



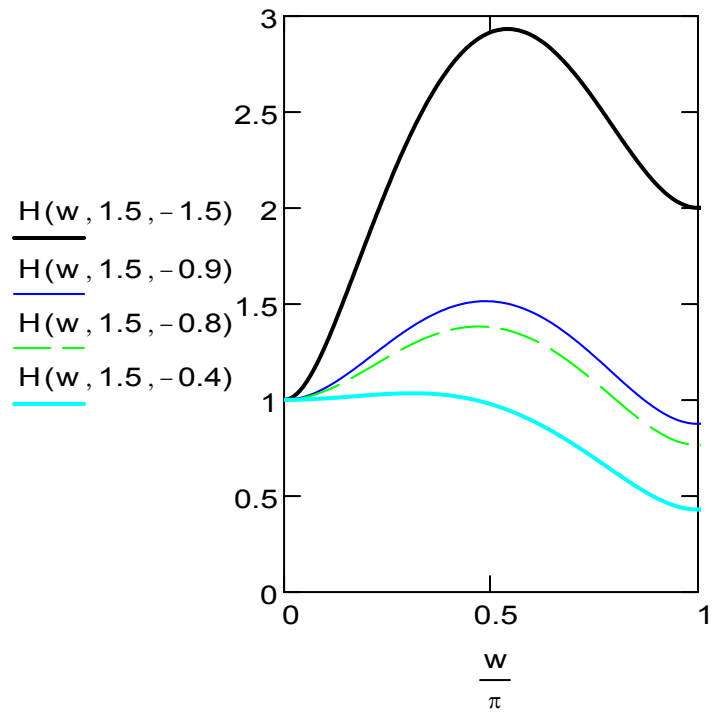
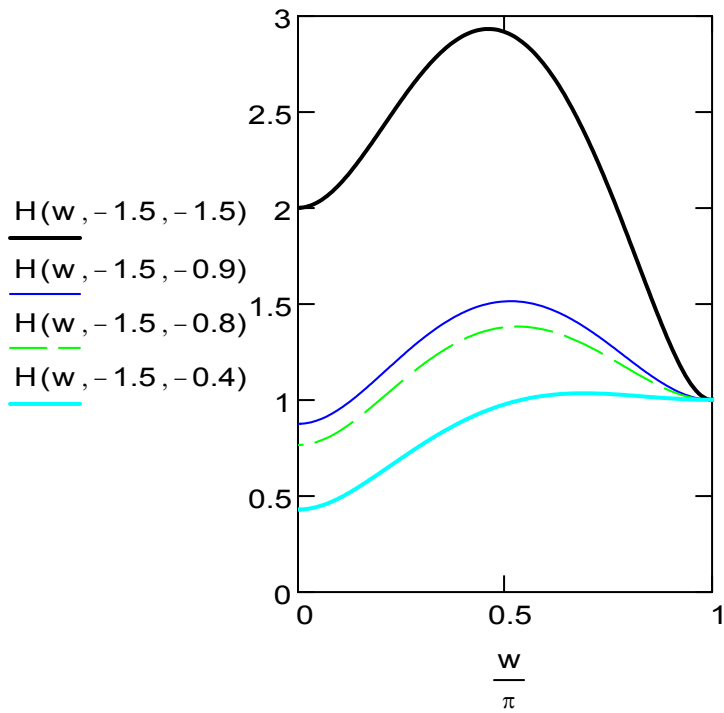
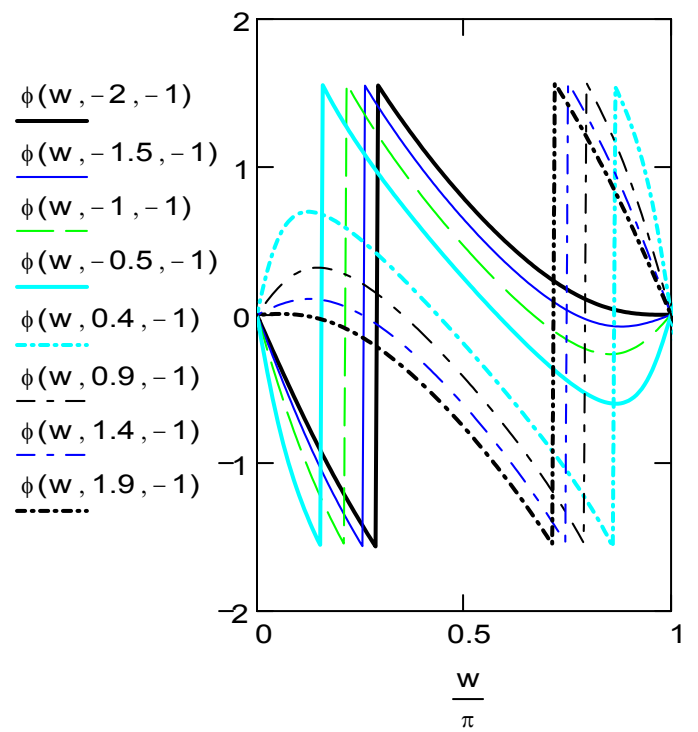
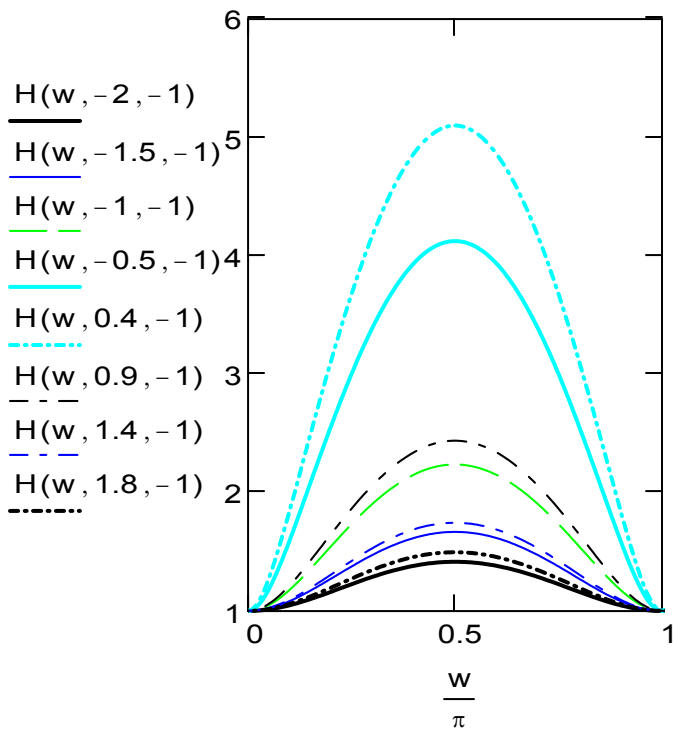
$$H(w, a1, a2) := \frac{\sqrt{a1^2 + (1 - a2)^2 + 2 \cdot a1 \cdot (1 + a2) \cdot \cos(w) + 4 \cdot a2 \cdot \cos(w)^2}}{a2 + 1 + |a1|}$$

$$\phi(w, a1, a2) := \operatorname{atan}\left[\frac{-(a1 \cdot \sin(w) + a2 \cdot \sin(2w))}{1 + a1 \cdot \cos(w) + a2 \cdot \cos(2w)}\right]$$

$$z1(a1, a2) := \frac{-a1}{2} + \sqrt{\frac{a1^2}{4} - a2}$$

$$z2(a1, a2) := \frac{-a1}{2} - \sqrt{\frac{a1^2}{4} - a2}$$

# Полосовой Фильтр



$$wp(a1, a2) := \arccos\left(-a1 \cdot \frac{1 + a2}{4a2}\right)$$

$$\frac{wp(-1.5, -1.5)}{\pi} = 0.46$$

$$\frac{wp(1.5, -1.5)}{\pi} = 0.54$$

$$\frac{wp(-1.5, -0.8)}{\pi} = 0.53$$

$$\frac{wp(1.5, -0.8)}{\pi} = 0.47$$

$$\frac{wp(-1.5, -0.4)}{\pi} = 0.69$$

$$\frac{wp(1.5, -0.4)}{\pi} = 0.31$$

$$A(a_2) := 4a_2 \quad B(a_1, a_2) := 2a_1 \cdot (1 + a_2) \quad C(a_1, a_2) := a_1^2 + (1 - a_2)^2$$

$$b_1(a_1, a_2) := \frac{-B(a_1, a_2) - \sqrt{\frac{B(a_1, a_2)^2 - 4 \cdot A(a_2) \cdot C(a_1, a_2)}{2}}}{2A(a_2)}$$

$$b_2(a_1, a_2) := \frac{-B(a_1, a_2) + \sqrt{\frac{B(a_1, a_2)^2 - 4 \cdot A(a_2) \cdot C(a_1, a_2)}{2}}}{2A(a_2)}$$

$$w_1(a_1, a_2) := \arccos(b_1(a_1, a_2)) \quad w_2(a_1, a_2) := \arccos(b_2(a_1, a_2))$$

$$Q(a_1, a_2) := \frac{w_2(a_1, a_2)}{w_2(a_1, a_2) - w_1(a_1, a_2)}$$

$$b_1(-1, -1) = 0.791$$

$$b_2(-1, -1) = -0.791$$

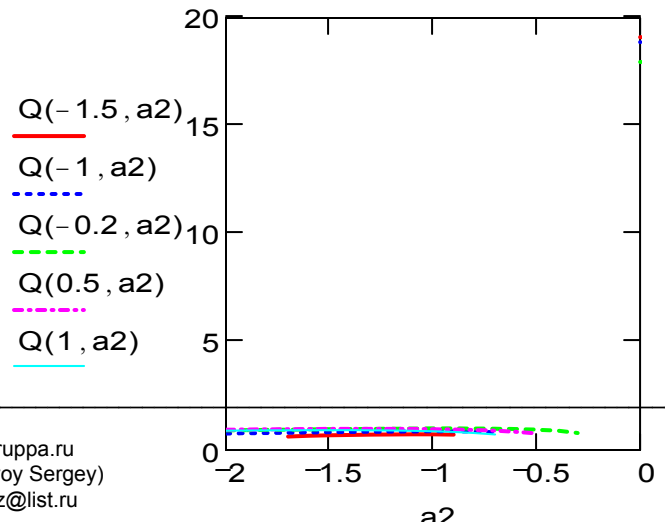
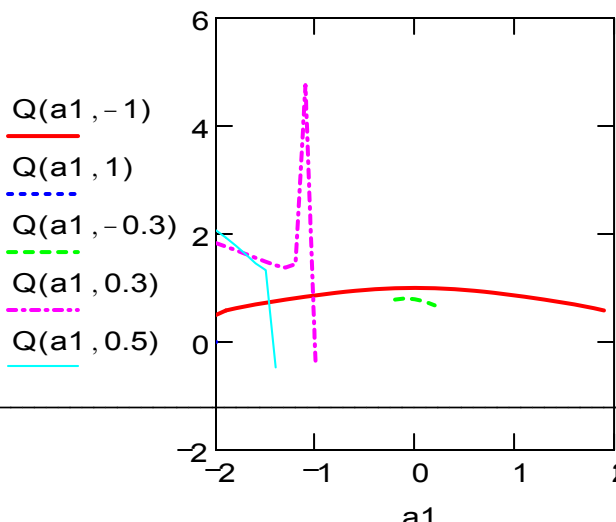
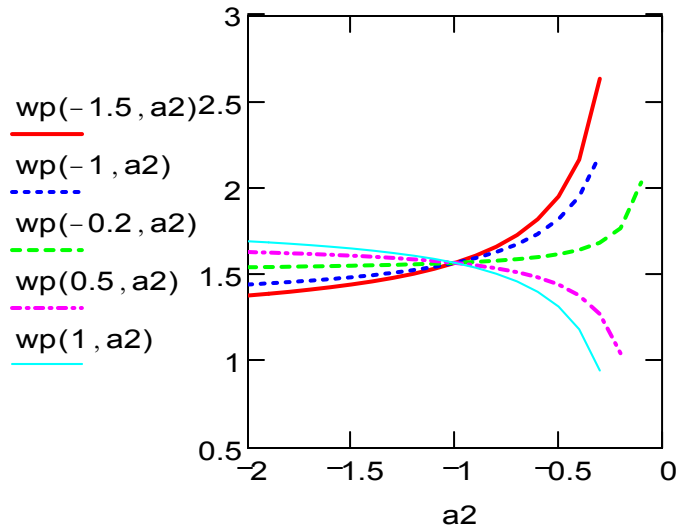
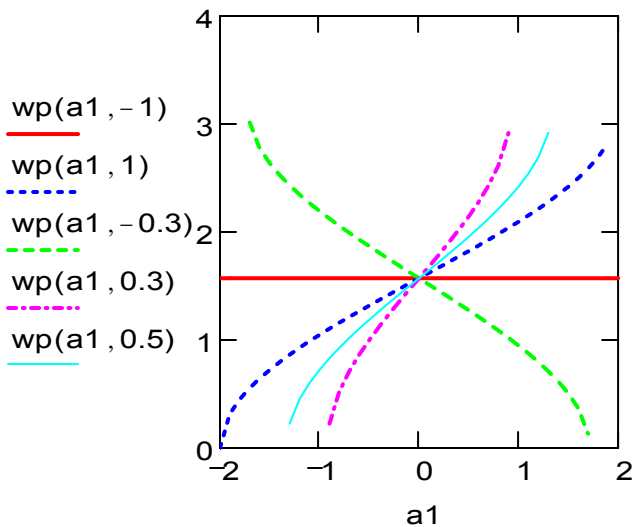
$$\frac{w_1(-1, -1)}{\pi} = 0.21$$

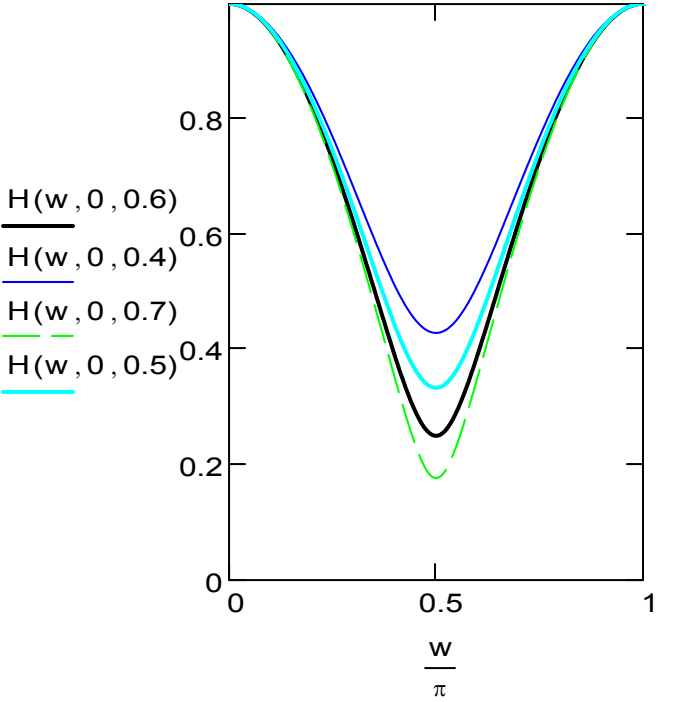
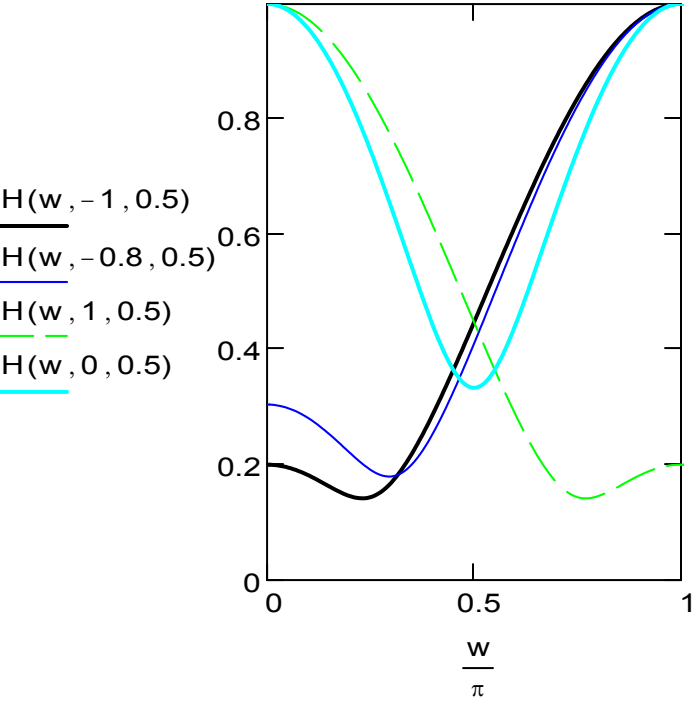
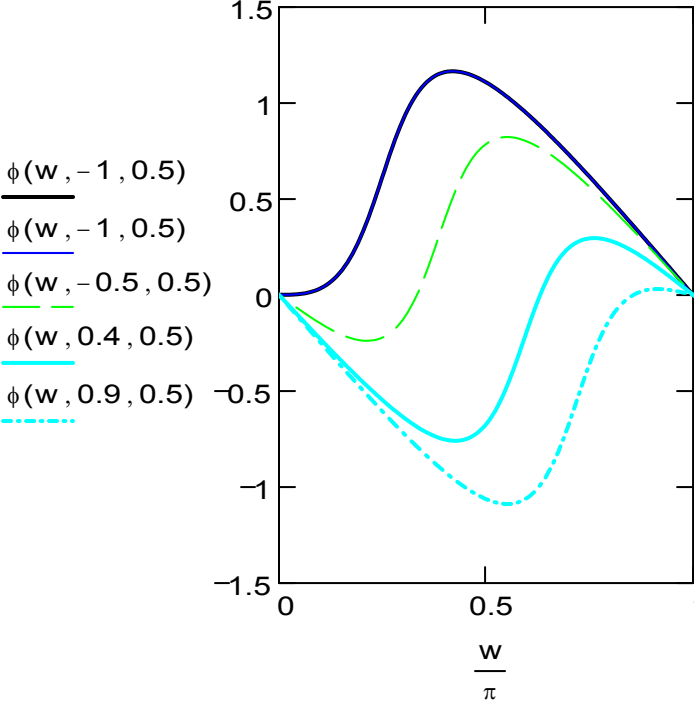
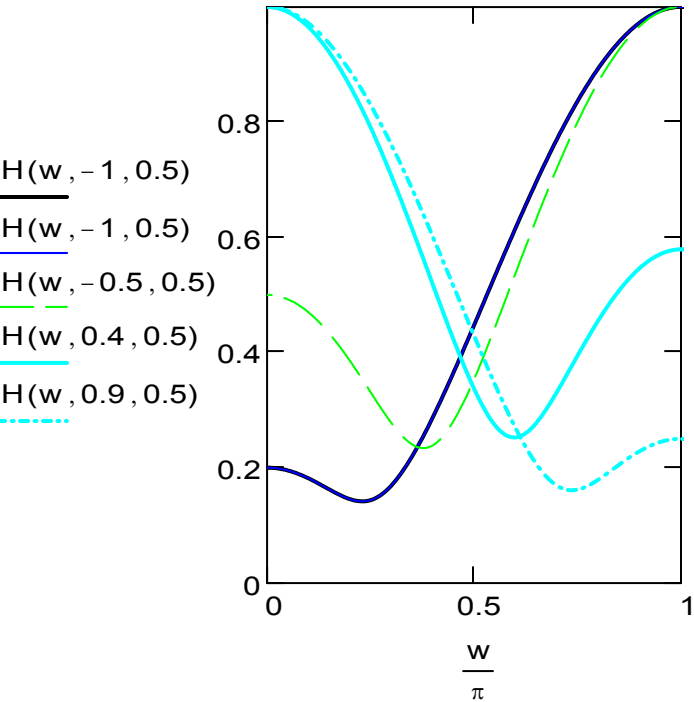
$$\frac{w_2(-1, -1)}{\pi} = 0.79$$

$$Q(-1, -1) = 0.861$$

$$a_1 := -2, -1.9 \dots 2$$

$$a_2 := -2, -1.9 \dots 0$$





$\underline{wp(a1, a2)} := \arccos\left(-a1 \cdot \frac{1+a2}{4a2}\right)$

$\frac{wp(0, 0.5)}{\pi} = 0.5$

$\frac{wp(-0.8, 0.5)}{\pi} = 0.295$

$\frac{wp(-1, 0.5)}{\pi} = 0.23$

$\frac{wp(-0.2, 0.5)}{\pi} = 0.452$

$\frac{wp(-1.1, 0.5)}{\pi} = 0.191$

$$A(a_2) := 4a_2 \quad B(a_1, a_2) := 2a_1 \cdot (1 + a_2) \quad C(a_1, a_2) := a_1^2 + (1 - a_2)^2$$

$$b_1(a_1, a_2) := \frac{-B(a_1, a_2) - \sqrt{B(a_1, a_2)^2 \cdot (-1) + 4 \cdot A(a_2) \cdot C(a_1, a_2)}}{2A(a_2)}$$

$$b_2(a_1, a_2) := \frac{-B(a_1, a_2) + \sqrt{B(a_1, a_2)^2 + 4 \cdot A(a_2) \cdot C(a_1, a_2)}}{2A(a_2)}$$

$$w_1(a_1, a_2) := \arccos(b_1(a_1, a_2)) \quad w_2(a_1, a_2) := \arccos(b_2(a_1, a_2))$$

$$Q(a_1, a_2) := \frac{w_1(a_1, a_2)}{w_1(a_1, a_2) - w_2(a_1, a_2)}$$

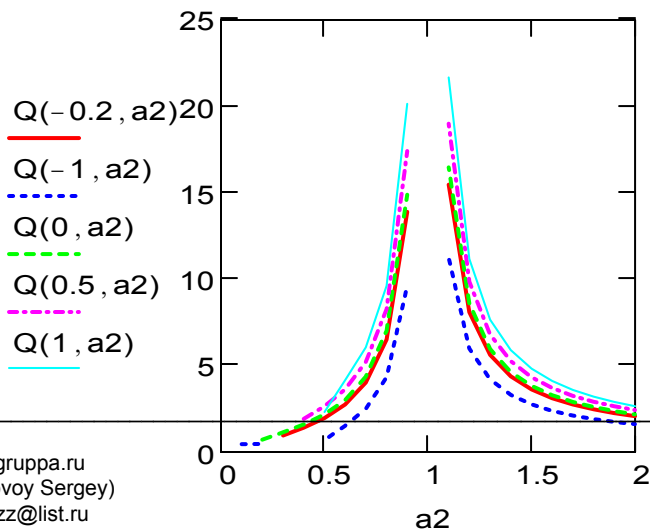
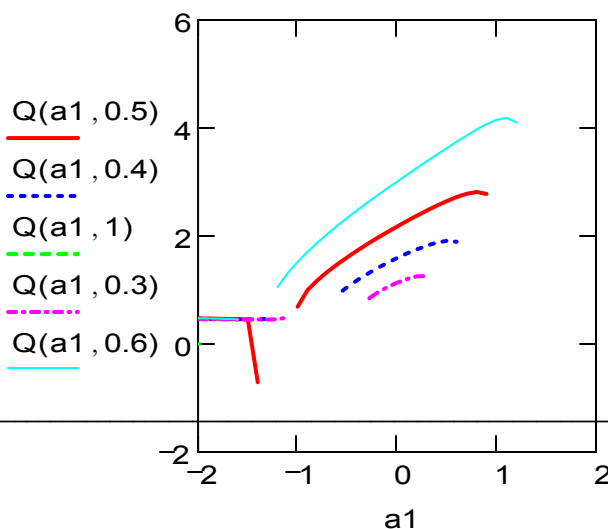
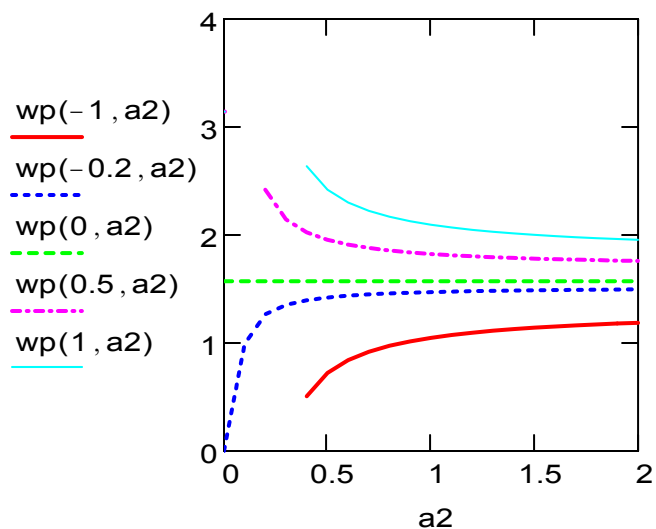
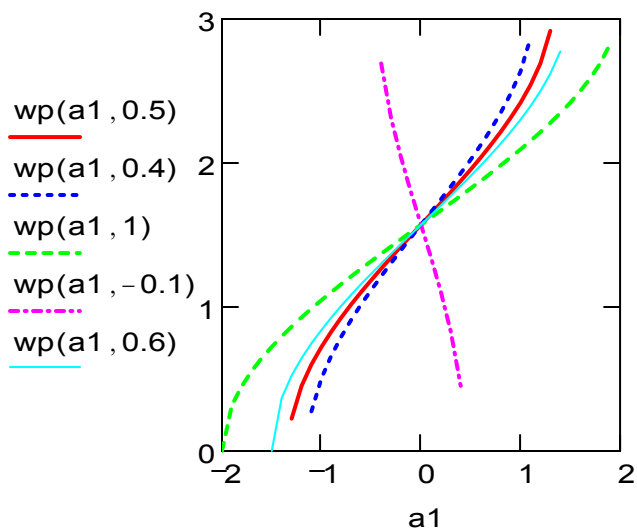
$$b_1(0, 0.5) = -0.354 \quad b_2(0, 0.5) = 0.354$$

$$\frac{w_1(0, 0.5)}{\pi} = 0.615 \quad \frac{w_2(0, 0.5)}{\pi} = 0.385$$

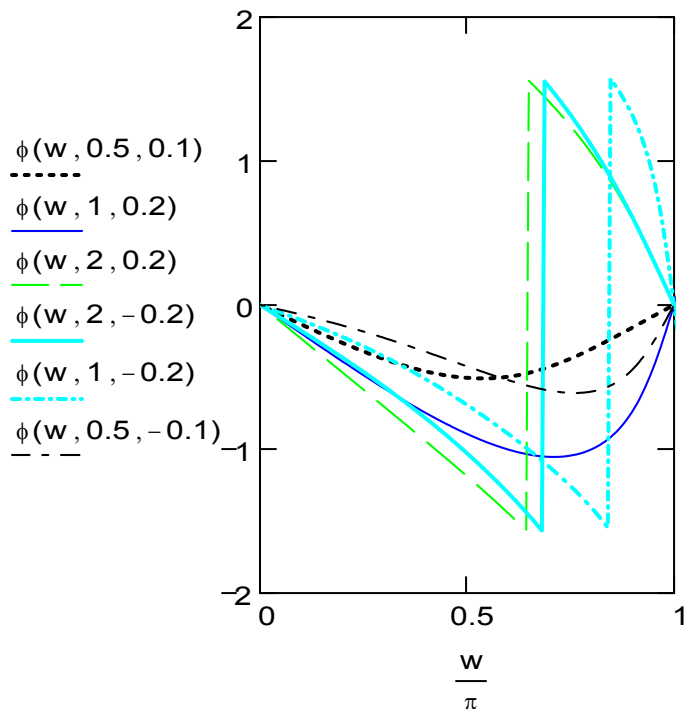
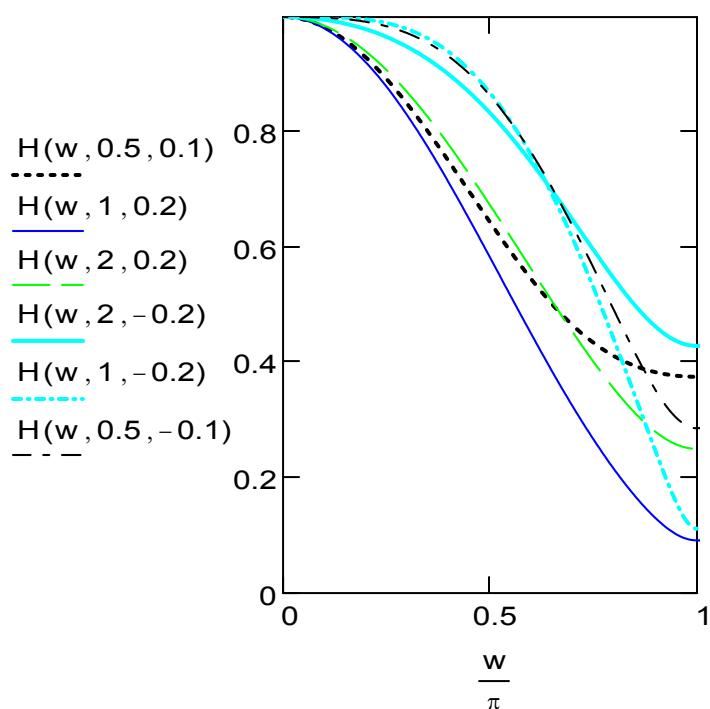
$$Q(0, 0.5) = 2.173$$

$$a_1 := -2, -1.9 \dots 2$$

$$a_2 := 0, 0.1 \dots 2$$



ФНЧ



$$A(a_2) := 4a_2 B(a_1, a_2) := 2a_1 \cdot (1 + a_2) C(a_1, a_2) := a_1^2 + (1 - a_2)^2$$

$$wc(a_1, a_2) := \arccos \left[ \frac{-B(a_1, a_2) + \sqrt{B(a_1, a_2)^2 - 2A(a_2)} \cdot [2C(a_1, a_2) - (|a_1| + a_2 + 1)^2]}{2A(a_2)} \right]$$

$$\frac{wc(0.5, 0.1)}{\pi} = 0.44$$

$$\frac{wc(2, 0.2)}{\pi} = 0.469$$

$$\frac{wc(1, -0.2)}{\pi} = 0.639$$

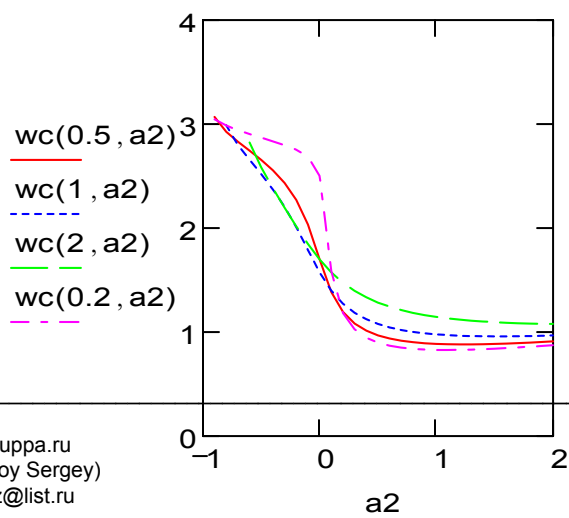
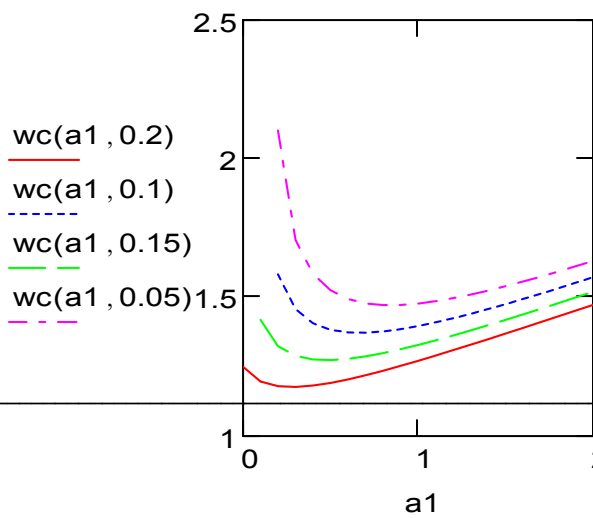
$$\frac{wc(1, 0.2)}{\pi} = 0.404$$

$$\frac{wc(2, -0.2)}{\pi} = 0.641$$

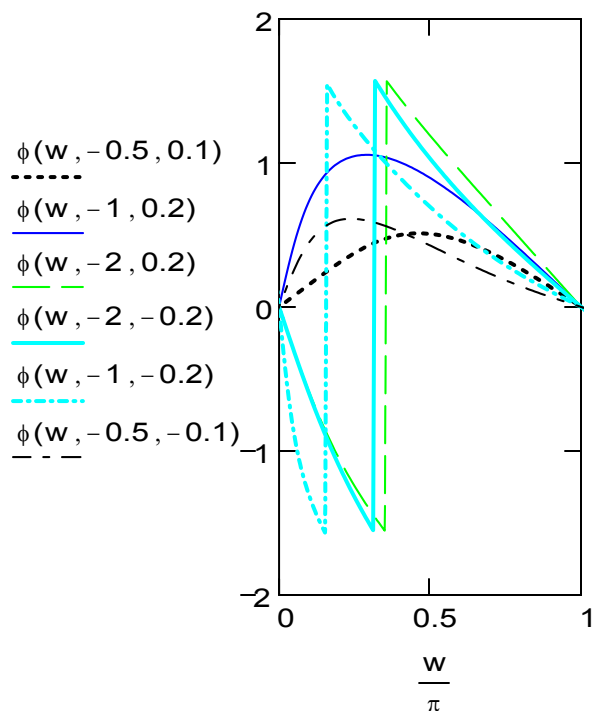
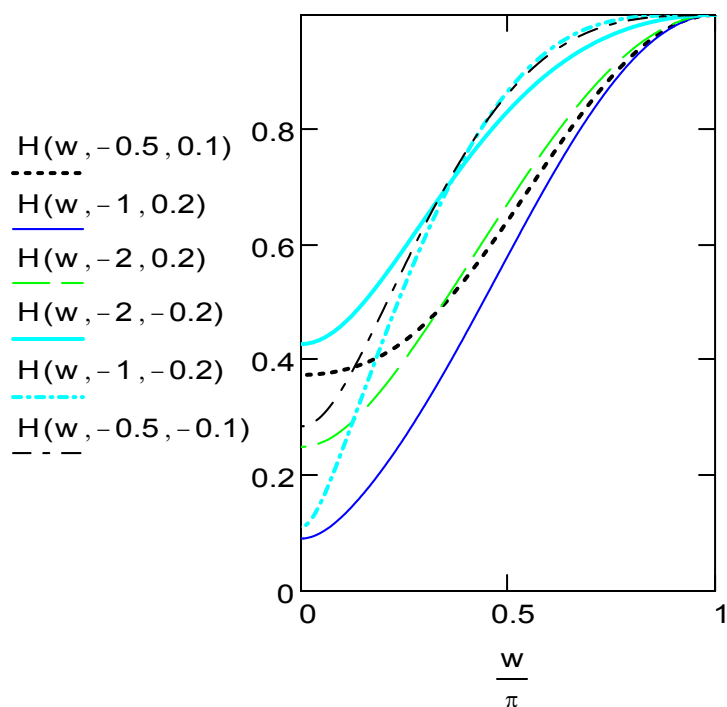
$$\frac{wc(0.5, -0.1)}{\pi} = 0.647$$

$a_1 := 0, 0.1 \dots 2$

$a_2 := -2, -1.9 \dots 2$



ФВЧ



$$\text{wc}(a_1, a_2) := \arccos \left[ \frac{-B(a_1, a_2) - \sqrt{B(a_1, a_2)^2 - 2A(a_2)} \cdot [2C(a_1, a_2) - (|a_1| + a_2 + 1)^2]}{2A(a_2)} \right]$$

$$\frac{\text{wc}(-0.5, 0.1)}{\pi} = 0.56$$

$$\frac{\text{wc}(-2, 0.2)}{\pi} = 0.531$$

$$\frac{\text{wc}(-1, -0.2)}{\pi} = 0.361$$

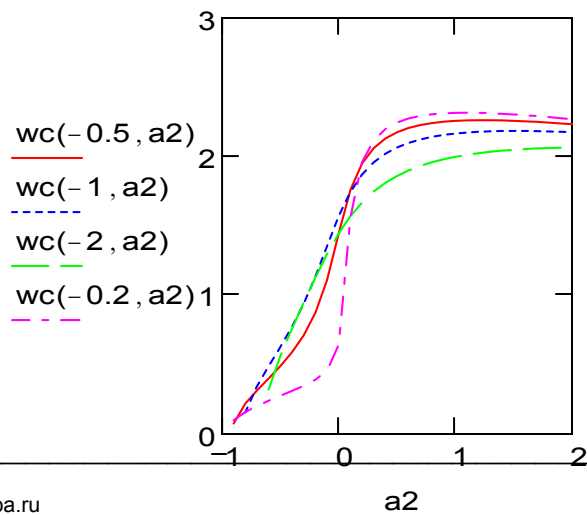
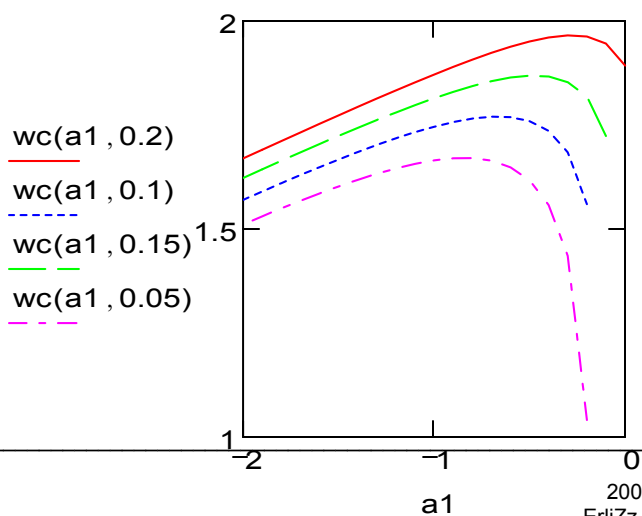
$$\frac{\text{wc}(-1, 0.2)}{\pi} = 0.596$$

$$\frac{\text{wc}(-2, -0.2)}{\pi} = 0.359$$

$$\frac{\text{wc}(-0.5, -0.1)}{\pi} = 0.353$$

$a_1 := 0, -0.1 \dots -2$

$a_2 := -2, -1.9 \dots 2$



## 2 Временные характеристики

$$\delta(n) := \begin{cases} 1 & \text{if } n = 0 \\ 0 & \text{otherwise} \end{cases} \quad \text{one}(n) := \begin{cases} 1 & \text{if } n \geq 0 \\ 0 & \text{otherwise} \end{cases}$$

$$h(n, a1, a2) := \delta(n) + a1 \cdot \delta(n-1) + a2 \cdot \delta(n-2) \quad g(n, a1, a2) := \text{one}(n) + a1 \cdot \text{one}(n-1) + a2 \cdot \text{one}(n-2)$$

$$\text{rect}(n, ni) := \text{one}(n) - \text{one}(n - ni)$$

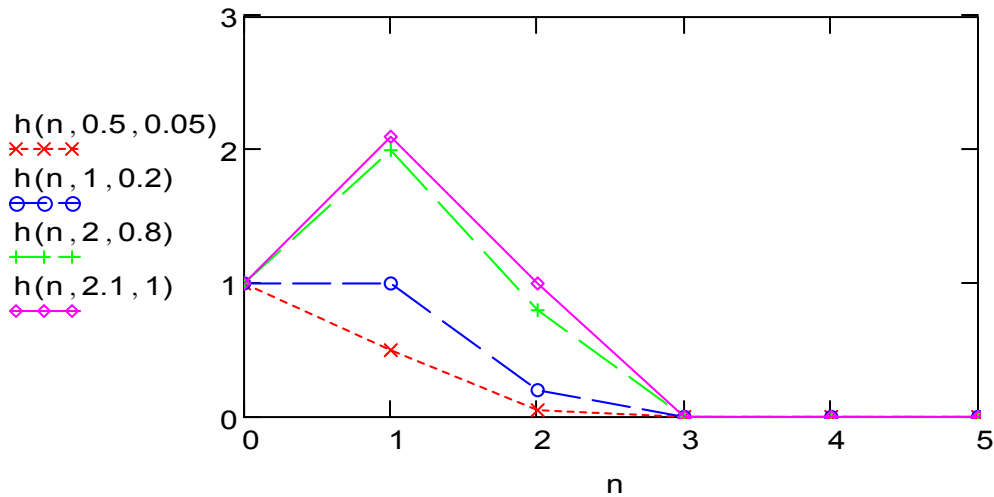
$$\text{RR}(n, w, ni) := \sin(w \cdot n) \cdot (\text{one}(n) - \text{one}(n - ni))$$

$$n := 0 \dots 10$$

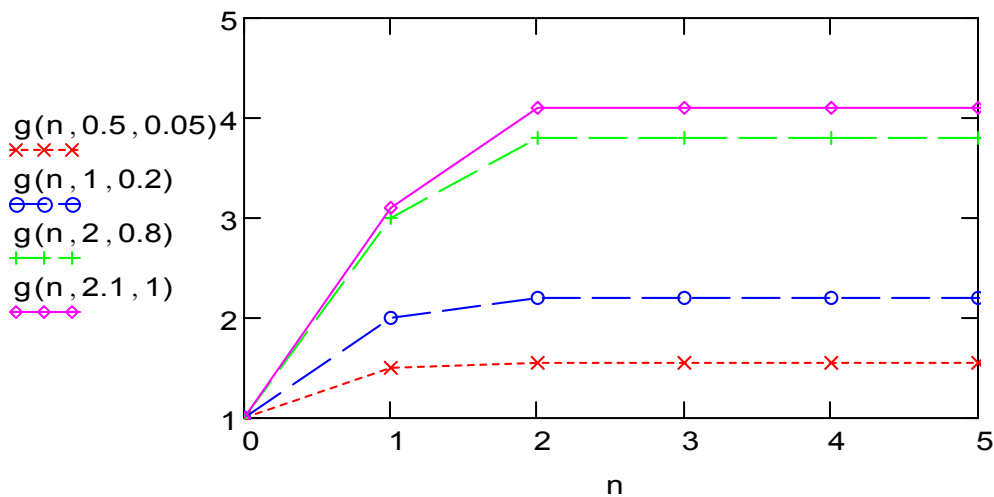
$$\text{opr}(a1, a2) := \begin{cases} m \leftarrow 0 \\ \text{while } |h(m, a1, a2)| > 0.1 \\ \quad m \leftarrow m + 1 \\ \text{opr} \leftarrow m \end{cases}$$

### 2.1 ФНЧ

#### 2.1.1 Импульсная и переходная характеристики



$$\begin{aligned} \text{opr}(0.5, 0.05) &= 2 \\ \text{opr}(1, 0.2) &= 3 \\ \text{opr}(2, 0.8) &= 3 \\ \text{opr}(2.1, 1) &= 3 \end{aligned}$$

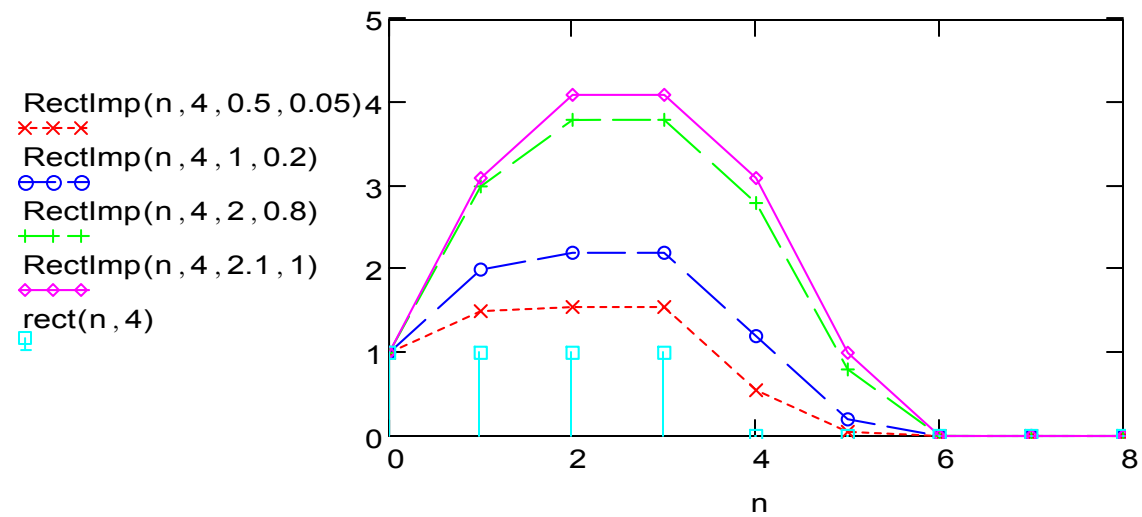


$$\text{opr}_G(a1, a2) := \begin{cases} m \leftarrow 0 \\ \text{while } (1 + a1 + a2) - |g(m, a1, a2)| > 0.1 \\ \quad m \leftarrow m + 1 \\ \text{opr} \leftarrow m \end{cases}$$

$$\begin{aligned} \text{opr}_G(0.5, 0.05) &= 1 \\ \text{opr}_G(1, 0.2) &= 2 \\ \text{opr}_G(2, 0.8) &= 2 \\ \text{opr}_G(2.1, 1) &= 2 \end{aligned}$$



$\text{RectImp}(n, ni, a1, a2) := \text{rect}(n, ni) + a1 \cdot \text{rect}(n - 1, ni) + a2 \cdot \text{rect}(n - 2, ni)$



$\tau\phi(ni, a1, a2) :=$

$m \leftarrow 0$ while $(1 + a1 + a2) -  \text{RectImp}(m, ni, a1, a2)  > 0.1$ $m \leftarrow m + 1$ opr $\leftarrow m$	
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$$\tau\phi(4, 0.5, 0.05) = 1$$

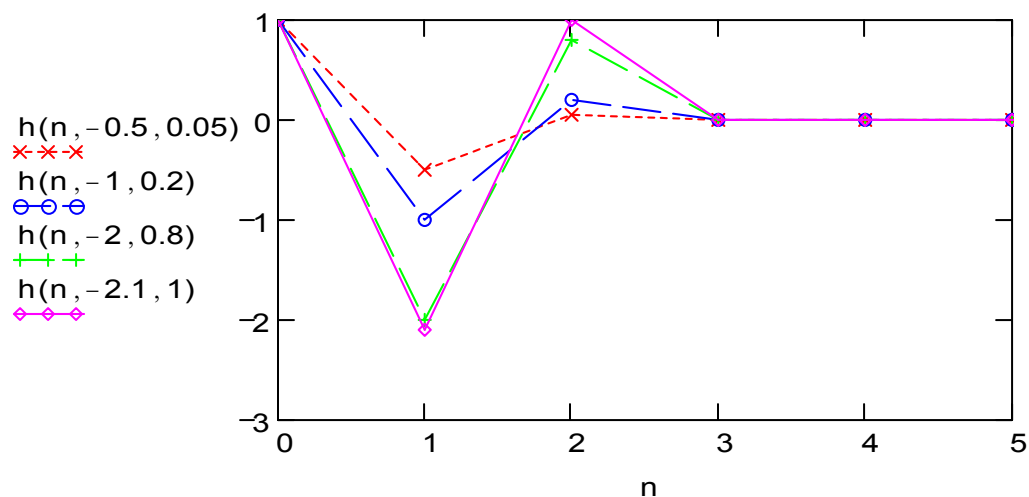
$$\tau\phi(4, 1, 0.2) = 2$$

$$\tau\phi(4, 2, 0.8) = 2$$

$$\tau\phi(4, 2.1, 1) = 2$$

## 2,2 ФВЧ

### 2.1.1 Импульсная и переходная характеристики

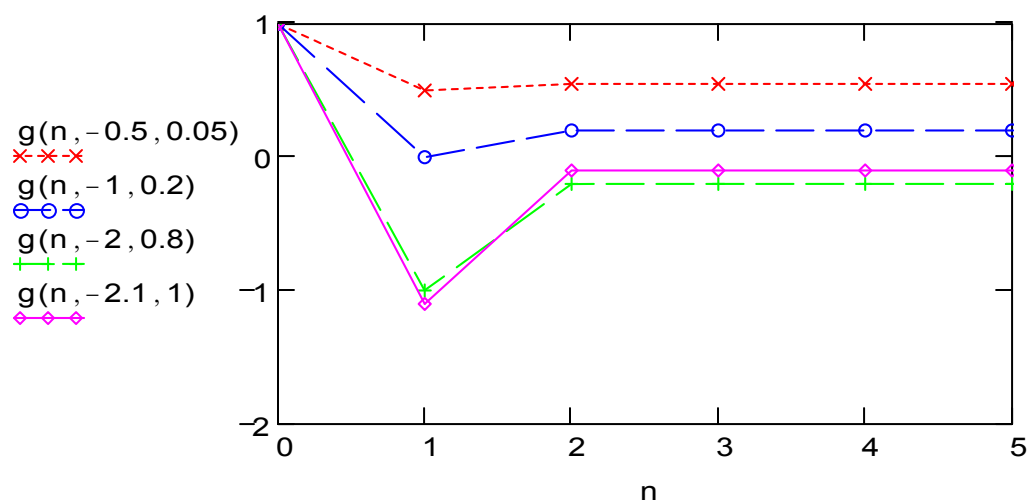


$$\text{opr}(-0.5, 0.05) = 2$$

$$\text{opr}(-1, 0.2) = 3$$

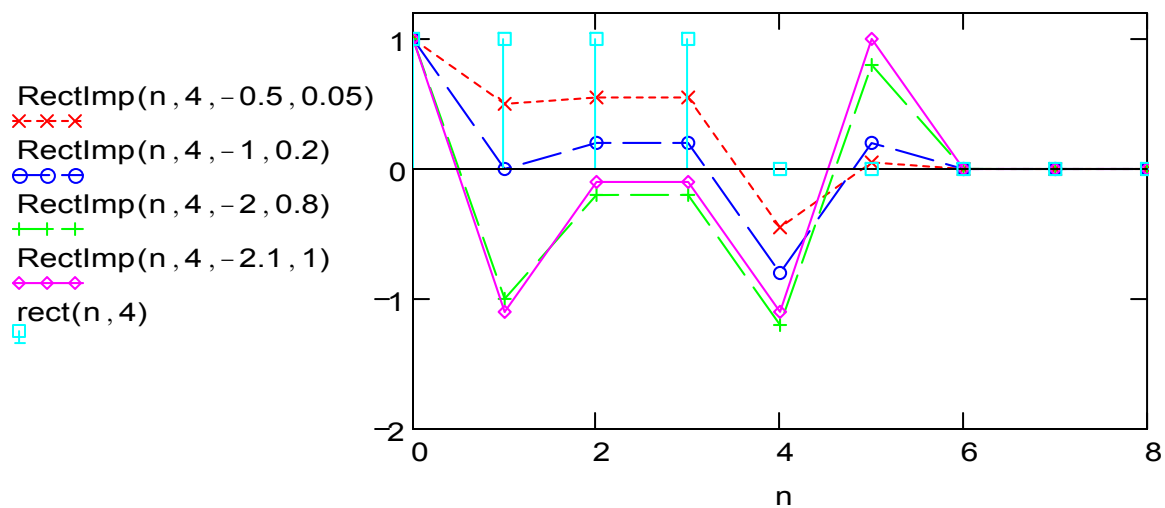
$$\text{opr}(-2, 0.8) = 3$$

$$\text{opr}(-2.1, 1) = 3$$



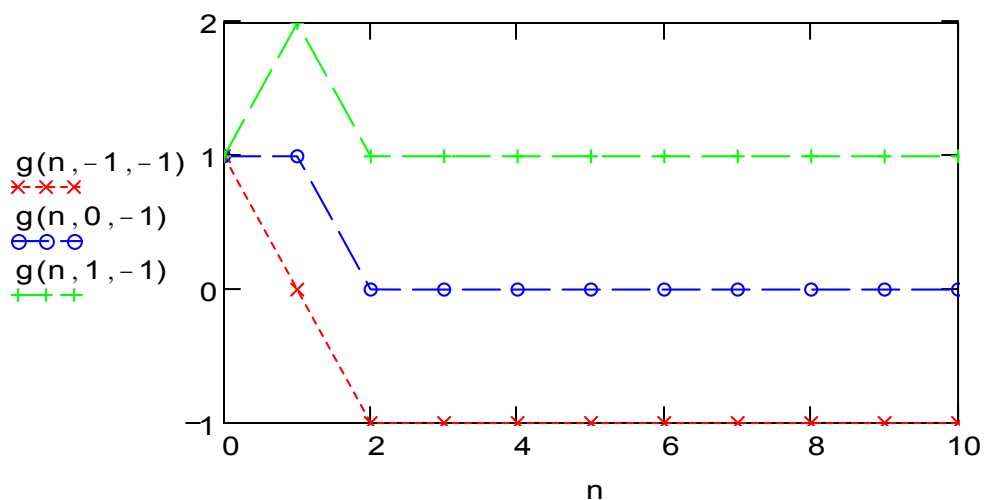
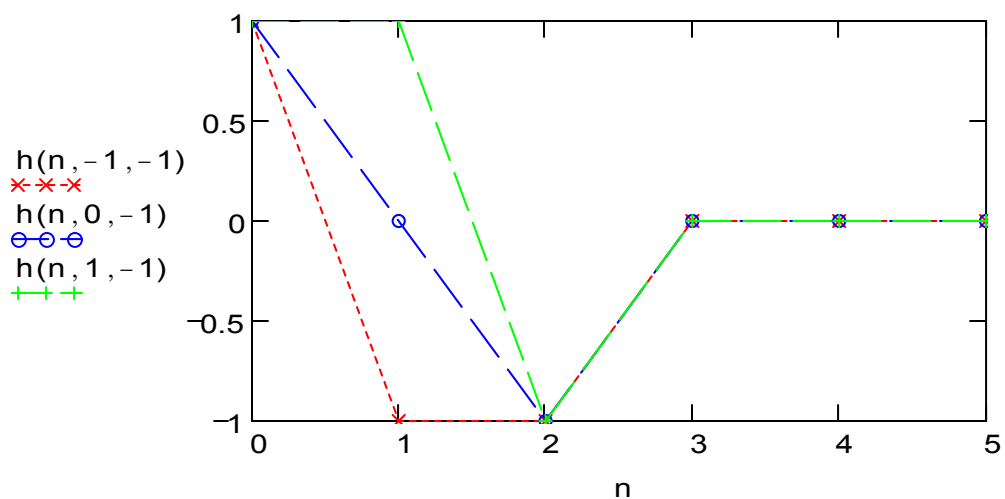
### 2,2 Воздействие на прямоугольный импульс

$$\text{RectImp}(n, n_i, a_1, a_2) := \text{rect}(n, n_i) + a_1 \cdot \text{rect}(n - 1, n_i) + a_2 \cdot \text{rect}(n - 2, n_i)$$



## Полосовой Фильтр

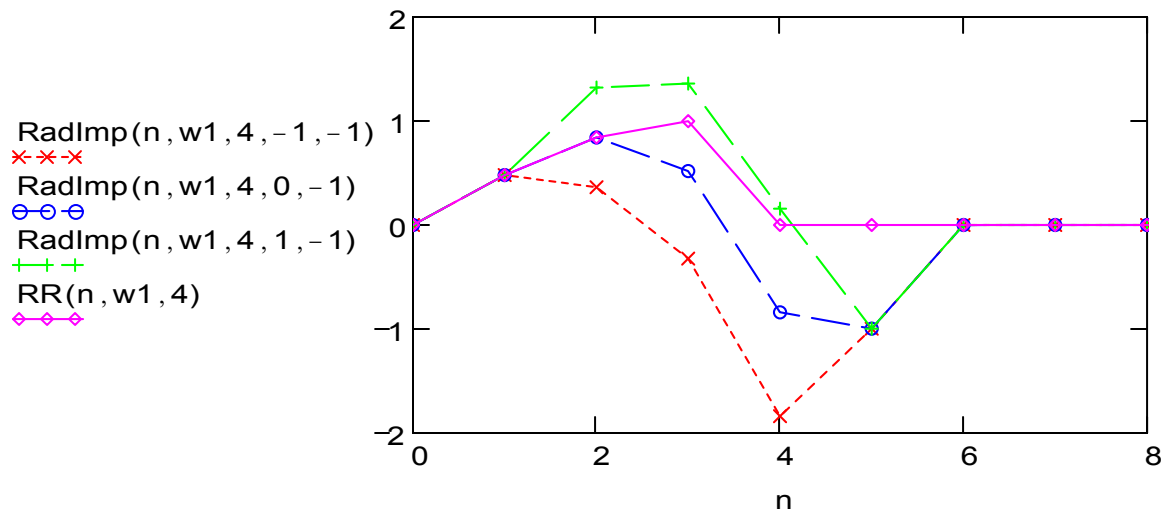
### 2.1.1 Импульсная и переходная характеристики



### 2, 2 Воздействие на прямоугольный радиоимпульс

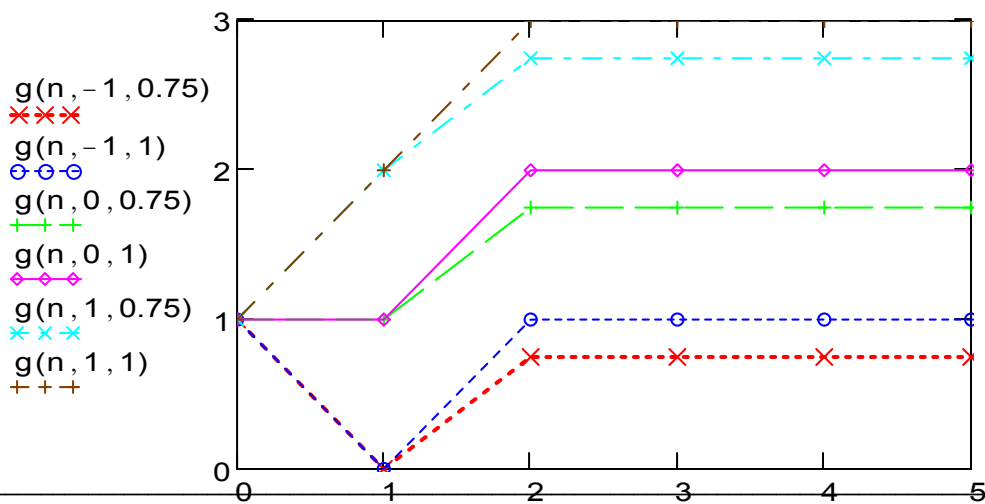
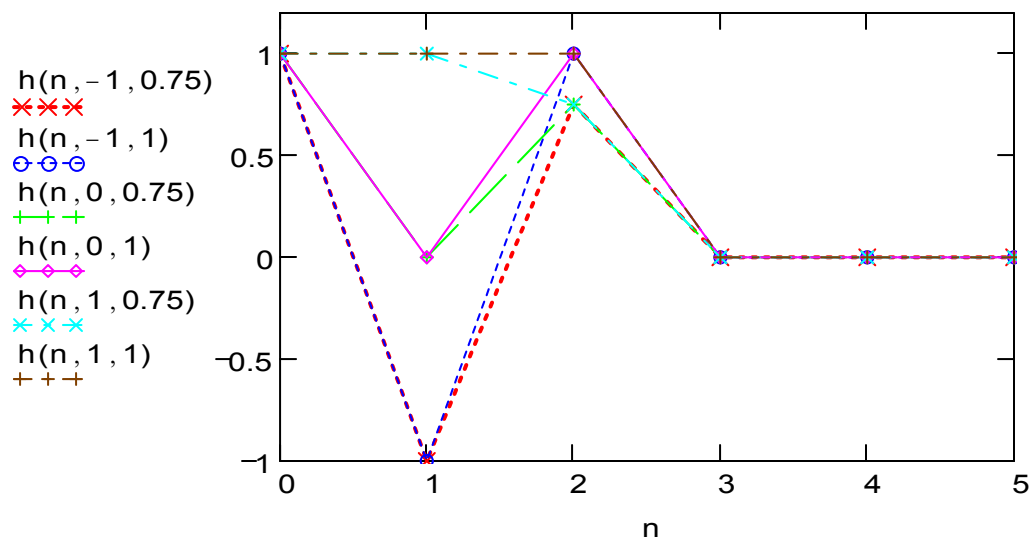
$$w1 := \frac{wp(-1, -1)}{\pi}$$

$$\text{RadImp}(n, ww, ni, a1, a2) := \text{RR}(n, ww, ni, a1, \text{RR}(n-1, ww, ni) + a2 \cdot \text{RR}(n-2, ww, ni))$$



## Режекторный Фильтр

### 2.1.1 Импульсная и переходная характеристики



## 2, 2 Воздействие на прямоугольный радиоимпульс

$$w1 := \frac{wp(-1, 1)}{\pi} \quad w1 = 0.333$$

$$RadImp(n, ww, ni, a1, a2) := RR(n, ww, ni) + a1 \cdot RR(n - 1, ww, ni) + a2 \cdot RR(n - 2, ww, ni)$$

