

# Greedy Algorithms

August 23, 2025

# Interval Scheduling

## Input

- $n$  tasks;
- a start time  $s_i$  for each task  $i$ ;
- a finish time  $f_i$  for each task  $i$ ;

## Desired output

A set  $S \subseteq [n]$  of non-overlapping tasks maximizing  $|S|$ .

# Examples

# Different Greedy Approaches

- Smallest Interval

# Different Greedy Approaches

- Smallest Interval
- Earliest Start Time

# Earliest Finish Time Greedy Algorithm

- 1 Sort all jobs by non-decreasing  $f_i$
- 2 Let  $A = \{\}$ ;
- 3 Check all jobs by non-decreasing  $f_i$   
If (Job  $i$  does not overlap jobs in  $A$ ) Then  $A \leftarrow A \cup \{i\}$
- 4 Output  $A$

# Examples

# Running Time Analysis



# Correctness

- Greedy outputs a valid solution;
- Greedy outputs an optimal solution among all valid solutions.

# High Level Intuition

# Formal Proof by Induction

# Formal Proof by Induction

# Variants

- Different values for different jobs.
- Multiple machines.
- Online setting.

Homework 1 comments.

Thanks!