DAT565/DIT407 Assignment 4

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This paper is addressing the assignment 3 study queries within the *Introduction to Data Science & AI* course, DIT407 at the University of Gothenburg and DAT565 at Chalmers. The main source of information for this project is derived from the lectures and Skiena [1]. Assignment 4 is about correlation and linear regression.

Problem 1: Splitting the data

The dataset is large enough to be separated into a train and a test set. We use the function train_test_split with a test size of 0.2.

Problem 2: Single-variable model

To identify the variable with the strongest linear relationship with the target variable, we use the corr function specifying the Pearson method to get a correlation matrix between all the variables, and take the column corresponding to the target variable.

The variable with the highest absolute pearson coefficient is the Human development index, with a value of 0.92. Fig 2 shows the linear regression applied on the test set, using the model built on the train set. The model has a slope of 48.2, an intercept of 37.3, and a determination coefficient of 0.86. These values obviously slightly change depending on the seed used to split the data. The mean squared error for is 9.45.

Problem 3: Non-linear relationship

To explore variables with non-linear relationships, we initially assess Spearman correlation coefficients, Figure 3. Initially, we eliminate the variable exhibiting the strongest Pearson correlation, namely 'Human Development Index (value)'. Subsequently, we examine the Spearman correlation.

Our analysis reveals that 'Median Age, as of 1 July (years)' exhibits the most robust Spearman correlation. Subsequently, we develop a linear model using this variable to determine the mean squared error, which amounts to 13.58, Figure 5a.

Next, we apply transformations to the variable using logarithmic, square root, and reciprocal functions, respectively Figure 4. For each transformation,

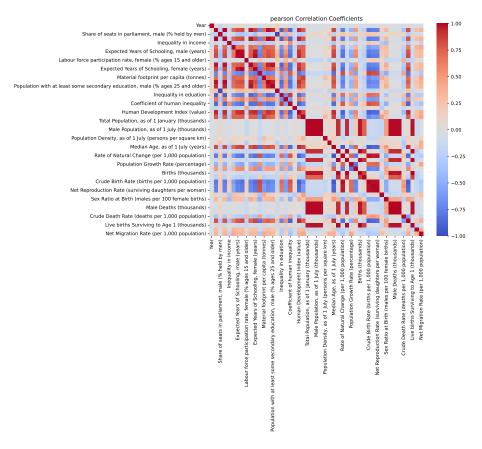


Figure 1: Correlation Pearson

we train a linear model to ascertain the resulting mean squared error. The logarithmic transformation yields the lowest mean squared error, measuring 11.52. Figure 5b.

Before transformation, the Pearson correlation registers at 0.898, while after transformation, it increases marginally to 0.913.

Problem 4: Mulitple linear regression

We employ Spearman correlation analysis to identify variables with strong correlations. Utilizing a predefined threshold, we pinpoint variables with significant impact. Through experimentation with various thresholds, we determine that a threshold of 0.85 yields favorable results without excessive variable inclusion.

The identified variables include: Expected Years of Schooling, female (years), Coefficient of human inequality, Gross National Income Per Capita (2017), Median Age as of 1 July (years), Rate of Natural Change (per 1,000 population), Crude Birth Rate (births per 1,000 population), Total Fertility Rate (live births per woman), and Net Reproduction Rate (surviving daughters per woman).

Conducting a multiple linear regression analysis results in a mean squared

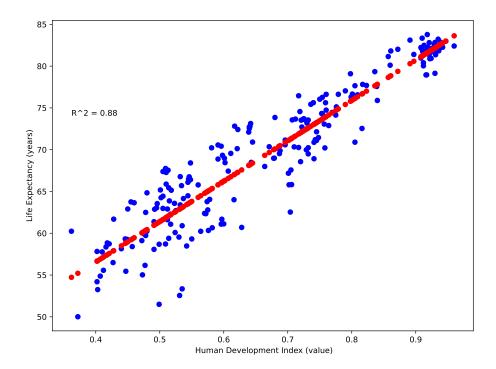


Figure 2: Linear Regression Human Development Index (value)

error of 2.03. The coefficients for the model are as follows: [19, -571, 243338, 61, 1.7, -2.1, 1.9, 3].

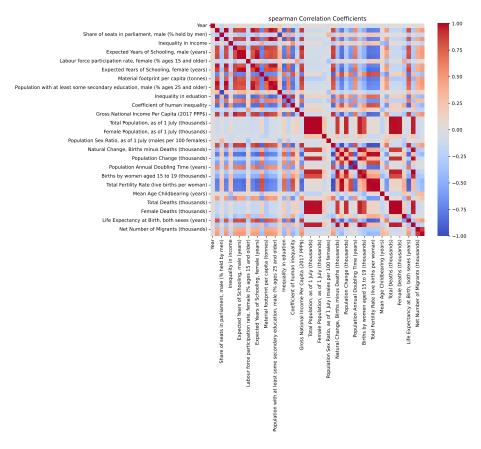


Figure 3: Correlation Spearman

References

[1] Steven S Skiena. The Data Science Design Manual. Retrieved 2024-01-20. 2024. URL: https://ebookcentral.proquest.com/lib/gu/detail.action?docID=6312797.

Appendix: Source Code

```
from matplotlib import pyplot
   import numpy as np
   import pandas as pd
   from sklearn.model_selection import train_test_split
   from sklearn.linear_model import LinearRegression
   import seaborn as sns
   from sklearn.metrics import mean_squared_error
8
   from sklearn.metrics import r2_score
10
   def calculate_correlation(data, variable, method):
       # Compute Pearson correlation coefficients
11
12
        correlation_matrix = data.corr(method = method)
13
```

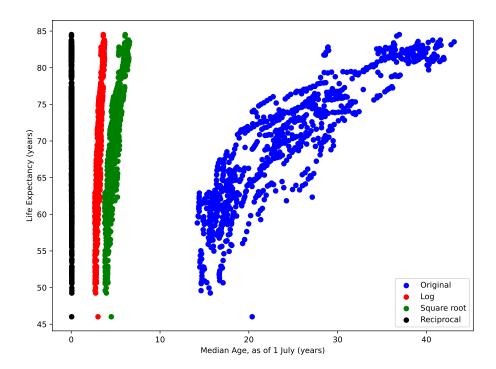


Figure 4: Linear transformation

```
14
       # Extract correlation coefficients of the target variable (life

→ expectancy)
15
        correlation_with_life_expectancy = correlation_matrix[variable]
        # Remove the target variable from the correlation coefficients
16
17
        correlation_without_life_expectancy =

    correlation_with_life_expectancy.drop(variable)

18
19
       # Find the variable with the highest absolute correlation

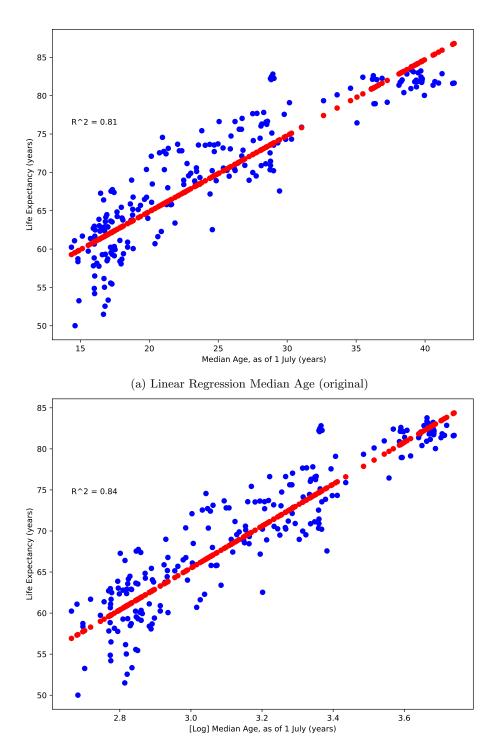
→ coefficient

20
        strongest\_correlation\_variable =
            21
        strongest_correlation_coefficient =

→ correlation_without_life_expectancy.abs().max()
        print(f"The_variable_'{strongest_correlation_variable}'_has_the
23
            \hookrightarrow \ \texttt{coefficient\_of\_\{strongest\_correlation\_coefficient:.2f}\}."
            \hookrightarrow )
24
25
        fig, ax = pyplot.subplots(figsize = (10, 8))
26
        sns.heatmap(correlation_matrix, annot=False, cmap='coolwarm')
       ax.set_title(method + '_Correlation_Coefficients')
fig.savefig(method + "_correlation.pdf", bbox_inches='tight')
27
28
29
30
        return strongest_correlation_variable, correlation_matrix
31
32
33
   def train_linear_regression_model(X_train, X_test, y_train, y_test,

    variables , prefix = ''):

34
       # Train a linear regression model using the variable with the
```



(b) Linear Regression Median Age (log)

Figure 5: Linear Regression Median Age

```
→ strongest correlation

35
        model = LinearRegression().fit(X_train, y_train)
36
        # Make predictions
        y_pred = model.predict(X_test)
37
        r2 = r2\_score(y\_test, y\_pred)
38
39
         , rows = X_test.shape
40
        if rows == 1:
             fig , ax = pyplot.subplots(figsize=(8, 6), layout=')
41
                ax.scatter(X_test, y_test, color='blue')
ax.scatter(X_test, y_pred, color='red')
ax.set_xlabel(prefix + "_" + variables)
42
43
44
45
            ax.set_ylabel('Life_Expectancy_(years)
            ax.text(0.1, 0.7, f'R^2 = \{r2:.2f\}', ha='center', va='
46

    center', transform=ax.transAxes)
47
             filename = prefix + "_linear_regression_" + variables + ".
                ⇔ pdf"
48
             filename = filename.replace('_', '_').lower()
49
             fig.savefig(filename, bbox_inches='tight')
50
51
52
        mse = mean_squared_error(y_test, y_pred)
53
        print("Trained_model_with_the_following_variables_" + prefix +
            \hookrightarrow ":", variables)
        \mathbf{print} \, (\, f\, \text{``The\_mean\_squared\_error\_for\_is\_} \{ mse : .\, 2 \, f \, \} \, .\, \text{``} \, )
54
55
56
    def transform_variable(X_train, y_train, correlation_variable):
57
        pd.options.mode.chained\_assignment = None
58
59
        X_train_selected = X_train[[correlation_variable]]
60
61
        X_train_selected['log'] = np.log(X_train[[correlation_variable
            → ]])
62
        X_train_selected['sqrt'] = np.sqrt(X_train[[
            X_train_selected['reciprocal''] = 1/(X_train[[
63

→ correlation_variable]])
64
65
        fig, ax = pyplot.subplots(figsize=(8, 6), layout='constrained')
66
        ax.scatter(X_train_selected.iloc[:, 0], y_train, color='blue',
            → label='Original')
        ax.scatter(X_train_selected['log'], y_train, color='red', label
67
            \hookrightarrow = 'Log')
        ax.scatter(X_train_selected['sqrt'], y_train, color='green',
68
            → label='Square_root')
        ax.scatter(X_train_selected['reciprocal'], y_train, color='
69
        70
71
        ax.set_xlabel(correlation_variable)
72
73
        ax.legend()
        fig.savefig("linear_transformation.pdf", bbox_inches='tight')
74
75
76
    file_path = "../life_expectancy.csv"
    life_expectancy = pd.read_csv(file_path, sep=',',).dropna()
77
    LEB = 'Life_Expectancy_at_Birth,_both_sexes_(years)
78
79
    life_expectancy.set_index('Country', inplace=True)
80
81
    life_expectancy_train , life_expectancy_test = train_test_split(
        \hookrightarrow life_expectancy, test_size=0.2)
82
    X_train = life_expectancy_train.drop(LEB, axis=1)
```

```
84 X_test = life_expectancy_test.drop(LEB, axis=1)
85 y_train = life_expectancy_train [LEB]
86
    y_test = life_expectancy_test [LEB]
87
88
89
90
    strongest\_pearson\_correlation\_variable\;,\;\; correlation\_pearson\; =\;
        91
    train_linear_regression_model(X_train[[
        \hookrightarrow strongest_pearson_correlation_variable]], X_test[[

    strongest_pearson_correlation_variable]], y_train, y_test,

→ strongest_pearson_correlation_variable)

92
    strongest_spearman_correlation_variable, correlation_spearman =
93

→ calculate_correlation (life_expectancy_train.drop (

→ strongest_pearson_correlation_variable , axis=1), LEB,

→ spearman ')

    train_linear_regression_model(X_train[[

→ strongest_spearman_correlation_variable]], X_test[[

→ strongest_spearman_correlation_variable | | , y_train , y_test ,

    strongest_spearman_correlation_variable)

95
    {\tt transform\_variable} \, (\, {\tt X\_train} \,\, , \  \, {\tt y\_train} \,\, ,

→ strongest_spearman_correlation_variable)

    train_linear_regression_model(np.log(X_train[[

→ strongest_spearman_correlation_variable]]), np.log(X_test[[
→ strongest_spearman_correlation_variable]]), y_train, y_test,
→ strongest_spearman_correlation_variable, "[Log]")
    train_linear_regression_model(np.sqrt(X_train[[

    strongest_spearman_correlation_variable]]), np.sqrt(X_test[[
        train_linear_regression_model(1/(X_train[[
        \hookrightarrow \ strongest\_spearman\_correlation\_variable]]) \ , \ 1/(X\_test[[
        99
100
    threshold = 0.85
101
    correlation_spearman_no_LEB = correlation_spearman.drop([LEB])
102
    relevant_variables = correlation_spearman_no_LEB [abs(
        train_linear_regression_model(X_train[relevant_variables], X_test[
        \hookrightarrow \ relevant\_variables \,] \,\,, \ \ y\_train \,\,, \ \ y\_test \,\,, \ \ relevant\_variables \,)
```