DAT565/DIT407 Assignment 5

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This paper is addressing the assignment 3 study queries within the $Introduction\ to\ Data\ Science\ &\ AI$ course, DIT407 at the University of Gothenburg and DAT565 at Chalmers. The main source of information for this project is derived from the lectures and Skiena [1]. Assignment 5 is about distance and network methods.

Problem 1: Preprocessing the dataset

Problem 2: Determining the appropriate number of clusters

Problem 3: Visualizing the classes

Problem 4: Evaluating clustering

Problem 5: Agglomerative clustering

References

[1] Steven S Skiena. The Data Science Design Manual. Retrieved 2024-01-20. 2024. URL: https://ebookcentral.proquest.com/lib/gu/detail.action?docID=6312797.

Appendix: Source Code

```
from umap import UMAP
1
   import pandas as pd
3 import matplotlib.pyplot as plt
   {\bf from} \ \ {\bf sklearn.preprocessing} \ \ {\bf import} \ \ {\bf StandardScaler}
   from sklearn.cluster import KMeans
6 from sklearn.random_projection import GaussianRandomProjection
   from sklearn.metrics import rand_score
   import itertools
   from sklearn.metrics import accuracy_score
10
   from scipy.cluster.hierarchy import dendrogram, linkage
   from sklearn.cluster import AgglomerativeClustering
12
13 # Load the seeds dataset
14
   random_state = 79
   15
17
18 X = seeds.drop(columns=['species']) # Features
19
   y = seeds['species']
20
21 # Normalize the data
22
    scaler = StandardScaler()
23
    X_normalized = scaler.fit_transform(X)
24
25
    seeds_normalized = pd.DataFrame(X_normalized, columns=X.columns)
26
    seeds_normalized['species'] = y
27
28
   X = seeds_normalized.drop(columns=['species'])
29
30
    def plot_inertia(X):
        inertia_values = []
31
32
        for k in range (1, 11):
            kmeans = KMeans(n_clusters=k, random_state=random_state).
33
                \hookrightarrow fit (X)
            inertia_values.append(kmeans.inertia_)
34
35
        plt.plot(range(1, 11), inertia_values, marker='o')
        plt.xlabel('Number of Clusters (k)')
plt.ylabel('Inertia')
plt.title('Inertia's Number of Clusters')
37
38
39
        plt.grid(True)
40
41
        plt.show()
42
    def plot_features(features, y, colors):
43
        num_features = len(features)
44
45
        num\_rows = num\_features - 1
46
        num\_cols = num\_features - 1
47
48
        fig, axes = plt.subplots(num_rows, num_cols, figsize=(15, 15))
49
        for i in range(num_rows):
```

```
51
                for j in range(num_cols):
                     if i != j:
 52
                          ax = axes[i, j]

ax.scatter(X[features[i]], X[features[j]], c=y.map(
 53
54
                               ⇔ colors))
                          ax.set_xlabel(features[i])
55
 56
                          ax.set_ylabel(features[j])
57
                          ax.set_title(f'Scatter-plot-between-{features[i]}-

    and { features [ j ] } ')

 58
59
           plt.tight_layout()
60
           plt.show()
 61
     \begin{array}{lll} \textbf{def} & \texttt{plot\_gaussian\_random\_projection} \, (X, \ y, \ \texttt{colors} \,) \colon \\ \end{array}
62
63
           grp = GaussianRandomProjection(n_components=2, random_state=
                → random_state)
64
           projected = grp.fit_transform(X)
 65
          \begin{array}{ll} plt.\,fig\,ure\,(\,fig\,siz\,e\,=\,(8,\ 6)\,)\\ plt.\,scatter\,(\,projected\,[:\,,\ 0]\,,\ projected\,[:\,,\ 1]\,,\ c=\!y\,.\\ map(\,colors\,)\,)\\ plt.\,xlabel\,(\,\,'Component\,\cdot\,1\,\,') \end{array}
66
67
 68
           plt.ylabel('Component-2')
plt.title('Scatter-plot-after-Gaussian-Random-Projection')
 69
 70
 71
           plt.show()
 72
 73
      def plot_umap(X, y, colors):
           umap_model = UMAP(n_components=2)
 74
 75
           umap = umap_model.fit_transform(X)
 76
 77
           plt.figure(figsize=(8, 6))
 78
           plt.scatter(umap[:, 0], umap[:, 1], c=y.map(colors))
 79
           plt.xlabel('UMAP-Component-1
           plt.ylabel('UMAP-Component-2')
plt.title('UMAP-Projection-of-Seed-Data')
80
 81
           plt.show()
 82
83
 84
 85
 86
      def find-permutation(n_clusters, true_labels, cluster_labels):
87
           permutations = itertools.permutations(range(n_clusters))
88
           best\_permutation = None
 89
           best_accuracy = 0
 90
           for permutation in permutations:
                {\tt permuted\_labels} = [\, {\tt permutation} \, [\, {\tt label} \, ] \  \, \begin{array}{c} \textbf{for} \\ \textbf{label} \end{array} \, \textbf{in}
91
                     92
                accuracy = accuracy_score(permuted_labels, true_labels)
93
                if accuracy > best_accuracy:
 94
                     best_accuracy = accuracy
95
                     best_permutation = permutation
96
           return best_permutation, best_accuracy
97
98
      def plot_dendrogram(n_clusters, X, y):
99
100
           linkage_options = ['ward', 'complete', 'average', 'single']
101
           best\_accuracy = 0
102
           best_linkage = None
103
104
           for linkage_option in linkage_options:
105
                clustering = AgglomerativeClustering(n_clusters=len(y.

    unique()), linkage=linkage_option)

106
                cluster = clustering.fit(X)
107
                permutation, accuracy = find_permutation(n_clusters, y,
```

```
⇔ cluster.labels_)
108
109
             if accuracy > best_accuracy:
110
                 best_accuracy = accuracy
111
                 best_linkage = linkage_option
112
        Z = linkage(X, method=best_linkage)
113
        plt.figure(figsize=(12, 6))
114
        dendrogram (Z, labels=y.values, leaf_rotation=90, leaf_font_size
115
             \hookrightarrow =8)
         plt.title(f"Dendrogram for {best_linkage}-linkage, Accuracy: {
116
        117
118
119
         plt.show()
120
121
    plot_inertia(X)
    colors = {1: 'red', 2: 'blue', 3: 'green'}
122
123
    features = seeds_normalized.columns
    \verb|plot_features| ( features , y, colors )
124
125
    plot_gaussian_random_projection(X, y, colors)
126
    plot_umap(X, y, colors)
127
128
129
    kmeans = KMeans(n_clusters=len(y.unique()), random_state=
        → random_state)
130
    kmeans. fit (X)
    kmeans_labels = kmeans.labels_
131
132
133
    rand_index = rand_score(y, kmeans_labels)
134
    print("Rand-score:", rand_index)
135
    all_labels = pd. Series (kmeans_labels)._append(y)
136
137
    all_unique_labels = all_labels.unique()
138
    best\_permutation, best\_accuracy = find\_permutation(len(
139

→ all_unique_labels), y, kmeans_labels)
140
    print("Best-Accuracy:", best_accuracy)
141
142
    print("Best - Permutation:", best_permutation)
143
    plot_dendrogram(len(all_unique_labels), X, y)
144
```