

$$H(\omega, b1, b2) := \frac{b2 + 1 - |b1|}{\sqrt{4 \cdot b2 \cdot \cos(\omega)^2 + [2 \cdot b1 \cdot (1 + b2) \cdot \cos(\omega)] + [b1^2 + (1 - b2) \cdot 2]}}$$

$$A(b1, b2) := 4b2 \quad B(b1, b2) := 2 \cdot b1 \cdot (1 + b2) \quad C(b1, b2) := b1^2 + (1 - b2)^2$$

$$\omega c1(b1, b2) := \arccos \left[ \frac{-B(b1, b2) + \sqrt{B(b1, b2)^2 - 4 \cdot A(b1, b2) \cdot [C(b1, b2) - 2 \cdot [b2 + 1 - (|b1|)^2]]}}{2 \cdot A(b1, b2)} \right]$$

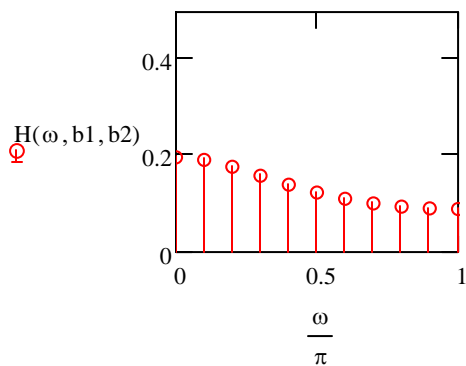
$$\omega c2(b1, b2) := \arccos \left[ \frac{-B(b1, b2) - \sqrt{B(b1, b2)^2 - 4 \cdot A(b1, b2) \cdot [C(b1, b2) - 2 \cdot [b2 + 1 - (|b1|)^2]]}}{2 \cdot A(b1, b2)} \right]$$

$$\phi(\omega, b1, b2) := \operatorname{atan} \left( \frac{b1 \cdot \sin(\omega) + b2 \cdot \sin(2\omega)}{1 + b1 \cdot \cos(\omega) + b2 \cdot \cos(2\omega)} \right)$$

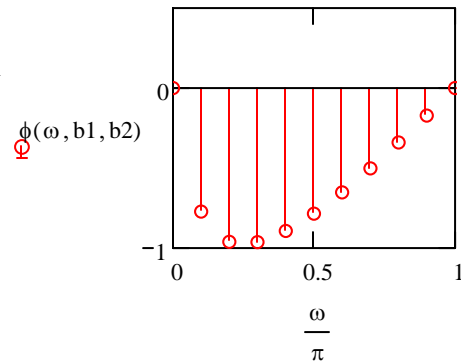
$$\omega := 0, 0.1\pi \dots \pi$$

## ФНЧ

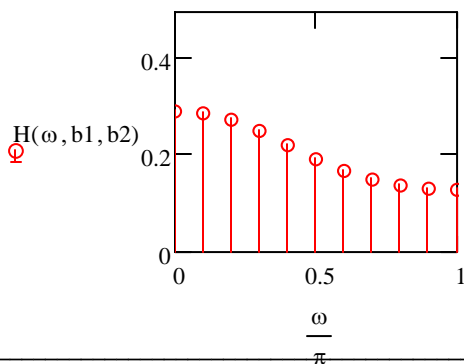
$$b1 := -0.5 \quad b2 := 0.1$$



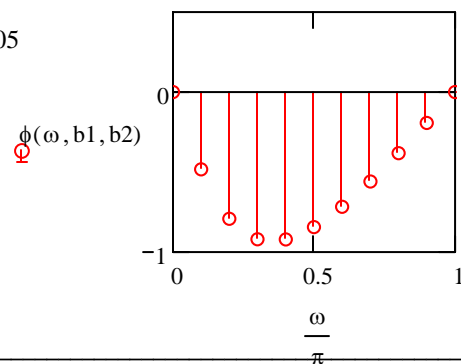
$$\omega c2(b1, b2) = 0.931$$



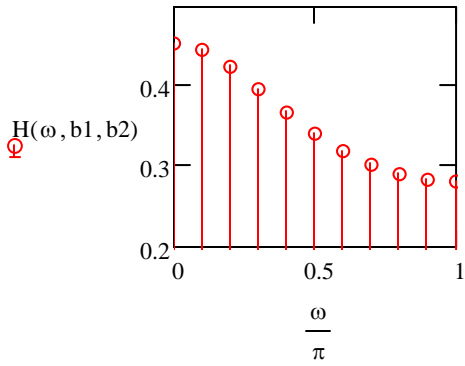
$$b1 := -0.5 \quad b2 := 0.2$$



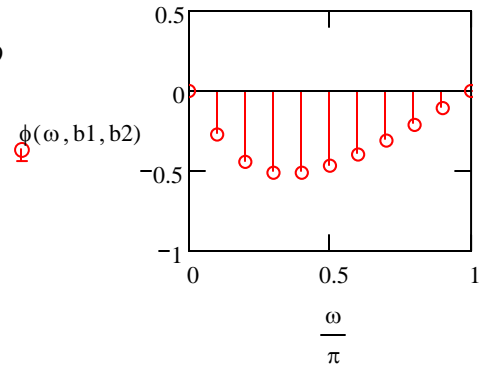
$$\omega c2(b1, b2) = 1.205$$



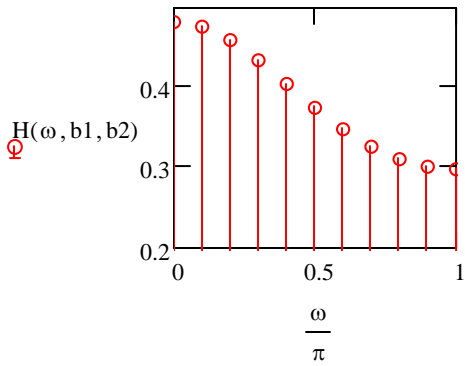
$\underline{b1} := -0.5 \quad \underline{b2} := 0.01$



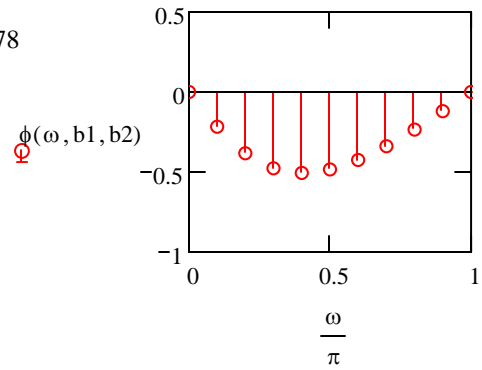
$\omega c2(b1, b2) = 1.859$



$\underline{b1} := -0.5 \quad \underline{b2} := 0.05$

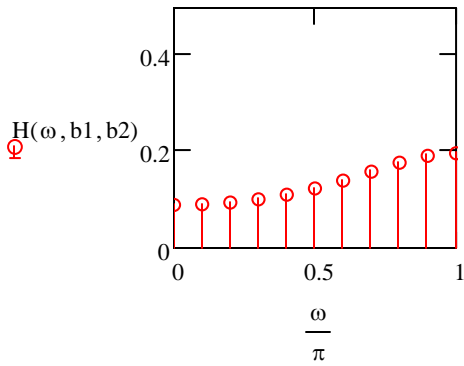


$\omega c2(b1, b2) = 1.978$

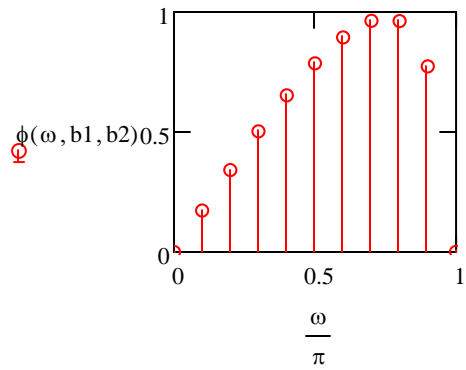


**ΦB4**

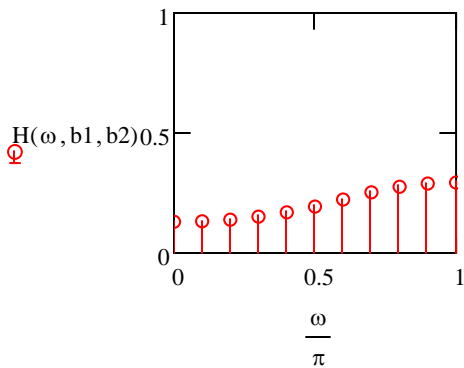
$\underline{b1} := 0.9 \quad \underline{b2} := 0.1$



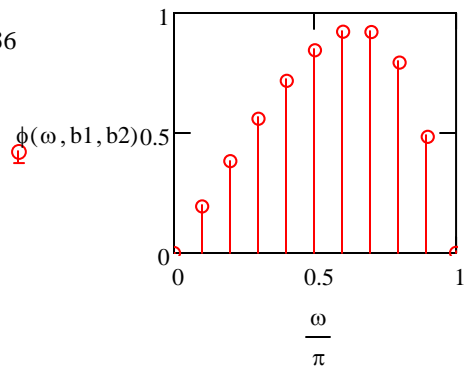
$\omega c1(b1, b2) = 2.211$



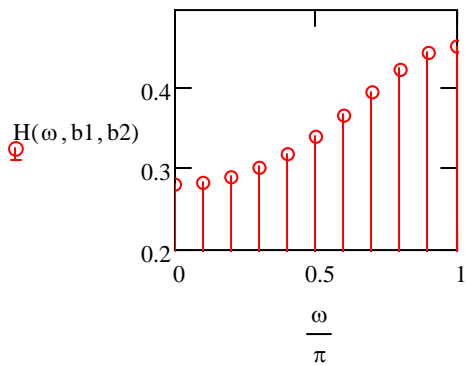
$\underline{b1} := 0.9 \quad \underline{b2} := 0.2$



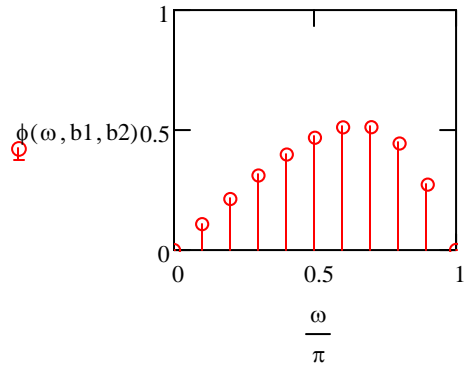
$\omega c1(b1, b2) = 1.936$



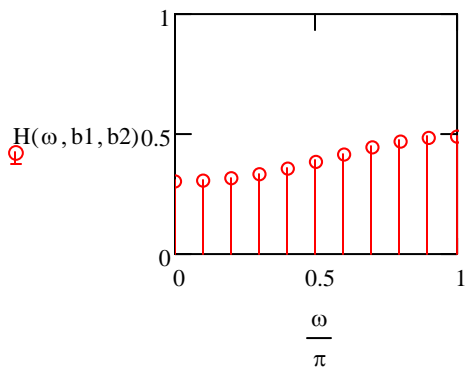
$$\underline{b1} := 0.5 \quad \underline{b2} := 0.01$$



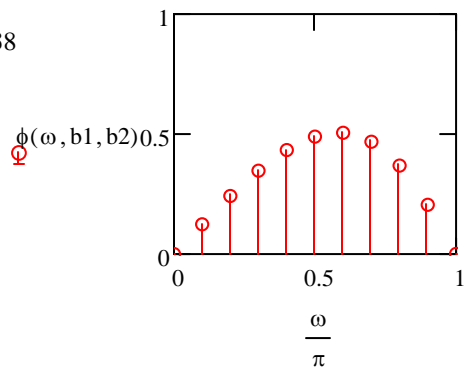
$$\omega c1(b1, b2) = 1.283$$



$$\underline{b1} := 0.5 \quad \underline{b2} := 0.06$$



$$\omega c1(b1, b2) = 1.138$$



### Полосовой Фильтр

$$wr(b1, b2) := \arccos \left[ \frac{-b1 \cdot (1 + b2)}{4b2} \right]$$

$$a1(b1, b2) := \frac{-B(b1, b2) + \sqrt{-B(b1, b2)^2 + 4 A(b1, b2) \cdot C(b1, b2)}}{2 A(b1, b2)}$$

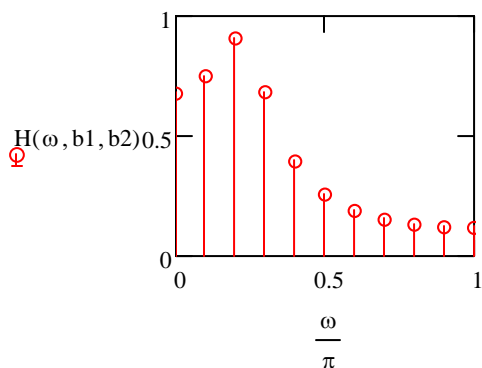
$$a2(b1, b2) := \frac{-B(b1, b2) - \sqrt{-B(b1, b2)^2 + 4 A(b1, b2) \cdot C(b1, b2)}}{2 \cdot A(b1, b2)}$$

$$Q(b1, b2) := \frac{wr(b1, b2)}{\arccos(a2(b1, b2)) - \arccos(a1(b1, b2))}$$

$$w1(b1, b2) := \arccos(a1(b1, b2))$$

$$w2(b1, b2) := \arccos(a2(b1, b2))$$

$$\underline{b2} := 0.9 \quad \underline{b1} := -1.5$$

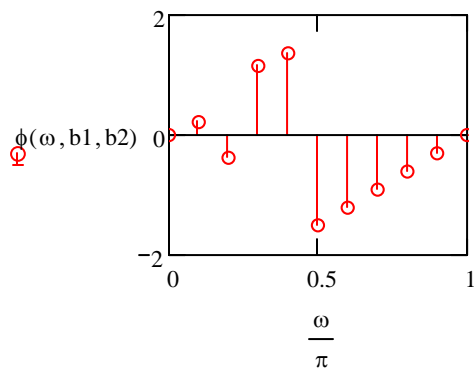


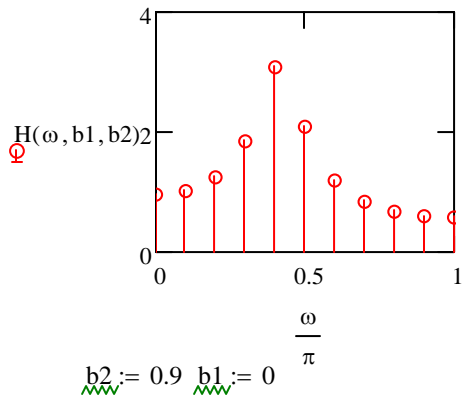
$$wr(b1, b2) = 0.657$$

$$w2(b1, b2) = 0.708$$

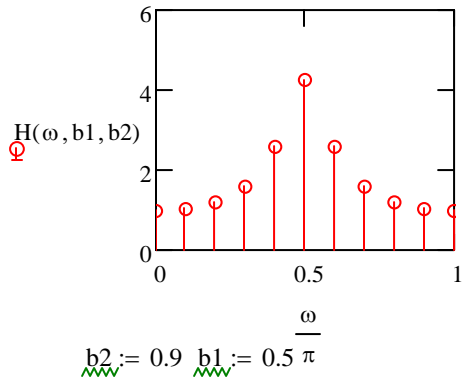
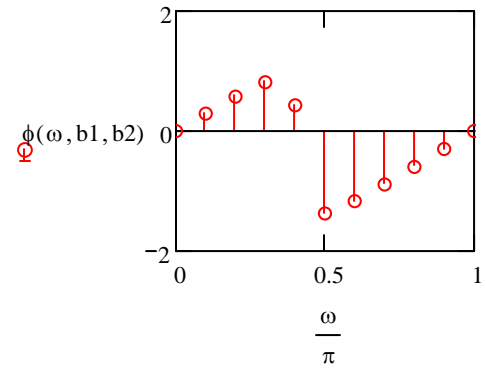
$$w1(b1, b2) = 0.602$$

$$Q(b1, b2) = 6.203$$

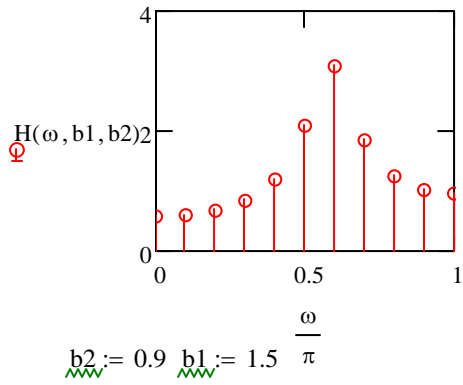
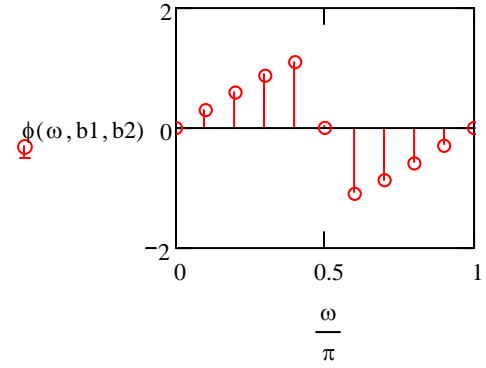




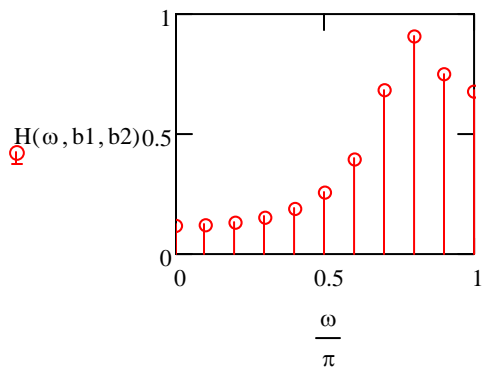
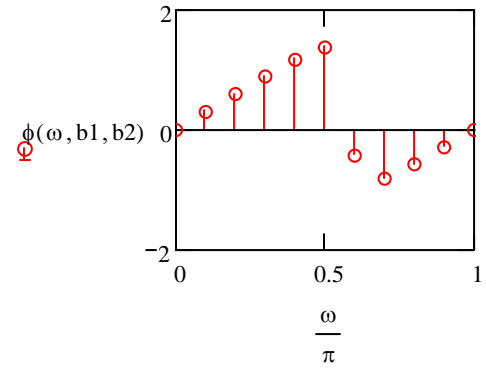
$$\begin{aligned} wr(b1, b2) &= 1.304 \\ w2(b1, b2) &= 1.356 \\ w1(b1, b2) &= 1.251 \\ Q(b1, b2) &= 12.36 \end{aligned}$$



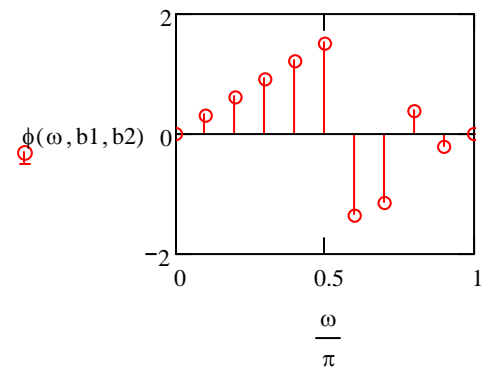
$$\begin{aligned} wr(b1, b2) &= 1.571 \\ w2(b1, b2) &= 1.624 \\ w1(b1, b2) &= 1.518 \\ Q(b1, b2) &= 14.895 \end{aligned}$$

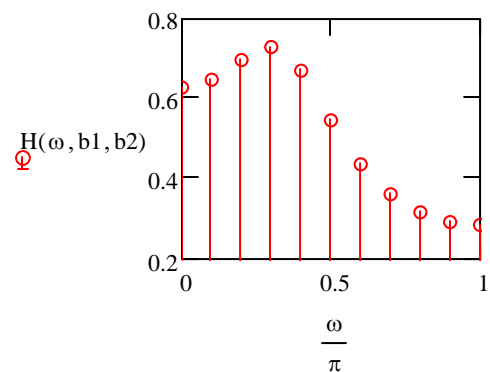


$$\begin{aligned} wr(b1, b2) &= 1.838 \\ w2(b1, b2) &= 1.891 \\ w1(b1, b2) &= 1.785 \\ Q(b1, b2) &= 17.424 \end{aligned}$$



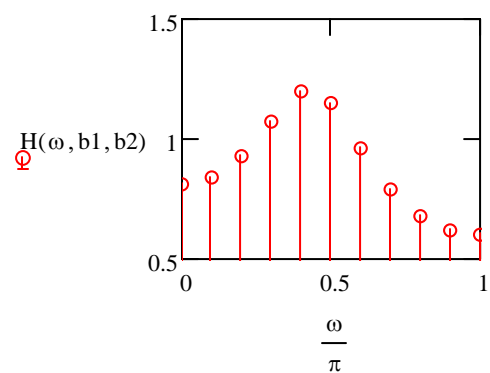
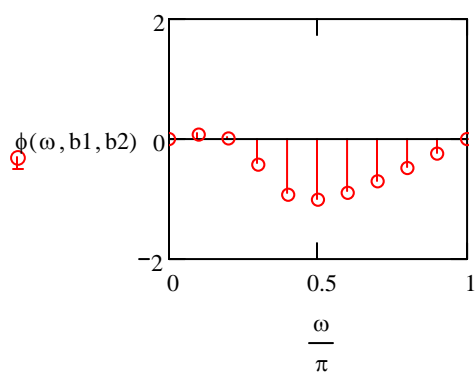
$$\begin{aligned} wr(b1, b2) &= 2.484 \\ w2(b1, b2) &= 2.539 \\ w1(b1, b2) &= 2.433 \\ Q(b1, b2) &= 23.447 \end{aligned}$$





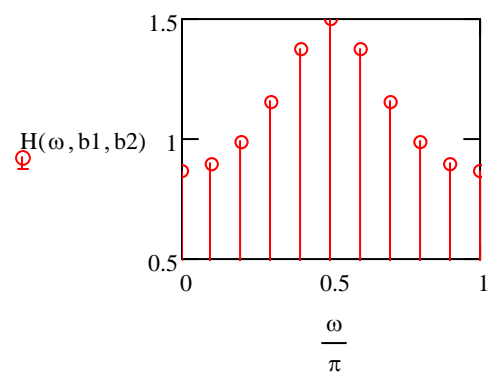
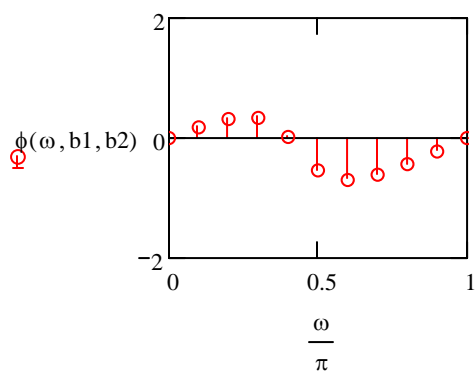
$b2 := 0.5$   $b1 := -0.3$

$wr(b1, b2) = 0.927$   
 $w2(b1, b2) = 1.257$   
 $w1(b1, b2) = 0.47$   
 $Q(b1, b2) = 1.178$



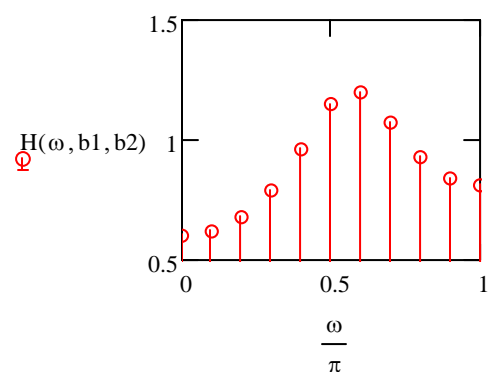
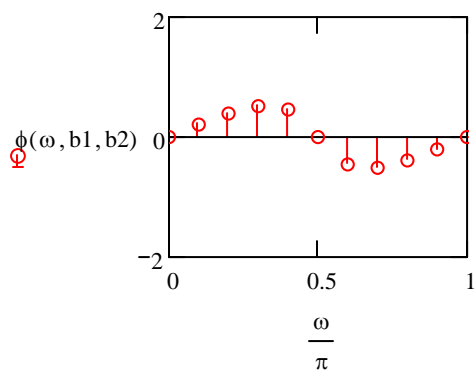
$b2 := 0.5$   $b1 := 0$

$wr(b1, b2) = 1.344$   
 $w2(b1, b2) = 1.692$   
 $w1(b1, b2) = 0.964$   
 $Q(b1, b2) = 1.846$



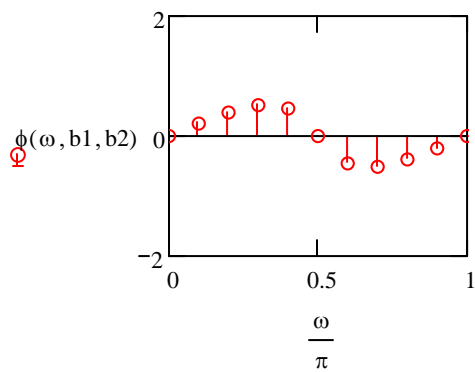
$b2 := 0.5$   $b1 := 0.3$

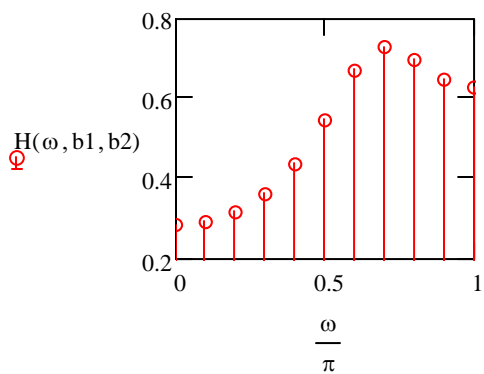
$wr(b1, b2) = 1.571$   
 $w2(b1, b2) = 1.932$   
 $w1(b1, b2) = 1.209$   
 $Q(b1, b2) = 2.173$



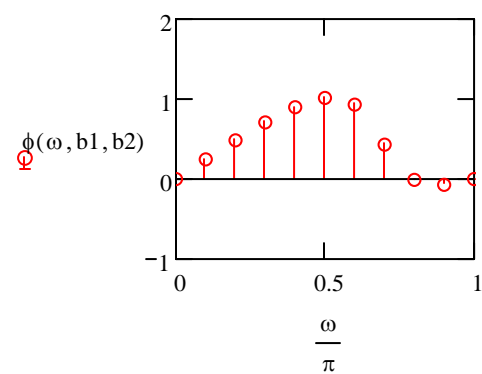
$b2 := 0.5$   $b1 := 0.8$

$wr(b1, b2) = 1.798$   
 $w2(b1, b2) = 2.178$   
 $w1(b1, b2) = 1.45$   
 $Q(b1, b2) = 2.47$

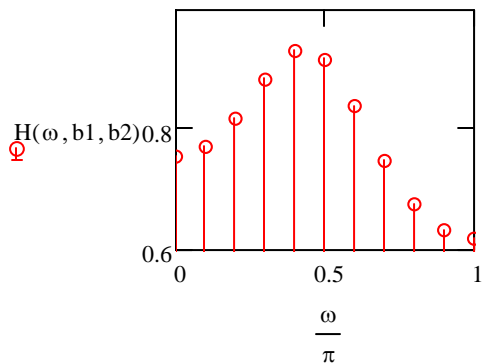




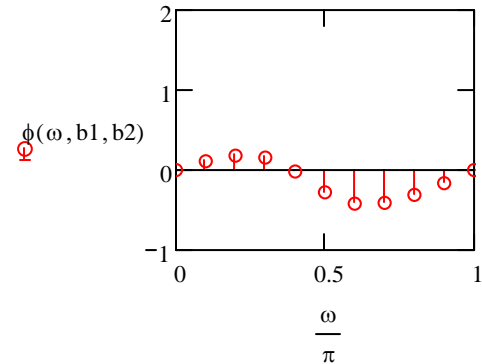
$$\begin{aligned} wr(b1, b2) &= 2.214 \\ w2(b1, b2) &= 2.672 \\ w1(b1, b2) &= 1.884 \\ Q(b1, b2) &= 2.813 \end{aligned}$$



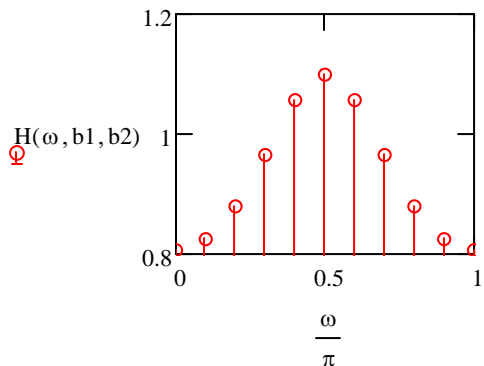
$b2 := 0.3 \quad b1 := -0.2$



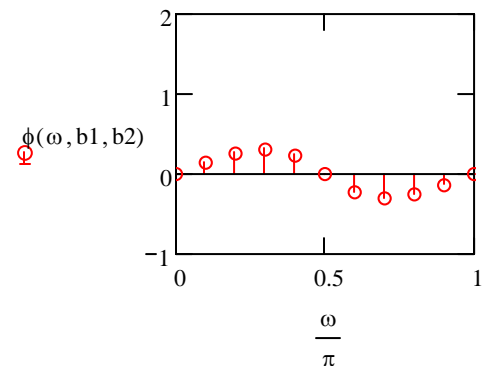
$$\begin{aligned} wr(b1, b2) &= 1.352 \\ w2(b1, b2) &= 1.995 \\ w1(b1, b2) &= 0.564 \\ Q(b1, b2) &= 0.945 \end{aligned}$$



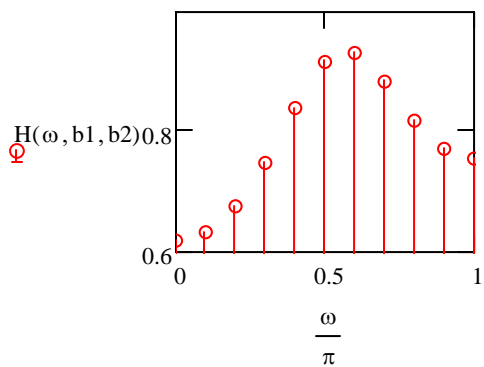
$b2 := 0.3 \quad b1 := 0$



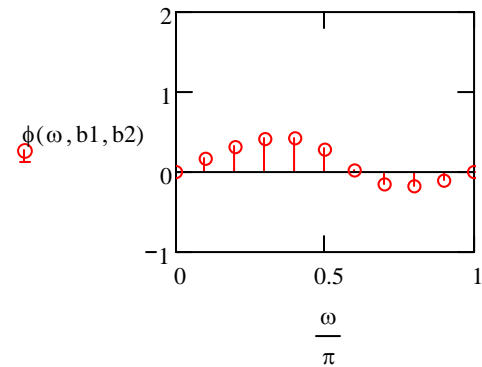
$$\begin{aligned} wr(b1, b2) &= 1.571 \\ w2(b1, b2) &= 2.264 \\ w1(b1, b2) &= 0.878 \\ Q(b1, b2) &= 1.133 \end{aligned}$$



$b2 := 0.3 \quad b1 := 0.2$



$$\begin{aligned} wr(b1, b2) &= 1.789 \\ w2(b1, b2) &= 2.577 \\ w1(b1, b2) &= 1.147 \\ Q(b1, b2) &= 1.251 \end{aligned}$$



$$a1(b1, b2) := \frac{-B(b1, b2) + \sqrt{\frac{B(b1, b2)^2 - 4 \cdot A(b1, b2) \cdot C(b1, b2)}{2}}}{2 \cdot A(b1, b2)}$$

$$wr(b1, b2) := \arccos\left[\frac{-b1 \cdot (1 + b2)}{4b2}\right]$$

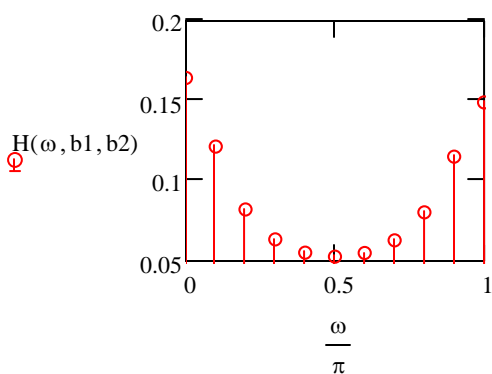
$$a2(b1, b2) := \frac{-B(b1, b2) - \sqrt{\frac{B(b1, b2)^2 - 4 \cdot A(b1, b2) \cdot C(b1, b2)}{2}}}{2 \cdot A(b1, b2)}$$

$$w1(b1, b2) := \arccos(a1(b1, b2))$$

$$Q(b1, b2) := \frac{wr(b1, b2)}{\arccos(a2(b1, b2)) - \arccos(a1(b1, b2))}$$

$$w2(b1, b2) := \arccos(a2(b1, b2))$$

$$b2 := -0.8b1 := -0.1$$

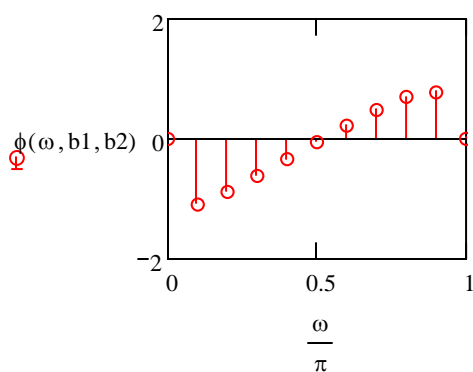


$$wr(b1, b2) = 1.577$$

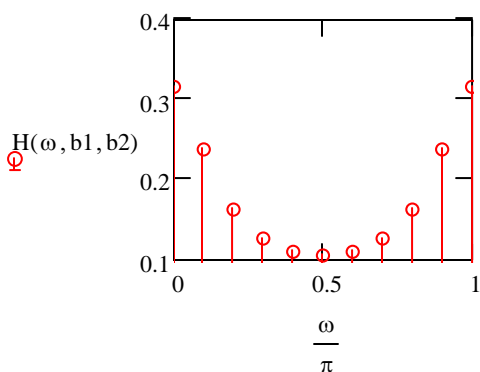
$$w2(b1, b2) = 0.786$$

$$w1(b1, b2) = 2.373$$

$$Q(b1, b2) = -0.994$$



$$b2 := -0.8b1 := 0$$

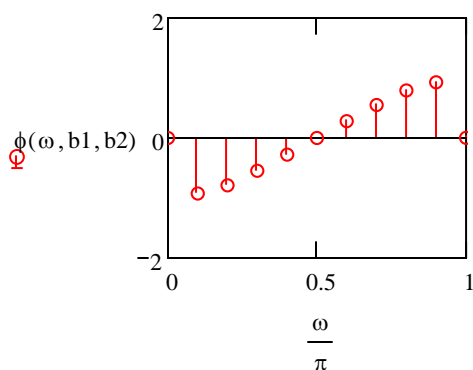


$$wr(b1, b2) = 1.571$$

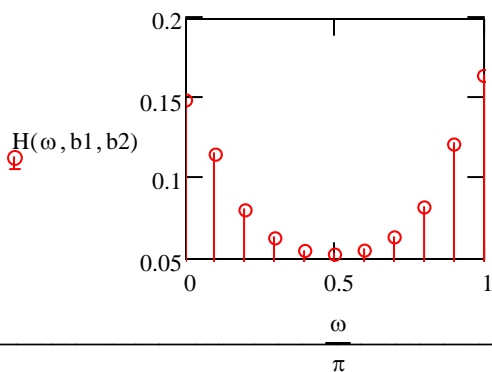
$$w2(b1, b2) = 0.779$$

$$w1(b1, b2) = 2.362$$

$$Q(b1, b2) = -0.992$$



$$b2 := -0.8b1 := 0.1$$

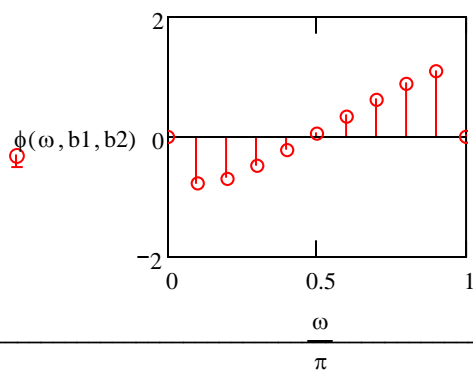


$$wr(b1, b2) = 1.565$$

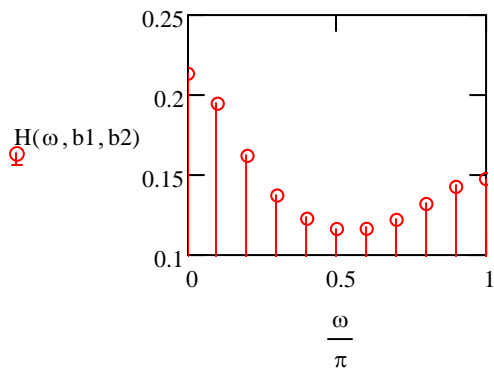
$$w2(b1, b2) = 0.769$$

$$w1(b1, b2) = 2.355$$

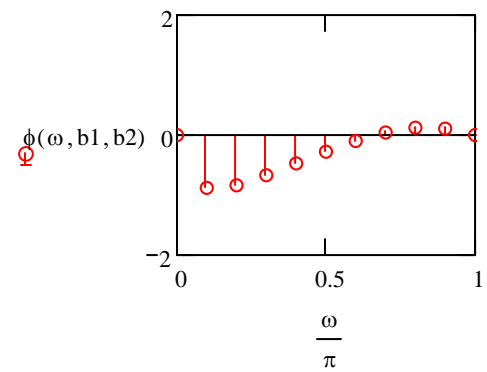
$$Q(b1, b2) = -0.986$$



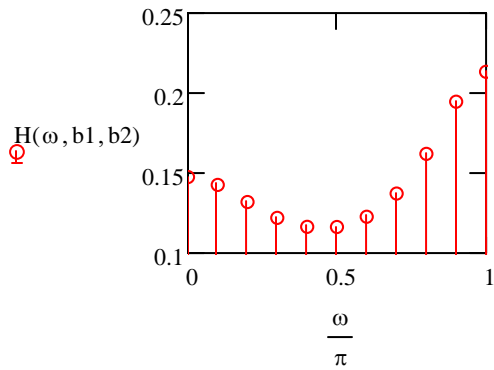
$$b1 := -0.4 \quad b2 := -0.4$$



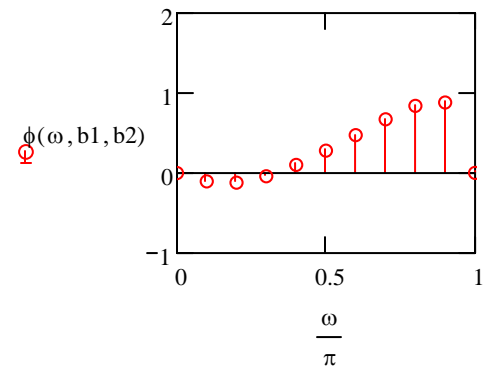
$$\begin{aligned} wr(b1, b2) &= 1.721 \\ w2(b1, b2) &= 0.835 \\ w1(b1, b2) &= 2.899 \\ Q(b1, b2) &= -0.834 \end{aligned}$$



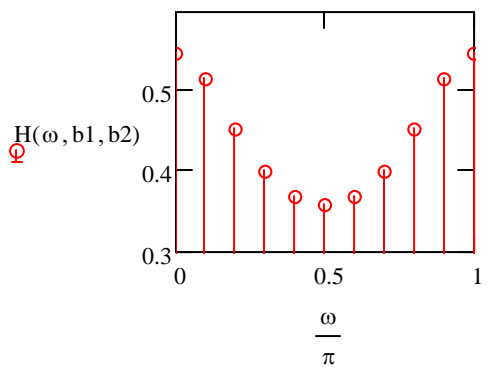
$b1 := 0.4$   $b2 := -0.4$



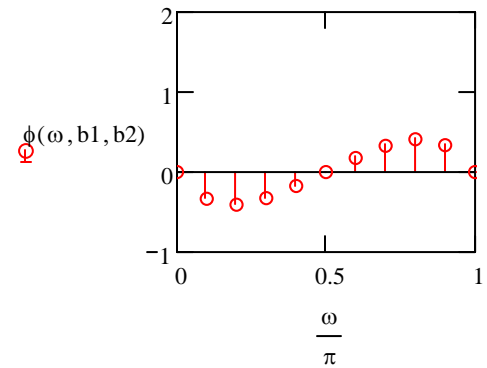
$$\begin{aligned} wr(b1, b2) &= 1.42 \\ w2(b1, b2) &= 0.242 \\ w1(b1, b2) &= 2.306 \\ Q(b1, b2) &= -0.688 \end{aligned}$$



$b1 := 0$   $b2 := -0.4$

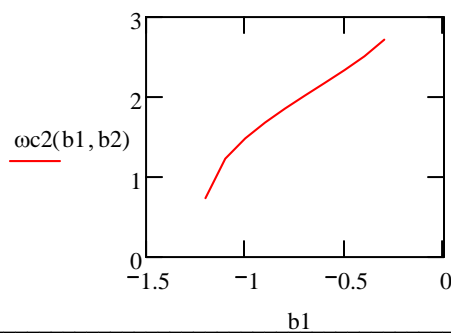
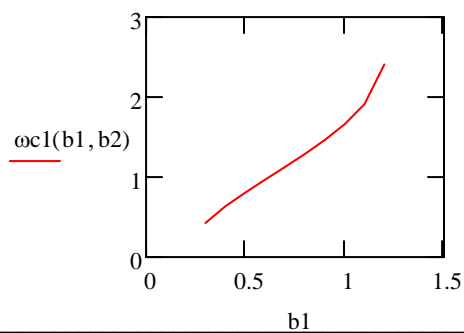


$$\begin{aligned} wr(b1, b2) &= 1.571 \\ w2(b1, b2) &= 0.672 \\ w1(b1, b2) &= 2.47 \\ Q(b1, b2) &= -0.874 \end{aligned}$$



### Графики зависимостей $\omega c$ от $b1$ и $b2$ для ФНЧ и ФВЧ

$b1 := -2, -1.9 \dots 2$   $b2 := 0.5$



$b2 := -1, -0.9 \dots 1$   $b1 := 0.2$



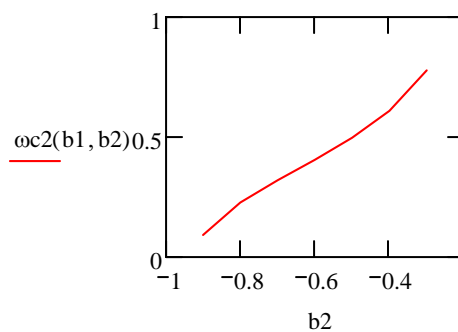
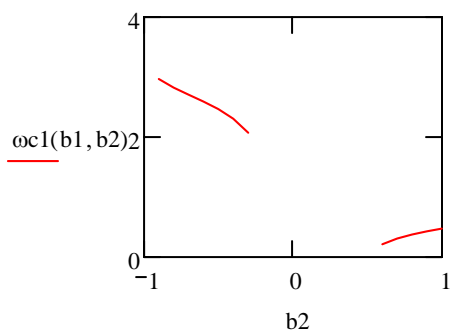
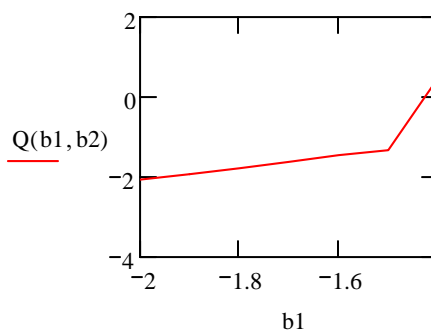
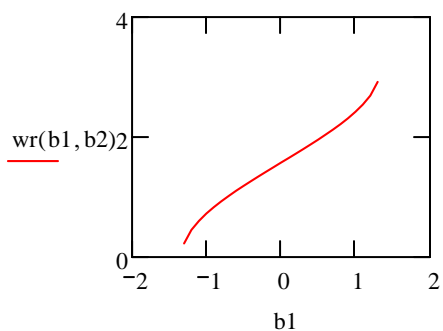
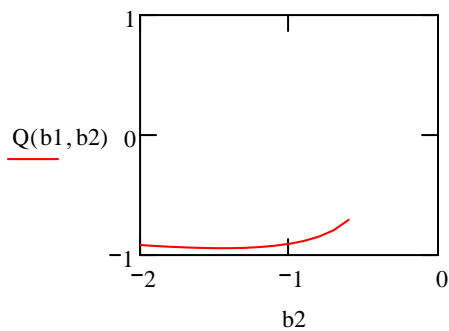
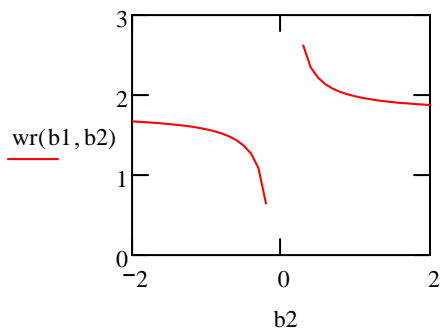


График зависимостей  $\omega p(b1)$  и  $\omega p(b2)$ ,  $Q(b1)$  и  $Q(b2)$  для ПФ

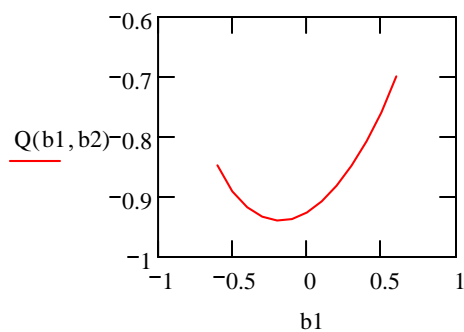
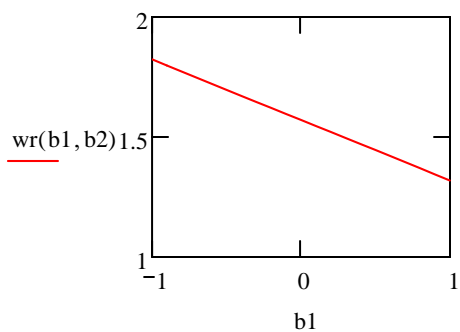
$b1 := -2, -1.9 \dots 2$   $b2 := 0.5$



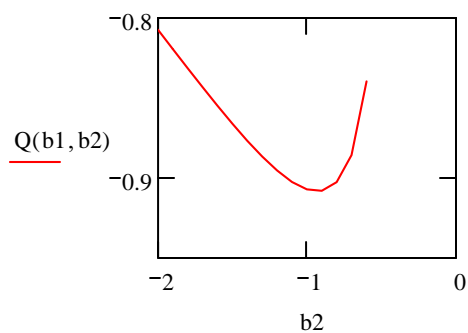
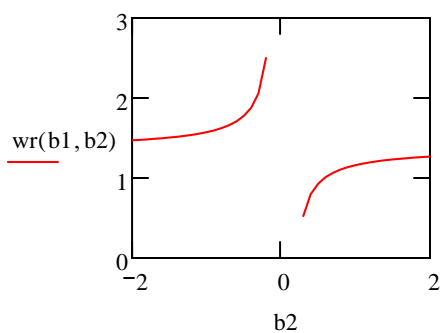
$b2 := -2, -1.9 \dots 2$   $b1 := 0.8$



www  $b1 := -1, -0.9 \dots 1$        $b2 := -0.5$



www  $b2 := -2, -1.9 \dots 2$        $b1 := -0.8$



### Временные характеристики

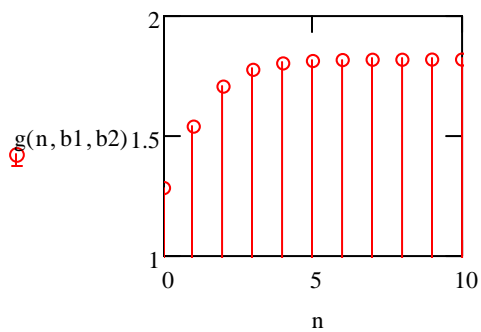
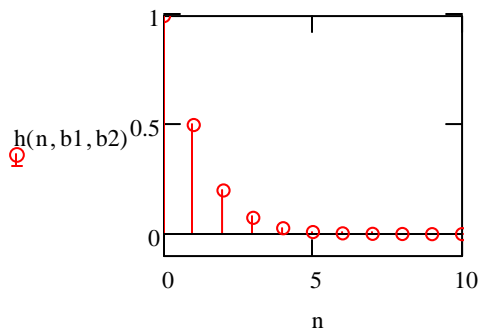
$$p2(b1, b2) := \left( \sqrt{\frac{b1^2 - 4 \cdot b2}{4}} + \frac{-b1}{2} \right)$$

$$p1(b1, b2) := \left( -\sqrt{\frac{b1^2 - 4 \cdot b2}{4}} + \frac{-b1}{2} \right)$$

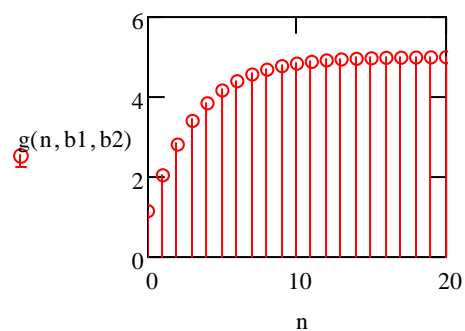
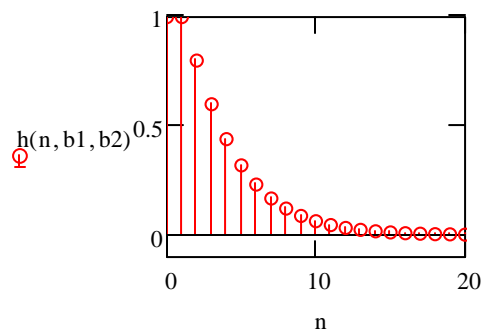
$n := 0, 1 \dots 10$        $\omega0 := 1$

$$h(n, b1, b2) := \frac{p1(b1, b2)^{n+1} - p2(b1, b2)^{n+1}}{p1(b1, b2) - p2(b1, b2)}$$

$$\text{www } g(n, b1, b2) := \frac{1}{1 + b1 + b2} + \frac{1 \cdot \left( \frac{p1(b1, b2)^{n+2}}{p1(b1, b2) - p2(b1, b2)} - \frac{p2(b1, b2)^{n+2}}{p2(b1, b2) - 1} \right)}{p1(b1, b2) - p2(b1, b2)}$$



$n := 0, 1 \dots 20$       $b1 := -1$     $b2 := 0.2$

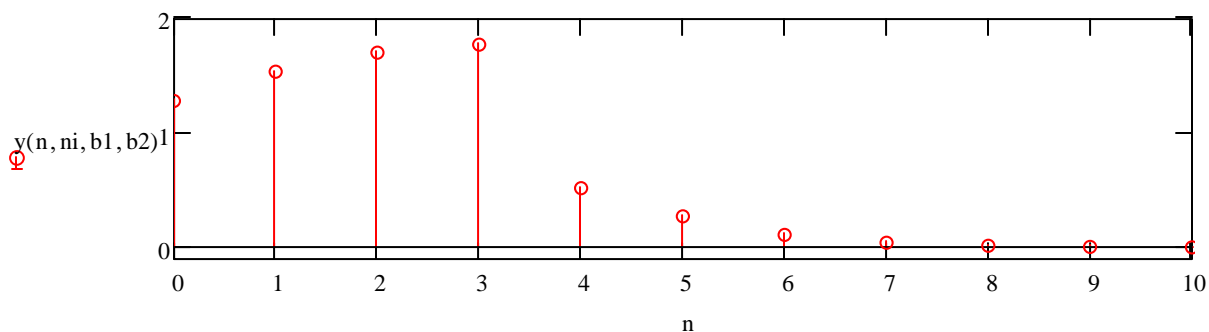


Воздействие прямоугольного импульса

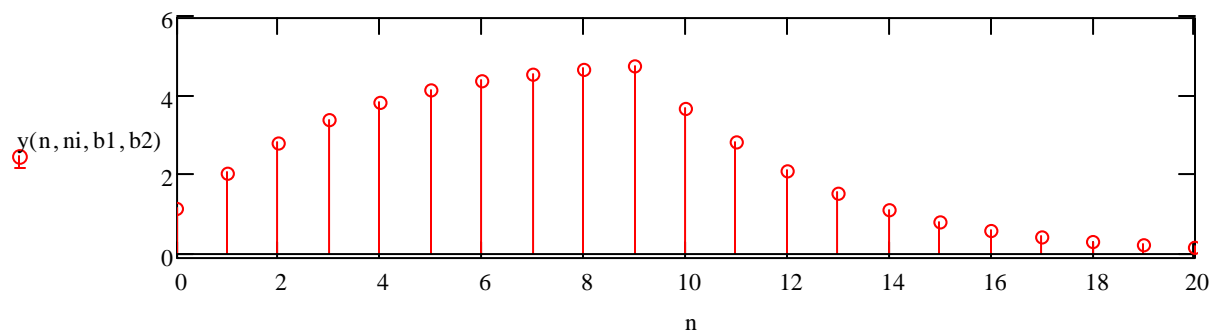
$$l(n) := \begin{cases} 1 & \text{if } n \geq 0 \\ 0 & \text{otherwise} \end{cases}$$

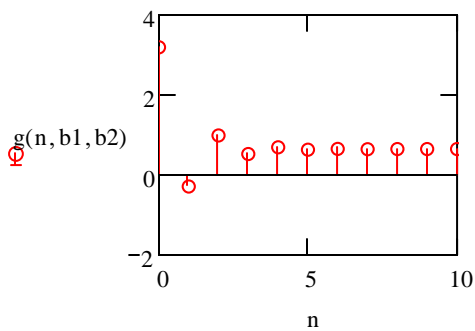
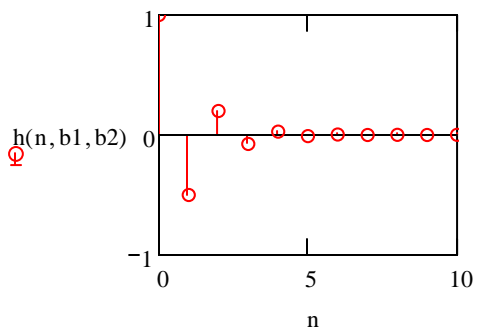
$$y(n, ni, b1, b2) := g(n, b1, b2) \cdot l(n) - g(n - ni, b1, b2) \cdot l(n - ni)$$

$n := 0, 1 \dots 10$       $b1 := -0.5$     $b2 := 0.05$     $ni := 4$

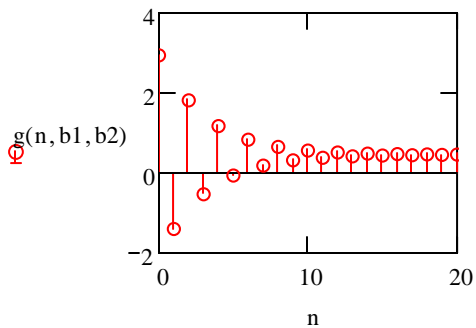
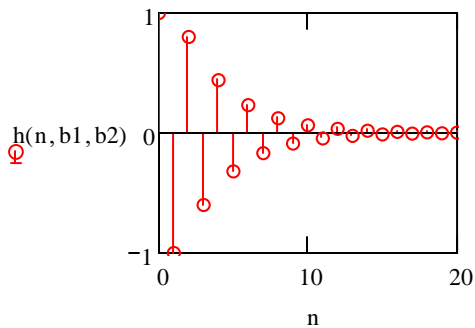


$n := 0, 1 \dots 20$       $b1 := -1$     $b2 := 0.2$     $ni := 10$





$n := 0, 1 \dots 20$      $b1 := 1$      $b2 := 0.2$

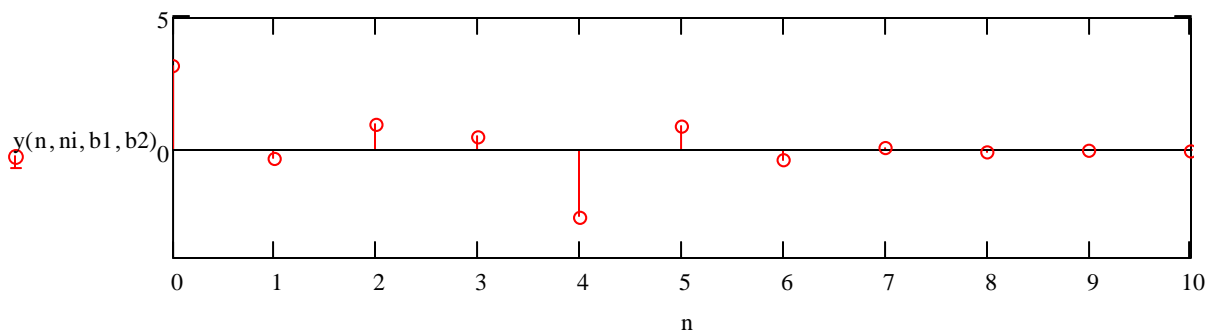


Воздействие прямоугольного импульса

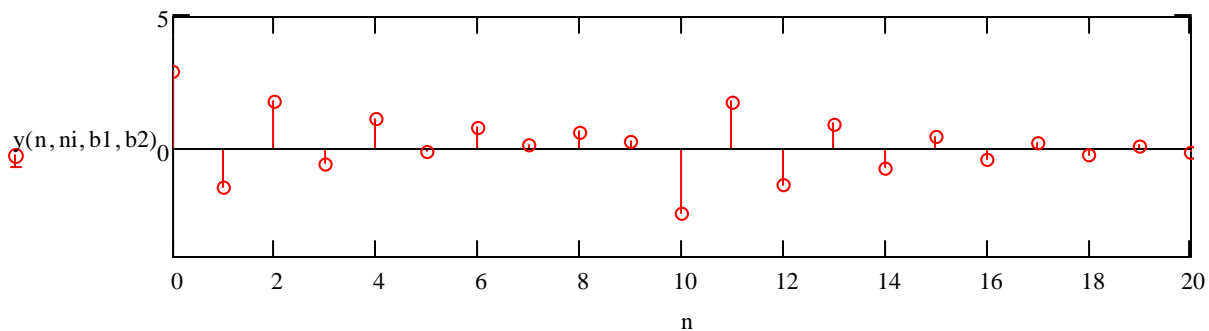
$$l(n) := \begin{cases} 1 & \text{if } n \geq 0 \\ 0 & \text{otherwise} \end{cases}$$

$$y(n, ni, b1, b2) := g(n, b1, b2) \cdot l(n) - g(n - ni, b1, b2) \cdot l(n - ni)$$

$n := 0, 1 \dots 10$      $b1 := 0.5$      $b2 := 0.05$      $ni := 4$

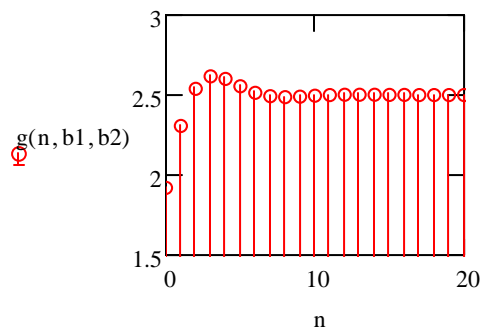
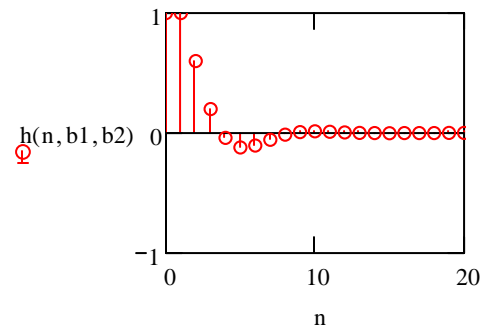


$n := 0, 1 \dots 20$      $b1 := 1$      $b2 := 0.2$      $ni := 10$

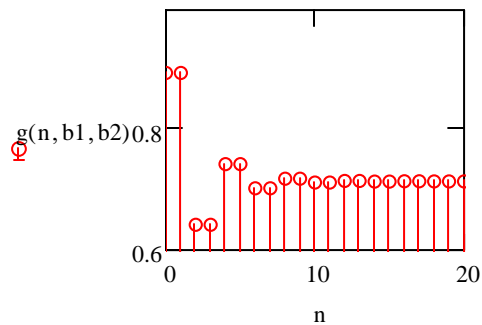
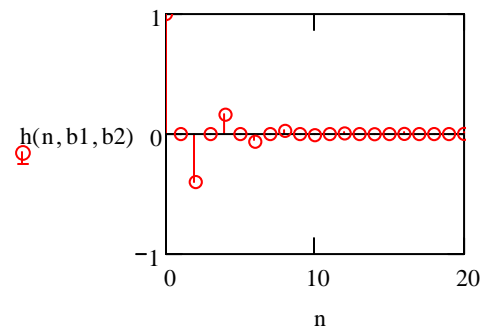


$$g(n, b1, b2) := \frac{1}{1 + b1 + b2} + \text{Im} \left( \frac{p2(b1, b2)^{n+2}}{p2(b1, b2) - 1} \right)$$

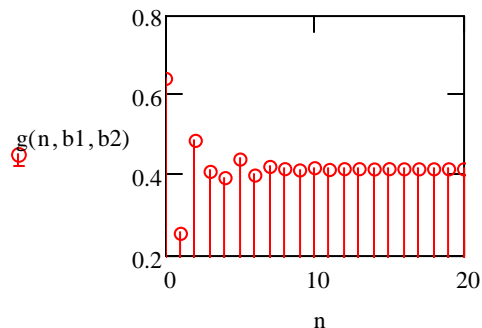
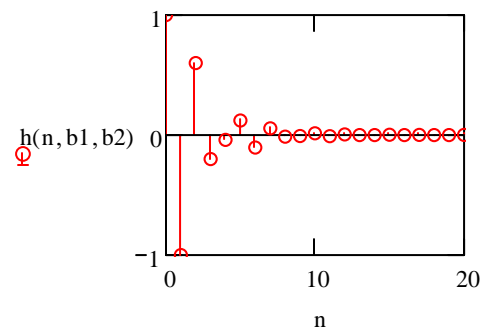
b1 := -1   b2 := 0.4   n := 0, 1 .. 20



b1 := 0   b2 := 0.4   n := 0, 1 .. 20



b1 := 1   b2 := 0.4   n := 0, 1 .. 20



$$j := \sqrt{-1} \quad \text{wr}(b1, b2) := \arccos \left[ \frac{-b1 \cdot (1 + b2)}{4b2} \right]$$

$$y1cx(n, b1, b2) := l(n) \cdot \left[ \frac{\exp[j \cdot \text{wr}(b1, b2) \cdot (n + 2)]}{\exp(j \cdot \text{wr}(b1, b2))^2 + b1 \cdot \exp(j \cdot \text{wr}(b1, b2)) + b2} + \frac{1}{2 \cdot j \cdot \text{wr}(b1, b2)} \cdot \left( \frac{p1(b1, b2)^{n+2}}{p1(b1, b2) - \exp(j \cdot \text{wr}(b1, b2))} - \frac{p2(b1, b2)}{p2(b1, b2) - \exp(j \cdot \text{wr}(b1, b2))} \right) \right]$$

$$ycx(n, ni, b1, b2) := -\exp(j \cdot \text{wr}(b1, b2) \cdot ni) \cdot y1cx(n - ni, b1, b2) + y1cx(n, b1, b2)$$

$$y2cx(n, ni, b1, b2) := \exp(j \cdot \text{wr}(b1, b2) \cdot ni) \cdot y1cx(n - ni, b1, b2)$$

**Реакция на воздействие прямоугольного радиоимпульса**

$$y2(n, ni, b1, b2) := \sqrt{\text{Re}(y2cx(n, ni, b1, b2))^2 + \text{Im}(y2cx(n, ni, b1, b2))^2}$$

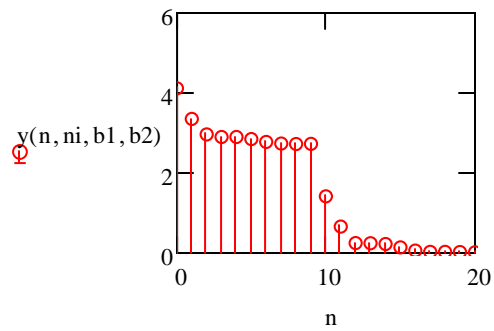
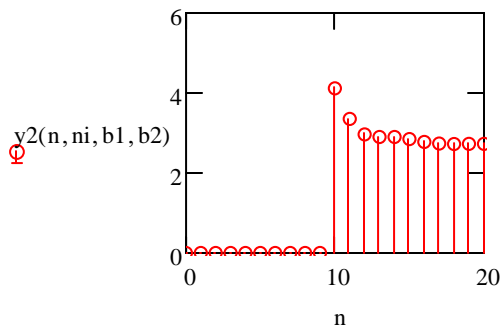
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ErlZz (Sutkovoy Sergey)

ehmal2@list.ru

$$y(n, ni, b1, b2) := \sqrt{\text{Re}(ycx(n, ni, b1, b2))^2 + \text{Im}(ycx(n, ni, b1, b2))^2}$$

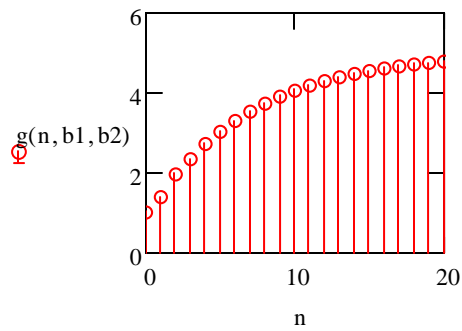
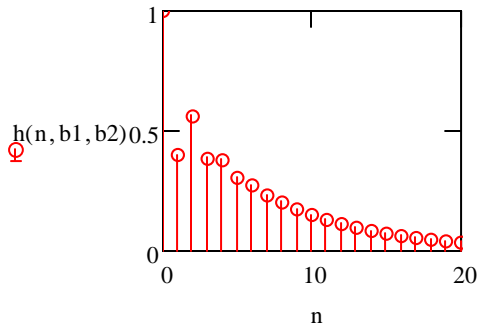
$n := 0, 1 \dots 20$        $ni := 10$        $b1 := -1$        $b2 := 0.4$



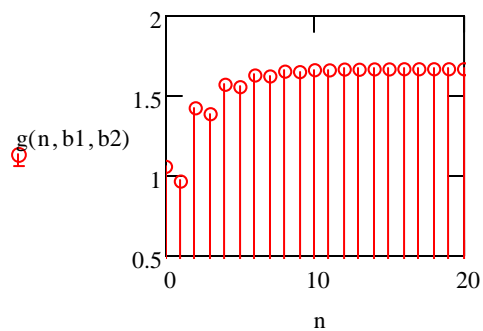
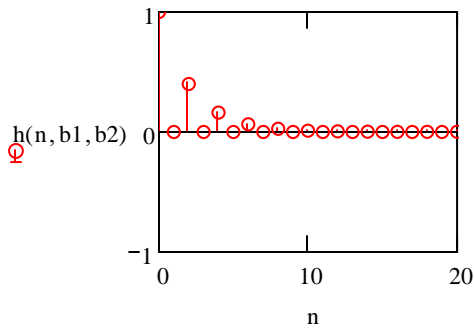
### Режекторный Фильтр

$$g(n, b1, b2) := \frac{1}{1 + b1 + b2} + \frac{1 \cdot \left( \frac{p1(b1, b2)^{n+2}}{p1(b1, b2) - p2(b1, b2)} - \frac{p2(b1, b2)^{n+2}}{p2(b1, b2) - 1} \right)}{p1(b1, b2) - p2(b1, b2)}$$

$b1 := -0.4$        $b2 := -0.4$        $n := 0, 1 \dots 20$

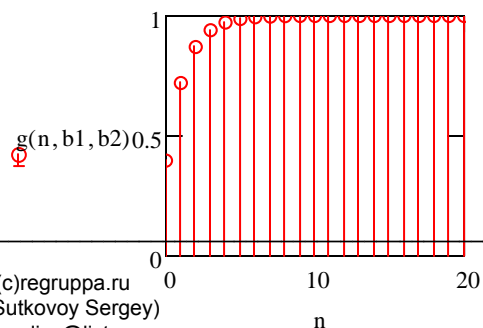
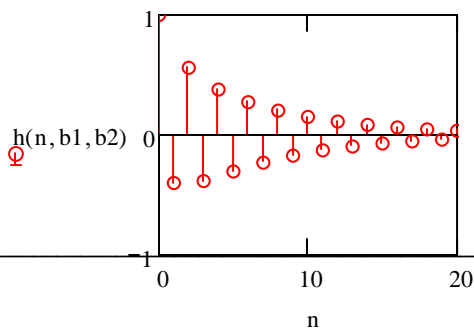


$b1 := 0$        $b2 := -0.4$        $n := 0, 1 \dots 20$



$$g(n, b1, b2) := \frac{1}{1 + b1 + b2} + 2 \cdot \text{Re} \left[ \frac{p2(b1, b2)^{n+2}}{(p2(b1, b2) - 1) \cdot (p2(b1, b2) - p1(b1, b2))} \right]$$

$b1 := 0.4$        $b2 := -0.4$        $n := 0, 1 \dots 20$



$$j := \sqrt{-1} \quad wr(b1, b2) := \arccos \left[ \frac{-b1 \cdot (1 + b2)}{4b2} \right]$$

$$y1cx(n, b1, b2) := 1(n) \cdot \left[ \frac{\exp[j \cdot wr(b1, b2) \cdot (n + 2)]}{\exp(j \cdot wr(b1, b2))^2 + b1 \cdot \exp(j \cdot wr(b1, b2)) + b2} + \frac{1}{2 \cdot j \cdot wr(b1, b2)} \cdot \left( \frac{p1(b1, b2)^{n+2}}{p1(b1, b2) - \exp(j \cdot wr(b1, b2))} - \frac{p2(b1, b2)}{p2(b1, b2) - \exp(j \cdot wr(b1, b2))} \right) \right]$$

$$ycx(n, ni, b1, b2) := -\exp(j \cdot wr(b1, b2) \cdot ni) \cdot y1cx(n - ni, b1, b2) + y1cx(n, b1, b2)$$

$$y2cx(n, ni, b1, b2) := \exp(j \cdot wr(b1, b2) \cdot ni) \cdot y1cx(n - ni, b1, b2)$$

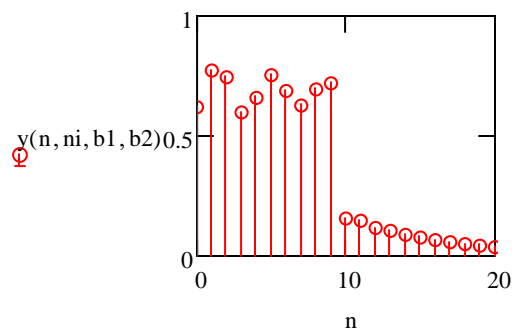
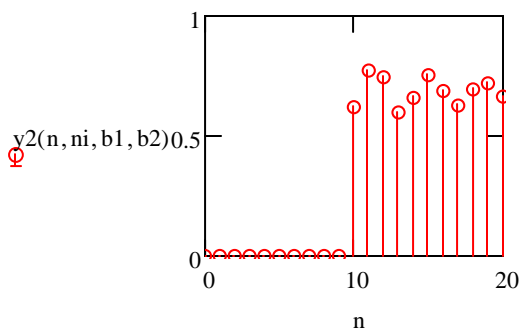
### Реакция на воздействие прямоугольного радиоимпульса

$$y2(n, ni, b1, b2) := \sqrt{\operatorname{Re}(y2cx(n, ni, b1, b2))^2 + \operatorname{Im}(y2cx(n, ni, b1, b2))^2}$$

$$y(n, ni, b1, b2) := \sqrt{\operatorname{Re}(ycx(n, ni, b1, b2))^2 + \operatorname{Im}(ycx(n, ni, b1, b2))^2}$$

$$b1 := -0.4 \quad b2 := -0.4$$

$$n := 0, 1 \dots 20 \quad ni := 10$$



$$\frac{y^{n+2}}{(j \cdot wr(b1, b2))} \Bigg) \Bigg]$$



$$\frac{y^{n+2}}{(j \cdot wr(b1, b2))} \Bigg) \Bigg|$$