

разностное уравнение для рекурсивной цепи первого порядка:

$$y(n) := x(n) - b1 \cdot y(n-1) \quad |b1| < 1$$

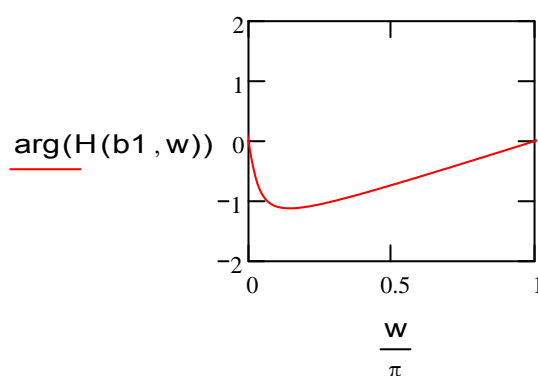
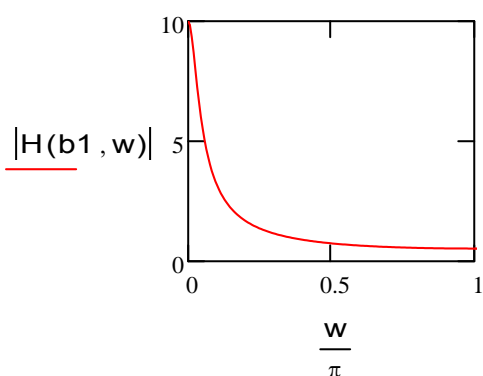
частотная характеристика: $H(b1, w) := \frac{1}{1 + b1 \cdot \cos(w) - i \cdot b1 \cdot \sin(w)}$

АЧХ $|H(b1, w)|$

ФЧХ $\arg(H(b1, w))$

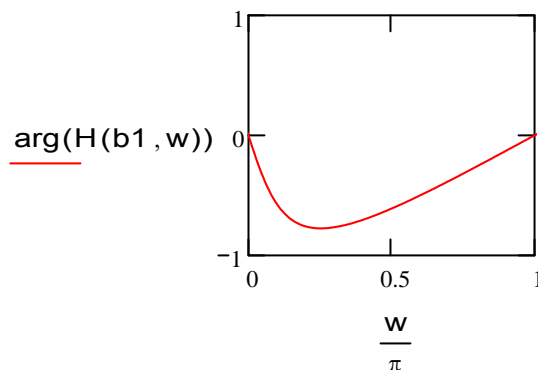
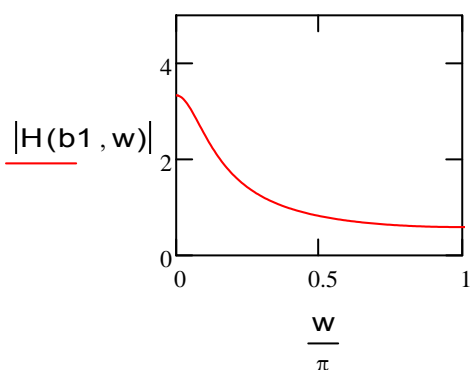
Частота_Среза $Wc(b) := \arccos\left(\frac{b^2 - 4|b| + 1}{2b}\right)$

(1) $b1 := -0.9$



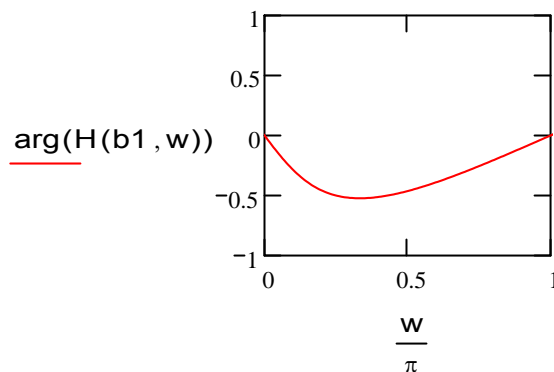
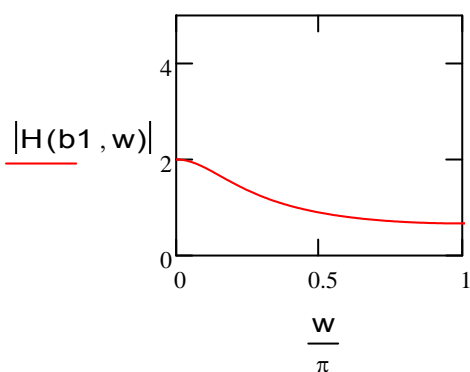
$Wc(b1) = 0.105$

(2) $b1 := -0.7$



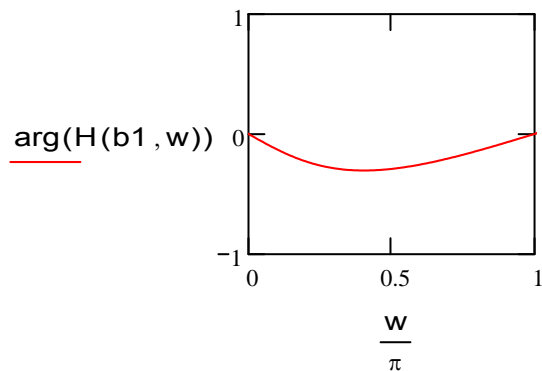
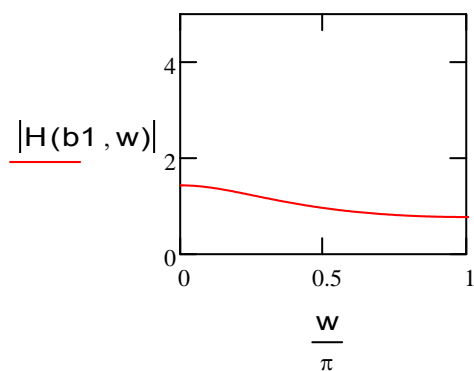
$Wc(b1) = 0.361$

(3) $b1 := -0.5$



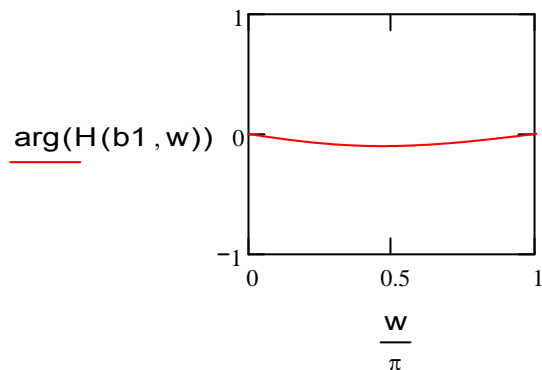
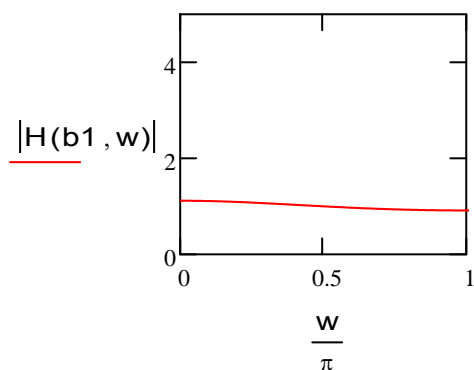
$Wc(b1) = 0.723$

(4) $b1 := -0.3$



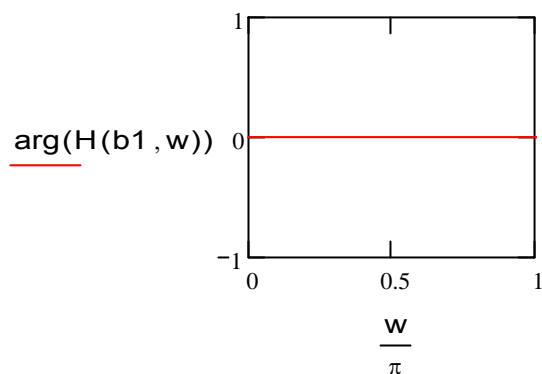
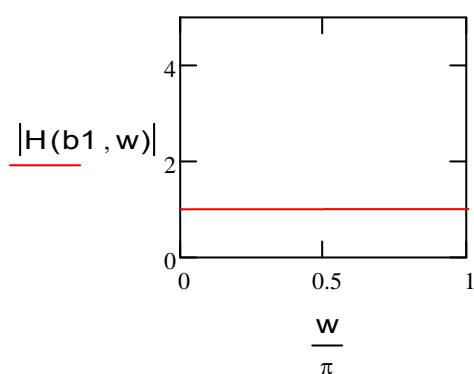
$Wc(b1) = 1.386$

(5) $b1 := -0.1$



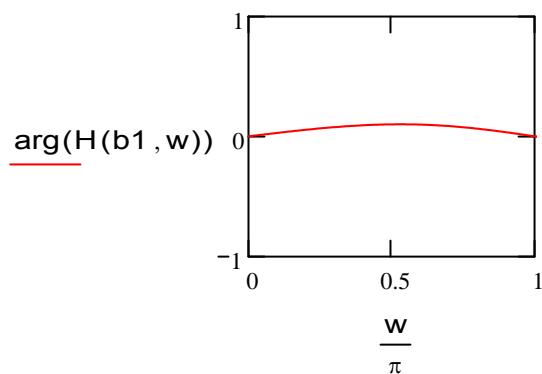
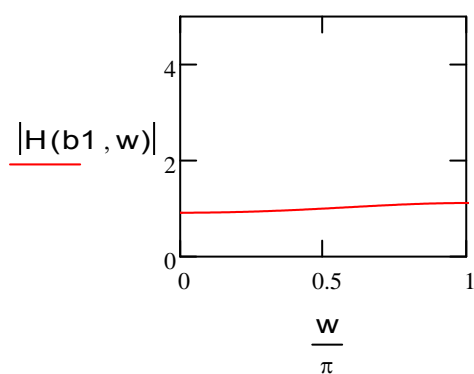
$Wc(b1) = 3.142 - 1$

(6) $b1 := 0.0001$



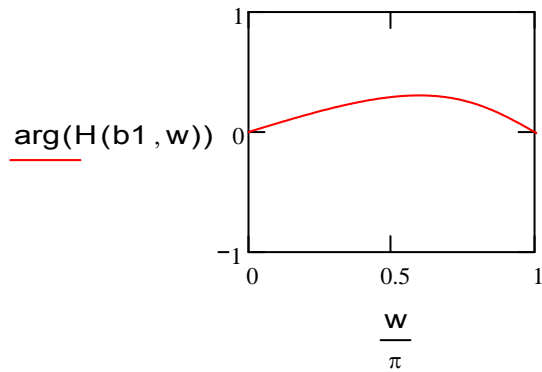
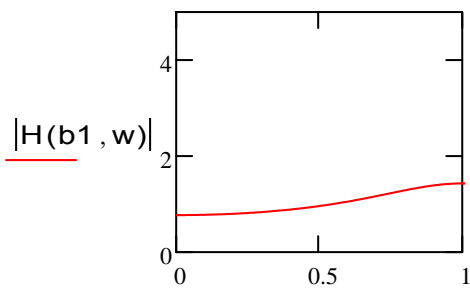
$Wc(b1) = 9.21i$

(7) $b1 := 0.1$



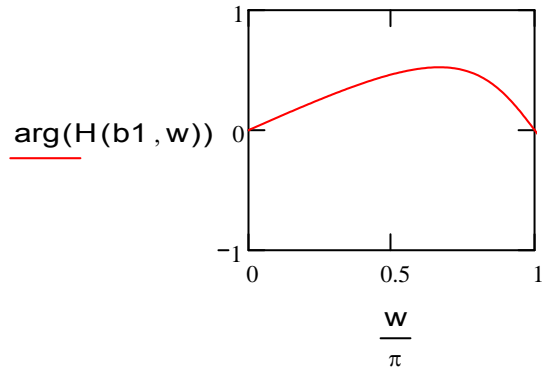
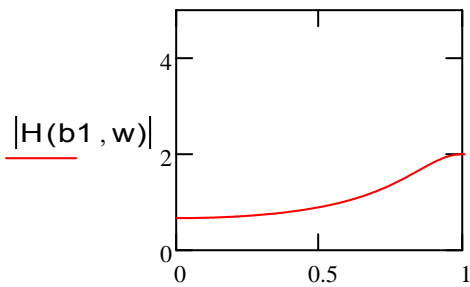
$Wc(b1) = 1.78i$

(8) $\underline{b1} := 0.3$



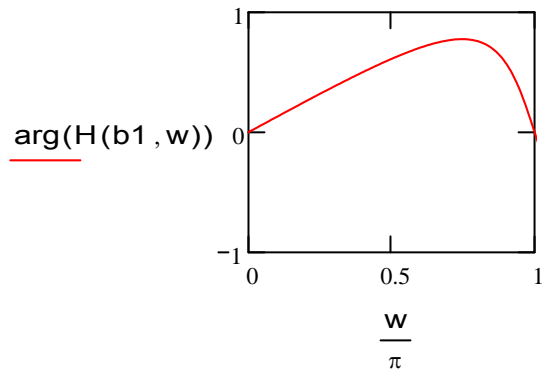
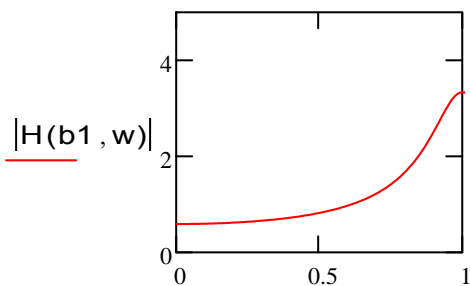
$Wc(b1) = 1.755$

(9) $\underline{b1} := 0.5$ $\frac{w}{\pi}$



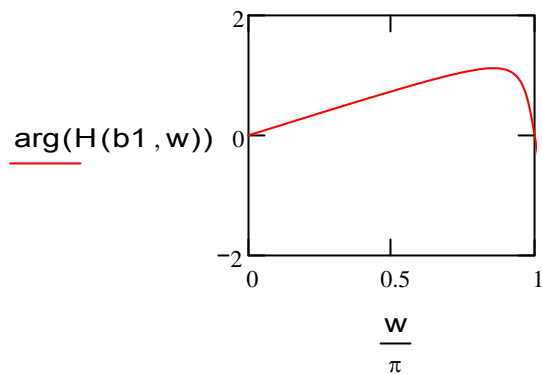
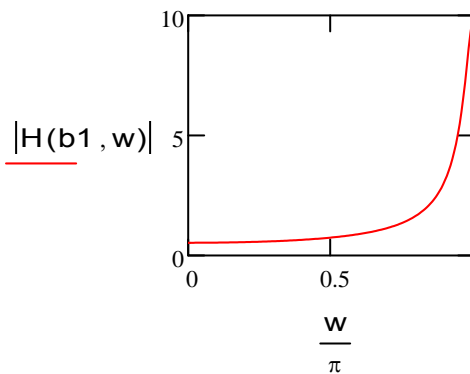
$Wc(b1) = 2.419$

(10) $\underline{b1} := 0.7$ $\frac{w}{\pi}$

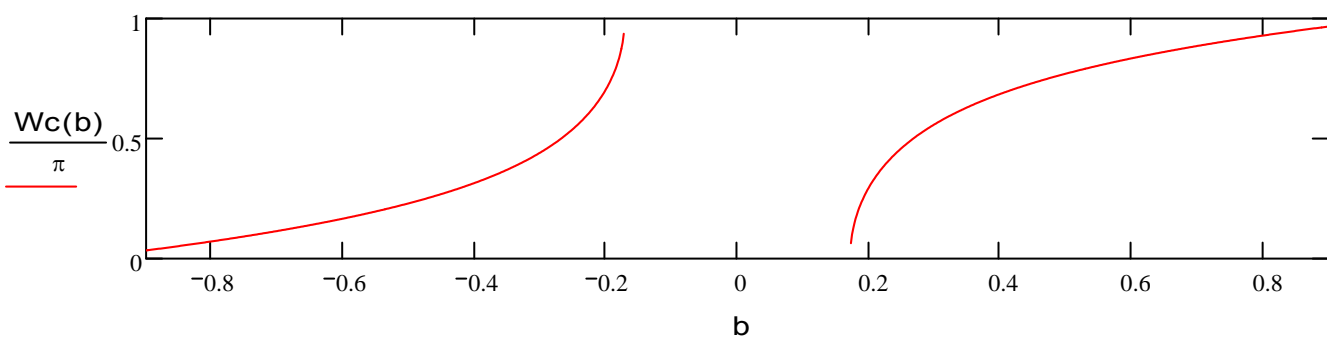


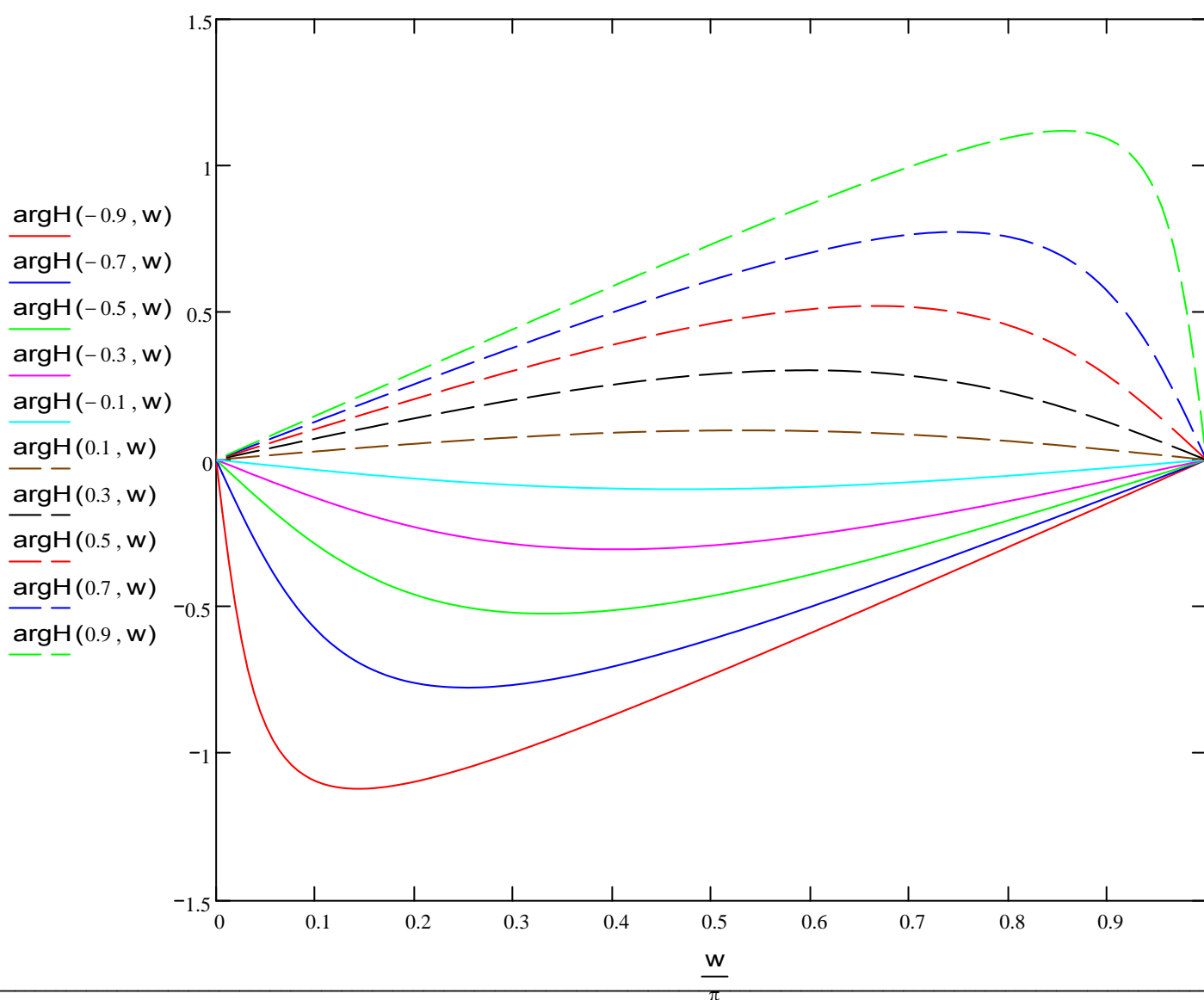
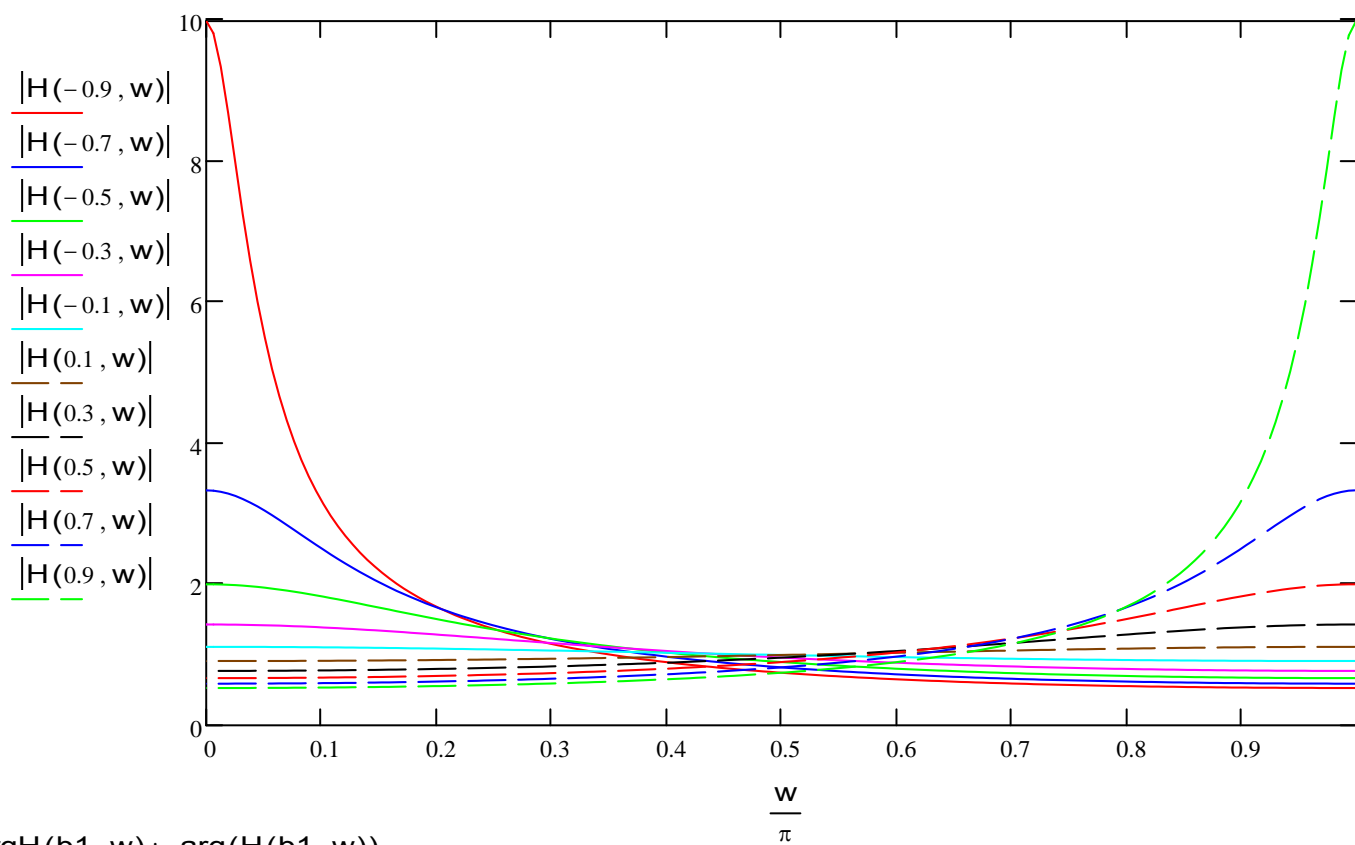
$Wc(b1) = 2.781$

(11) $\underline{b1} := 0.9$ $\frac{w}{\pi}$



$Wc(b1) = 3.036$





Импульсная Характеристика

$n := 0 \dots 10$

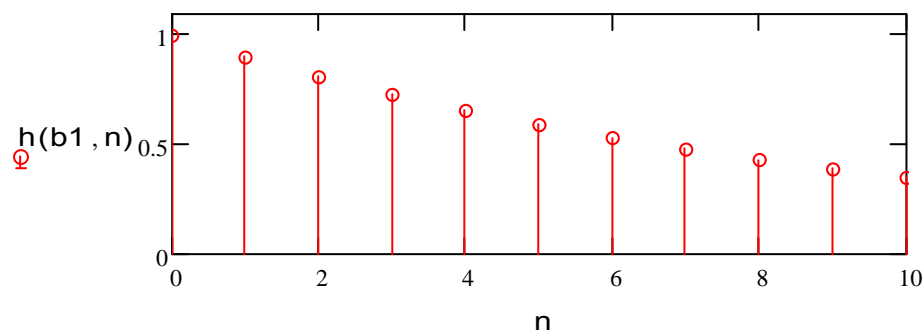
$\text{one}(n) := 1$

$h(b1, n) := (-b1)^n \cdot \text{one}(n)$

$\text{opr}(b1) :=$

```
m ← 0
while |h(b1, m)| > 0.1
  m ← m + 1
opr ← m
```

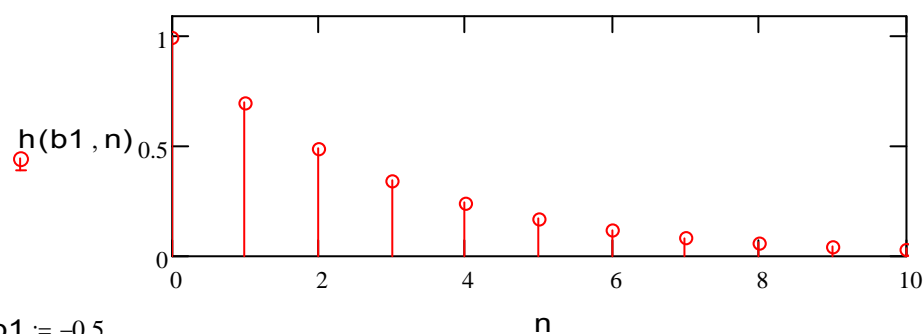
$b1 := -0.9$



$\text{opr}(b1) = 22$

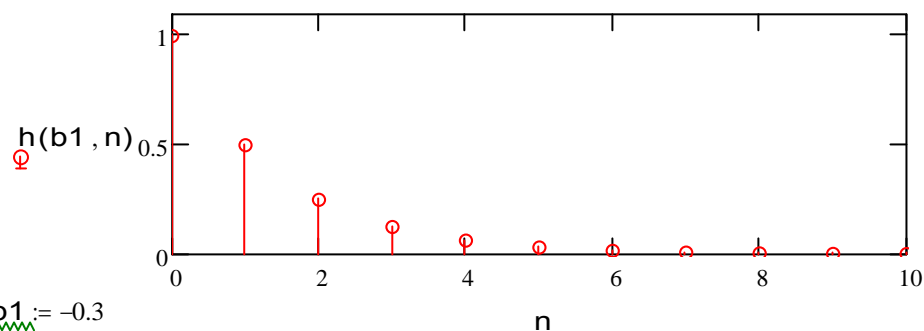


$b1 := -0.7$



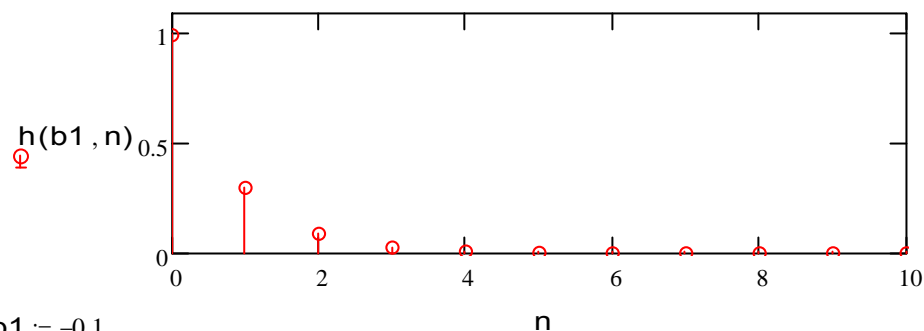
$\text{opr}(b1) = 7$

$b1 := -0.5$



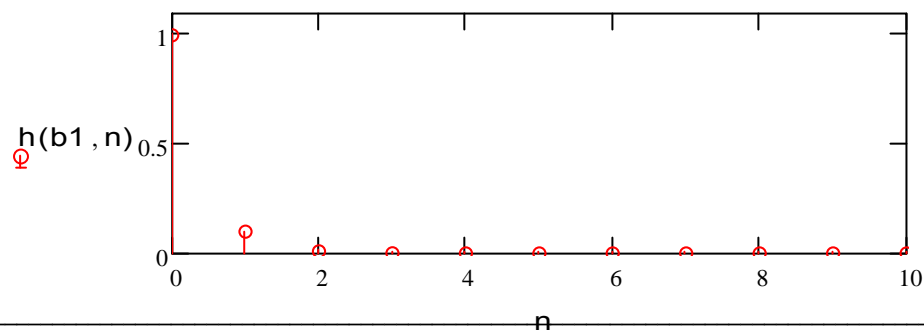
$\text{opr}(b1) = 4$

$b1 := -0.3$



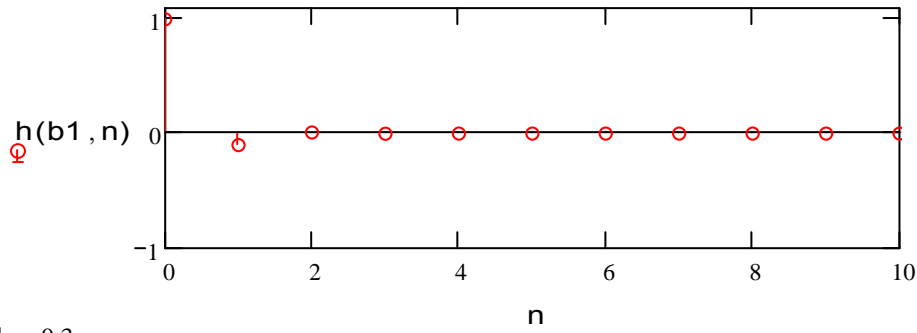
$\text{opr}(b1) = 2$

$b1 := -0.1$



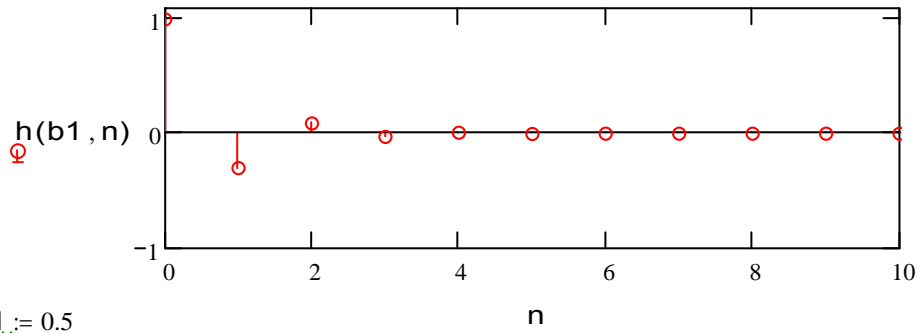
$\text{opr}(b1) = 1$

$b1 := 0.1$



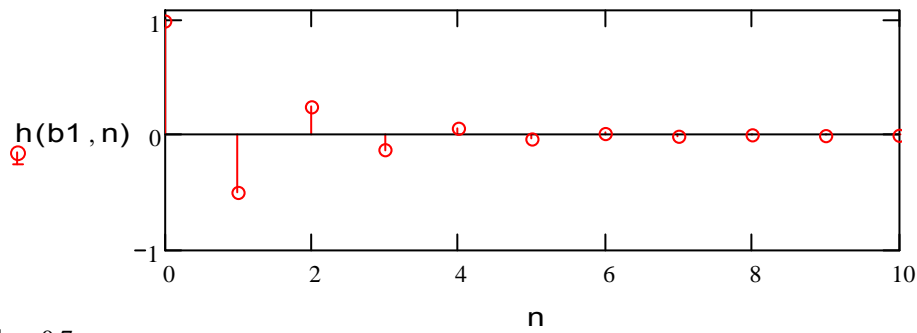
$opr(b1) = 1$

$b1 := 0.3$



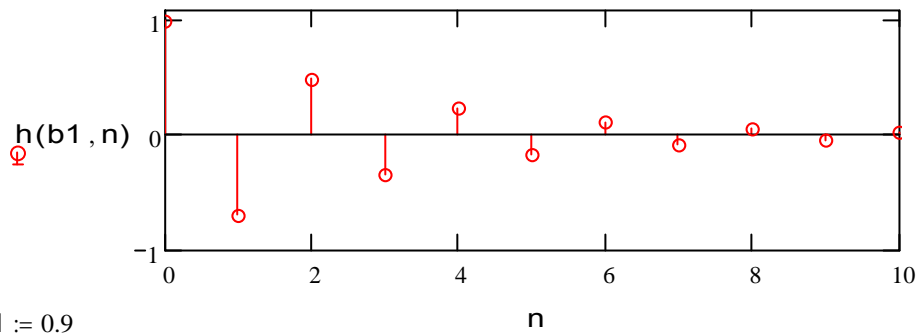
$opr(b1) = 2$

$b1 := 0.5$



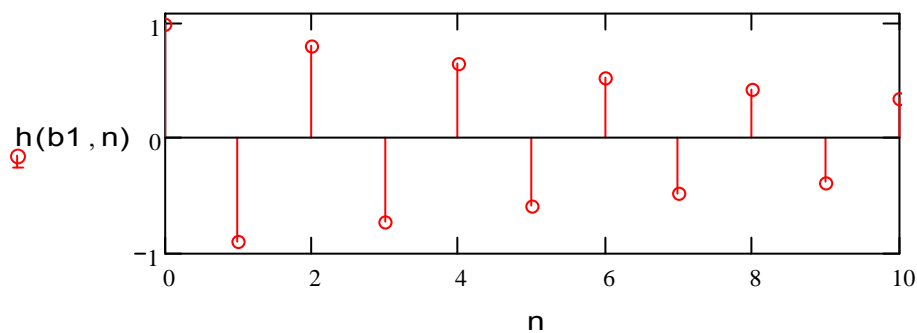
$opr(b1) = 4$

$b1 := 0.7$



$opr(b1) = 7$

$b1 := 0.9$



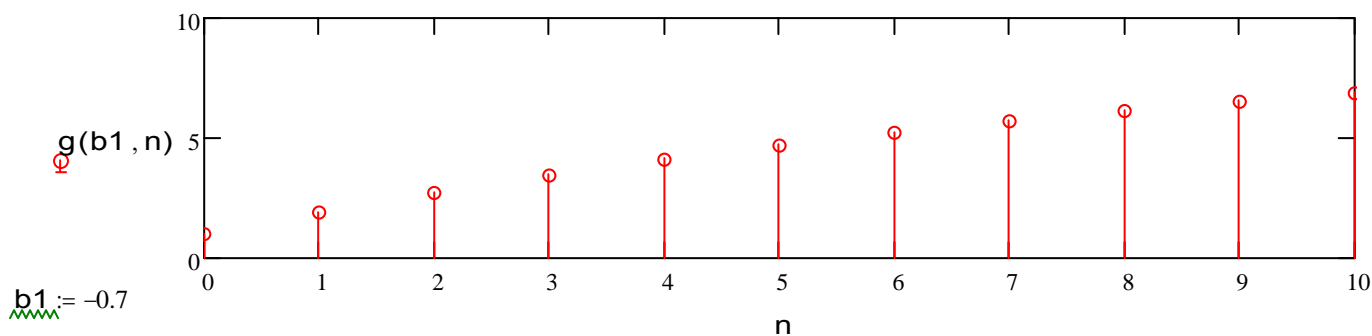
$opr(b1) = 22$

Переходная Характеристика

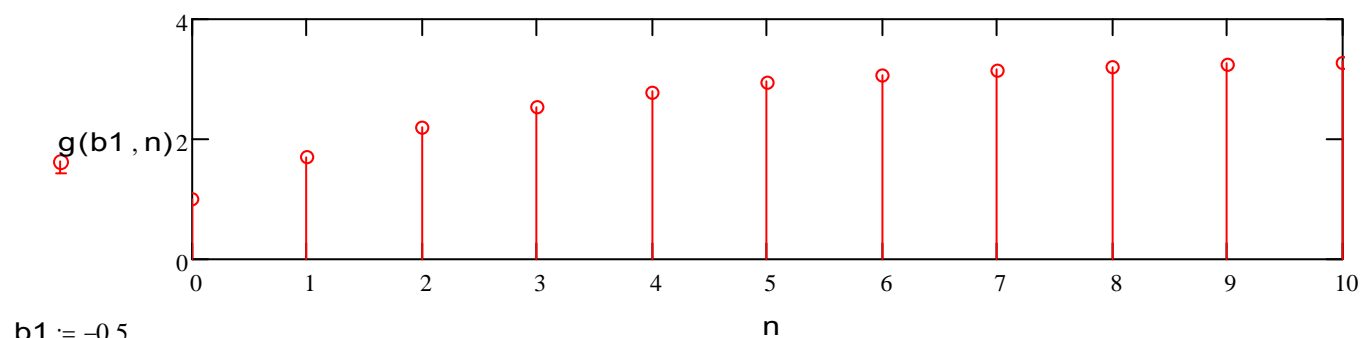
$n := 0 \dots 10$

$$g(b1, n) := \frac{1 - (-b1)^{n+1}}{1 + b1}$$

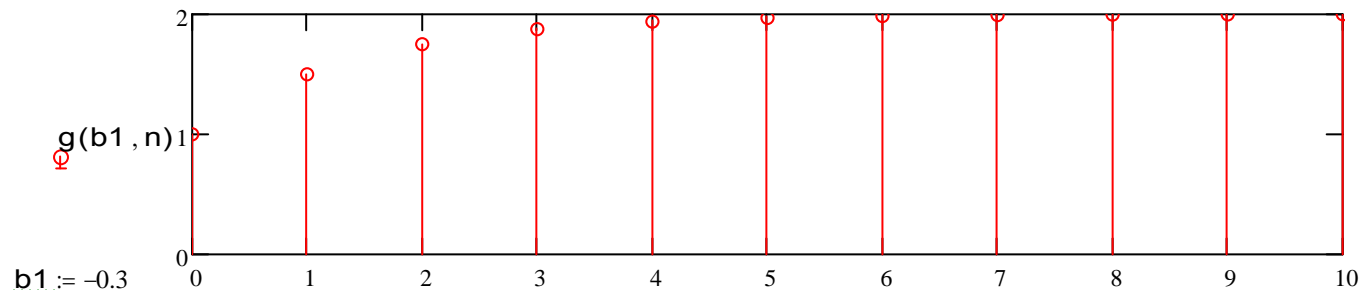
$b1 := -0.9$



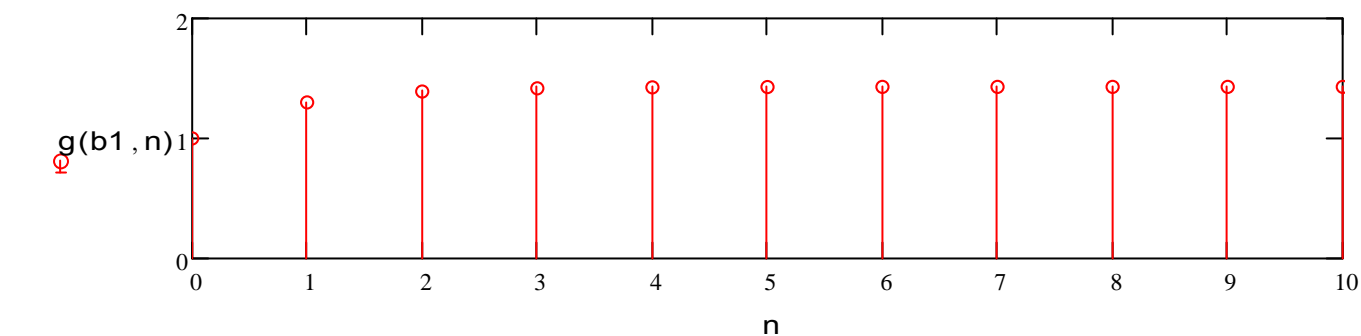
$b1 := -0.7$



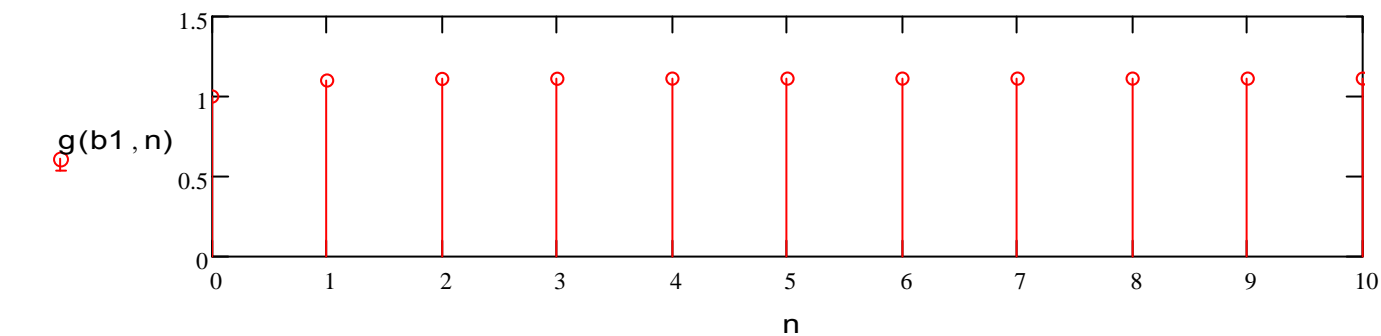
$b1 := -0.5$



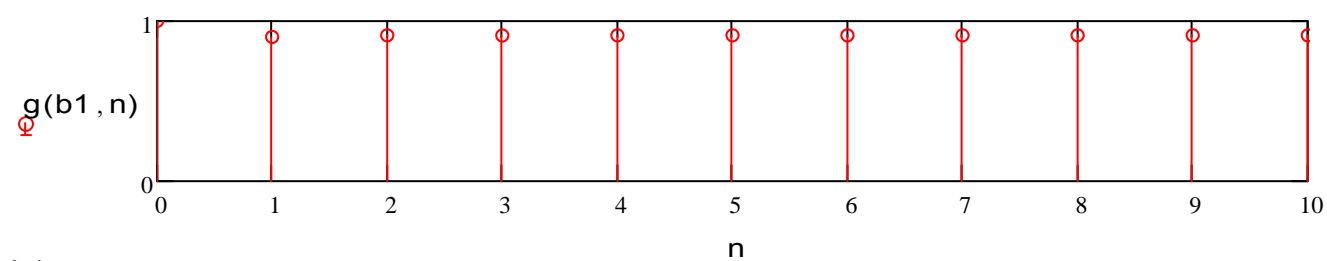
$b1 := -0.3$



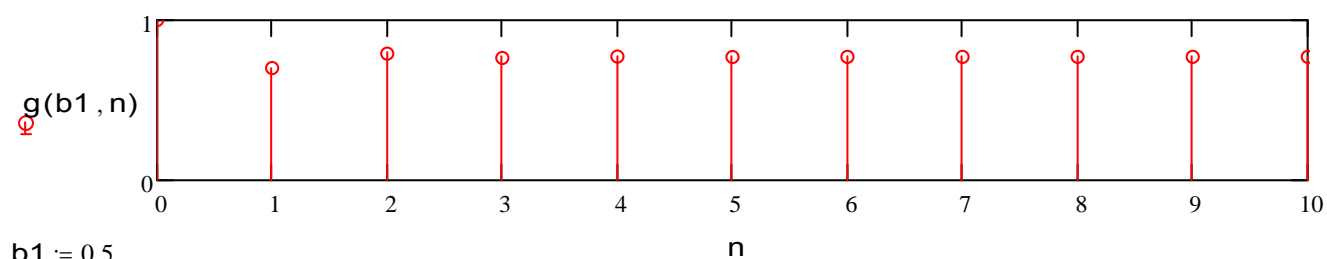
$b1 := -0.1$



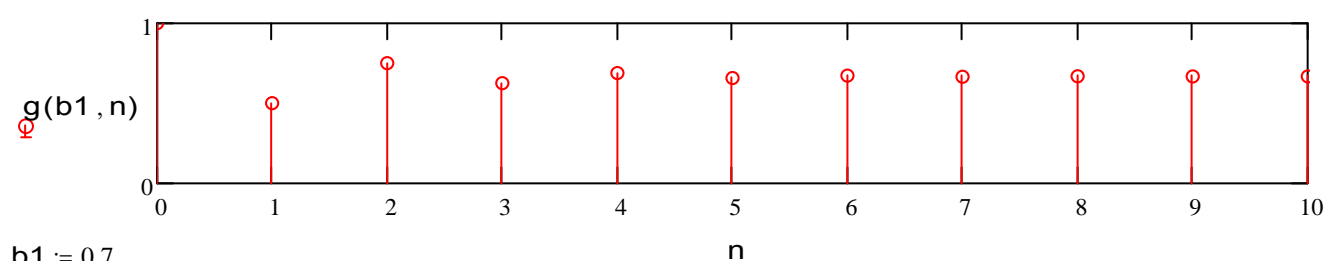
$b1 := 0.1$



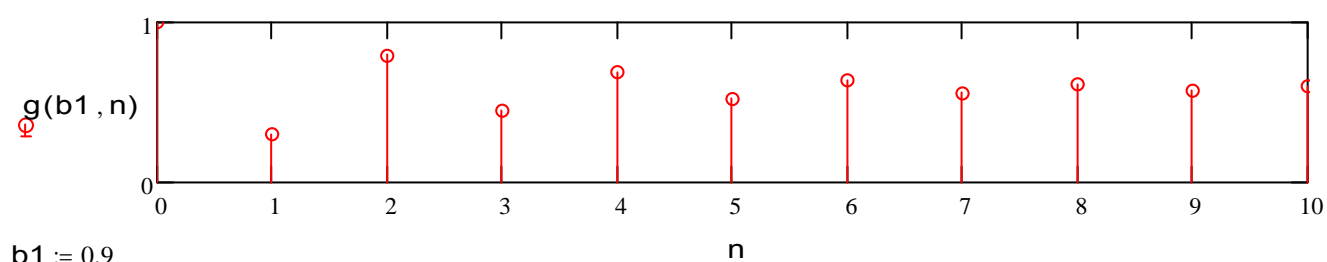
$b1 := 0.3$



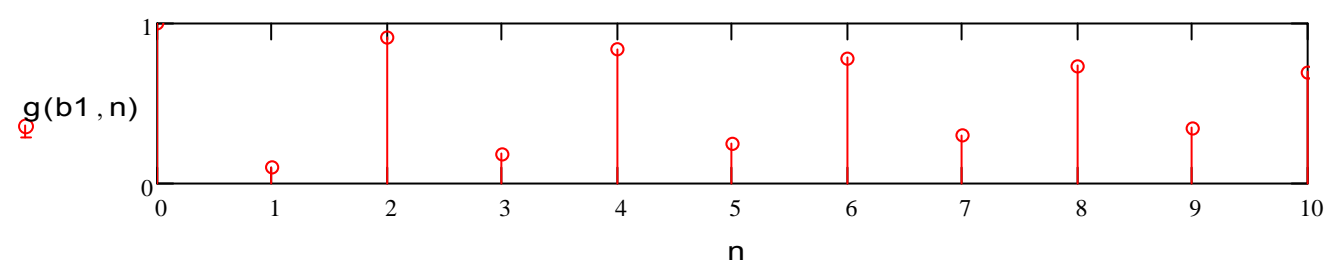
$b1 := 0.5$



$b1 := 0.7$



$b1 := 0.9$

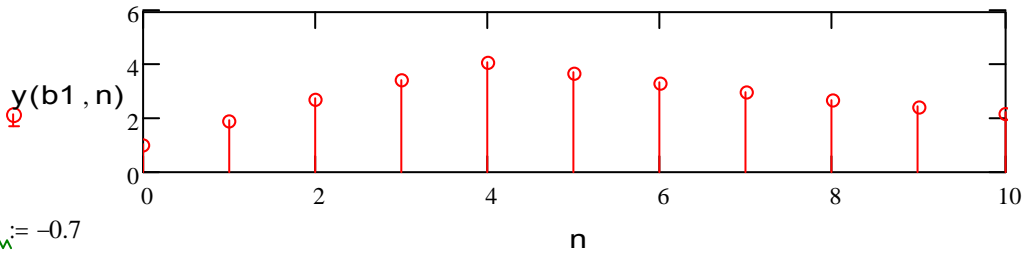
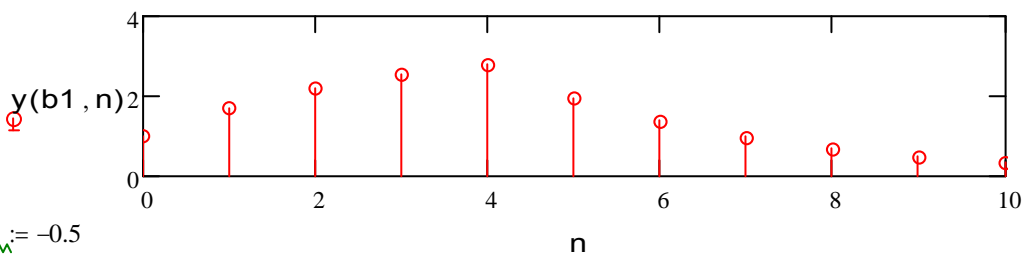
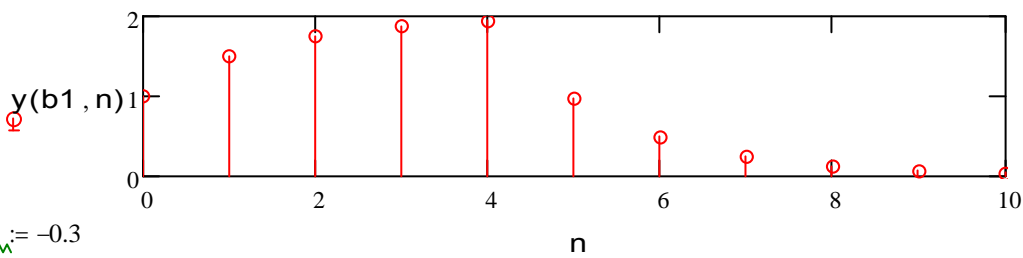
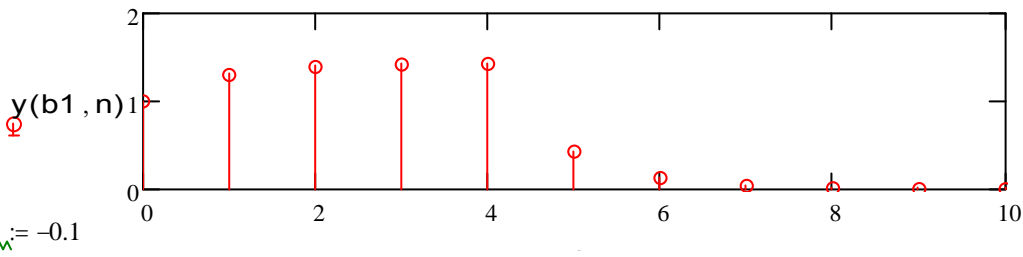
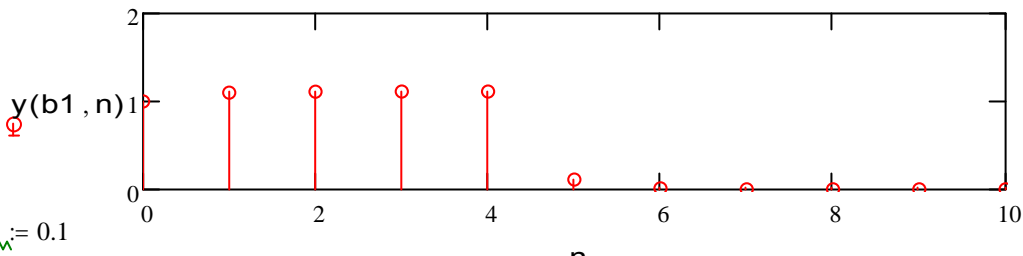
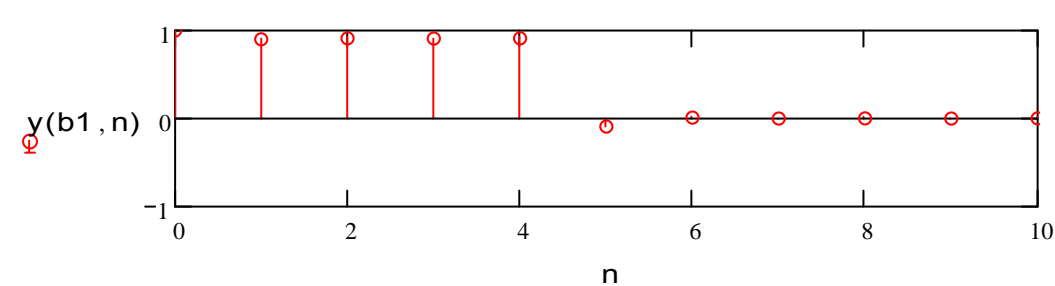


$$\text{one}(n, n_i) := \begin{cases} 1 & \text{if } n \geq n_i \\ 0 & \text{otherwise} \end{cases}$$

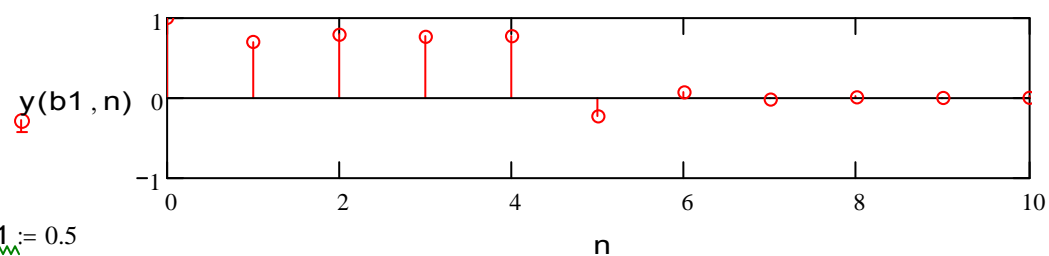

 $n_i := 5 \quad n := 0 \dots 10$

$$y_1(b_1, n) := \frac{1 - (-b_1)^{n+1}}{1 + b_1} \cdot \text{one}(n, 0) \quad y_2(b_1, n) := \frac{1 - (-b_1)^{n-n_i+1}}{1 + b_1} \cdot \text{one}(n, n_i)$$

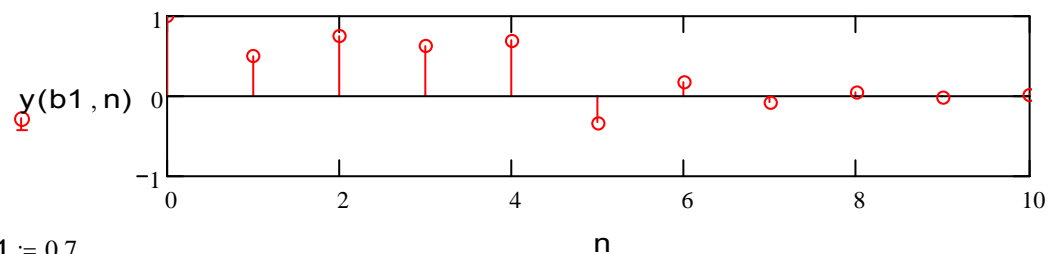
$$y(b_1, n) := y_1(b_1, n) - y_2(b_1, n)$$

 $b_1 := -0.9$

 $b_1 := -0.7$

 $b_1 := -0.5$

 $b_1 := -0.3$

 $b_1 := -0.1$

 $b_1 := 0.1$


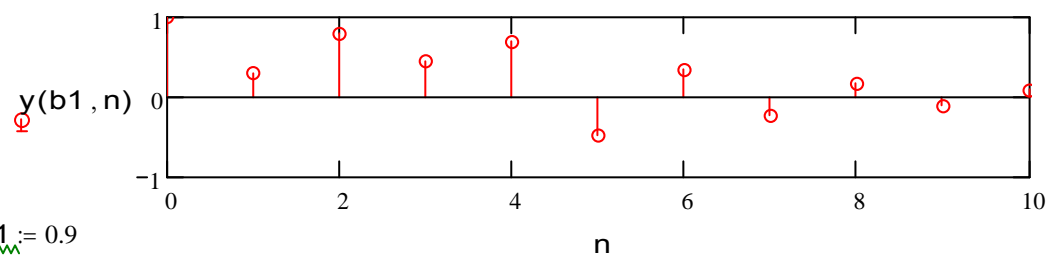
$b1 := 0.3$



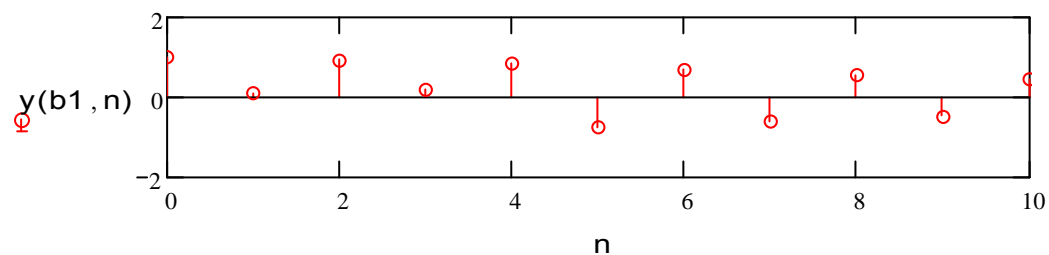
$b1 := 0.5$



$b1 := 0.7$



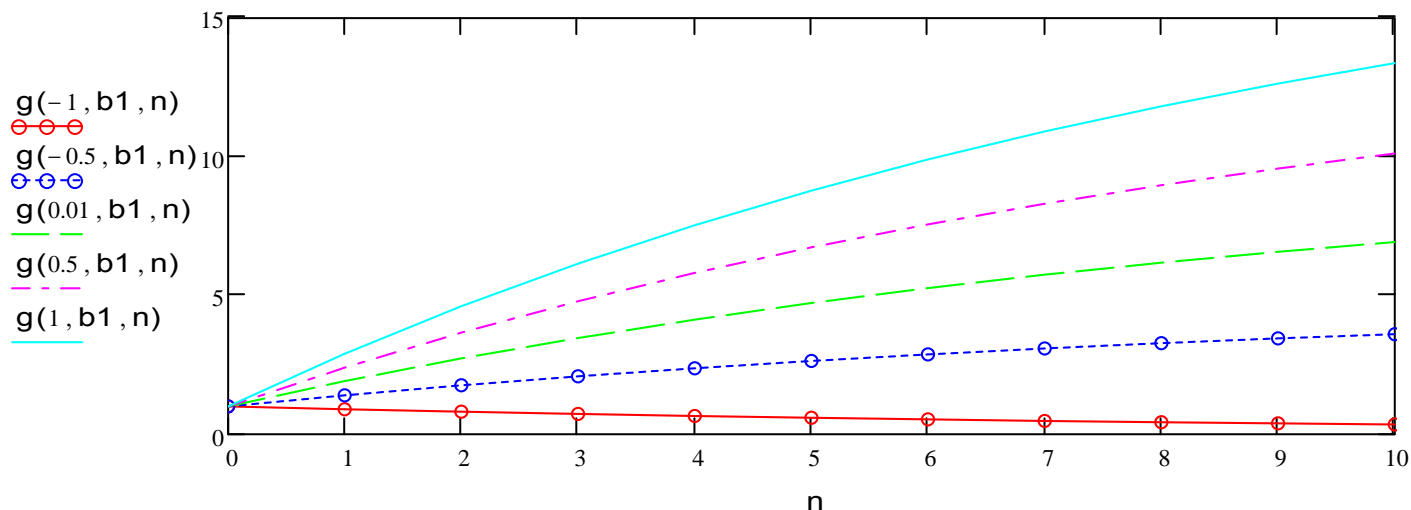
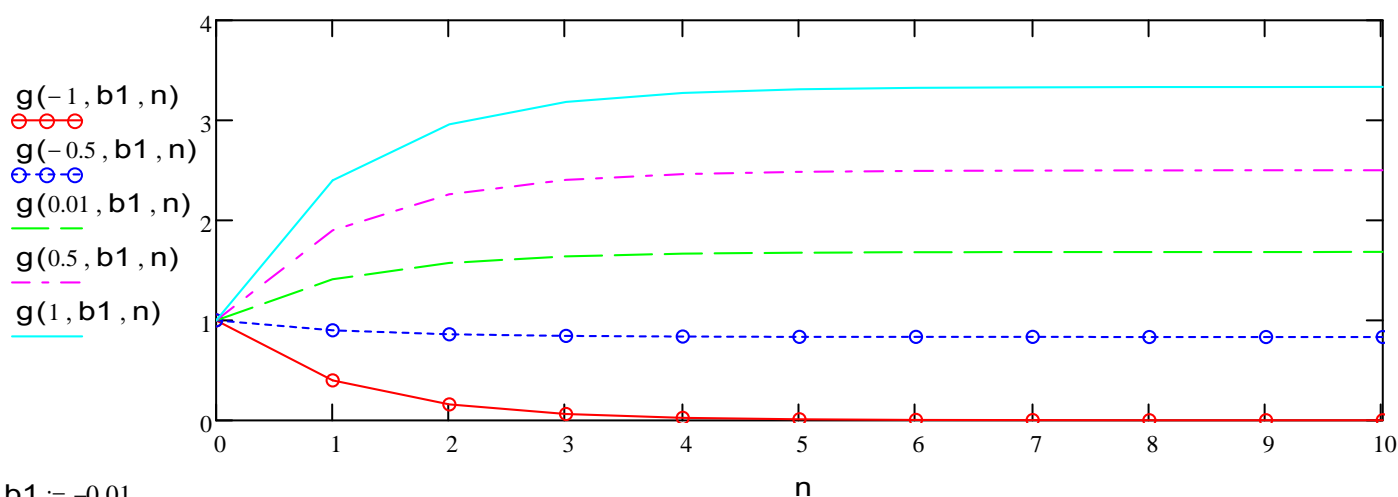
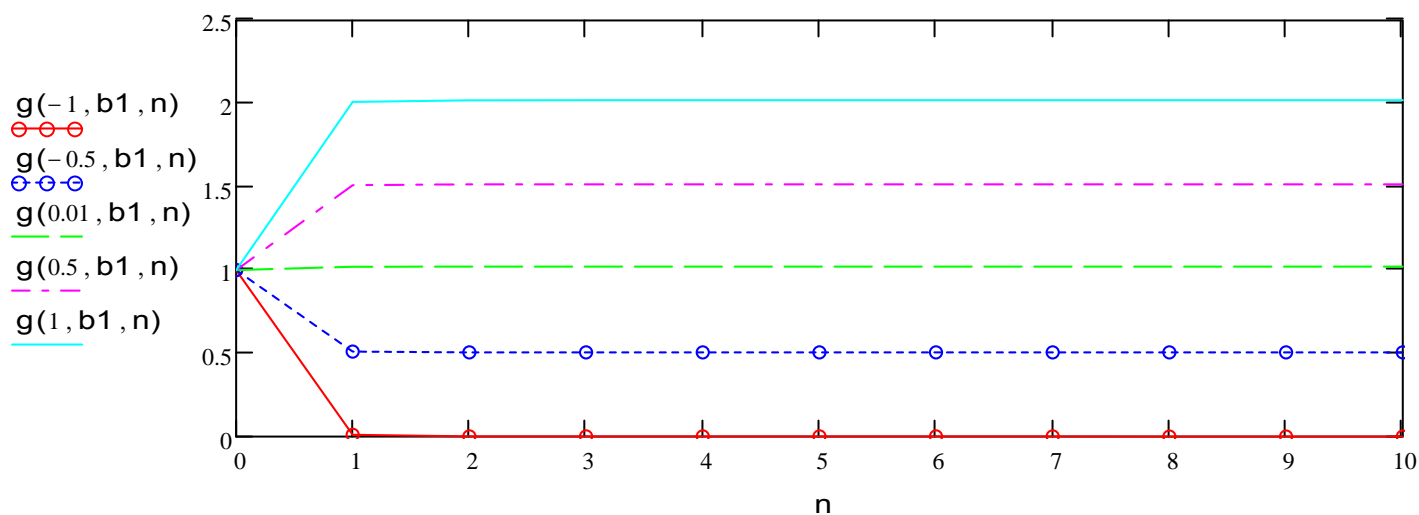
$b1 := 0.9$



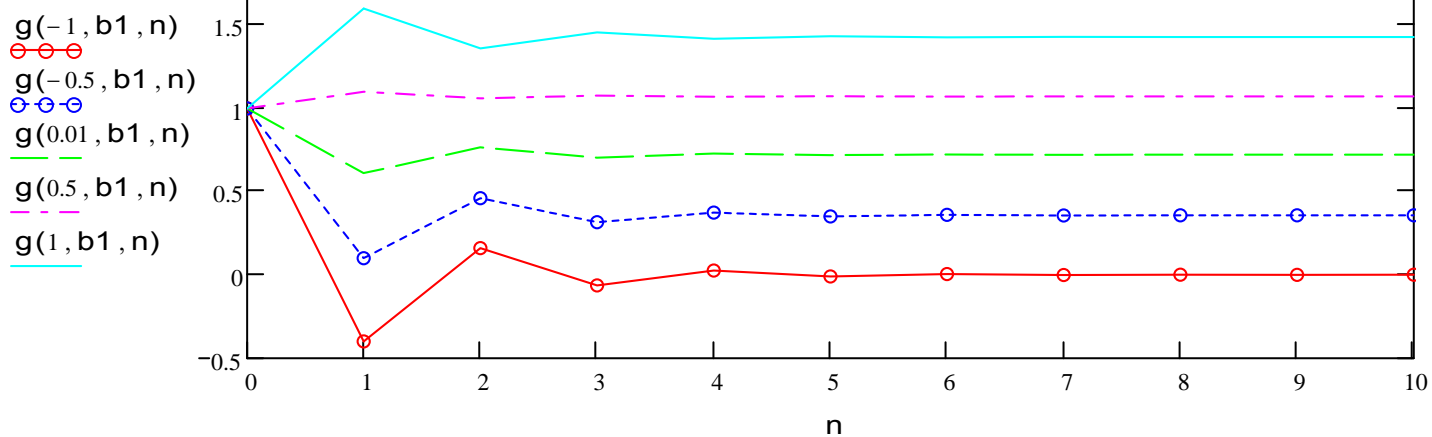
Переходная Характеристика

 $n := 0 \dots 10$

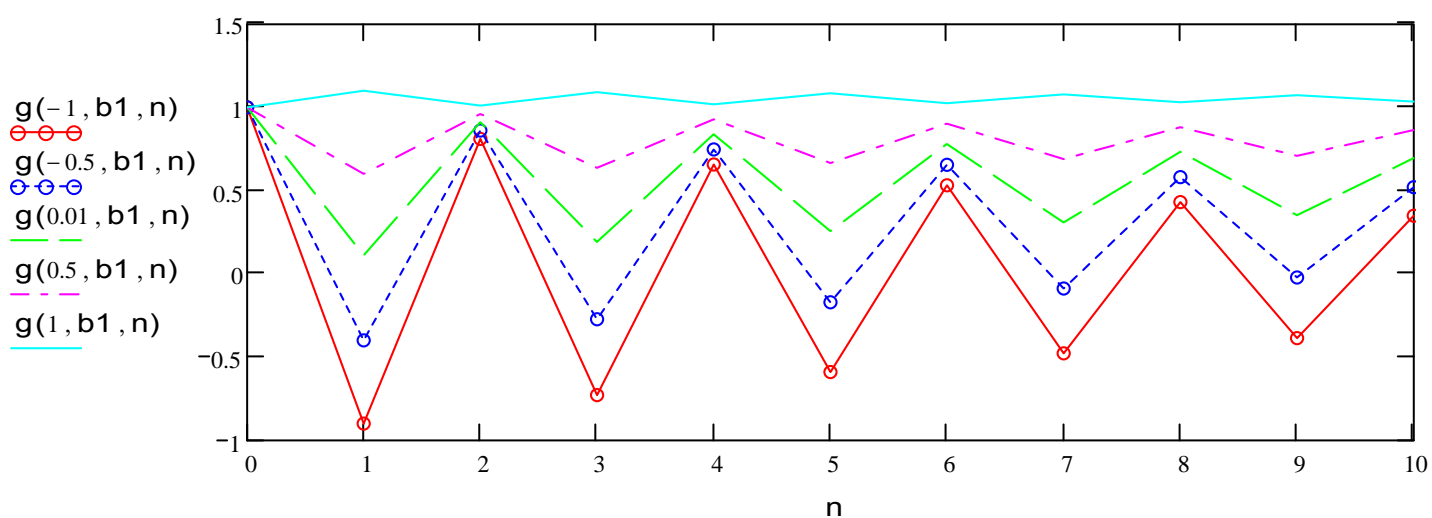
$$g(a1, b1, n) := \frac{1 + a1 - (a1 - b1)(-b1)^n}{1 + b1}$$

 $b1 := -0.9$

 $b1 := -0.4$

 $b1 := -0.01$


$b1 := 0.4$



$b1 := 0.9$



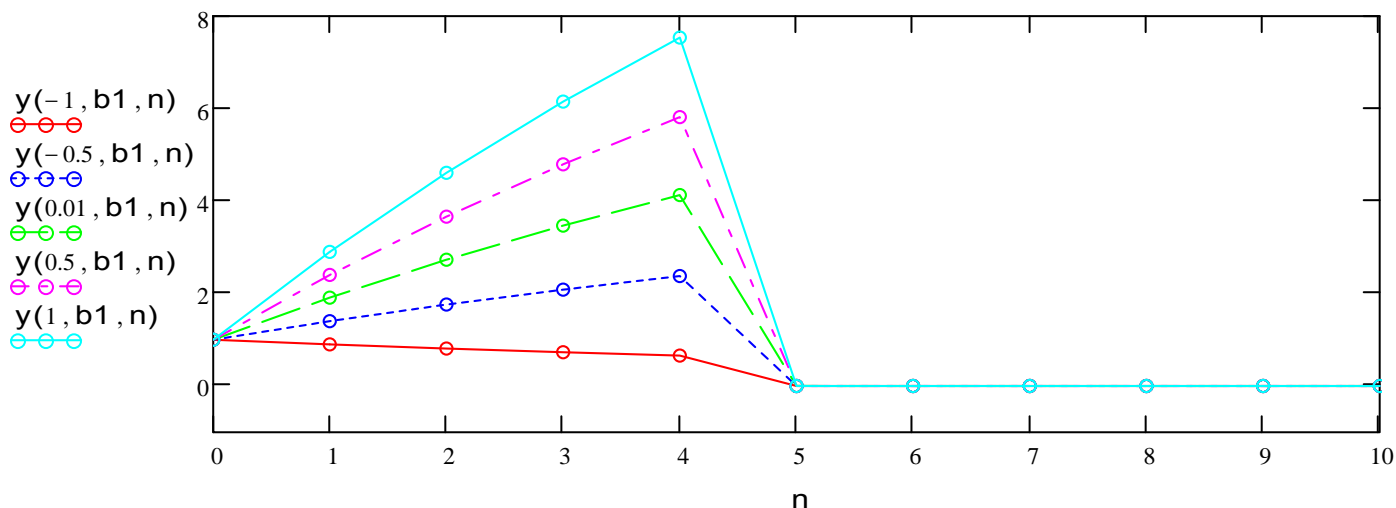
$n_i := 5 \quad n := 0 \dots 10$

$y_1(a_1, b_1, n) := g(a_1, b_1, n) \cdot \text{one}(n, 0)$

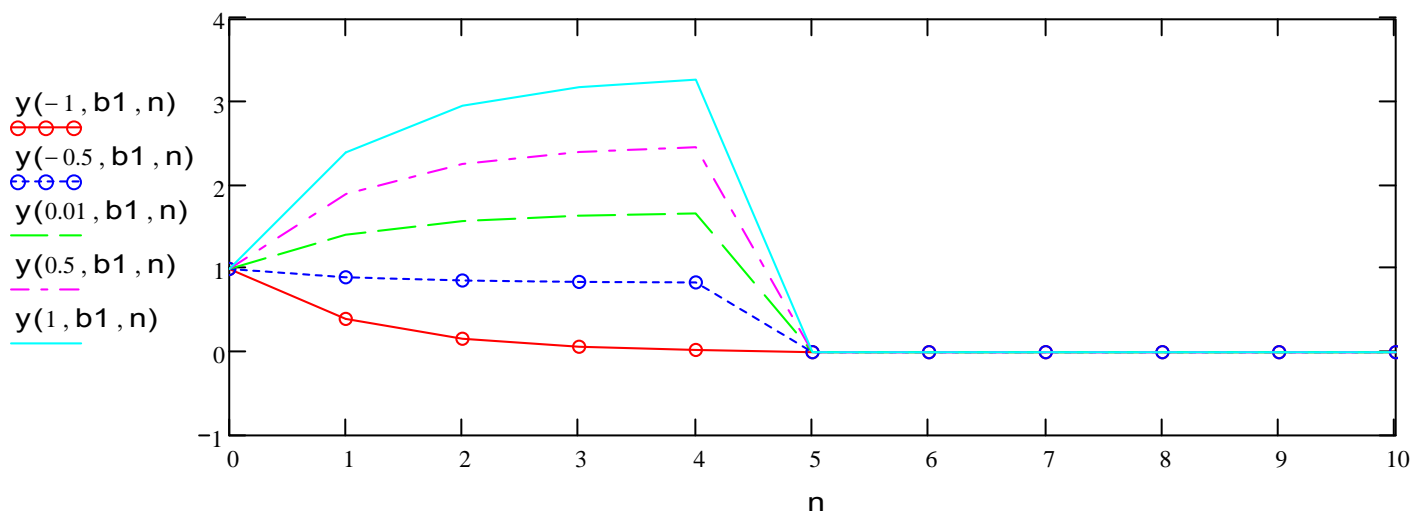
$y_2(a_1, b_1, n) := g(a_1, b_1, n) \cdot \text{one}(n, n_i)$

$y(a_1, b_1, n) := y_1(a_1, b_1, n) - y_2(a_1, b_1, n)$

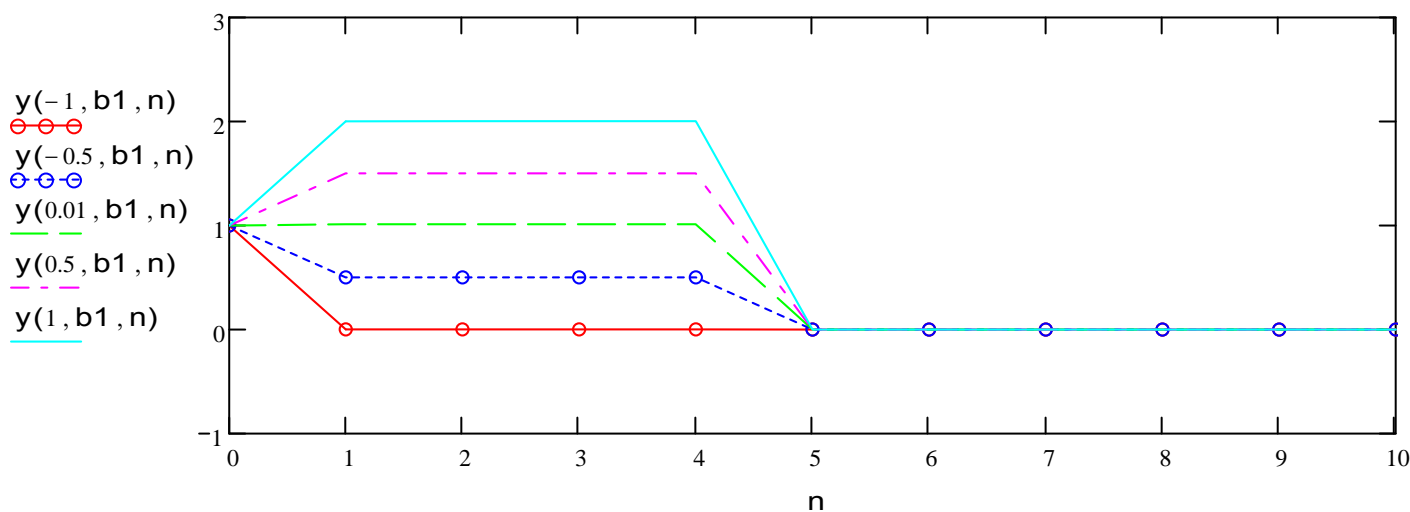
$b_1 := -0.9$



$b_1 := -0.4$

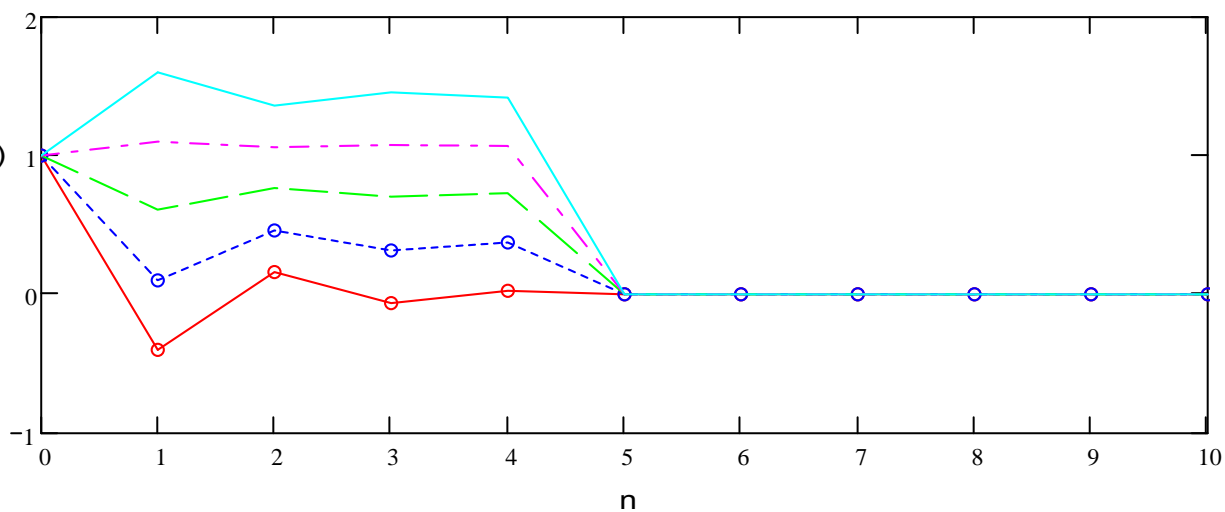


$b_1 := -0.001$



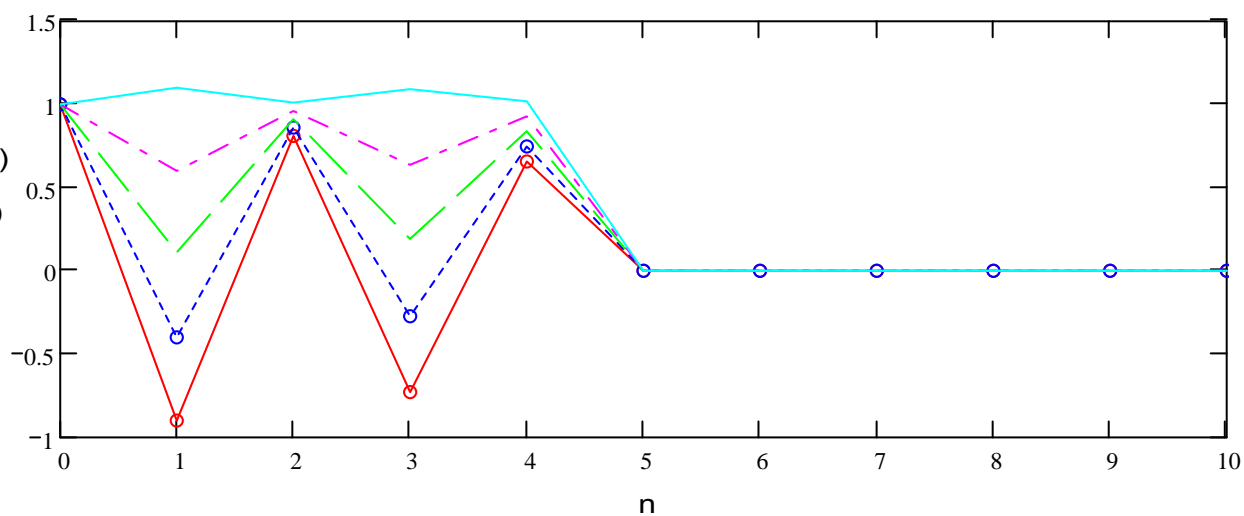
$b1 := 0.4$

$y(-1, b1, n)$
 $y(-0.5, b1, n)$
 $y(0.01, b1, n)$
 $y(0.5, b1, n)$
 $y(1, b1, n)$



$b1 := 0.9$

$y(-1, b1, n)$
 $y(-0.5, b1, n)$
 $y(0.01, b1, n)$
 $y(0.5, b1, n)$
 $y(1, b1, n)$



.78i

