Question

Buycoins Inc is listed on the LSE with a stock price of £12.75 - the company is not known to pay dividends. We need to price a put option with a strike of \$10 maturing in 6 months. The continuously-compounded risk-free rate is 2.75%/year, the mean return on the stock is 6%/year, and the standard deviation of the stock return is 20%/year. What is the Black-Scholes put price?

Solution:

To calculate the Black-Scholes put price

$$P = Ke^{-rt} * N(-d_2) - S_oN(-d_1)$$

$$d_1 = \frac{ln\left(\frac{S_O}{K}\right) + \left(r + \frac{\sigma^2}{2}\right)t}{\sigma\sqrt{t}}$$
 , $d_2 = d_1 - \sigma\sqrt{t}$

Where:

C₀ = Current stock price

K = Strike stock price

 σ = represents the underlying volatility

r = risk-free interest rate

t = duration in years

N(d₁) and N(d₂) are cumulative distribution functions for a standard normal distribution

Given:

$$S_0 = £12.75$$
, K = £10, r= 2.75%, σ = 40%, T = 6months(1/2 years)

Calculating the d₁ and d₂

$$d_1 = \frac{\ln(\frac{S_0}{K}) + (r + \frac{\sigma^2}{2})t}{\sigma\sqrt{t}}$$

$$= \frac{\ln(\frac{12.75}{10}) + (0.0275 + \frac{0.4^2}{2})0.5}{0.4\sqrt{0.5}}$$

$$= \frac{0.243 + 0.05375}{0.2828} = 1.049$$

$$d_2 = d_1 - \sigma \sqrt{t}$$

$$= 1.049 - 0.4\sqrt{0.5}$$

$$= 0.7663$$

Checking the normal distribution table for $N(-d_1)$ and $N(-d_2)$

$$N(d_1) = 0.85314, N(d_2) = 0.77935$$

$$N(-d_1) = 1 - N(d_1)$$

= 1 - 0.85314
= 0.14686
 $N(-d_2) = 1 - N(d_2)$
= 1- 0.77935

Calculating the put price

= 0.23065

$$P = Ke^{-rt} * N(-d_2) - S_oN(-d_1)$$

$$= 10e^{-0.0275*0.5}(0.23065) - 12.75(0.14686)$$

$$= 2.275 - 1.4686$$

$$= 0.40255$$

The Put Price is £ 0.40255