB \\ A &\rightarrow aA \mid \Lambda \\ B &\rightarrow aB \mid bB \mid \Lambda \end{aligned}$$

- a. Find the language generated by the grammar.
- b. What is the type of the grammar according to Chomsky hierarchy? Why?
- c. Design another grammar with a more restrictive type that generates the same expression you found in (a). (e.g. if the given grammar is Type-1 design a Type-2 or Type-3 grammar.)
- d. What is the type of the grammar you designed in (c)? Why?

IMPORTANT: You must do this homework by hand and submit it using the box in the secreteriat.