

Data Structures

Trees

Tree Definition

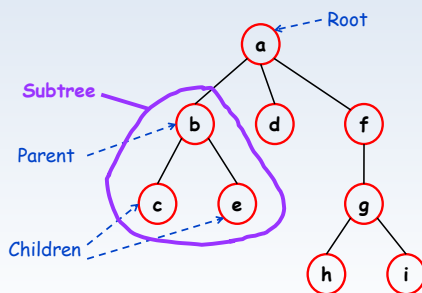
- The tree is a finite set of nodes.
 - There is a special node called the **root**.
 - The remaining nodes make up n separate, disjoint sets.
 - Each set has a separate tree structure.
 - These sets are called **subtrees**.
- The nodes one level below each node are the **child** nodes of that node.
- The node located one level above a node on the way to the root is the **parent** node.

2

ITÜ, BLG 221E Data Structures, G. Eryigit, S. Kabadayi © 2012

Trees

Example

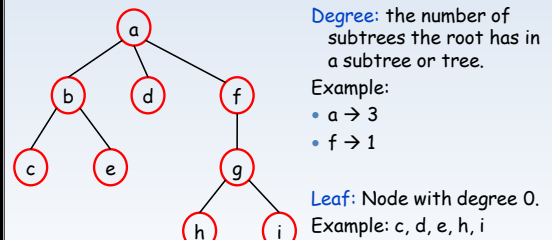


3

ITÜ, BLG 221E Data Structures, G. Eryigit, S. Kabadayi © 2012

Trees

Definitions

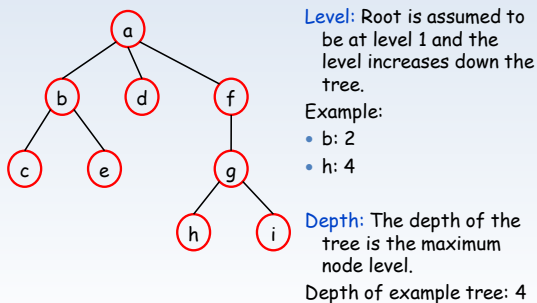


4

ITÜ, BLG 221E Data Structures, G. Eryigit, S. Kabadayi © 2012

Trees

Definitions



5

ITÜ, BLG 221E Data Structures, G. Eryigit, S. Kabadayi © 2012

Trees

Why a Tree?

- The list structure is not suited to storing and accessing large amounts of data.
 - Especially if fast access is desired.
- Many operations can be realized with $O(\log n)$ complexity on the tree structure.
 - For now, it suffices for us to know that tree operations, on average, can be performed much faster than list operations.
- Due to this speedup, tree structures are used in databases and many areas where indexing is necessary.
- In this course, we will study in detail the binary search tree, which is the simplest tree structure.
- You will learn about different tree structures in Advanced Data Structures.

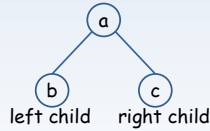
6

ITÜ, BLG 221E Data Structures, G. Eryigit, S. Kabadayi © 2012

Trees

Binary Tree

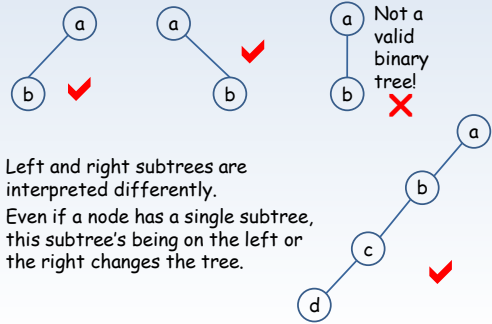
- Every node has at most two subtrees.
 - The degree of a node cannot be larger than 2.
- Subtrees are called left and right subtrees.



ITÜ, BLG 221E Data Structures, G. Eryigit, S. Kabadayi © 2012

Trees

Binary Tree Examples



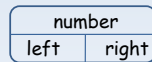
- Left and right subtrees are interpreted differently.
- Even if a node has a single subtree, this subtree's being on the left or the right changes the tree.

ITÜ, BLG 221E Data Structures, G. Eryigit, S. Kabadayi © 2012

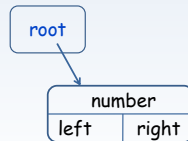
Trees

Data Structure

```
struct node {
    int number;
    node *left;
    node *right;
};
```



```
struct tree {
    node *root;
};
```

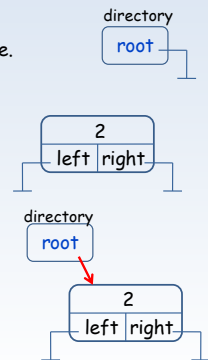


ITÜ, BLG 221E Data Structures, G. Eryigit, S. Kabadayi © 2012

Trees

Using the Tree Type

- We must first create an empty tree.
tree directory;
directory.root = NULL;
- Let us create a new node. Let the number in the node be "2".
node *p;
p = new node;
p->number = 2;
p->left = p->right = NULL;
- Let us add this node as the root to our "directory".
directory.root = p;

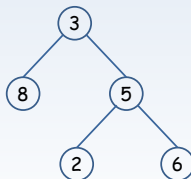


ITÜ, BLG 221E Data Structures, G. Eryigit, S. Kabadayi © 2012

Trees

Tree Representation

- From this point forward, we will not show left and right pointers in the diagrams. These always exist at each node.
- A simpler diagram:



ITÜ, BLG 221E Data Structures, G. Eryigit, S. Kabadayi © 2012

Trees

Tree Traversal

- Traversing a binary tree by visiting all nodes can be done in three ways:
 - Preorder
 - Inorder
 - Postorder
- All three types of traversals are, by definition, recursive operations.

ITÜ, BLG 221E Data Structures, G. Eryigit, S. Kabadayi © 2012

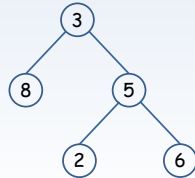
Trees

Preorder

- Traversal order
 - First, node itself
 - Then, left subtree
 - Finally, right subtree
- This operation repeats for each node.

Example:

3 8 5 2 6



13 ITÜ, BLG 221E Data Structures, G. Eryigit, S. Kabadayi © 2012

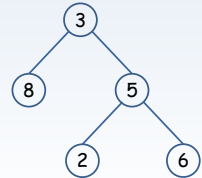
Trees

Inorder

- Traversal order
 - First, left subtree
 - Then, node itself
 - Finally, right subtree
- This operation repeats for each node.

Example:

8 3 2 5 6



14 ITÜ, BLG 221E Data Structures, G. Eryigit, S. Kabadayi © 2012

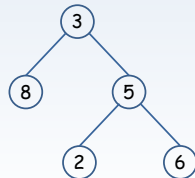
Trees

Postorder

- Traversal order
 - First, left subtree
 - Then, right subtree
 - Finally, node itself
- This operation repeats for each node.

Example:

8 2 6 5 3



15 ITÜ, BLG 221E Data Structures, G. Eryigit, S. Kabadayi © 2012

Trees

Coding the Traversal Methods

- All three traversal methods can easily be programmed recursively.
- Let us assume that the previously defined structure called "directory" has been created.
- Let us write the traversal functions that will work on this structure and print the data in the nodes to the screen.

16 ITÜ, BLG 221E Data Structures, G. Eryigit, S. Kabadayi © 2012

Trees

Preorder Function

```

void Preorder(node *nptr) {
    if (nptr) {
        cout << nptr->number << endl;
        Preorder(nptr->left);
        Preorder(nptr->right);
    }
}
  
```

17 ITÜ, BLG 221E Data Structures, G. Eryigit, S. Kabadayi © 2012

Trees

Inorder Function

```

void Inorder(node *nptr) {
    if (nptr) {
        Inorder(nptr->left);
        cout << nptr->number << endl;
        Inorder(nptr->right);
    }
}
  
```

18 ITÜ, BLG 221E Data Structures, G. Eryigit, S. Kabadayi © 2012

Trees

Postorder Function

```
void Postorder(node *nptr) {
    if (nptr) {
        Postorder(nptr->left);
        Postorder(nptr->right);
        cout << nptr->number << endl;
    }
}
```

19

ITU, BLG 221E Data Structures, G. Eryigit, S. Kabadayi © 2012

Trees

Iterative Inorder Function

```
void Inorder(node *root) {
    node *current;
    char flag = 1;
    stack s;
    s.create();
    current = root;
    while (flag) {
        while (current != NULL) {
            s.push(current);
            current = current->left;
        }
        if (!s.isEmpty()) {
            current = s.pop();
            cout << current->number
                << endl;
            current = current->right;
        }
        else
            flag = 0;
    }
}
```

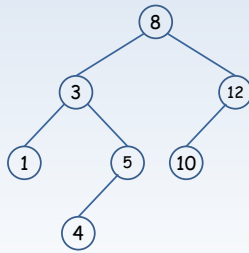
20

ITU, BLG 221E Data Structures, G. Eryigit, S. Kabadayi © 2012

Trees

Iterative Inorder Example

- Let us solve using the stack:
1 3 4 5 8 10 12



21

ITU, BLG 221E Data Structures, G. Eryigit, S. Kabadayi © 2012

Trees