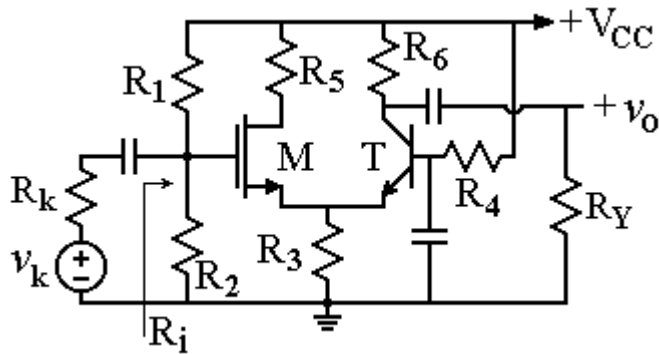


IMPORTANT: Besides your calculator and the sheets you use for calculations you are only allowed to have an A4 sized "copy sheet" during this exam. Notes, problems and alike are not permitted. Please submit your "copy sheet" along with your solutions. You may get your "copy sheet" back after your solutions have been graded. **Do not forget to write down units and convert units carefully!**

## ELE222(E) INTRODUCTION TO ELECTRONICS (20517-20521)

Final Exam ✍ 1 June 2010 ⌚ 12.00-14.00

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1. For the amplifier circuit shown on the left,  $V_{CC}=12V$ ,  $R_k=20k\Omega$ ,  $R_Y=20k\Omega$ , and all capacitors are ideal. Transistor parameters are  $\beta_n=10mA/V^2$ ,  $V_{TH}=1V$ ,  $\lambda=0$  for the MOSFET, and  $I_S=I_0=2 \times 10^{-15}A$ ,  $h_{fe}=\beta_F=50$ ,  $V_A=\infty$  for the BJT ( $V_T=25.9\text{ mV}$  @  $T=300K$ ).

a) Determine the values of resistors  $R_1$ ,  $R_2$ ,  $R_3$ ,  $R_4$ ,  $R_5$  and  $R_6$  so that  $V_G=5V$ ,  $V_{DS}=3.5V$ ,  $V_{CE}=4V$ ,  $V_E=3V$ ,  $I_D=10 \cdot I_C$  and  $r_i=R_i=100k\Omega$  (12 points).

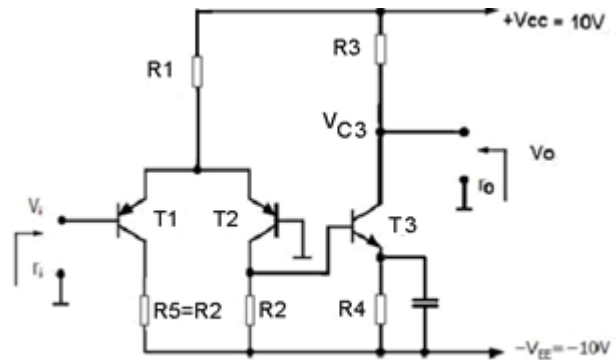
b) Calculate the AC gain of the circuit,  $v_o/v_k$ . (15 points)  
HINT :: You need to work on small signal circuit.

c) If AC input signal  $v_k$ 's amplitude is 50mV, what is the amplitude of the AC voltage  $v_d$  on the D(rain) of the MOSFET (8 points)?

2. For the BJTs on the right  $h_{fe}=\beta_F=250$ ,  $|V_{BE}|=0.6V$  and  $V_A=\infty$ .

a) For  $V_i=0V$  determine resistor values and CMRR such that  $V_{C3}=0V$ ,  $r_i=62k$ ,  $r_o=10k$  and  $|v_o/v_i|=6400$ .  
Remember  $R_1 \gg r_{e2}$  and  $V_T=25mV$  (25 points).

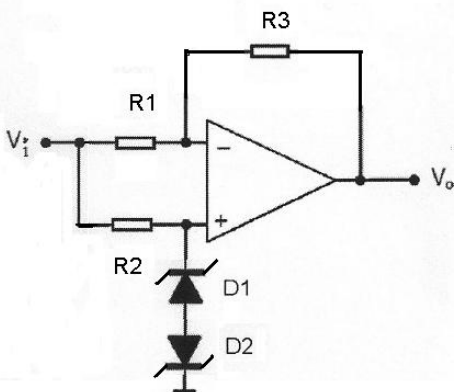
b) Using cutoff and saturation conditions for  $T_3$  ( $V_{CESAT}=0V$  for  $T_3$ ) determine the range of  $v_o$ . What is the maximum value of  $A$  to observe an undistorted output signal when a sinusoidal voltage with amplitude  $A$  is applied to the input (8 points)?



3. For the circuit shown on the left assume  $V_{CC}=10V$ ,  $-V_{EE}=-10V$ , the OPAMP is ideal, and  $V_Z=3.3V$ ,  $V_{DO}=0.7V$ ,  $I_{zmin}=0A$ .

a) Find the function realized by the circuit when  $V_i$  changes in the range  $-15V$  to  $15V$ . Analyze the circuit when the two Zener diodes are conducting and when they are not conducting (20 points).

b) For the conditions analyzed in a), draw the transfer function of the circuit (i.e.,  $V_o$  as a function of  $V_i$ ) for  $R_2=R_3=2 \times R_1$  and indicate important values (12 points).



GOOD LUCK!!!!

# ÇÖZÜMLER/SOLUTIONS:

a)  $V_S = V_E = 3V \rightarrow V_{GS} = V_G - V_S = 2V$

$V_{DS} = 3,5V > V_{GS} - V_{TH} = 1V$  (5V)

$\Rightarrow$  MOSFET kisilmada

$I_D = \frac{\beta_n}{2} (V_{GS} - V_{TH})^2 = 5mA = 10 I_C$

$\Rightarrow I_C = 0,5mA$

$V_{CC} - V_D = 5,5V = R_5 I_D \rightarrow R_5 = 1,1k\Omega$

$V_{DS} + V_S = 6,5V$  (0,5mA)

$V_{CC} - V_C = 5V = R_6 I_C \rightarrow R_6 = 10k\Omega$

$V_C + V_{CE} = 7V$

$V_{CC} - V_B = 8,32V = R_4 I_B \rightarrow R_4 = 832k\Omega$

$V_{BE} + V_E = 3,68V$   
 $V_{BE} = 0,68V$   
 $\frac{I_C}{\beta_F} = 10\mu A$

$V_E = (I_E + I_S) R_3 = \left(\frac{\beta_F + 1}{\beta_F} I_C + I_D\right) R_3$

$= 5,51mA \times R_3 = 3V \rightarrow R_3 = 544,5\Omega$

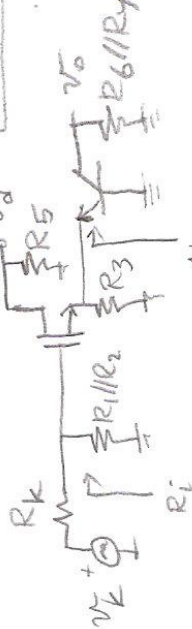
$V_G = 5V = \frac{R_2}{R_1 + R_2} V_{CC} \rightarrow \frac{R_2}{R_1 + R_2} = \frac{5}{12}$  (12V)

AC için  $R_i = R_1 // R_2 = 100k\Omega$

$\Rightarrow \frac{R_1 R_2}{R_1 + R_2} = R_1 \frac{5}{12} = 100k\Omega \rightarrow R_1 = 240k\Omega$  (\*\*)

(\*) + (\*\*)  $\Rightarrow R_2 = 171,4k\Omega$

b) AC eğer (c) de isteniyor



$g_m = \beta_n (V_{GS} - V_{TH}) = 10mS$

$g_{mT} = \frac{I_C}{V_T} = 19,3mS$  (47,3Ω)

$\frac{v_o}{v_k} = \frac{R_i}{R_i + R_k} \cdot \frac{g_{mT} (R_3 // \frac{1}{g_{mT}})}{1 + g_{mT} (R_3 // \frac{1}{g_{mT}})} \cdot g_{mT} (R_6 // R_4)$

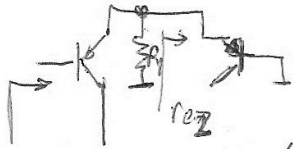
$= 0,833 \times 0,321 \times 128,7 = 34,4$  (47,3Ω)

c)  $\frac{v_d}{v_k} = \frac{R_i}{R_i + R_k} \cdot \frac{-g_{mT} R_5}{1 + g_{mT} (R_3 // \frac{1}{g_{mT}})}$

$= 0,833 \times (-7,468) = -6,223$

$v_d$  'nin genliği'  $= 6,223 \times 50mV = 0,311V$

( $v_k$  ile ters fazda)



$$r_i = \beta r_{e1} + r_{e2} // R_1$$

Es transistorlar  $\rightarrow r_{e1} = r_{e2} \left\{ \begin{array}{l} R_1 \gg r_{e2} \\ 25mV \\ \downarrow \\ 62000 \end{array} \right. \rightarrow r_i = \beta r_{e2} \rightarrow r_{e2} = 124 \Omega$

$$r_{e2} = \frac{V_T}{I_{E2}} \rightarrow I_{E2} \approx 200 \mu A$$

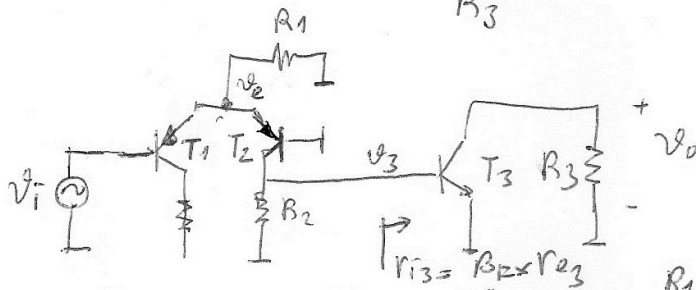
$$I_{R1} = 2 I_{E2} = 2 I_{E1} = 400 \mu A$$

$$I_{R1} = \frac{V_{CC} - V_{EB}}{R_1} \rightarrow R_1 \approx 23300 \Omega$$

$$r_o = 10K \rightarrow R_3 = 10K \Omega (V_A = \infty)$$

$$I_{E3} \approx I_{C3} = \frac{V_{CC} - V_{C3}^{OV}}{R_3} = 1mA$$

$$r_{e3} = \frac{V_T}{I_{E1}} = 25 \Omega$$



$$\frac{v_o}{v_i} = \frac{v_2}{v_i} \times \frac{v_3}{v_2} \times \frac{v_o}{v_3} = \frac{R_1 // r_{e2}}{r_{e1} + R_1 // r_{e2}} \times \frac{(\beta r_{e3}) // R_2}{r_{e2}} \times \left( - \frac{R_3}{r_{e3}} \right)$$

$$\approx \frac{1}{2} \frac{R_2 // (\beta r_{e3})}{r_{e2}} \times - \frac{R_3}{r_{e3}} = -6400 \rightarrow R_2 // (\beta r_{e3}) = 32$$

$$\rightarrow R_2 \approx 11K \Omega$$

$$I_{C2} = I_{R2} + I_{B3} \left( \frac{I_{C3}}{\beta_F} \right) \rightarrow R_4 \approx 1550 \Omega$$

$$I_{R2} = \frac{V_{BE3} + I_{E3} \times R_4}{R_2}$$

$$CMRR = \frac{2R_1 + r_{e2}}{2r_{e2}} \approx 188$$

$$yada \quad 20 \log \left( \frac{2R_1 + r_{e2}}{2r_{e2}} \right) \approx 45dB$$

b)  $I_{C3} \approx 0 \rightarrow V_o^+ = V_{Omax} = 10V$

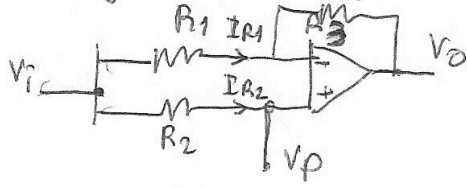
Transistor doymada  $V_o^- = V_{omin} = -V_{EB} + V_{E3} + V_{CEsat}$

$$= -10 + 1/55 \times 0V = -8,45 \quad I_{E3} R_4$$

Bu durumda altan önce kırılmaya başlar  $A = \left| \frac{V_{omin}}{V} \right| = \frac{8,45}{6400} = 1,32mV$

a)  $V_i$  değiştirildiğinde  
liğin da diğ otlardan

$-V_Z - V_{D0} \leq V_i \leq V_{D0} + V_Z$  ara-  
akım akmaz.



$$\left. \begin{aligned} I_{R2} &= 0 \rightarrow V_+ = V_i \\ I_{R1} &= \frac{V_i - V_-}{R1} = \frac{V_i - V_+}{R1} = 0 \end{aligned} \right\} \begin{aligned} V_o &= V_+ = V_i \\ \frac{V_o}{V_i} &= 1 \end{aligned}$$

(yeterince küçük)

$I_Z > I_{Zmin} \approx 0$  kabul edil-  
diğinden diğ otların uçla-  
rında zener gerilimi  
oluşur ve  $V_i > 4V$  ve  
 $V_i < -4V$  için  $V_p$  sabit  
kabul edilebilir.

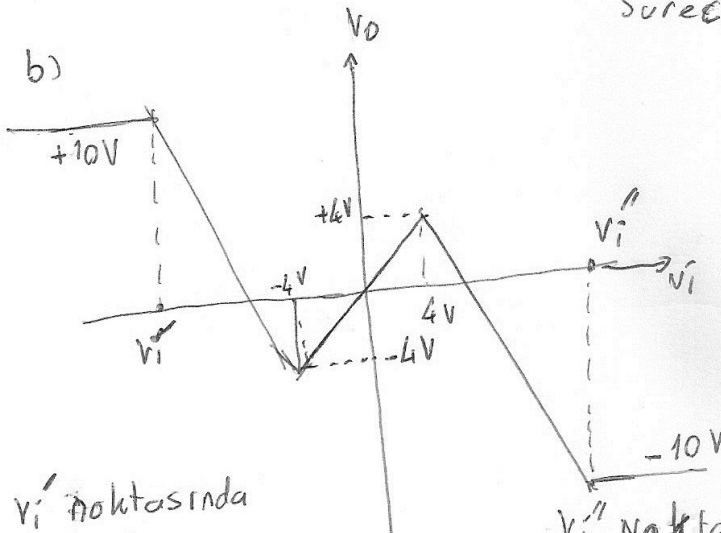
$$\left. \begin{aligned} D_2 \text{ normal} \\ D_1 \text{ Zener} \\ V_i > V_{D0} + V_Z = V_p^+ \quad V_p^+ = 4V \\ 0,7V \quad 3,3V \\ V_i < -V_{D0} - V_Z = V_p^- \quad V_p^- = -4V \\ D_1 \text{ normal} \quad D_2 \text{ Zener} \end{aligned} \right\}$$

Bu durumda

$$\frac{V_i - V_p}{R1} = \frac{V_p - V_o}{R3} \rightarrow V_o = -V_i \frac{R3}{R1} + V_p \left(1 + \frac{R3}{R1}\right)$$

$$R3 = 2R1 \rightarrow \boxed{V_o = -2V_i + 3 \cdot V_p}$$

(Bu bağıntı  $-V_Z \leq V_o \leq V_{D0}$  olduğu  
sürecek geçerlidir.)



$V_i'$  noktasında  
 $V_o = 10V$   
 $10 = -2V_i' - 12$   
 $V_i' = -11V$

$V_i''$  noktasında  
 $V_o = -10V$   
 $-10 = -2V_i'' + 12$   
 $V_i'' = +11V$

$$\textcircled{1} -15 < V_i < -11V$$

$$V_o = 10V$$

$$\textcircled{2} -11V \leq V_i < -4V$$

$$V_o = -2V_i - 12$$

$$\textcircled{3} -4V \leq V_i \leq 4V$$

$$V_o = V_i$$

$$\textcircled{4} 4 < V_i \leq 11V$$

$$V_o = -2V_i + 12$$

$$\textcircled{5} 11V \leq V_i < -15V$$

$$V_o = -10V$$