



MRC Cognition  
and Brain  
Sciences Unit



UNIVERSITY OF  
CAMBRIDGE

# **EEG/MEG 2:**

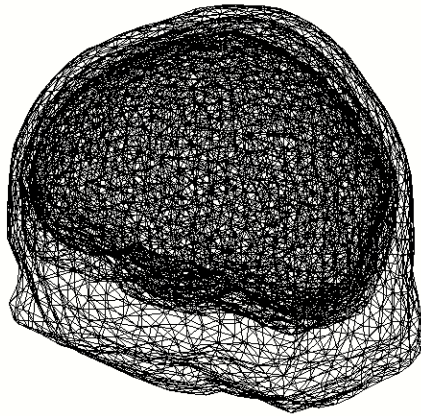
## **Head and Forward Modelling**

Olaf Hauk

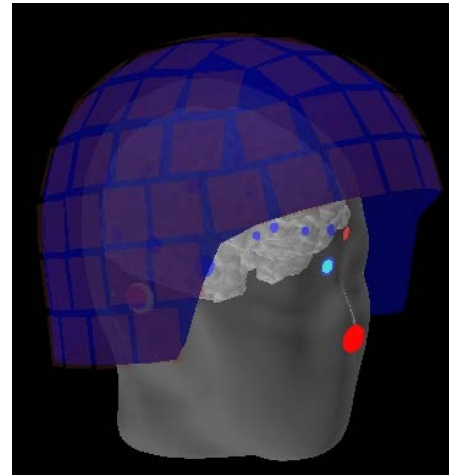
[olaf.hauk@mrc-cbu.cam.ac.uk](mailto:olaf.hauk@mrc-cbu.cam.ac.uk)

# Ingredients for Source Estimation

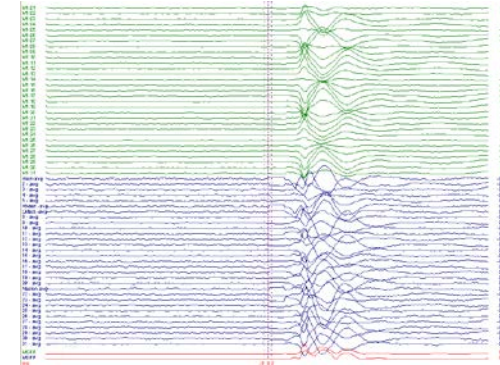
Volume Conductor/  
Head Model



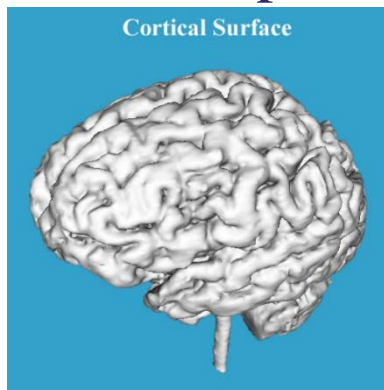
Coordinate  
Transformation



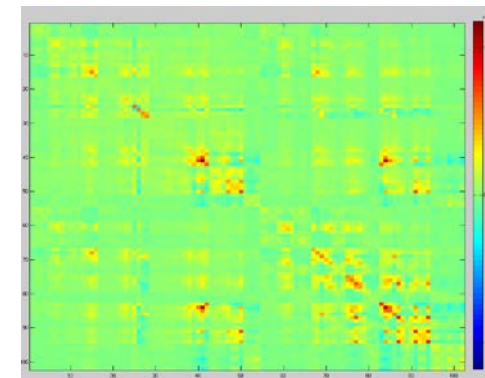
MEG data



Source Space

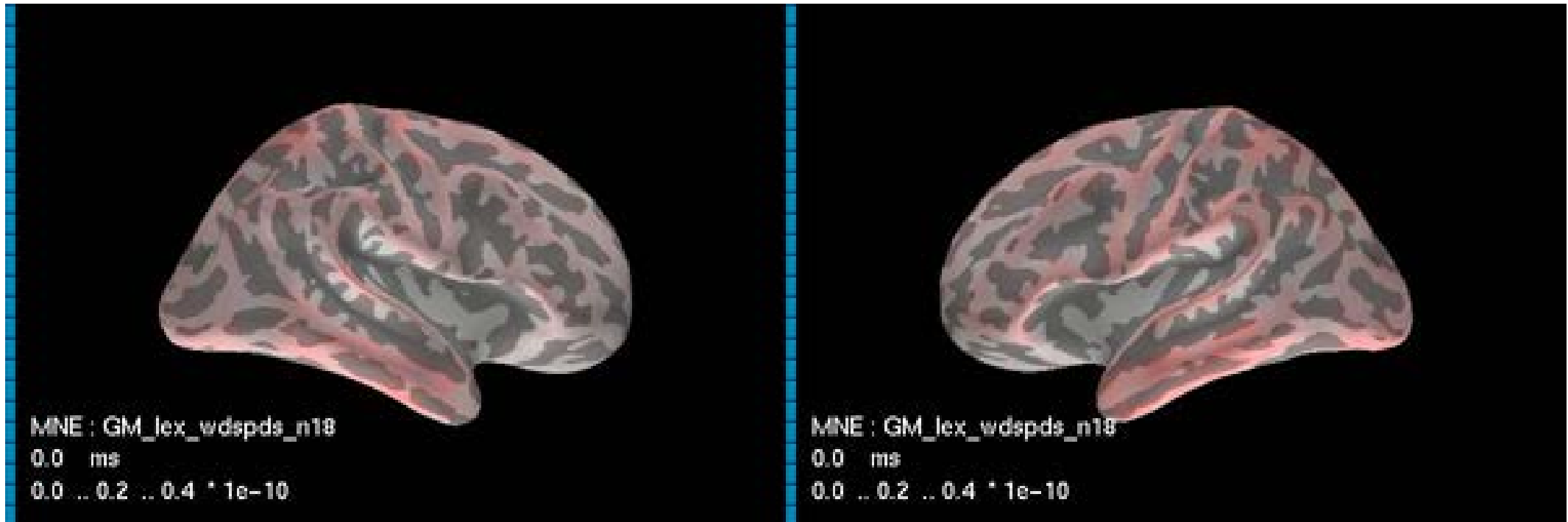


Noise/Covariance Matrix



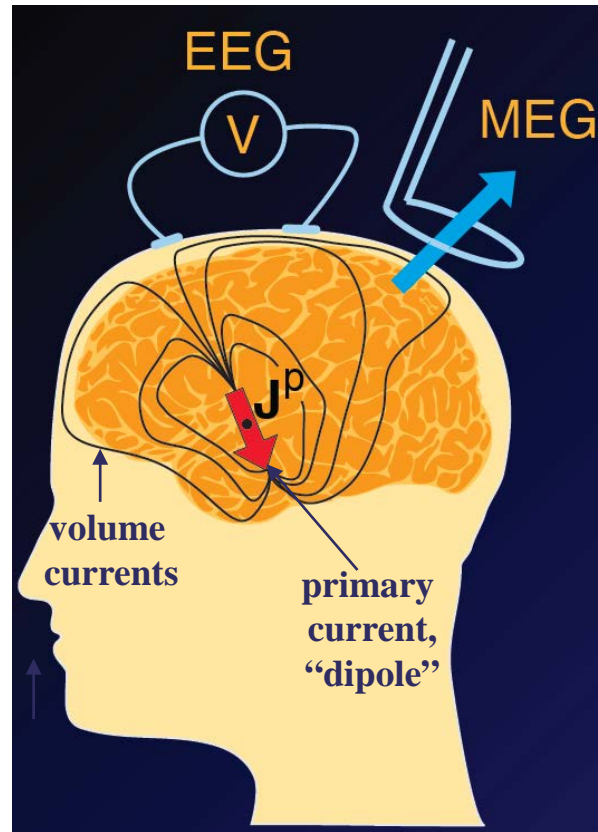
# Our Goal: Spatio-Temporal Brain Dynamics

## “Brain Movies”

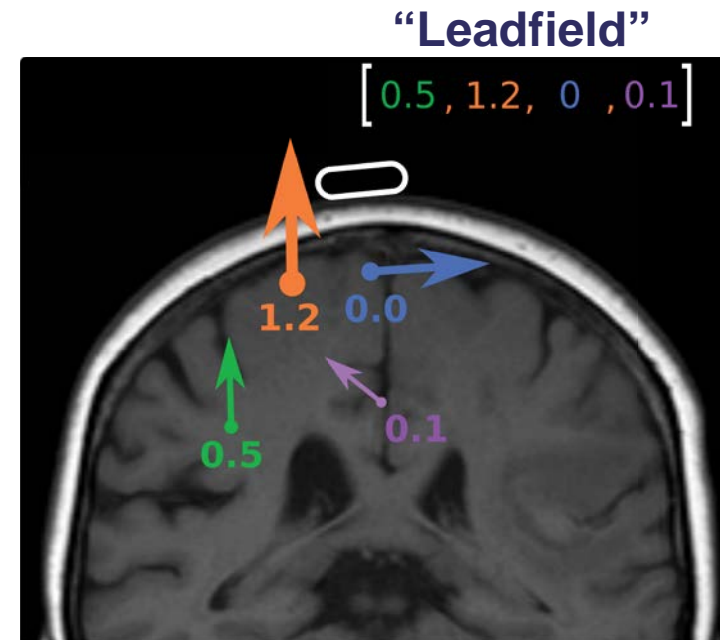


# We Have To First State The Forward Problem In Order To Solve The Inverse Problem

EEG/MEG measure the  
primary sources indirectly

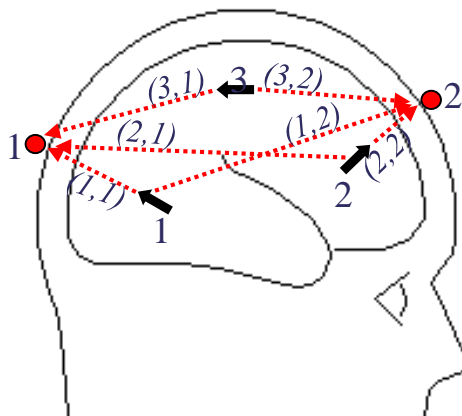


Sensors are differently sensitive  
to different sources



Hauk, Stenroos, Tredner. In: Supek S, Aine C (eds), "Magnetoencephalography: From Signals to Dynamic Cortical Networks, 2nd Ed."

# The EEG/MEG Forward Problem



$$\begin{array}{c}
 \text{data} \quad \text{"leadfield"} \quad \text{dipoles} \\
 \begin{matrix} 1 \\ 2 \end{matrix} \cdot \begin{pmatrix} d_1 \\ d_2 \end{pmatrix} = \begin{pmatrix} 0.5 & 0 & 0.3 \\ 0 & 1 & -0.3 \end{pmatrix} \begin{pmatrix} j_1 \\ j_2 \\ j_3 \end{pmatrix} \begin{matrix} \nwarrow 1 \\ \nearrow 2 \\ \nwarrow 3 \end{matrix} \\
 \text{?} \\
 \text{inversion} \\
 \begin{matrix} \nwarrow 1 \\ \nearrow 2 \\ \nwarrow 3 \end{matrix} \begin{pmatrix} j_1 \\ j_2 \\ j_3 \end{pmatrix} = \begin{pmatrix} 1.5034 & 0.1241 \\ 0.2483 & 0.9379 \\ 0.8276 & -0.2069 \end{pmatrix} * \begin{pmatrix} d_1 \\ d_2 \end{pmatrix} \begin{matrix} 1 \\ 2 \end{matrix} \cdot
 \end{array}$$

$$j_1 + j_2 = 1$$

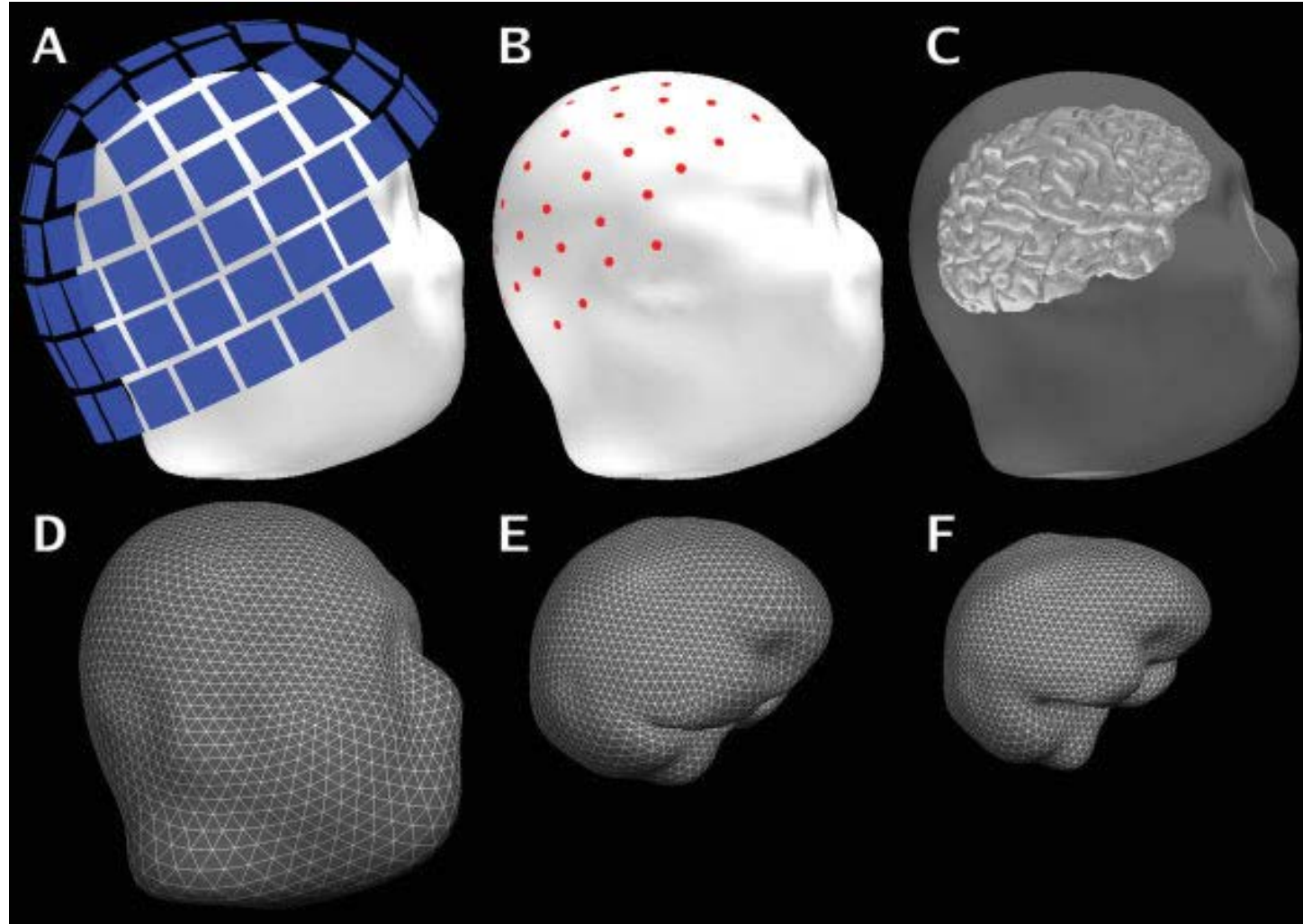
under-determined problem, no unique solution

$$\mathbf{d} = \mathbf{L}\mathbf{j}$$

**d**: data (n\_sensors x 1) **L**: "leadfield" (n\_sensors x n\_dipoles), **j**: dipoles (n\_dipoles x 1)

Usually n\_dipoles >> n\_sensors.

# Ingredients for a head model



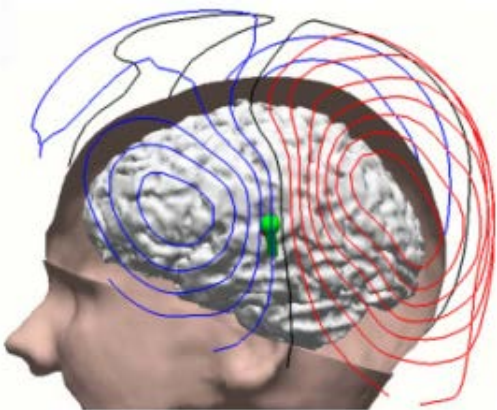
Goldenholz et al., HBM 2009  
<https://pubmed.ncbi.nlm.nih.gov/18465745/>

If you don't have individual MRIs: Standard head models and spherical approximations are available.

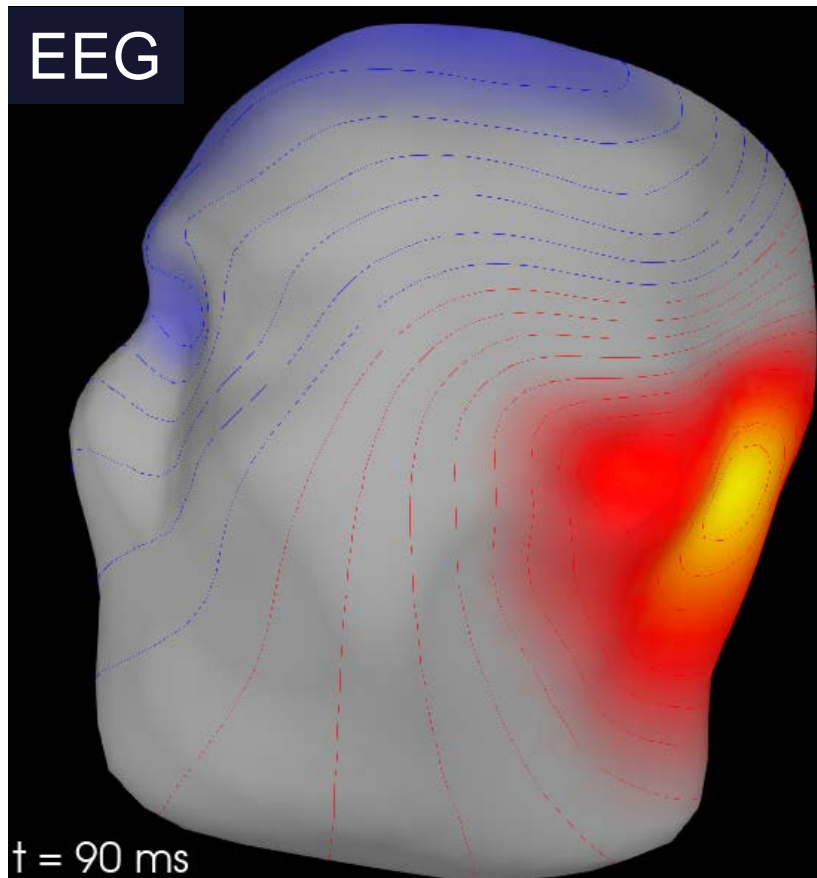


# Example: Auditorily Evoked Activity

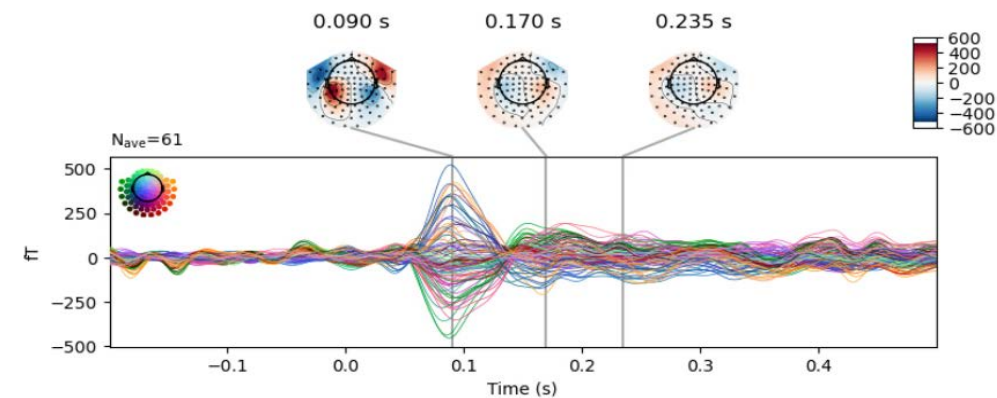
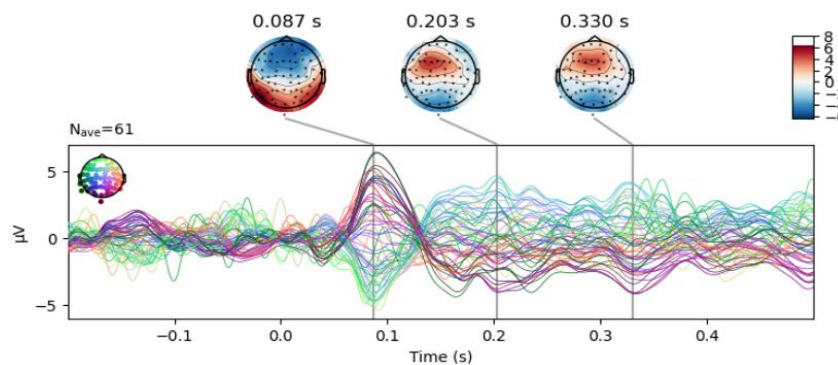
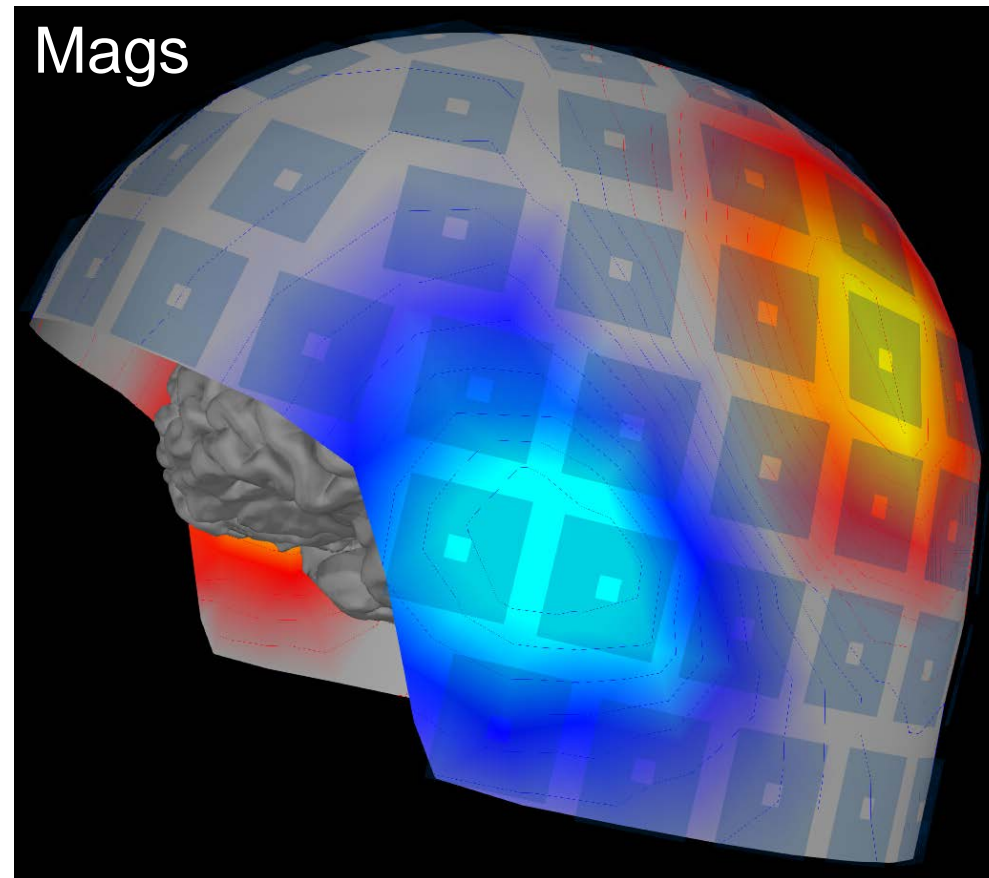
Tone to right ear



EEG

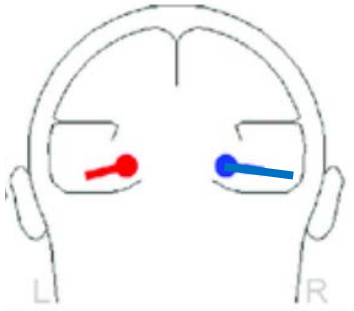


Mags

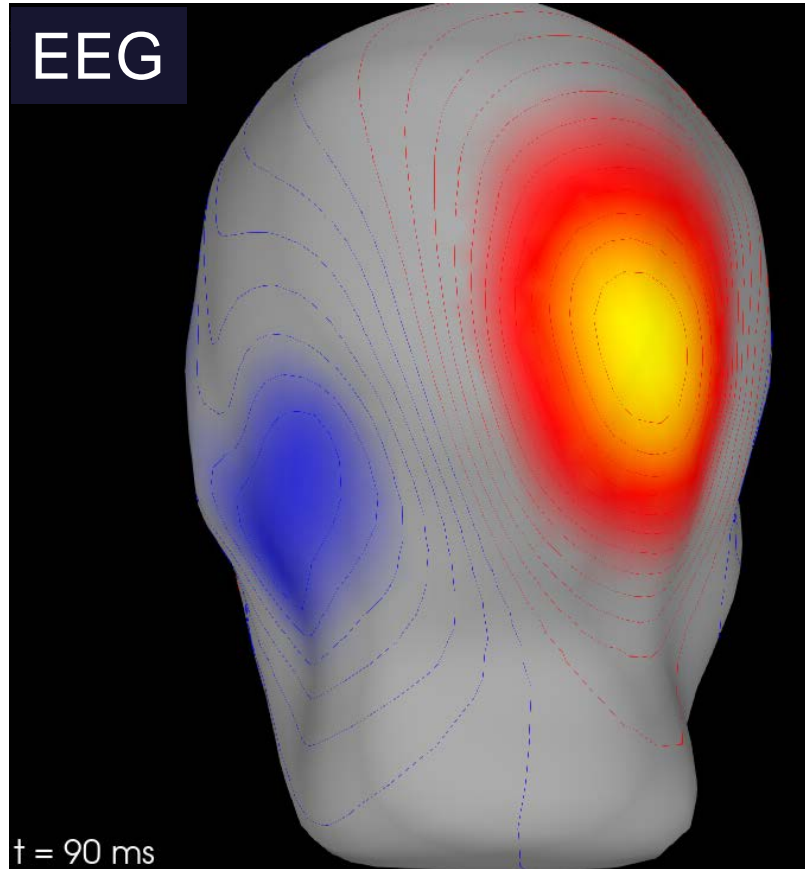


# Example: Visually Evoked Activity ~100 ms

Checkerboard to  
left visual field

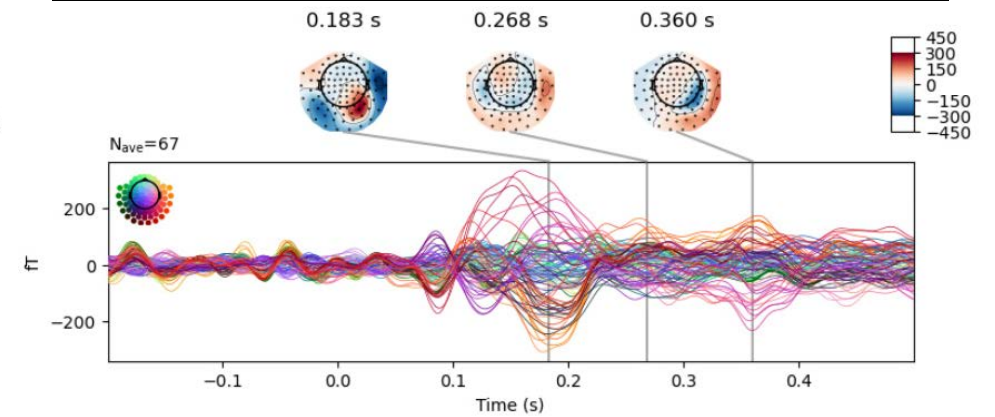
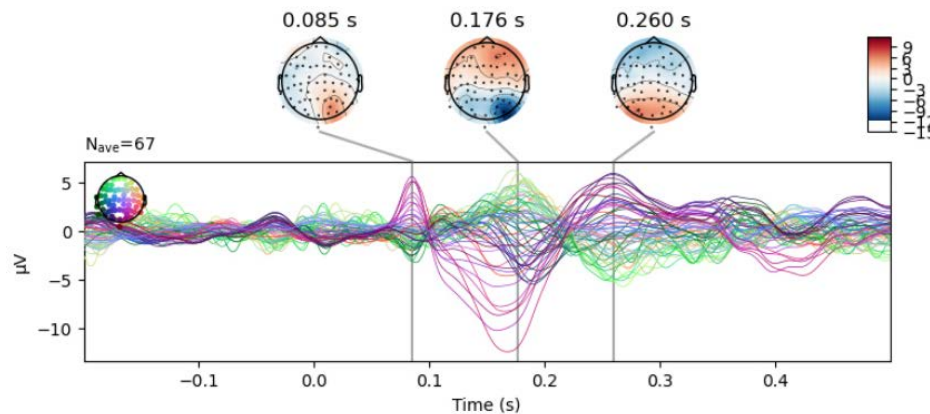
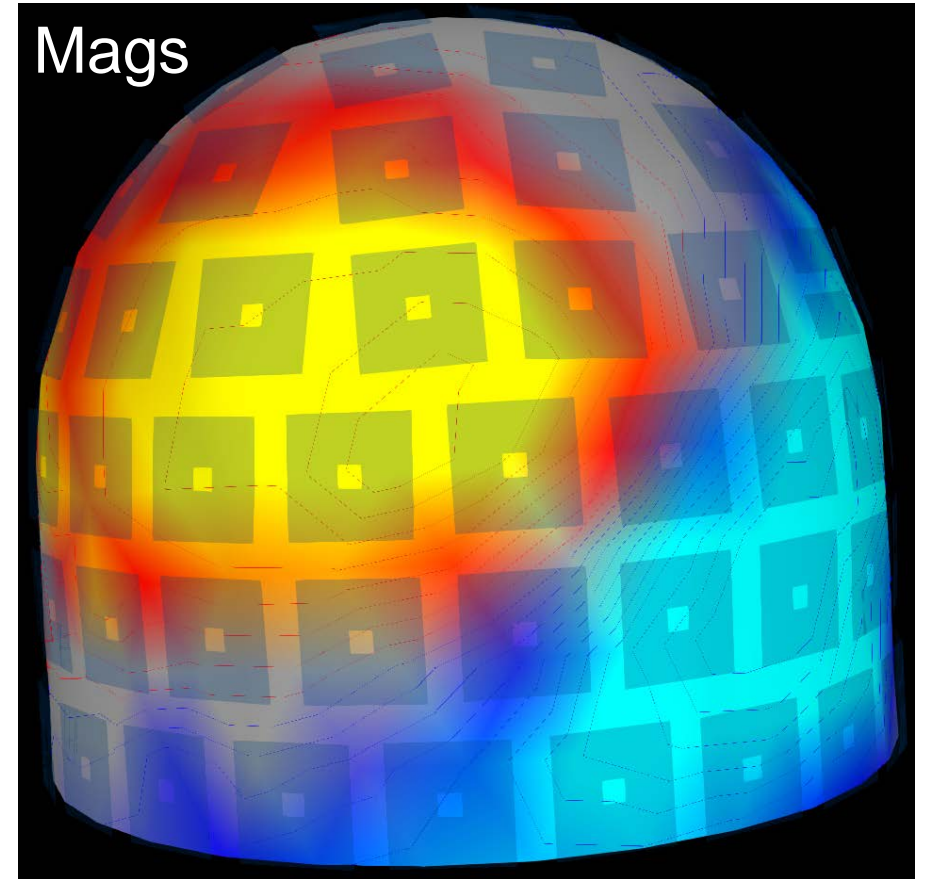


EEG



t = 90 ms

Mags





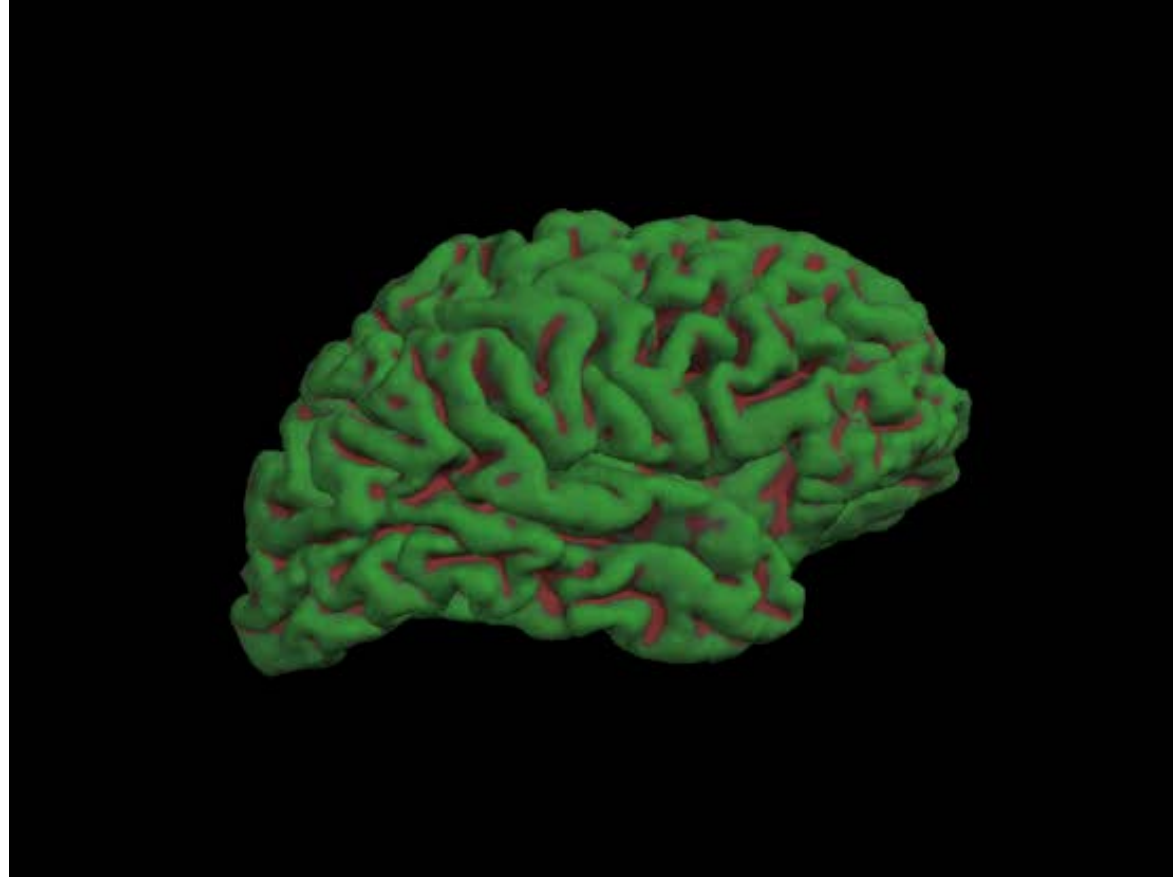


# The Forward Problem and Head Modelling

# Source Spaces

## Source Space

Where active sources may be located, e.g. grey matter, 3D volume



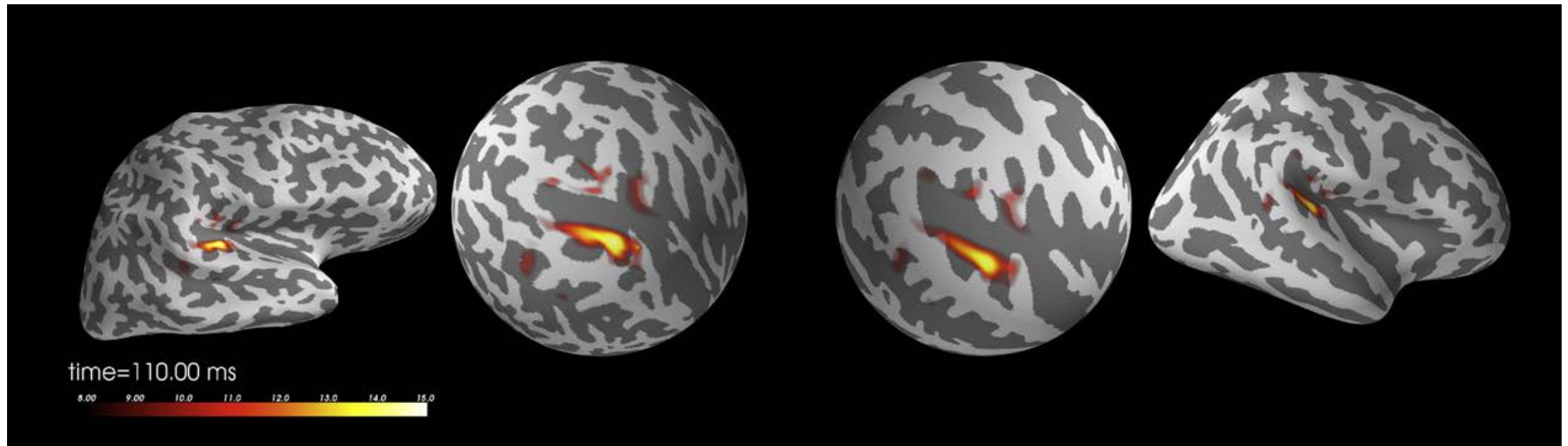
<http://www.cogsci.ucsd.edu/~sereno/movies.html>

Sometimes “standard head models” are used, when no individual MRIs available.

SPM uses the same “canonical mesh” as source space for every subjects, but adjusts it individually.

# Normalising (Morphing) Cortical Surfaces

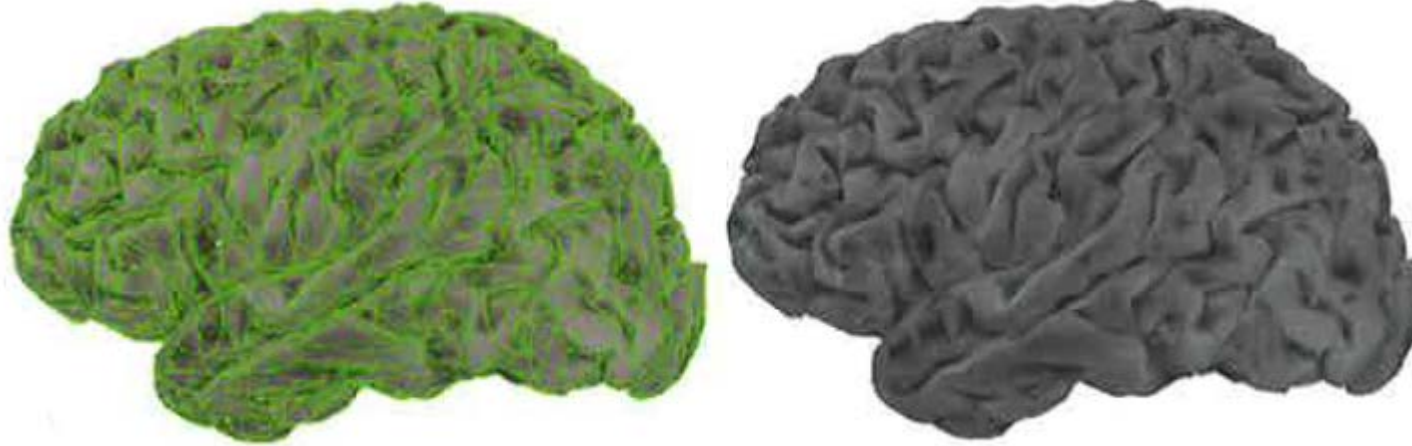
Morphing from individual to standard brain



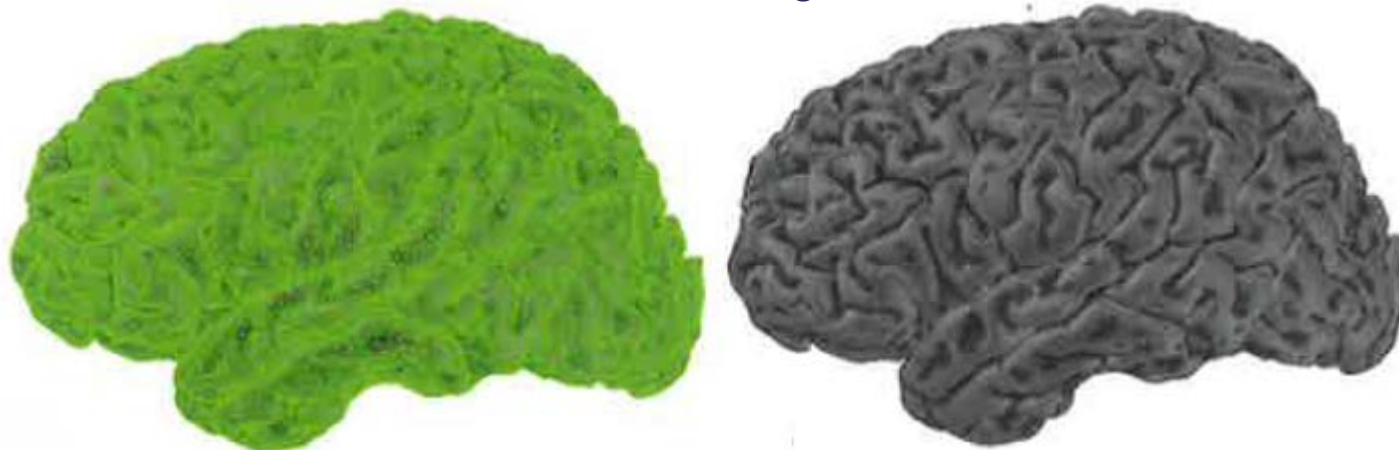


# Spatial Sampling of Cortical Surfaces

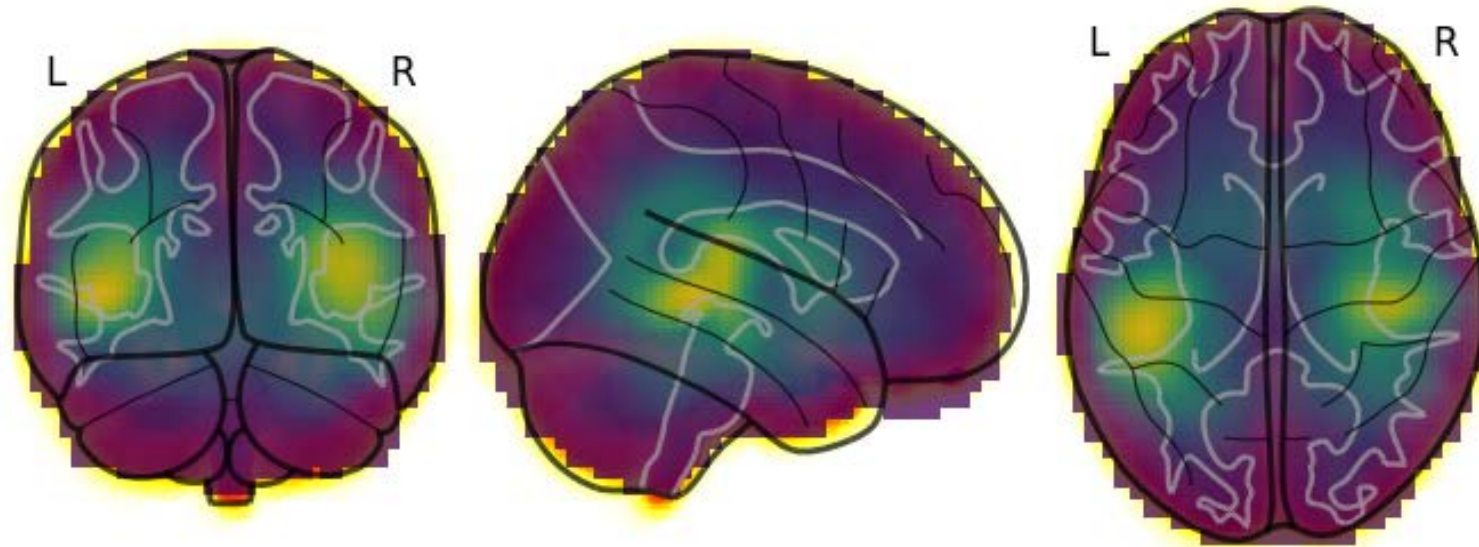
10.034 vertices, 20.026 triangles of 10 mm<sup>2</sup> surface area  
Sufficient for most EEG/MEG applications



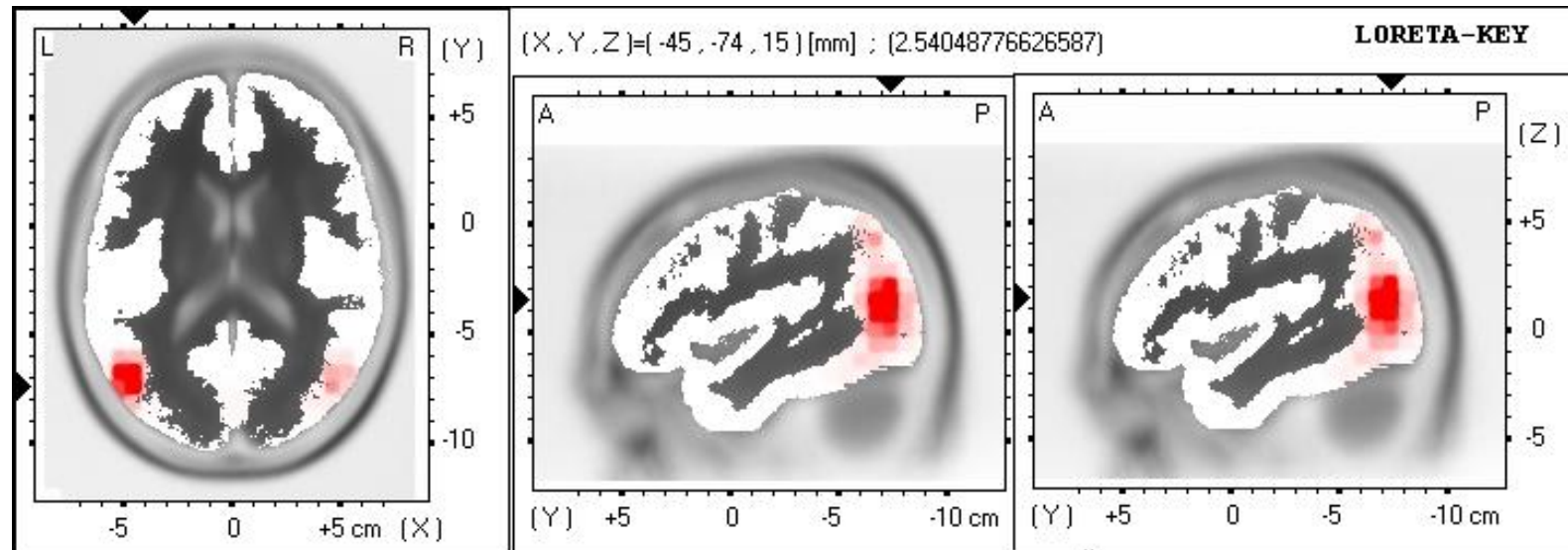
79.124 vertices, 158.456 triangles of 1.3 mm<sup>2</sup> surface area



# Volumetric Source Spaces Are Possible

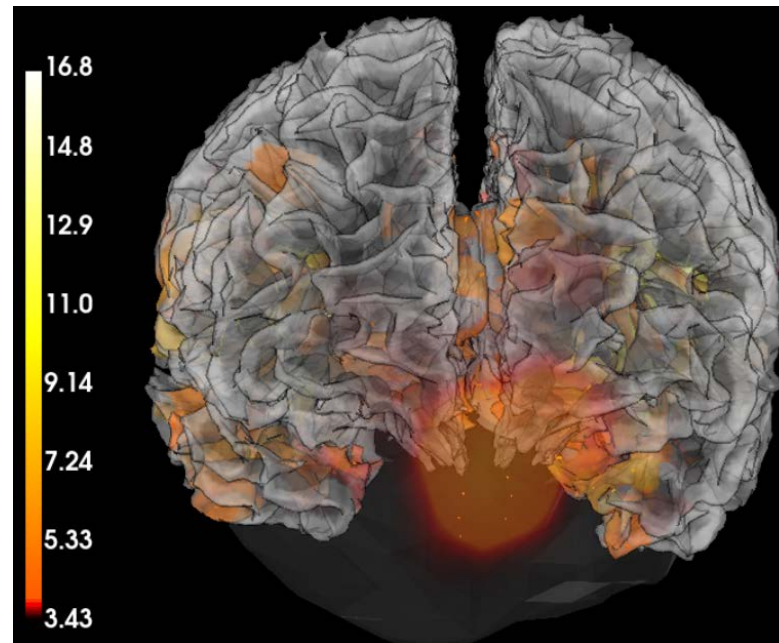
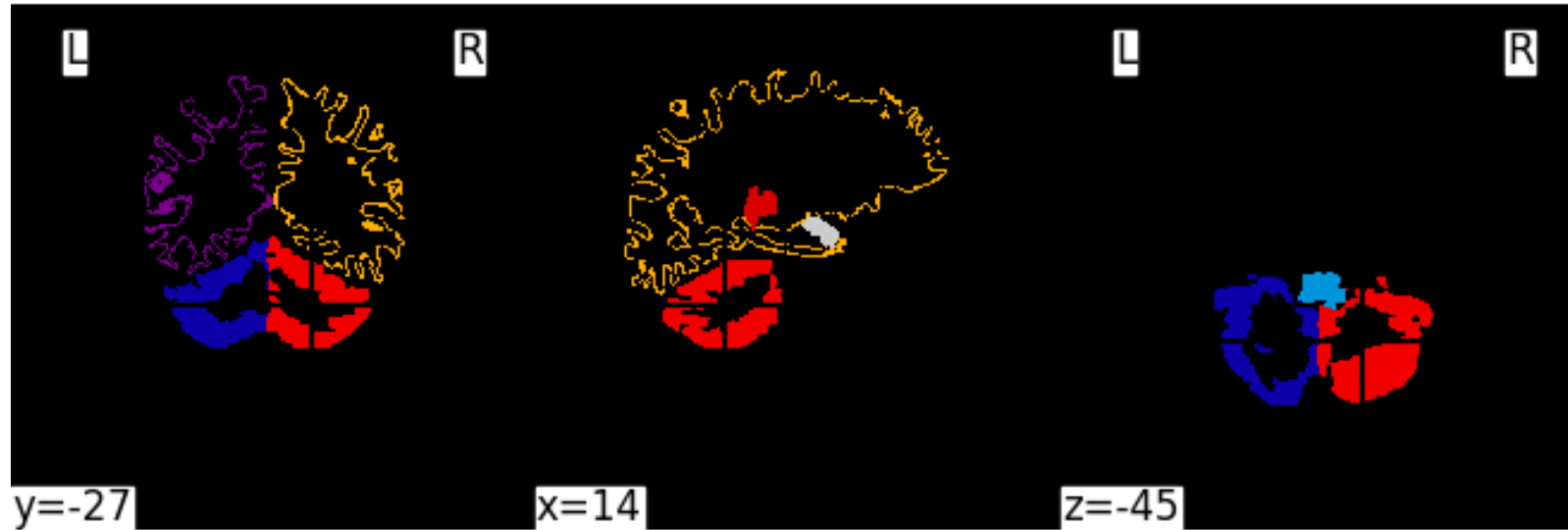


[https://mne.tools/dev/auto\\_examples/inverse/morph\\_volume\\_stc.html](https://mne.tools/dev/auto_examples/inverse/morph_volume_stc.html)



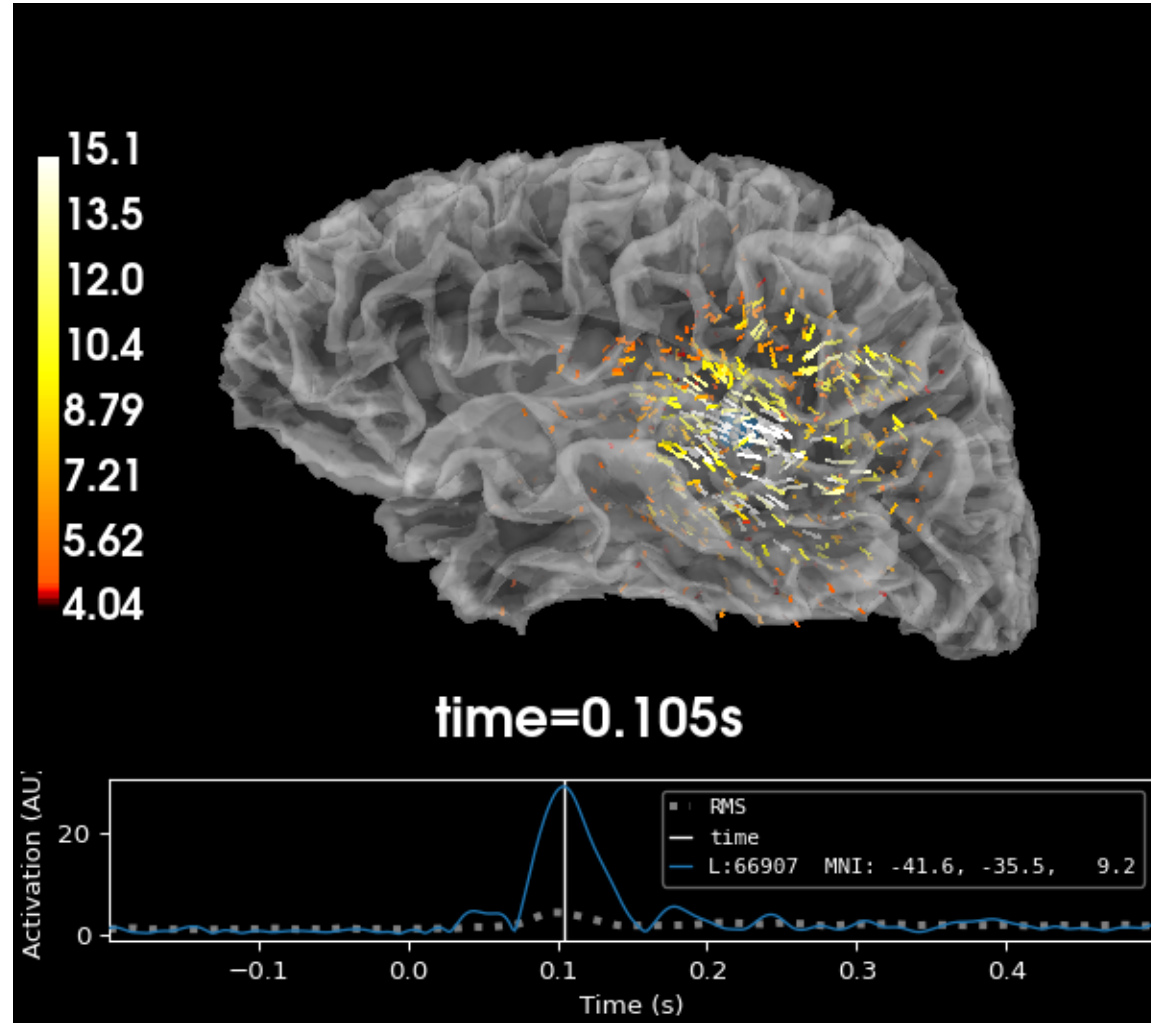
# Mixed Source Spaces

Cortical and Sub-Cortical Sources

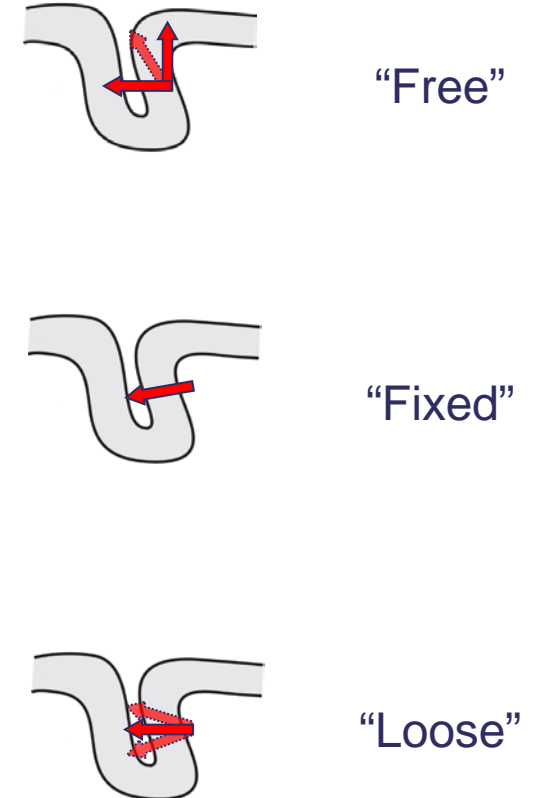


# Source Orientations

Current sources have a direction and/or orientation.



Constraints on source orientation:

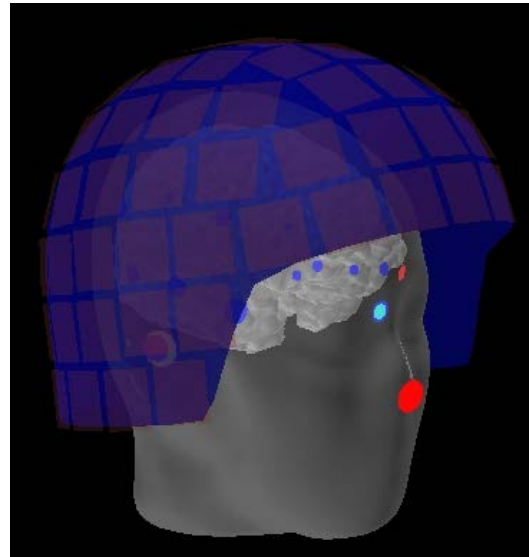




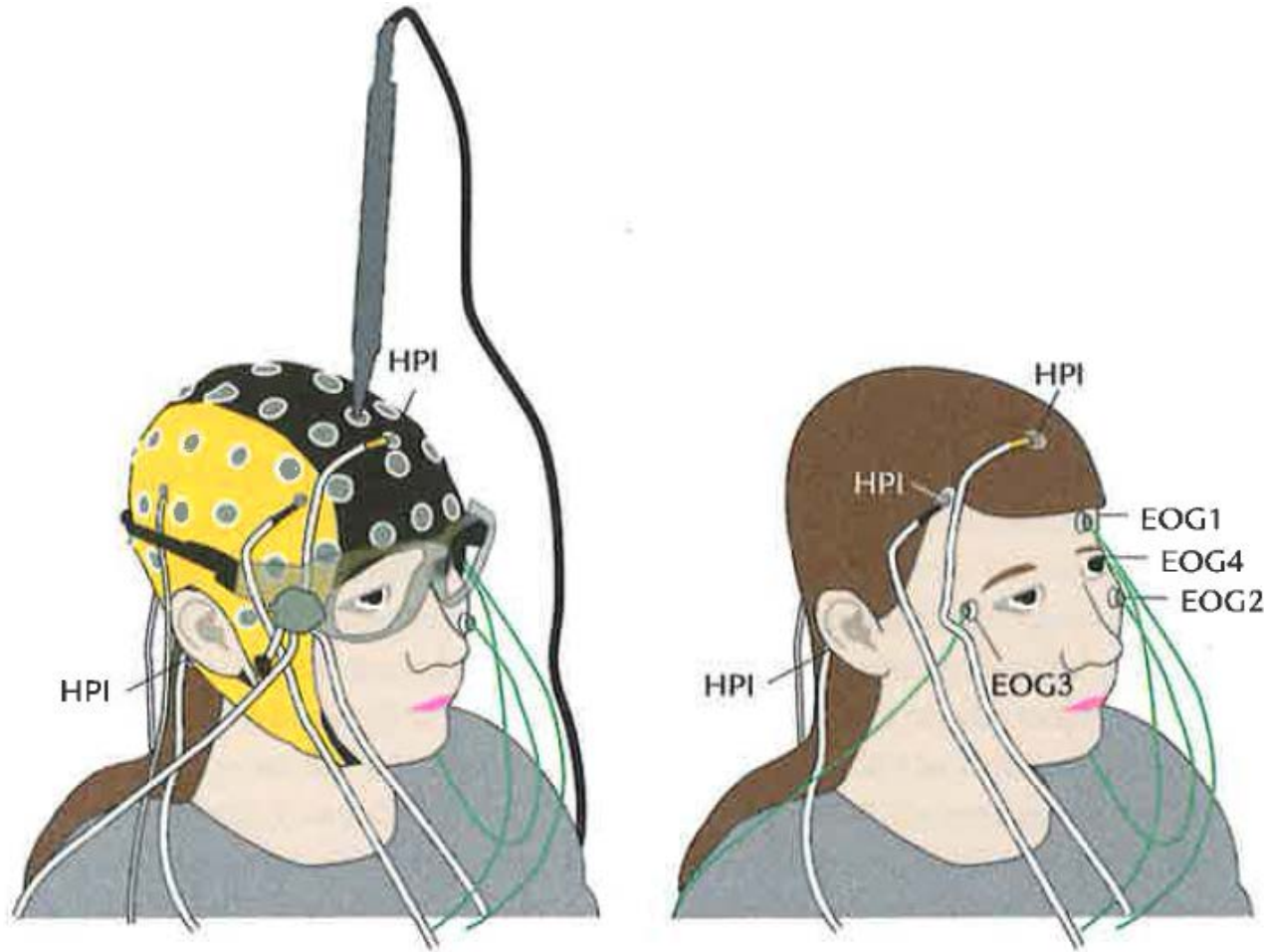


# Coregistration of EEG/MEG and MRI Spaces

Coordinate  
Transformation



# Coregistration of EEG/MEG and MRI Spaces

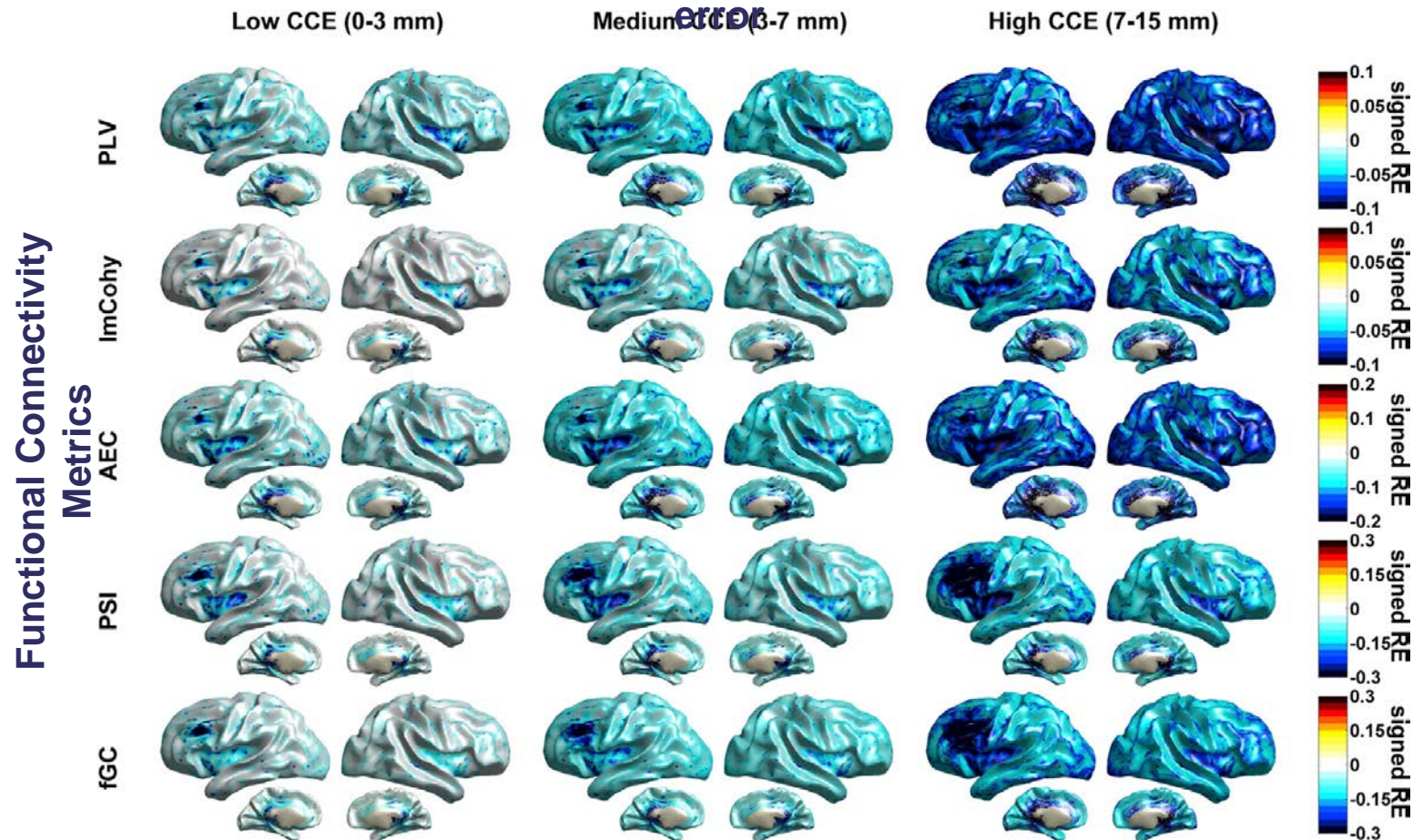


MNE-Python tutorial: <https://www.youtube.com/watch?v=ALV5qqMHlIQ>

# Accurate Coregistration Is Important

Coregistration errors affect the forward model, and therefore everything that follows.

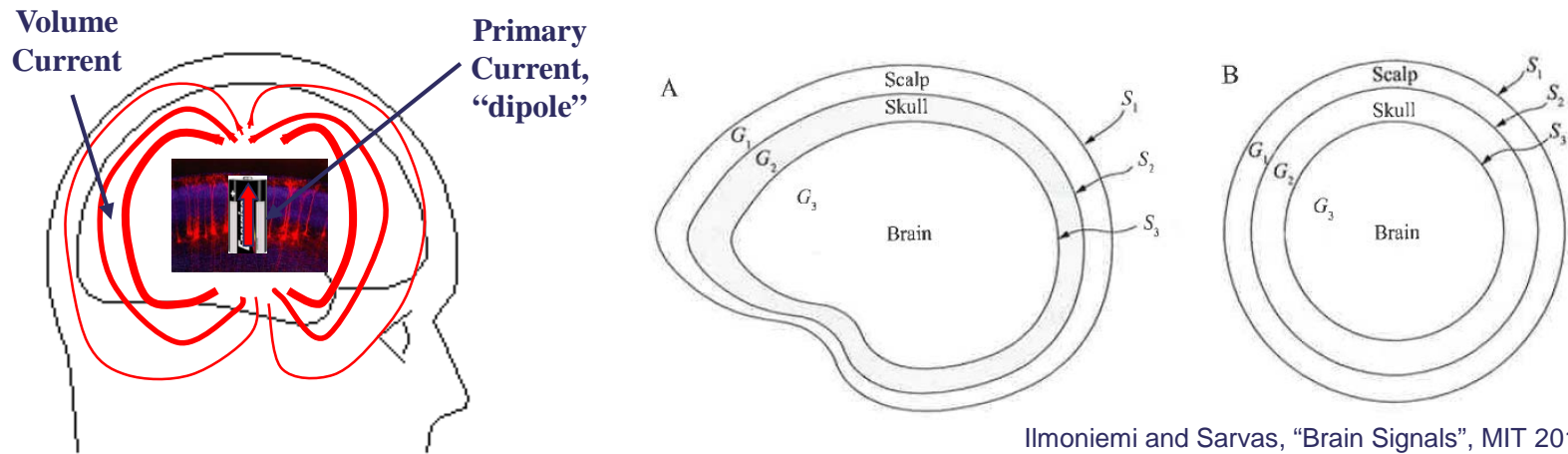
For example, connectivity analysis:  
3 levels of coregistration





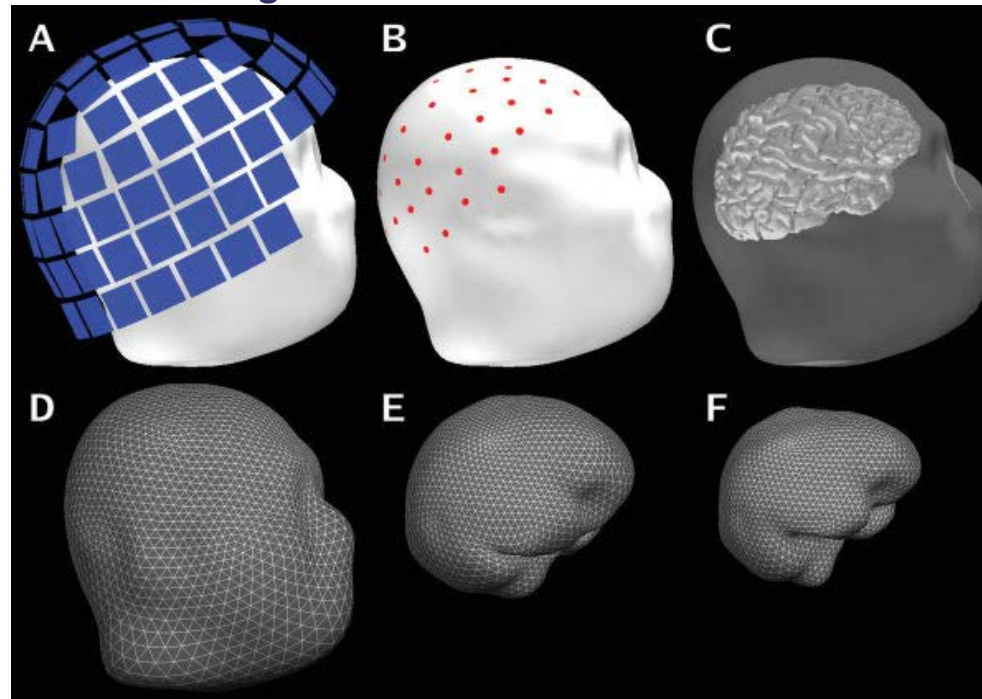
# Head Models

# Boundary Element Model (BEM)



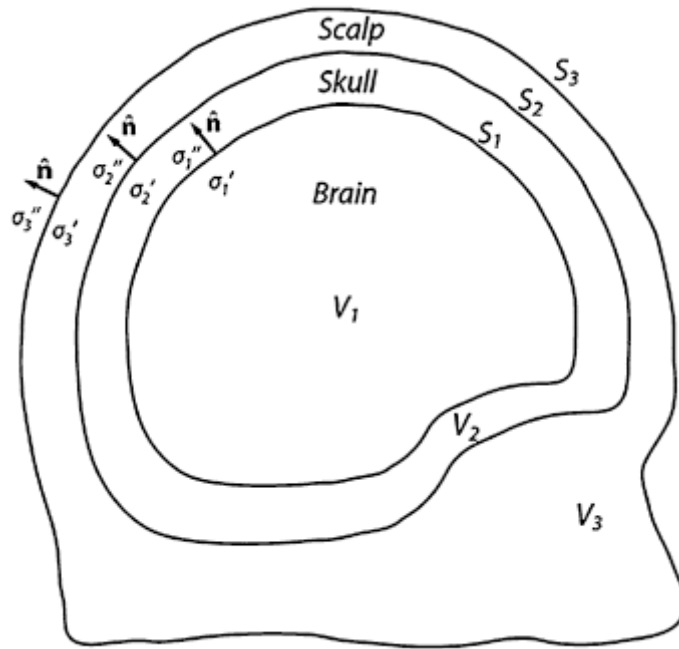
Ilmoniemi and Sarvas, "Brain Signals", MIT 2019

## Ingredients for a head model



Goldenholz et al., HBM 2009

# Boundary Element Model (BEM)



Electric potential

$$\sigma(\mathbf{r}) V(\mathbf{r}) = \frac{1}{4\pi} \sum_j (\sigma_j' - \sigma_j'') \int_{S_j} dS_j' \mathbf{n}(\mathbf{r}') \cdot \frac{\mathbf{r}' - \mathbf{r}}{|\mathbf{r}' - \mathbf{r}|^3} V(\mathbf{r}') + \frac{1}{4\pi} \int_V d^3r' \mathbf{J}^p(\mathbf{r}') \cdot \frac{\mathbf{r} - \mathbf{r}'}{|\mathbf{r} - \mathbf{r}'|^3},$$

Magnetic Field

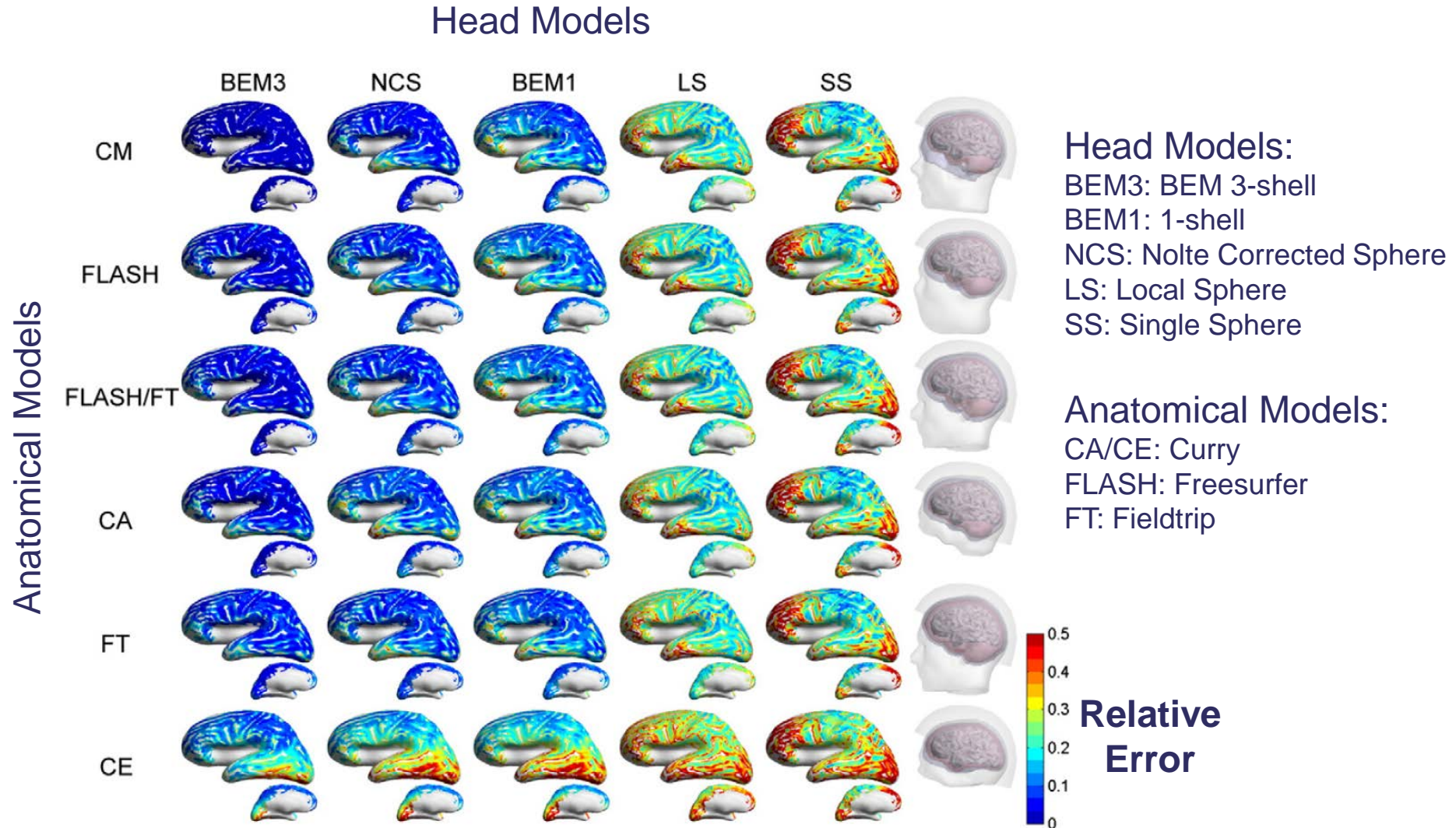
$$\mathbf{B}^p(\mathbf{r}) = \frac{\mu_0}{4\pi} \int_V \mathbf{J}^p(\mathbf{r}') \times \nabla' \frac{1}{|\mathbf{r} - \mathbf{r}'|} d^3r',$$

$$\mathbf{B}^R(\mathbf{r}) = -\frac{\mu_0}{4\pi} \sum_i \sigma_i \int_{V_i} \nabla' V(\mathbf{r}') \times \nabla' \frac{1}{|\mathbf{r} - \mathbf{r}'|} d^3r',$$

Heller & Volegov, in Magnetoencephalography by Supek & Aine (eds), Springer 2019

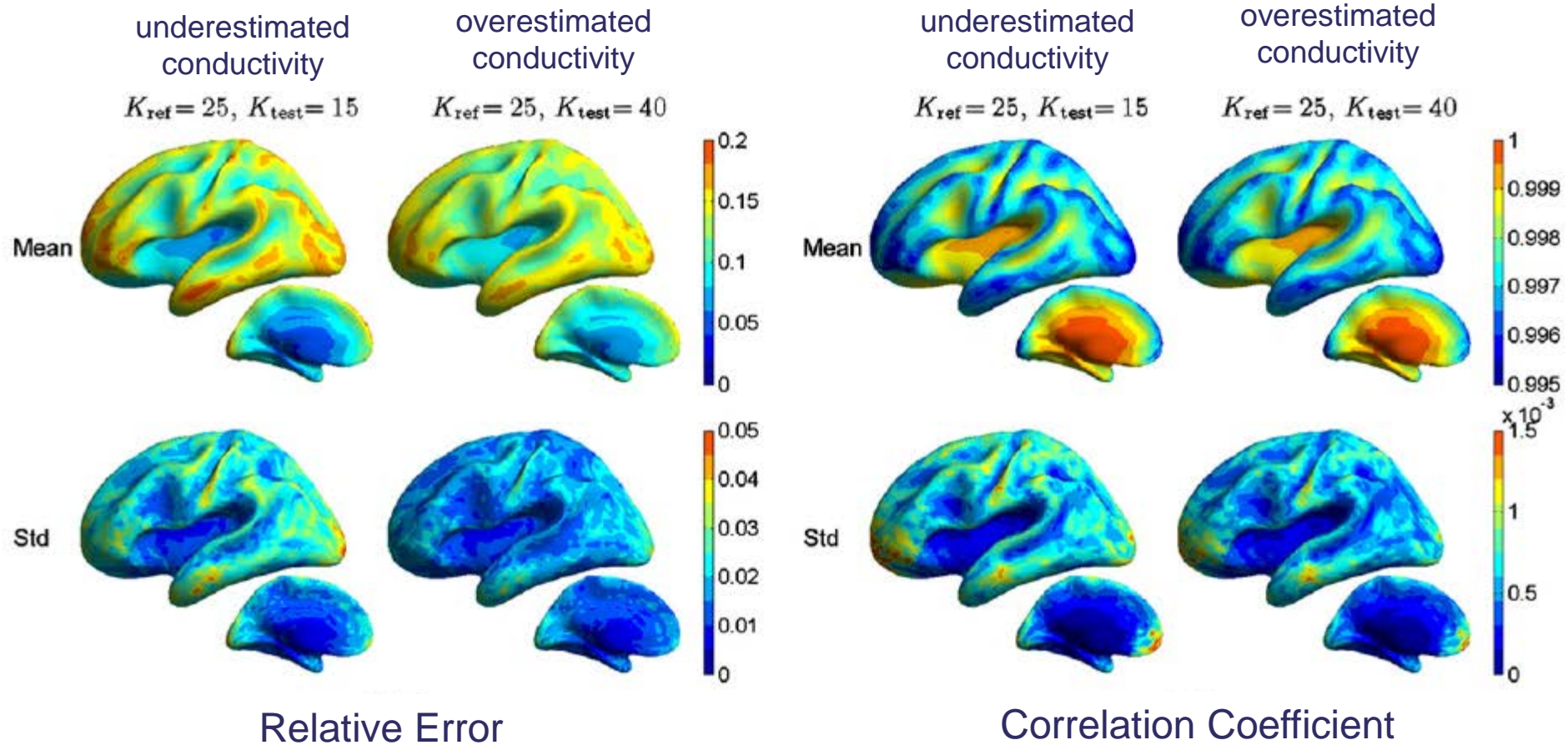
- Volume currents depend on conductivity distribution within the whole head volume.
- EEG measurements on the scalp are the result of volume currents, and are strongly affected by head geometry.
- MEG measurements are the sum of magnetic fields from primary and volume currents, but the magnetic fields of currents close to the source are much stronger than at larger distances.
- Thus, MEG signals are less affected by head geometry (e.g. skull and scalp). We usually only use one compartment (inner skull) for MEG (unless in combination with EEG).

# The Effect of Head Model Accuracy for MEG





# Boundary Element Models Are Relatively Robust Against Conductivity Errors

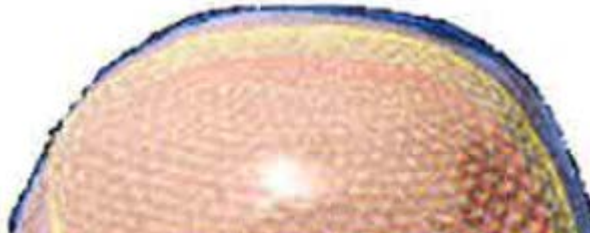


# Head Models With Different Levels of Detail

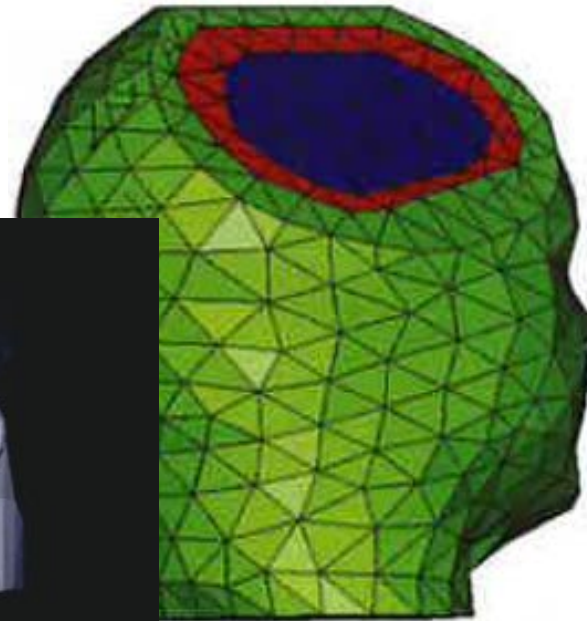
Spheres



Boundary Element Model  
(BEM)



Finite Element Model  
(FEM)



Kraftwerk, 1986

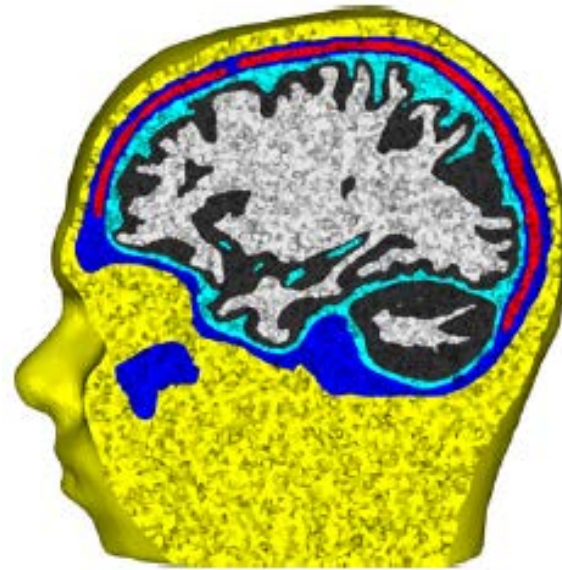
# Finite Element Models (FEMs)

The use of 3-layer (brain, skull, scalp) BEM models based on individual MRI images is state-of-the-art for EEG/MEG source estimation.

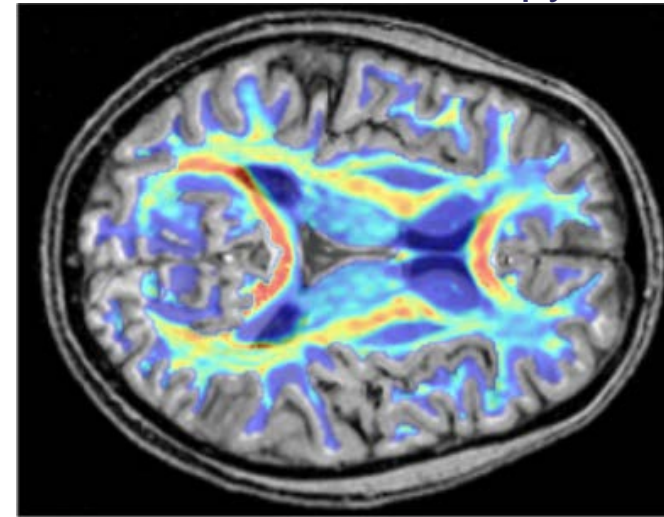
For MEG-only, single shell BEMs and local/corrected sphere models can provide reasonable approximations.

But heads are more complex:

White Matter  
Gray Matter  
CSF  
Skull  
Compacta  
Skull  
Spongiosa  
Skin



Fractional Anisotropy



Vorwerk et al., NI 2014

It is not obvious how to translate this into more accurate estimate for conductivity distributions.

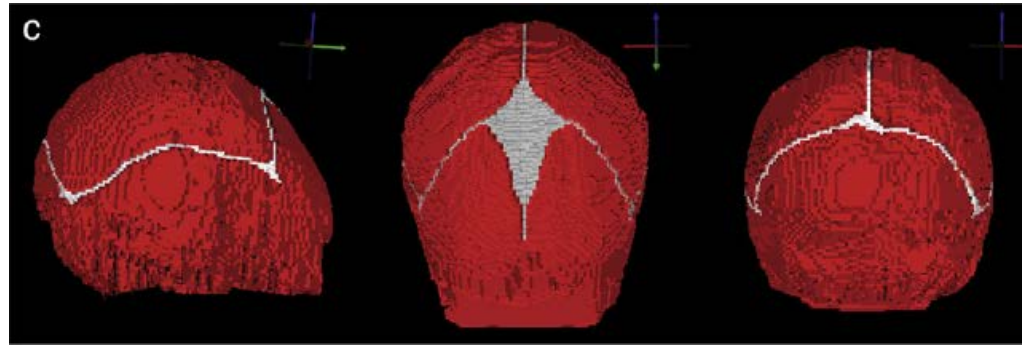
# Conductivities Of Tissues Can Only Be Approximated

**Table 2** Isotropic conductivity values of single tissue types used in human head volume conductor modeling

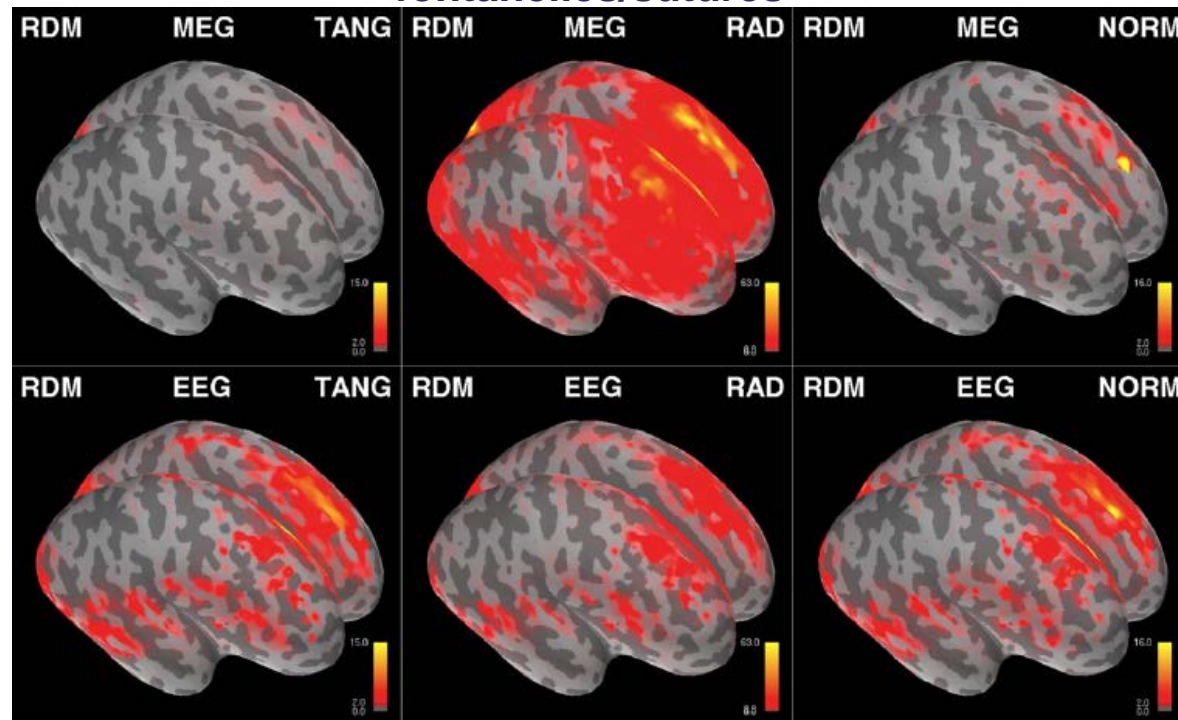
Tissue	Conductivity in S/m	Reference
Brain gray matter	0.45	Logothetis et al. <a href="#">2007</a>
Brain white matter	0.1	Akhtari et al. <a href="#">2010</a>
Spinal cord and cerebellum	0.16	Haueisen et al. <a href="#">1995</a>
Cerebrospinal fluid	1.79	Baumann et al. <a href="#">1997</a>
Hard bone (compact bone)	0.004	Tang et al. <a href="#">2008</a>
Soft bone (spongiform bone)	0.02	Akhtari et al. <a href="#">2002</a>
Blood	0.6	Gabriel et al. <a href="#">2009</a>
Muscle	0.1	Gabriel et al. <a href="#">1996</a> , <a href="#">2009</a>
Fat	0.08	Gabriel et al. <a href="#">2009</a>
Eye	1.6	Pauly and Schwan <a href="#">1964</a> ; Lindenblatt and Silny <a href="#">2001</a>
Scalp	0.43	Geddes and Baker <a href="#">1967</a>
Soft tissue	0.17	Haueisen et al. <a href="#">1995</a>
Internal air	0.0001	Haueisen et al. <a href="#">1995</a>



# Infant Skulls – Fontanelles and Sutures



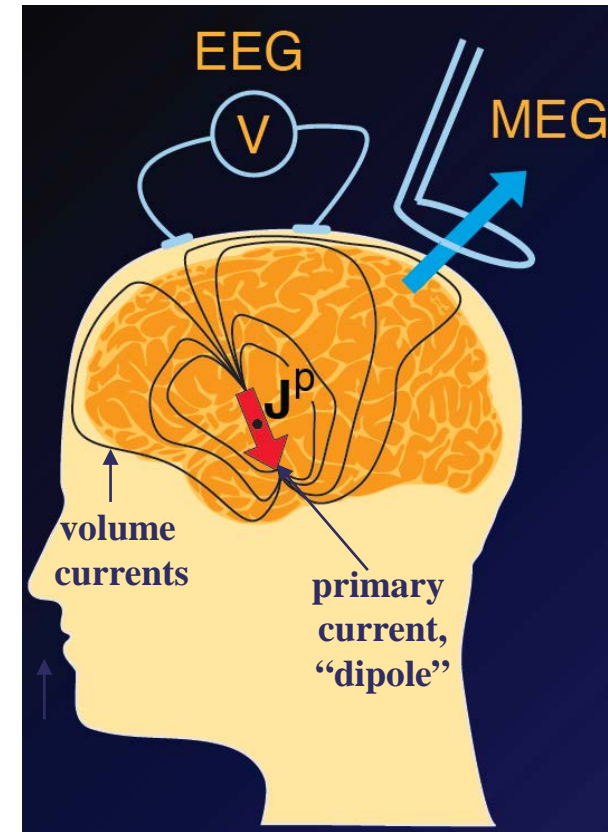
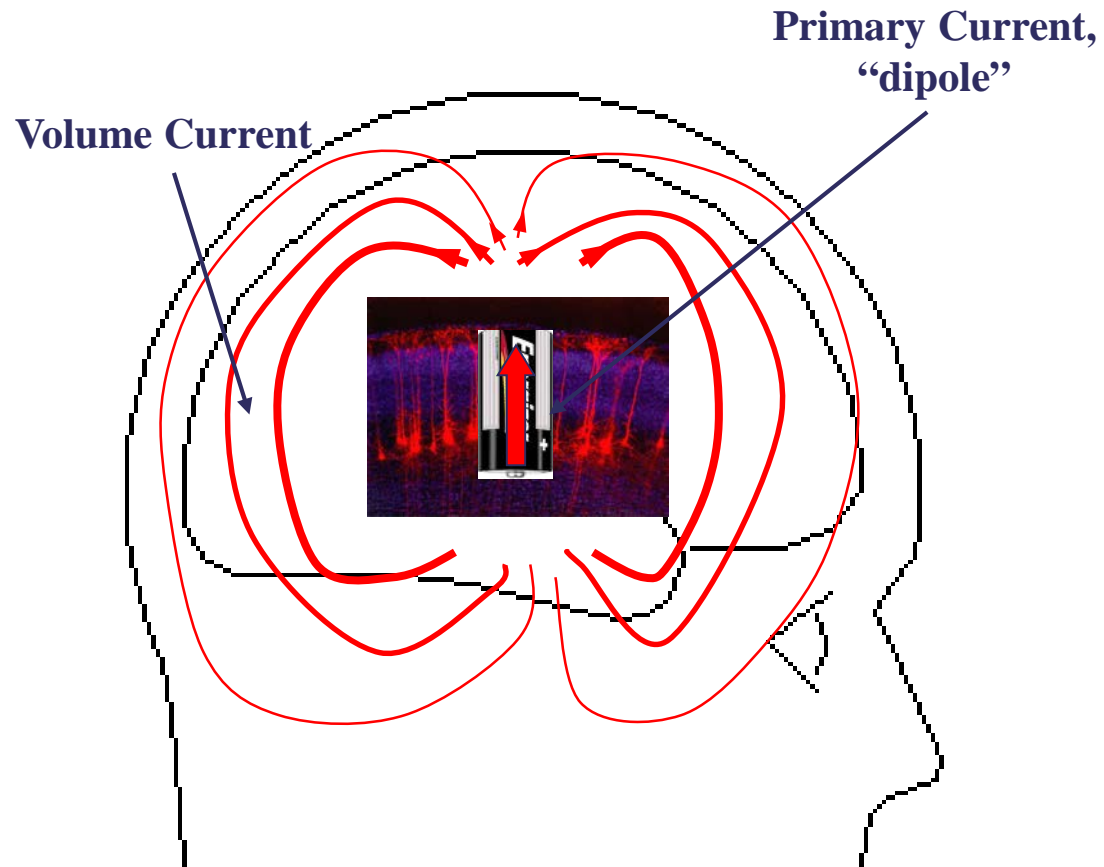
Relative error between models with and without fontanelles/sutures







# Different Sensitivities of EEG and MEG



<http://www.nmr.mgh.harvard.edu/meg/pdfs/talks/>

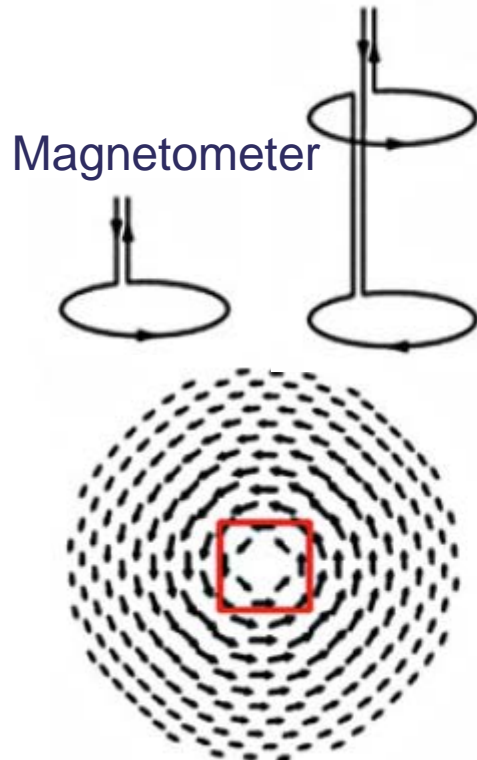
All effects are instantaneous.  
Volume currents affect both EEG and MEG –  
but EEG more than MEG

# Different Sensors and their Sensitivities (Leadfields)

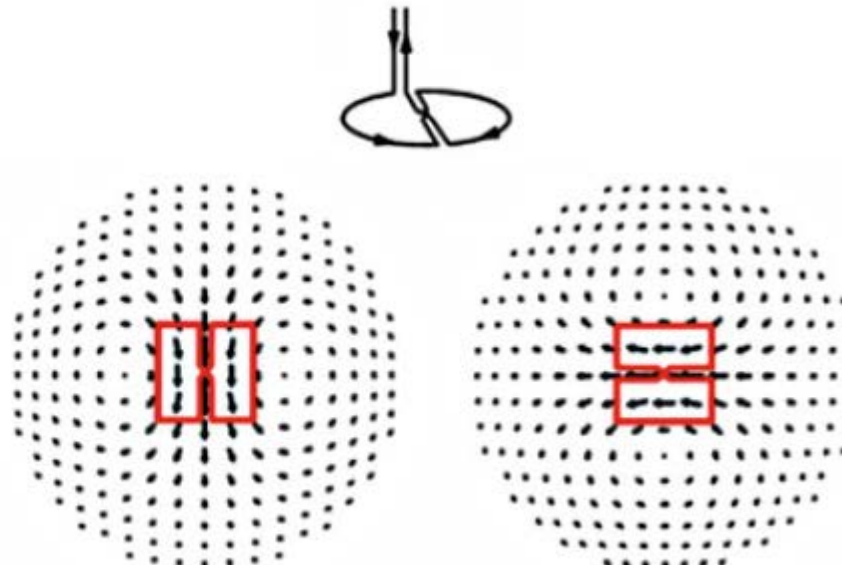
**Leadfields are “sensitivity profiles” of individual sensors.**

Each sensor is maximally sensitive to sources oriented along the arrows, and insensitive to sources perpendicular to the arrows.

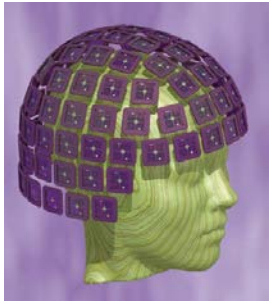
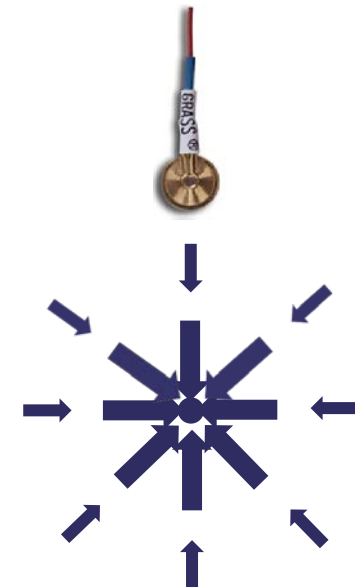
Axial Gradiometer



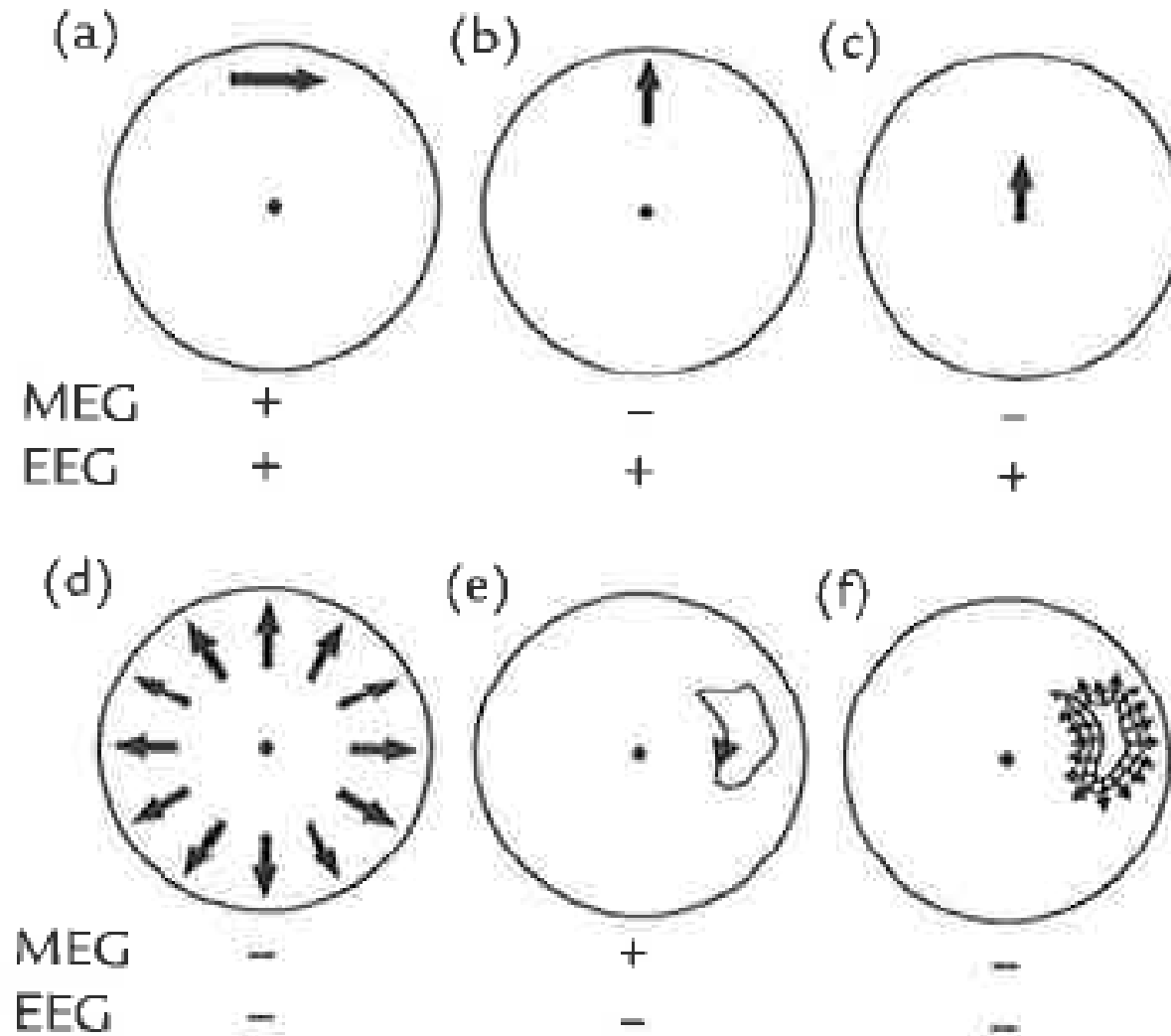
Planar Gradiometer(s)



EEG Electrode



# EEG and MEG Are Differentially Sensitive To Radial and Tangential Sources

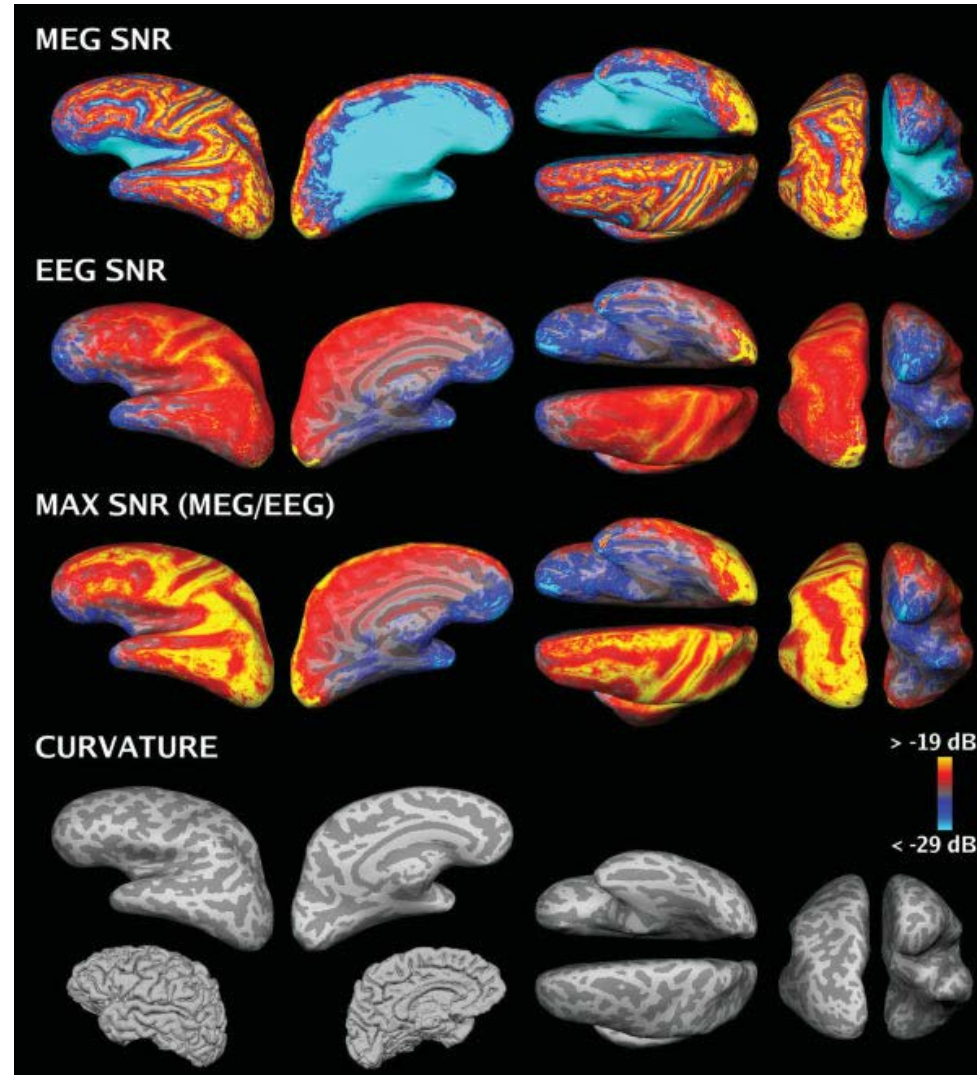


MEG is relatively insensitive to radial currents, and therefore also to deep currents.

Some complex source distributions may not produce EEG or MEG signals.

# Sensitivity Maps

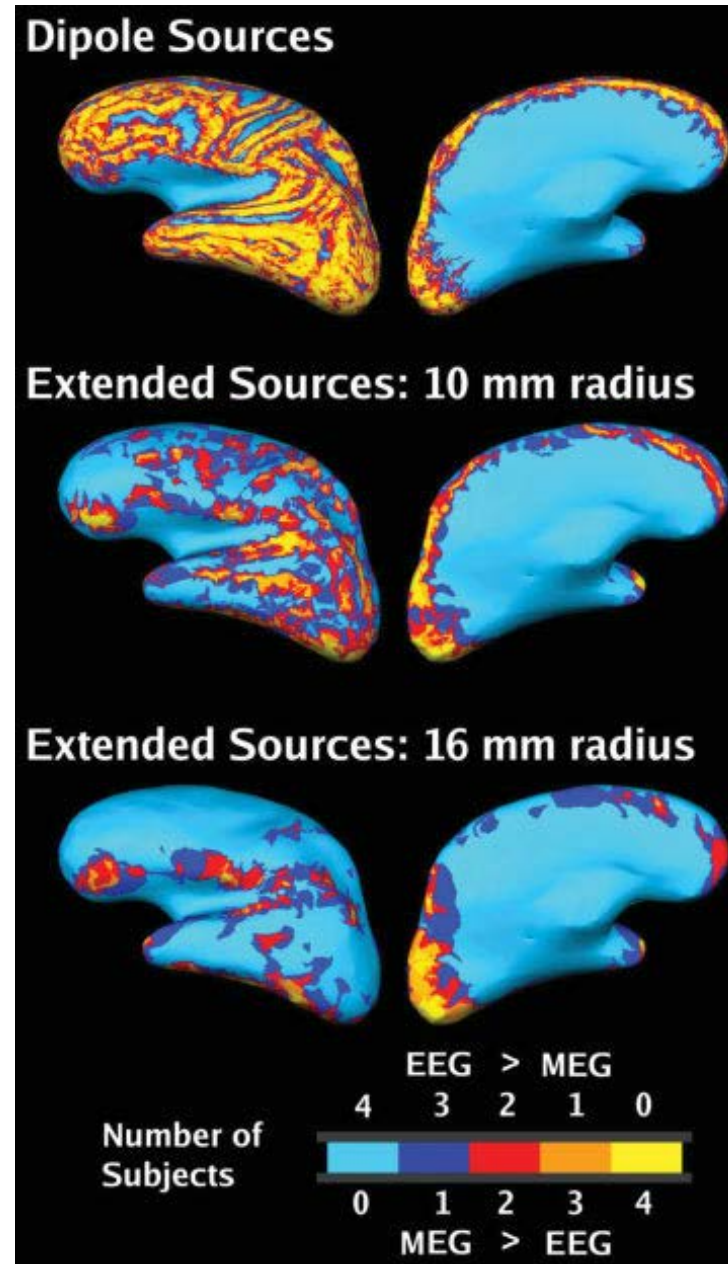
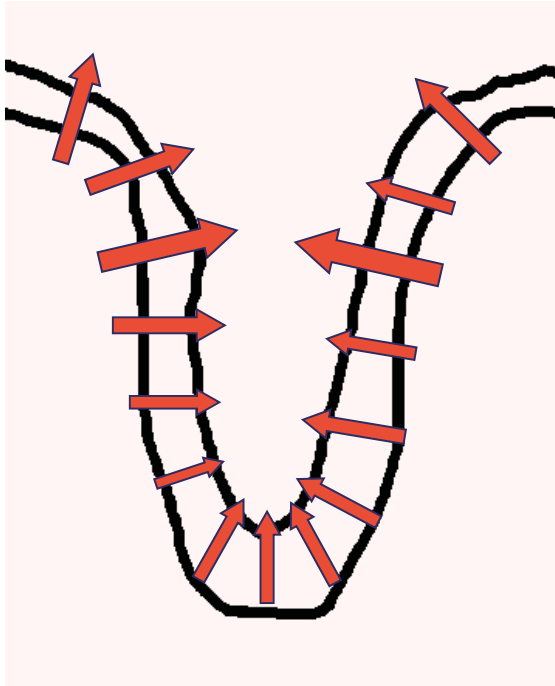
Sensor type, coverage and distance to sources strongly affect sensitivity and spatial resolution





# MEG Is Less Sensitive To Spatially Extended Sources Than EEG

Distributed source around sulcus





# Conclusion – Head Modelling

3-compartment BEM models are currently state-of-the-art for EEG/MEG source estimation.

Single-shell approximations are still common for MEG.

More detailed head models may increase accuracy, but require more accurate data and information, such as accurate MRI segmentations and conductivity values. (see e.g. Vorwerk et al., BioMeg Eng Online 2018) for Fieldtrip FEM pipeline)

There is no right or wrong, there are only different approximations – know your limits.

# Fixing Head Models

[https://mne.tools/stable/auto\\_tutorials/forward/80\\_fix\\_bem\\_in\\_blender.html](https://mne.tools/stable/auto_tutorials/forward/80_fix_bem_in_blender.html)



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# Thank you