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Computer Engineering Department
Assist. Prof. Feza BUZLUCA
Asist.Prof. Mustafa Ersel KAMAŞAK
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DIGITAL CIRCUITS FINAL EXAM SOLUTIONS (Question 1)

QUESTION 1 (20 Points):

$$\begin{aligned}f(A,B,C,D) &= A'B'CD + AB'CD + AC'D + AC'D' + A'B'CD' + ABCD + ACD' \\&= (A'+A)B'CD + AC'(D+D') + A'B'CD' + ABCD + ACD' \quad (\text{Inverse}) \\&= (B'+AB)CD + AC' + A'B'CD' + ACD' \quad (\text{absorbition}) \\&= B'CD + A(CD + C') + (A'B'+A)CD' \quad (\text{absorbition}) \\&= B'CD + AD + AC' + B'CD' + ACD' \\&= B'CD + AD + B'CD' + A(C'+CD') \quad (\text{absorbition}) \\&= B'CD + AD + B'CD' + AC' + AD' \\&= B'C(D + D') + A(D+C'+D') \quad (\text{inverse}) \\&= B'C + A\end{aligned}$$

b)

f	AB \ CD	CD			
		00	01	11	10
00	1	1	1	1	1
01	0	0	0	1	1
11	Φ	0	Φ	1	1
10	1	1	1	1	1

By considering 0 and Φ points we can obtain complement of f.

$$\bar{f} = B\bar{C} + BD$$

De Morgan:

$$\begin{aligned}f &= \overline{B\bar{C} + BD} = \overline{B\bar{C}} \cdot \overline{BD} \\&= (\bar{B} + C) \cdot (\bar{B} + \bar{D})\end{aligned}$$

Or by considering true (1) points:

$$f = \bar{B} + (C\bar{D})$$

Distributive Law:

$$f = (\bar{B} + C) \cdot (\bar{B} + \bar{D})$$

DIGITAL CIRCUITS FINAL EXAM (Question 2)

QUESTION 2 (40 Points):

a.

Z AB \ CD	CD			
	00	01	11	10
00	1	0	1	1
01	1	1	1	0
11	Φ	0	0	0
10	1	0	1	1

Set of all prime implicants:

$\bar{C}\bar{D}$, $\bar{B}C$, $\bar{B}\bar{D}$, $\bar{A}B\bar{C}$, $\bar{A}BD$, $\bar{A}CD$
A B C D E F

b.

Prime Implicant Chart:

	0	2	3	4	5	7	8	10	11	Cost
✓ A	X			X			X			6
✓ B		X	X					X	X	5
C	X	X					X	X		6
D				X	X					8
✓ E					X	X				7
F			X			X				7

c.

Cheapest sufficient set of prime implicants:

A + B + E: Cost=18

Cheapest expression: $Z = \bar{C}\bar{D} + \bar{B}C + \bar{A}BD$

QUESTION 3

$$a) Q_1^+ = A\bar{Q}_1 + \bar{B}Q_1$$

$$Q_0^+ = 1 \oplus Q_0 = \bar{Q}_0$$

$$Z = \bar{S}_1 S_0 + S_1 \bar{S}_0$$

$$= S_1 \oplus S_0 = Q_1 \oplus Q_0$$

Output is a function of
states \rightarrow Moore Model

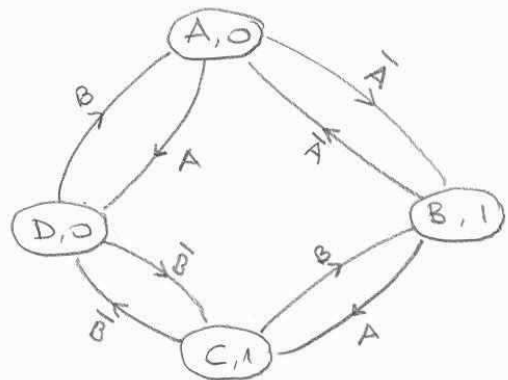
$Q_1^+ Q_0^+$	AB				Z
$Q_1 Q_0$	00	01	10	11	
00	01	01	11	11	0
01	00	00	10	10	1
10	11	01	11	01	1
11	10	00	10	00	0

A: 00

B: 01

C: 10

D: 11



$$b) Q_1^+ = D_1 = A\bar{Q}_1 + \bar{B}Q_1$$

$$Q_0^+ = D_0 = \bar{Q}_0$$

$$Z = Q_1 \oplus Q_0$$

