

Inverse in $O(1)$

```
0: #include <bits/stdc++.h>
1:
2: using namespace std;
3:
4: constexpr int mod = 1e9 + 696969;
5: constexpr int n = pow(mod, 1.0 / 3) + 1;
6: constexpr int n2 = n * n;
7: constexpr int mod_n = mod / n;
8:
9: int p[n2 + 1];
10: int f[n2 + 1];
11: int inv[mod_n + 1];
12:
13: void precalc() {
14:     for (int y = 1; y < n; y++) {
15:         for (int x = 0; x <= y; x++) {
16:             int i = x * n2 / y;
17:             if (!p[i]) {
18:                 p[i] = x * n + y;
19:             }
20:         }
21:     }
22:
23:     int f_cnt = 0;
24:     for (int i = 0; i <= n2; i++) {
25:         if (p[i]) {
26:             f[f_cnt++] = p[i];
27:         }
28:         p[i] = f_cnt;
29:     }
30:
31:     inv[1] = 1;
32:     for (int i = 2; i <= mod_n; i++)
33:         inv[i] = mod - (long long) (mod / i) * inv[mod % i] % mod;
34: }
35:
36: int inverse(int a) {
37:     int i = p[(long long) a * n2 / mod];
38:     int x = f[i] / n;
39:     int y = f[i] % n;
40:     int u = a * y - mod * x;
41:
42:     if (abs(u) > mod_n) {
43:         i--;
44:         x = f[i] / n;
45:         y = f[i] % n;
46:         u = a * y - mod * x;
47:     }
48:
49:     assert(abs(u) <= mod_n);
50:     return (long long) y * (u < 0 ? mod - inv[-u] : inv[u]) % mod;
51: }
52:
53: mt19937 rng(2137);
54:
55: int randint(int a, int b) {
56:     return uniform_int_distribution<int>(a, b)(rng);
57: }
58:
59: int main() {
60:     precalc();
61:
62:     for (int x = 1; x < mod; x++) {
63:         int x_inv = inverse(x);
64:         assert((long long) x * x_inv % mod == 1 || gcd(x, mod) > 1);
65:     }
66:     return 0;
67: }
```