benchmark_analysis

March 13, 2023

1 Benchmark Analysis

```
[1]: import sys
     !{sys.executable} -m pip install -r requirements.txt
    Requirement already satisfied: matplotlib in /opt/homebrew/lib/python3.11/site-
    packages (from -r requirements.txt (line 1)) (3.7.0)
    Requirement already satisfied: numpy in /opt/homebrew/lib/python3.11/site-
    packages (from -r requirements.txt (line 2)) (1.24.2)
    Requirement already satisfied: pandas in /opt/homebrew/lib/python3.11/site-
    packages (from -r requirements.txt (line 3)) (1.5.3)
    Requirement already satisfied: contourpy>=1.0.1 in
    /opt/homebrew/lib/python3.11/site-packages (from matplotlib->-r requirements.txt
    (line 1)) (1.0.7)
    Requirement already satisfied: cycler>=0.10 in
    /opt/homebrew/lib/python3.11/site-packages (from matplotlib->-r requirements.txt
    (line 1)) (0.11.0)
    Requirement already satisfied: fonttools>=4.22.0 in
    /opt/homebrew/lib/python3.11/site-packages (from matplotlib->-r requirements.txt
    (line 1)) (4.38.0)
    Requirement already satisfied: kiwisolver>=1.0.1 in
    /opt/homebrew/lib/python3.11/site-packages (from matplotlib->-r requirements.txt
    (line 1)) (1.4.4)
    Requirement already satisfied: packaging>=20.0 in
    /opt/homebrew/Cellar/jupyterlab/3.4.8 1/libexec/lib/python3.11/site-packages
    (from matplotlib->-r requirements.txt (line 1)) (21.3)
    Requirement already satisfied: pillow>=6.2.0 in
    /opt/homebrew/lib/python3.11/site-packages (from matplotlib->-r requirements.txt
    (line 1)) (9.4.0)
    Requirement already satisfied: pyparsing>=2.3.1 in
    /opt/homebrew/Cellar/jupyterlab/3.4.8_1/libexec/lib/python3.11/site-packages
    (from matplotlib->-r requirements.txt (line 1)) (3.0.9)
    Requirement already satisfied: python-dateutil>=2.7 in
    /opt/homebrew/Cellar/jupyterlab/3.4.8_1/libexec/lib/python3.11/site-packages
    (from matplotlib->-r requirements.txt (line 1)) (2.8.2)
    Requirement already satisfied: pytz>=2020.1 in
    /opt/homebrew/Cellar/jupyterlab/3.4.8_1/libexec/lib/python3.11/site-packages
    (from pandas->-r requirements.txt (line 3)) (2022.4)
```

```
Requirement already satisfied: six>=1.5 in
    /opt/homebrew/opt/six/lib/python3.11/site-packages (from python-
    dateutil>=2.7->matplotlib->-r requirements.txt (line 1)) (1.16.0)
    [notice] A new release of pip
    available: 22.3.1 -> 23.0.1
    [notice] To update, run:
    python3.11 -m pip install --upgrade pip
[2]: import matplotlib
     import matplotlib.pyplot as plt
     import numpy as np
     import pandas as pd
     import os
     from pathlib import Path
     from typing import List, Dict, Any
     %matplotlib inline
[3]: matplotlib.style.use('seaborn-v0_8')
[4]: root_dir = '/Users/diego/Desktop/BENCHMARK_NEBULAC_ALL'
[5]: GCC_TBB_COLOR = 'salmon'
     NVC_OMP_COLOR = 'green'
     NVC_GPU_COLOR = 'beige'
    1.1 Utils
[6]: def get_path(*entries):
         return os.path.join(*entries)
[7]: def ensure_file_existence(output_filename):
         Checks wheterh the path to the file exists. If not it creates the folder \Box
      ⇔structure and the final file.
         :param output_filename: path to the file
         :return:
         11 11 11
         # creates dirs etc if they do not exists
         output path = Path(output filename)
         if not os.path.exists(output_path.parent):
             os.makedirs(output_path.parent)
         output_path.touch(exist_ok=True) # will create file, if it exists will do_{\square}
      \hookrightarrow nothing
```

```
[8]: def extraction_pandas_frame_algo(path, COMP="TODO"):
         df = pd.read_csv(path)
         # dropping columns we do not care about
         df = df.drop(['iterations', 'bytes_per_second', 'items_per_second', "

¬'label', 'error_occurred', 'error_message'],
                      axis=1)
         # adding the problem size as column
         df = df[df['name'].str.endswith(('mean', 'median', 'stddev'))]
         df['n'] = df.apply(lambda x: x[0][x[0].find('/') + 1:x[0].rfind('_')], 
      ⇔axis=1)
         df = df.reset_index(drop=True)
         # convert to format
         #
                  real time
                                   cpu\_time time\_unit
                                                                                             stddev
      \rightarrowname
         results_gcc = df.groupby('n').apply(lambda sf: pd.Series(sf.iloc[0])).
      →reset_index(drop=True)
         results_gcc.n = results_gcc.n.astype(int)
         results_gcc = results_gcc.sort_values(['n'], ascending=True).
      →reset index(drop=True)
         results_gcc['C'] = np.arange(len(results_gcc))
         results_gcc['median_id'] = results_gcc['C'] * 3 + 1
         results_gcc['median'] = results_gcc['median_id'].apply(lambda x: df.
      →iloc[x]['real_time'])
         results_gcc['stddev_id'] = results_gcc['C'] * 3 + 2
         results_gcc['stddev'] = results_gcc['stddev_id'].apply(lambda x: df.
      →iloc[x]['real_time'])
         results_gcc = results_gcc.drop(['C', 'median_id', 'stddev_id'], axis=1)
         results_gcc['Compiler'] = COMP
         results_gcc['name'] = results_gcc.apply(lambda x: x[0].replace(str(x['n']),_

¬"").replace('/_mean', ''), axis=1)
         return results_gcc
[9]: # generate filename for threading
```

```
# extract threaded into dictionary
      def extraction pandas frame algo threaded(folder path:str, benchmark name:str, u
       ⇔threads_list:List[int], input_size:int = '1048576', COMP:str="TODO") → Any:
          result = pd.DataFrame()
          for t id in threads list:
              filename =
       aget_threading_file_name(benchmark_name=benchmark_name,thread_nr=t_id,input_size=input_size)
              file_path = get_path(folder_path,filename)
              data_frame = extraction_pandas_frame_algo(file_path,COMP=COMP)
              data frame['threads'] = t id
              result = pd.concat([result, data_frame], ignore_index=True)
          result = result.rename_axis(None, axis=1)
          return result
[10]: # calculate speedup based on seg runnings
      def calc speedup based seq(seq_df: pd.DataFrame, threads_df: pd.DataFrame,_
       speedup column_name:str, input_size:int = 1048576) -> pd.DataFrame:
          # calculate speedup
          seq_df = seq_df[seq_df['n'] == input_size]
          seq_time = seq_df['real_time'].iloc[0] # now its only a single digit
          threads_df['speedup'] = seq_time / threads_df['real_time']
          # clean df
          threads_df = threads_df.
       odrop(columns=['name','cpu_time','time_unit','median','stddev','Compiler','n','real_time'])
          threads_df = threads_df.rename(columns={'speedup':speedup_column_name})
          return threads df
[11]: def calc_speedup_based_par(threads_df: pd.DataFrame, speedup_column_name:str,__
       input_size:int = 1048576) -> pd.DataFrame:
          base_time = threads_df[threads_df['threads'] == 1].iloc[0]['real_time']
          threads_df['speedup'] = base_time / threads_df['real_time']
          # clean df
          threads df = threads df.
       ⇒drop(columns=['name','cpu_time','time_unit','median','stddev','Compiler','n','real_time'])
          threads_df = threads_df.rename(columns={'speedup':speedup_column_name})
          return threads_df
```

2 Nebulah all Core

Architecture: x86_64

CPU op-mode(s): 32-bit, 64-bit Byte Order: Little Endian

Address sizes: 43 bits physical, 48 bits virtual

CPU(s): 64
On-line CPU(s) list: 0-63
Thread(s) per core: 1
Core(s) per socket: 32
Socket(s): 2
NUMA node(s): 8

Vendor ID: AuthenticAMD

CPU family: 23 Model: 1

Model name: AMD EPYC 7551 32-Core Processor

Stepping: 2

CPU MHz: 2404.199 CPU max MHz: 2000.0000 CPU min MHz: 1200.0000 3992.24 BogoMIPS: Virtualization: AMD-V L1d cache: 32K L1i cache: 64K L2 cache: 512K L3 cache: 8192K

NUMA node0 CPU(s): 0,8,16,24,32,40,48,56

NUMA node1 CPU(s): 2,10,18,26,34,42,50,58

NUMA node2 CPU(s): 4,12,20,28,36,44,52,60

NUMA node3 CPU(s): 6,14,22,30,38,46,54,62

NUMA node4 CPU(s): 1,9,17,25,33,41,49,57

NUMA node5 CPU(s): 3,11,19,27,35,43,51,59

NUMA node6 CPU(s): 5,13,21,29,37,45,53,61

NUMA node7 CPU(s): 7,15,23,31,39,47,55,63

Flags: fpu vme de pse tsc msr pae mce cx8 apic sep mtrr pge mca cmov pat pse36 c

2.1 H1

Some parallel backends exhibit better performance and scalability when handling nested parallelism for homogeneous workloads

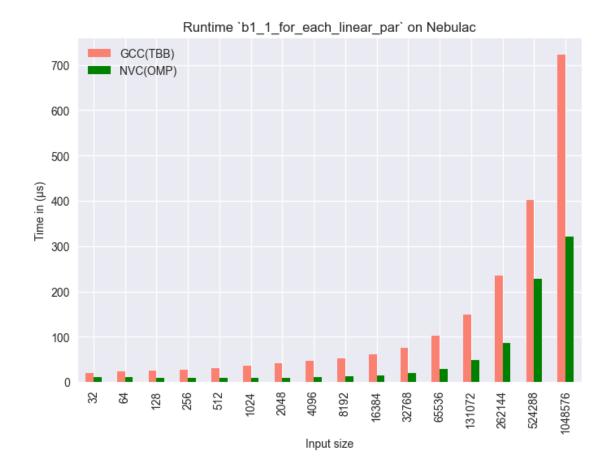
2.1.1 Time

Time Comparison - b1_1_for_each_linear_par Check how the runtime without constraining the threads develops with increasing input size

[12]:

```
# load data qcc (b1_1_for_each_linear_par)
b1_1_for_each_linear_par_gcc = extraction_pandas_frame_algo(root_dir + '/
 GCC_TBB/DEFAULT/b1_1_for_each_linear_par__Default.csv',COMP="GCC(TBB)")
b1_1_for_each_linear_par_gcc = b1_1_for_each_linear_par_gcc.
 drop(columns=['name','cpu time','time unit','median','stddev','Compiler'])
b1_1_for_each_linear_par_gcc = b1_1_for_each_linear_par_gcc.
 →rename(columns={'real_time':'GCC(TBB)'})
# load data nuhpc (b1_1_for_each_linear_par)
b1_1_for_each_linear_par_nvc_omp = extraction_pandas_frame_algo(root_dir + '/
→NVHPC_Multicore/DEFAULT/b1_1_for_each_linear_par__Default.csv', □

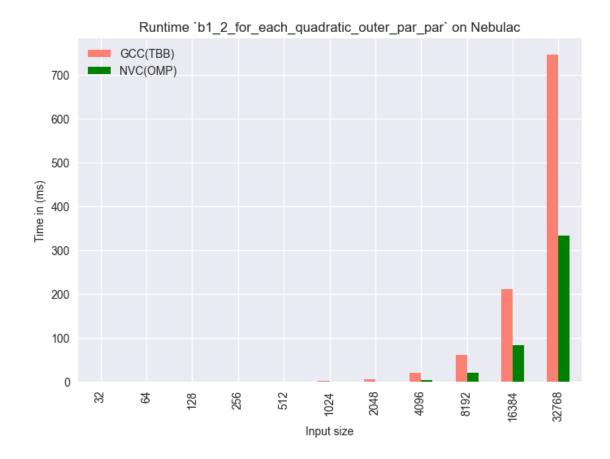
COMP="NVC(OMP)")
b1_1_for_each_linear_par_nvc_omp = b1_1_for_each_linear_par_nvc_omp.
 drop(columns=['name','cpu_time','time_unit','median','stddev','Compiler'])
b1_1_for_each_linear_par_nvc_omp = b1_1_for_each_linear_par_nvc_omp.
 →rename(columns={'real time':'NVC(OMP)'})
# merge for ploting
b1_1_for_each_linear_par_time_merged = pd.merge(b1_1_for_each_linear_par_gcc,__
 ⇒b1_1_for_each_linear_par_nvc_omp, on='n')
b1_1_for_each_linear_par_time_merged
# convert time from ns to microseconds because otherwise it will look really bad
b1_1_for_each_linear_par_time_merged['GCC(TBB)'] =__
 ⇒b1_1_for_each_linear_par_time_merged['GCC(TBB)'] / 1_000
b1 1 for each linear par time merged['NVC(OMP)'] = ____
 ⇒b1_1_for_each_linear_par_time_merged['NVC(OMP)'] / 1_000
# plot
b1_1_for_each_linear_par_time_merged.
 oplot(kind='bar',x='n',align='center',color=[GCC_TBB_COLOR,NVC_OMP_COLOR])
plt.ylabel('Time in (µs)')
plt.xlabel('Input size')
plt.title('Runtime `b1_1_for_each_linear_par` on Nebulac')
plt.show()
```



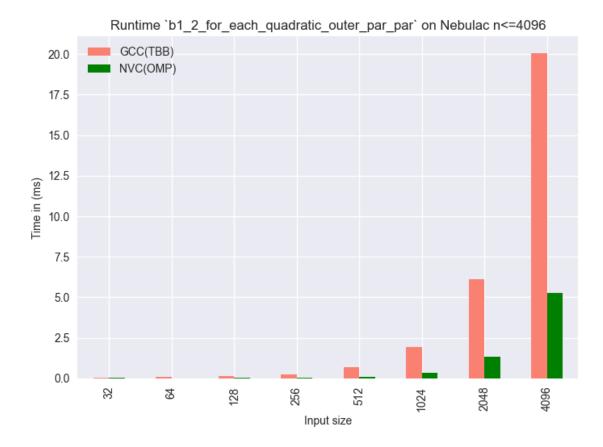
Time Comparison - b1_2_for_each_quadratic_outer_std::execution::parallel_policy_par Check how the runtime without constraining the threads develops with increasing input size

```
b1_2_for_each_quadratic_par_par_nvc_omp = extraction_pandas_frame_algo(root_dir_u
 →+ '/NVHPC Multicore/DEFAULT/b1_2 for each quadratic outer_std::execution::
 →parallel_policy_par__Default.csv',COMP="NVC(OMP)")
b1_2_for_each_quadratic_par_par_nvc_omp =
 ⇒b1_2_for_each_quadratic_par_par_nvc_omp.
 drop(columns=['name','cpu_time','time_unit','median','stddev','Compiler'])
b1_2_for_each_quadratic_par_par_nvc_omp =

¬'NVC(OMP)'})
# merge for ploting
b1_2_for_each_quadratic_par_par_time_merged = pd.
 →merge(b1_2_for_each_quadratic_par_par_gcc,_
 ⇒b1_2_for_each_quadratic_par_par_nvc_omp, on='n')
# convert time from ns to milliseconds because otherwise it will look really bad
b1_2_for_each_quadratic_par_par_time_merged['GCC(TBB)'] = ___
 ⇒b1_2_for_each_quadratic_par_par_time_merged['GCC(TBB)'] / 1_000_000
b1_2_for_each_quadratic_par_par_time_merged['NVC(OMP)'] =__
 ⇒b1_2_for_each_quadratic_par_par_time_merged['NVC(OMP)'] / 1_000_000
# plot
b1_2_for_each_quadratic_par_par_time_merged.
 oplot(kind='bar',x='n',align='center',color=[GCC_TBB_COLOR,NVC_OMP_COLOR])
plt.ylabel('Time in (ms)')
plt.xlabel('Input size')
plt.title('Runtime `b1_2_for_each_quadratic_outer_par_par` on Nebulac')
plt.show()
```



Adding a second graph because small numbers are not readable in the above graph



Time Comparison - b1_4_for_each_exponential_par Check how the runtime without constraining the threads develops with increasing input size

```
[15]: # load data gcc (b1_4_for_each_exponential_par)
b1_4_for_each_exponential_par_gcc = extraction_pandas_frame_algo(root_dir + '/
GCC_TBB/DEFAULT/b1_4_for_each_exponential_par__Default.csv',COMP="GCC(TBB)")

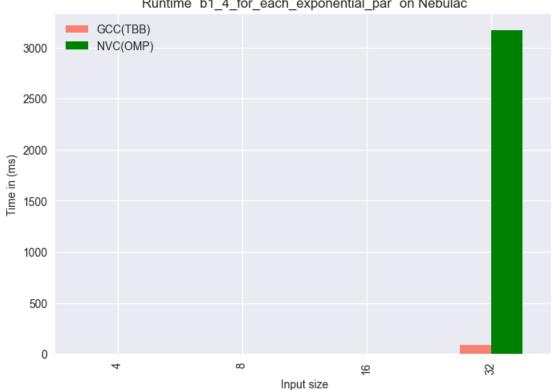
b1_4_for_each_exponential_par_gcc = b1_4_for_each_exponential_par_gcc.
Gdrop(columns=['name','cpu_time','time_unit','median','stddev','Compiler'])
b1_4_for_each_exponential_par_gcc = b1_4_for_each_exponential_par_gcc.
Grename(columns={'real_time':'GCC(TBB)'})

# load data nuhpc (b1_4_for_each_exponential_par)
b1_4_for_each_exponential_par_nvc_omp = extraction_pandas_frame_algo(root_dir +u GCSV',COMP="NVC(OMP)")

b1_4_for_each_exponential_par_nvc_omp = b1_4_for_each_exponential_par_nvc_omp.
Gdrop(columns=['name','cpu_time','time_unit','median','stddev','Compiler'])
```

```
b1_4_for_each_exponential_par_nvc_omp = b1_4_for_each_exponential_par_nvc_omp.
 →rename(columns={'real_time':'NVC(OMP)'})
# merge for ploting
b1 4 for each exponential par time merged = pd.
 omerge(b1_4_for_each_exponential_par_gcc,__
⇒b1_4_for_each_exponential_par_nvc_omp, on='n')
# convert time from ns to milliseconds because otherwise it will look really bad
b1_4_for_each_exponential_par_time_merged['GCC(TBB)'] =__
⇒b1 4 for each exponential par time merged['GCC(TBB)'] / 1 000 000
b1_4_for_each_exponential_par_time_merged['NVC(OMP)'] = ___
ab1_4 for each exponential par_time merged['NVC(OMP)'] / 1_000_000
print(b1_4_for_each_exponential_par_time_merged)
# plot
b1_4_for_each_exponential_par_time_merged.
 plt.ylabel('Time in (ms)')
plt.xlabel('Input size')
plt.title('Runtime `b1_4_for_each_exponential_par` on Nebulac')
plt.show()
                  NVC(OMP)
   GCC(TBB)
             n
  0.018690 4
                  0.012494
  0.121331 8
                  0.042570
 0.537180 16
                  1.722970
```

3 92.126600 32 3170.760000

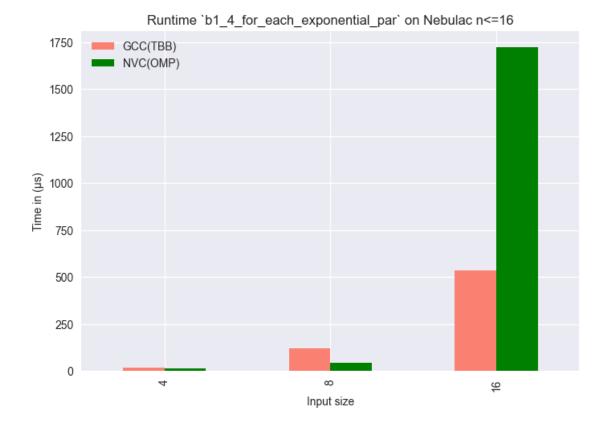


Runtime 'b1 4 for each exponential par' on Nebulac

Adding a second graph because small numbers are not readable in the above graph

```
[16]: b1_4_for_each_exponential_par_time_merged_sub_16 =
       ⇒b1 4 for each exponential par time merged[b1 4 for each exponential par time merged['n']
       <= 16٦
      # convert from milliseconds to microseconds
      b1_4_for_each_exponential_par_time_merged_sub_16['GCC(TBB)'] =__
       ⇒b1_4_for_each_exponential_par_time_merged_sub_16['GCC(TBB)'] * 1_000
      b1_4_for_each_exponential_par_time_merged_sub_16['NVC(OMP)'] =_
       ⇒b1_4_for_each_exponential_par_time_merged_sub_16['NVC(OMP)'] * 1_000
      # plot
      b1_4_for_each_exponential_par_time_merged_sub_16.
       plot(kind='bar',x='n',align='center',color=[GCC_TBB_COLOR,NVC_OMP_COLOR])
      print(b1_4_for_each_exponential_par_time_merged_sub_16)
      plt.ylabel('Time in (µs)')
      plt.xlabel('Input size')
```

```
plt.title('Runtime `b1_4 for_each_exponential_par` on Nebulac n<=16')
plt.show()
  GCC(TBB)
             n
                 NVC(OMP)
  18.6901 4
                  12.4941
1 121.3310
             8
                   42.5701
2 537.1800 16 1722.9700
/var/folders/42/fk0jfryd1dd1ztdldncqc1cw0000gn/T/ipykernel 78020/1969448607.py:4
: SettingWithCopyWarning:
A value is trying to be set on a copy of a slice from a DataFrame.
Try using .loc[row_indexer,col_indexer] = value instead
See the caveats in the documentation: https://pandas.pydata.org/pandas-
docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy
 b1_4_for_each_exponential_par_time_merged_sub_16['GCC(TBB)'] =
b1_4_for_each_exponential_par_time_merged_sub_16['GCC(TBB)'] * 1_000
/var/folders/42/fk0jfryd1dd1ztdldncqc1cw0000gn/T/ipykernel_78020/1969448607.py:5
: SettingWithCopyWarning:
A value is trying to be set on a copy of a slice from a DataFrame.
Try using .loc[row_indexer,col_indexer] = value instead
See the caveats in the documentation: https://pandas.pydata.org/pandas-
docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy
 b1_4_for_each_exponential_par_time_merged_sub_16['NVC(OMP)'] =
b1_4_for_each_exponential_par_time_merged_sub_16['NVC(OMP)'] * 1_000
```



2.1.2 Strong Scaling

$$S(p) = T(1) / T(p)$$

As based we use once the: * sequential algorithm * parallel algorithm (1 thread)

Strong Scaling - b1_1_for_each_linear 1 Million fixed input size with threads 1-64

Seq Base

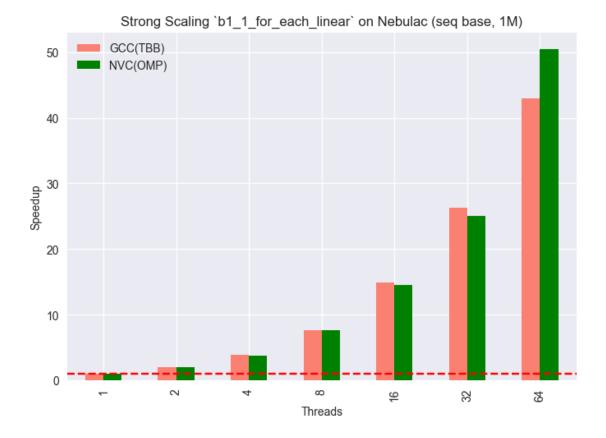
```
# NVC(OMP)
## load nuhpc (b1_1_for_each_linear_seq)
b1_1_for_each_linear_seq_nvc_omp = extraction_pandas_frame_algo(root_dir + '/
 →NVHPC_Multicore/DEFAULT/b1_1_for_each_linear_seq__Default.
 ## load nuhpc threaded b1_1_for_each_linear_par
b1_1_for_each_linear_threads_nvc_omp =__

-- extraction_pandas_frame_algo_threaded(root_dir + '/NVHPC_Multicore/

¬THREADS', 'b1_1_for_each_linear_par', [1,2,4,8,16,32,64], COMP="NVC(OMP)")

## calculate speedup
b1_1_for_each_linear_strong_scaling_seqbase_nvc_omp =_
 -calc_speedup_based_seq(b1_1_for_each_linear_seq_nvc_omp,b1_1_for_each_linear_threads_nvc_om
# merge for plotting
b1_1_for_each_linear_seq_speedup_merged = pd.
 →merge(b1_1_for_each_linear_strong_scaling_seqbase_gcc,__
 ab1_1_for_each_linear_strong_scaling_seqbase_nvc_omp, on='threads')
print(b1_1_for_each_linear_seq_speedup_merged)
# plot strong scaling
ax = b1_1_for_each_linear_seq_speedup_merged.
 oplot(kind='bar',x='threads',align='center',color=[GCC_TBB_COLOR,NVC_OMP_COLOR])
# adding horizontal line where there is speedup
ax.axhline(y=1, color='r', linestyle='--')
plt.ylabel('Speedup')
plt.xlabel('Threads')
plt.title('Strong Scaling `b1_1_for_each_linear` on Nebulac (seq base, 1M)')
plt.show()
  threads
            GCC(TBB)
                       NVC(OMP)
0
            0.997915 0.987061
        2 1.993628 1.971258
1
2
        4 3.966795 3.812405
3
        8 7.715379 7.682825
       16 14.945539 14.531737
4
5
       32 26.258819 25.007096
```

64 42.943653 50.463093



```
[18]: | ## efficiency graph
      b1_1_for_each_linear_seq_efficiency = b1_1_for_each_linear_seq_speedup_merged.
       ⇔copy()
      b1_1_for_each_linear_seq_efficiency['GCC(TBB)'] =__
       ⇔b1_1_for_each_linear_seq_efficiency['GCC(TBB)'] / ___
       ⇒b1_1_for_each_linear_seq_efficiency['threads']
      b1_1_for_each_linear_seq_efficiency['NVC(OMP)'] =_
       ⇒b1_1_for_each_linear_seq_efficiency['NVC(OMP)'] / ___
       ⇒b1_1_for_each_linear_seq_efficiency['threads']
      print(b1_1_for_each_linear_seq_efficiency)
      # plot efficiency
      ax = b1 1 for each linear seg efficiency.
       ⇔plot(x='threads',color=[GCC_TBB_COLOR,NVC_OMP_COLOR])
      # adding horizontal line where there is speedup
      ax.axhline(y=1, color='r', linestyle='--')
      plt.ylim(0.4,1.05)
```

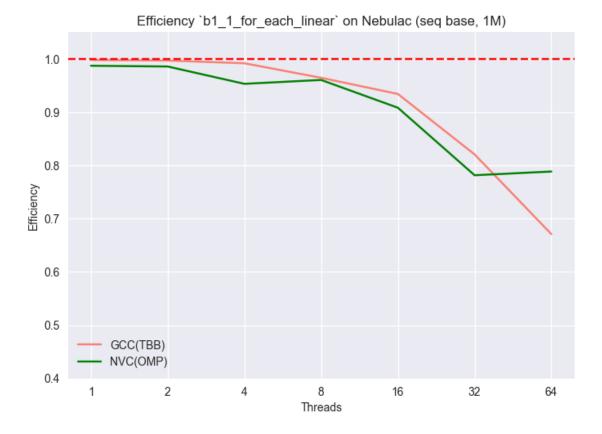
```
plt.xscale('log', base=2)
current_values = plt.gca().get_xticks()
plt.gca().set_xticklabels(['{:,.0f}'.format(x) for x in current_values])

plt.ylabel('Efficiency')
plt.xlabel('Threads')
plt.title('Efficiency `b1_1_for_each_linear` on Nebulac (seq base, 1M)')

plt.show()
```

/var/folders/42/fk0jfryd1dd1ztdldncqc1cw0000gn/T/ipykernel_78020/3790263233.py:1
8: UserWarning: FixedFormatter should only be used together with FixedLocator
plt.gca().set_xticklabels(['{:,.0f}'.format(x) for x in current_values])

```
threads GCC(TBB)
                    NVC(OMP)
        1 0.997915 0.987061
0
1
        2 0.996814 0.985629
2
        4 0.991699 0.953101
3
        8 0.964422 0.960353
4
       16 0.934096 0.908234
5
       32 0.820588 0.781472
6
       64 0.670995 0.788486
```



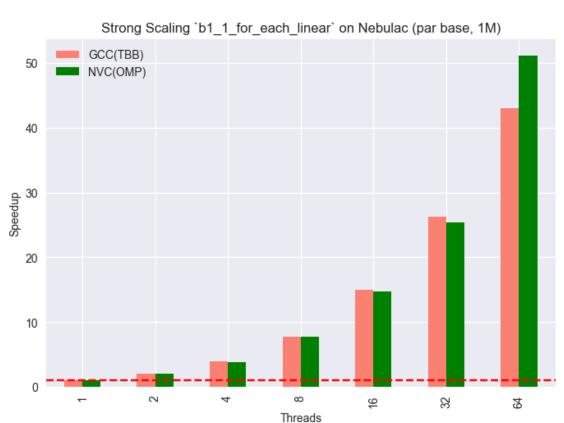
```
Par(1) Base
```

```
[19]: # GCC(TBB)
     ## load qcc threaded b1_1_for_each_linear_par
     b1_1_for_each_linear_threads_gcc = __
       ⇔extraction_pandas_frame_algo_threaded(root_dir + '/GCC_TBB/
      ## calc strong scaling
     b1_1_for_each_linear_strong_scaling_parbase_gcc =_
      Galc_speedup_based_par(b1_1_for_each_linear_threads_gcc, "GCC(TBB)")
     # NVC(OMP)
     ## load nuhpc threaded b1_1_for_each_linear_par
     b1_1_for_each_linear_threads_nvc_omp =

wextraction_pandas_frame_algo_threaded(root_dir + '/NVHPC_Multicore/
      THREADS', 'b1_1_for_each_linear_par', [1,2,4,8,16,32,64], COMP="NVC(OMP)")
     ## calc strong scaling
     b1_1_for_each_linear_strong_scaling_parbase_nvc_omp =_
       →calc_speedup_based_par(b1_1_for_each_linear_threads_nvc_omp, "NVC(OMP)")
     # merge for plotting
     b1_1_for_each_linear_seq_parbase_speedup_merged = pd.
      →merge(b1_1_for_each_linear_strong_scaling_parbase_gcc,__
      ab1_1_for_each_linear_strong_scaling_parbase_nvc_omp, on='threads')
     print(b1_1_for_each_linear_seq_parbase_speedup_merged)
     # plot strong scaling
     ax = b1_1_for_each_linear_seq_parbase_speedup_merged.
      oplot(kind='bar',x='threads',align='center',color=[GCC TBB COLOR,NVC OMP COLOR])
     # adding horizontal line where there is speedup
     ax.axhline(y=1, color='r', linestyle='--')
     plt.ylabel('Speedup')
     plt.xlabel('Threads')
     plt.title('Strong Scaling `b1_1_for_each_linear` on Nebulac (par base, 1M)')
     plt.show()
```

```
threads GCC(TBB) NVC(OMP)
0 1 1.000000 1.000000
1 2 1.997794 1.997099
```

```
2
        4
            3.975084
                       3.862382
3
        8
            7.731503
                       7.783538
4
          14.976772 14.722232
        16
5
       32 26.313694
                      25.334912
6
        64 43.033396
                      51.124609
```



```
# adding horizontal line where there is speedup
ax.axhline(y=1, color='r', linestyle='--')

plt.ylim(0.4,1.05)

plt.xscale('log', base=2)
current_values = plt.gca().get_xticks()
plt.gca().set_xticklabels(['{:,.0f}'.format(x) for x in current_values])

plt.ylabel('Efficiency')
plt.xlabel('Threads')
plt.title('Efficiency `b1_1_for_each_linear` on Nebulac (par base, 1M)')

plt.show()
```

```
threads GCC(TBB) NVC(OMP)

1 1.000000 1.000000

1 2 0.998897 0.998549

2 4 0.993771 0.965595

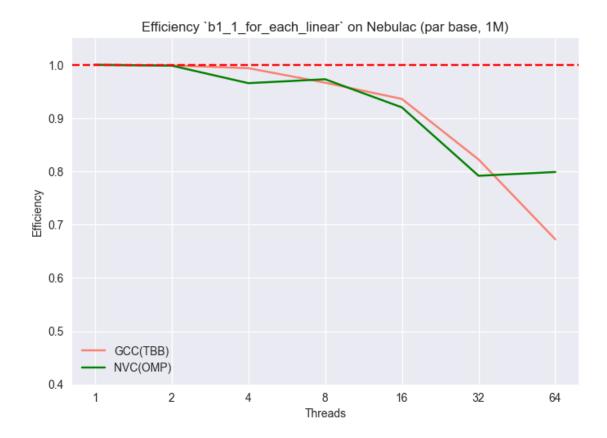
3 8 0.966438 0.972942

4 16 0.936048 0.920140

5 32 0.822303 0.791716

6 64 0.672397 0.798822
```

/var/folders/42/fk0jfryd1dd1ztdldncqc1cw0000gn/T/ipykernel_78020/3088997708.py:1
8: UserWarning: FixedFormatter should only be used together with FixedLocator
 plt.gca().set_xticklabels(['{:,.0f}'.format(x) for x in current_values])



 $\textbf{Strong Scaling - b1_2_for_each_quadratic} \quad 1 \ \, \text{Million fixed input size with threads 1-64}$

Seq Base Here we wont do it with seq base because its not really realistic

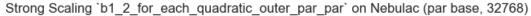
Par(1) Base

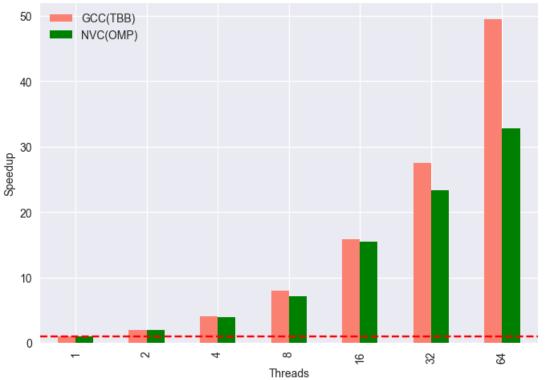
```
b1_2_for_each_quadratic_par_par_threads_nvc_omp =

-- extraction_pandas_frame_algo_threaded(root_dir + '/NVHPC_Multicore/
 →THREADS', 'b1_2_for_each_quadratic_outer_std::execution::
 parallel_policy_par',[1,2,4,8,16,32,64],COMP="NVC(OMP)",input_size=32768)
## calc strong scaling
b1_2_for_each_quadratic_par_par_scaling_parbase_nvc_omp =_
 ⇒calc speedup based par(b1 2 for each quadratic par par threads nvc omp, "NVC(OMP)")
# merge for plotting
b1_2_for_each_quadratic_par_par_speedup_merged = pd.
 omerge(b1_2_for_each_quadratic_par_par_scaling_parbase_gcc,_
 ab1_2_for_each_quadratic_par_par_scaling_parbase_nvc_omp, on='threads')
print(b1_2_for_each_quadratic_par_par_speedup_merged)
# plot strong scaling
ax = b1_2_for_each_quadratic_par_par_speedup_merged.
 plot(kind='bar',x='threads',align='center',color=[GCC_TBB_COLOR,NVC_OMP_COLOR])
# adding horizontal line where there is speedup
ax.axhline(y=1, color='r', linestyle='--')
plt.ylabel('Speedup')
plt.xlabel('Threads')
plt.title('Strong Scaling `b1_2_for_each_quadratic_outer_par_par` on Nebulacu
 ⇔(par base, 32768)')
plt.show()
   threads
            GCC(TBB)
                       NVC(OMP)
            1.000000
0
                       1.000000
         1
1
         2
            2.012084
                       1.989333
2
        4 4.028875
                       3.965606
3
           8.029452 7.085557
4
       16 15.840287 15.510771
```

5

32 27.573592 23.361771 64 49.508283 32.807058

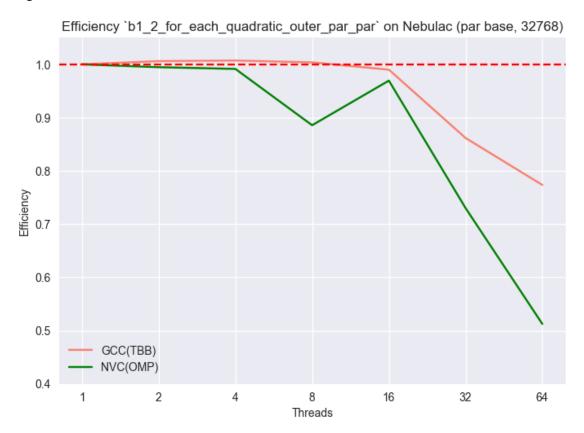




```
[22]: ## efficiency graph
     b1_2_for_each_quadratic_par_par_efficiency =_
      →b1_2_for_each_quadratic_par_par_speedup_merged.copy()
     b1_2_for_each_quadratic_par_par_efficiency['GCC(TBB)'] =__
      ⇔b1_2_for_each_quadratic_par_par_efficiency['GCC(TBB)'] / ___
      ⇒b1_2_for_each_quadratic_par_par_efficiency['threads']
     b1_2_for_each_quadratic_par_par_efficiency['NVC(OMP)'] =__
      ⇒b1_2_for_each_quadratic_par_par_efficiency['NVC(OMP)'] / ___
      print(b1_2_for_each_quadratic_par_par_efficiency)
     # plot efficiency
     ax = b1_2_for_each_quadratic_par_par_efficiency.
      →plot(x='threads',color=[GCC_TBB_COLOR,NVC_OMP_COLOR])
     # adding horizontal line where there is speedup
     ax.axhline(y=1, color='r', linestyle='--')
     plt.ylim(0.4, 1.05)
```

```
threads GCC(TBB)
                    NVC(OMP)
0
        1 1.000000 1.000000
        2 1.006042 0.994667
1
2
        4 1.007219 0.991402
3
        8 1.003681 0.885695
4
       16 0.990018 0.969423
5
       32 0.861675 0.730055
6
       64 0.773567 0.512610
```

/var/folders/42/fk0jfryd1dd1ztdldncqc1cw0000gn/T/ipykernel_78020/328153834.py:18
: UserWarning: FixedFormatter should only be used together with FixedLocator
plt.gca().set_xticklabels(['{:,.0f}'.format(x) for x in current_values])



Strong Scaling - b1_4_for_each_exponential 32 fixed input size with threads 1-64

Seq Base

```
[23]: # GCC
            ## load gcc (b1_4_for_each_exponential_seq)
            b1_4_for_each_exponential_seq_gcc = extraction_pandas_frame_algo(root_dir + '/
              GCC_TBB/DEFAULT/b1_4 for each exponential seq_Default.csv', COMP="GCC(TBB)")
            ## load gcc threaded b1_4_for_each_exponential_par
            b1_4_for_each_exponential_threads_gcc =_
              ⇔extraction_pandas_frame_algo_threaded(root_dir + '/GCC_TBB/
              →THREADS', 'b1_4_for_each_exponential_par', [1,2,4,8,16,32,64], COMP="GCC(TBB)", input_size=32)
            ## calculate speedup
            b1_4_for_each_exponential_strong_scaling_seqbase_gcc =_
              -calc_speedup_based_seq(b1_4_for_each_exponential_seq_gcc,b1_4_for_each_exponential_threads_
            # NVC(OMP)
            ## load nuhpc (b1_4_for_each_exponential_seq)
            b1_4_for_each_exponential_seq_nvc_omp = extraction_pandas_frame_algo(root_dir +_

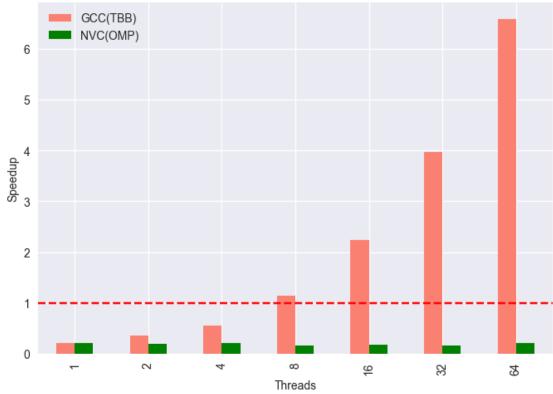
  '/NVHPC_Multicore/DEFAULT/b1_4 for each exponential seq_Default.

Graph of the state of th
            ## load nuhpc threaded b1_4_for_each_exponential_par
            b1_4_for_each_exponential_threads_nvc_omp =

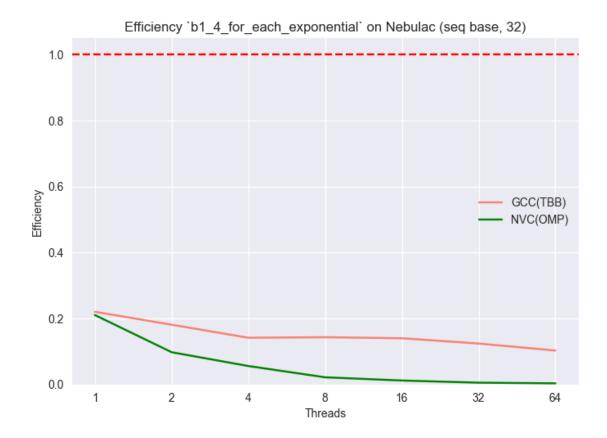
wextraction_pandas_frame_algo_threaded(root_dir + '/NVHPC_Multicore/
              ## calculate speedup
            b1_4_for_each_exponential_strong_scaling_seqbase_nvc_omp =_
              ⇒calc_speedup_based_seq(b1_4_for_each_exponential_seq_nvc_omp,b1_4_for_each_exponential_thre
            # merge for plotting
            b1_4_for_each_exponential_seq_speedup_merged = pd.
              ⇒merge(b1_4_for_each_exponential_strong_scaling_seqbase_gcc,_
              ⇒b1_4_for_each_exponential_strong_scaling_seqbase_nvc_omp, on='threads')
            print(b1_4_for_each_exponential_seq_speedup_merged)
            # plot strong scaling
            ax = b1_4_for_each_exponential_seq_speedup_merged.
              →plot(kind='bar',x='threads',align='center',color=[GCC_TBB_COLOR,NVC_OMP_COLOR])
            # adding horizontal line where there is speedup
```

	threads	GCC(TBB)	NVC(OMP)
0	1	0.220355	0.210447
1	2	0.362259	0.195431
2	4	0.566315	0.223379
3	8	1.145408	0.173250
4	16	2.241314	0.190904
5	32	3.970097	0.171405
6	64	6.585767	0.217449





```
[24]: ## efficiency graph
      b1_4_for_each_exponential_seq_efficiency =_
       ⇒b1_4_for_each_exponential_seq_speedup_merged.copy()
      b1 4 for each exponential seq efficiency['GCC(TBB)'] = [
       ⇒b1_4_for_each_exponential_seq_efficiency['GCC(TBB)'] / ___
       ⇒b1_4_for_each_exponential_seq_efficiency['threads']
      b1_4_for_each_exponential_seq_efficiency['NVC(OMP)'] =__
       ⇒b1_4_for_each_exponential_seq_efficiency['NVC(OMP)'] / ___
       ⇒b1_4_for_each_exponential_seq_efficiency['threads']
      print(b1_4_for_each_exponential_seq_efficiency)
      # plot efficiency
      ax = b1_4_for_each_exponential_seq_efficiency.
       aplot(x='threads',color=[GCC_TBB_COLOR,NVC_OMP_COLOR])
      # adding horizontal line where there is speedup
      ax.axhline(y=1, color='r', linestyle='--')
      plt.ylim(0,1.05)
      plt.xscale('log', base=2)
      current values = plt.gca().get xticks()
      plt.gca().set_xticklabels(['{:,.0f}'.format(x) for x in current_values])
      plt.ylabel('Efficiency')
      plt.xlabel('Threads')
      plt.title('Efficiency `b1_4_for_each_exponential` on Nebulac (seq base, 32)')
      plt.show()
     /var/folders/42/fk0jfryd1dd1ztdldncqc1cw0000gn/T/ipykernel 78020/4127874945.py:1
     8: UserWarning: FixedFormatter should only be used together with FixedLocator
       plt.gca().set_xticklabels(['{:,.0f}'.format(x) for x in current_values])
        threads GCC(TBB) NVC(OMP)
     0
              1 0.220355 0.210447
     1
              2 0.181129 0.097715
              4 0.141579 0.055845
     2
     3
              8 0.143176 0.021656
     4
             16 0.140082 0.011931
     5
             32 0.124066 0.005356
             64 0.102903 0.003398
     6
```



Par(1) Base

```
b1_4_for_each_exponential_strong_scaling_parbase_nvc_omp =
 Galc_speedup_based_par(b1_4_for_each_exponential_threads_nvc_omp,"NVC(OMP)")
# merge for plotting
b1 4 for each linear seq parbase speedup merged = pd.
 →merge(b1_4_for_each_exponential_strong_scaling_parbase_gcc,_
ub1_4_for_each_exponential_strong_scaling_parbase_nvc_omp, on='threads')
print(b1_4_for_each_linear_seq_parbase_speedup_merged)
# plot strong scaling
ax = b1_4_for_each_linear_seq_parbase_speedup_merged.
 aplot(kind='bar',x='threads',align='center',color=[GCC_TBB_COLOR,NVC_OMP_COLOR])
# adding horizontal line where there is speedup
ax.axhline(y=1, color='r', linestyle='--')
plt.ylabel('Speedup')
plt.xlabel('Threads')
plt.title('Strong Scaling `b1_4_for_each_exponential` on Nebulac (par base, ⊔
 →32)¹)
plt.show()
            GCC(TBB) NVC(OMP)
  threads
            1.000000 1.000000
        1
```

```
threads GCC(TBB) NVC(OMP)

1 1.000000 1.000000

1 2 1.643982 0.928644

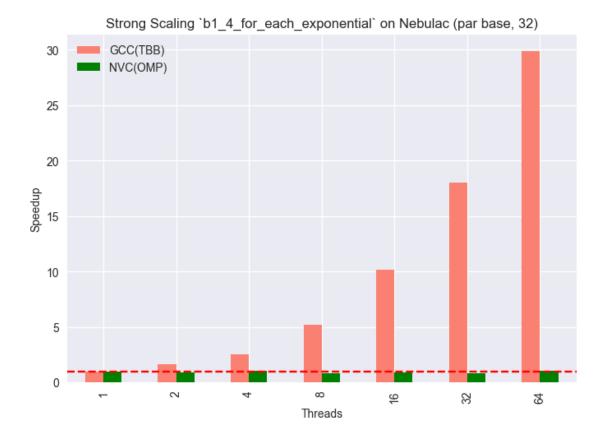
2 4 2.570017 1.061446

3 8 5.198022 0.823248

4 16 10.171399 0.907134

5 32 18.016857 0.814478

6 64 29.887137 1.033271
```



```
[26]: ## efficiency graph
     b1_4_for_each_linear_seq_parbase_efficiency =_
      ⇒b1_4_for_each_linear_seq_parbase_speedup_merged.copy()
     b1_4_for_each_linear_seq_parbase_efficiency['GCC(TBB)'] =__
      ⇔b1_4_for_each_linear_seq_parbase_efficiency['GCC(TBB)'] / ___
      b1_4_for_each_linear_seq_parbase_efficiency['NVC(OMP)'] =__
      ⇔b1_4_for_each_linear_seq_parbase_efficiency['NVC(OMP)'] / □
      ⇔b1_4_for_each_linear_seq_parbase_efficiency['threads']
     print(b1_4_for_each_linear_seq_parbase_efficiency)
     # plot efficiency
     ax = b1 4 for each linear seg parbase efficiency.
      →plot(x='threads',color=[GCC_TBB_COLOR,NVC_OMP_COLOR])
     # adding horizontal line where there is speedup
     ax.axhline(y=1, color='r', linestyle='--')
     plt.ylim(0,1.05)
```

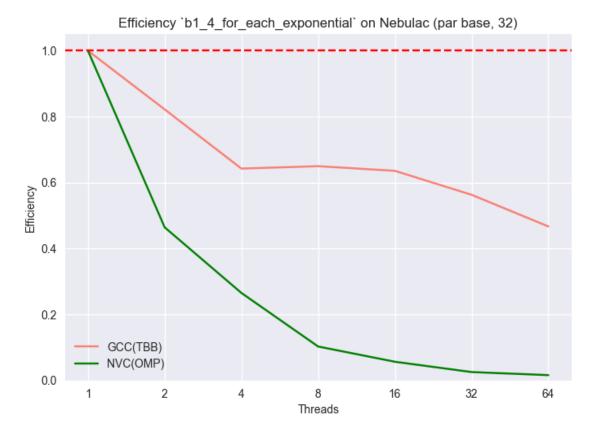
```
plt.xscale('log', base=2)
current_values = plt.gca().get_xticks()
plt.gca().set_xticklabels(['{:,.0f}'.format(x) for x in current_values])

plt.ylabel('Efficiency')
plt.xlabel('Threads')
plt.title('Efficiency `b1_4_for_each_exponential` on Nebulac (par base, 32)')

plt.show()
```

```
NVC(OMP)
  threads GCC(TBB)
0
        1 1.000000 1.000000
        2 0.821991 0.464322
1
2
        4 0.642504 0.265362
3
        8 0.649753 0.102906
4
       16 0.635712 0.056696
5
       32 0.563027
                     0.025452
6
       64 0.466987 0.016145
```

/var/folders/42/fk0jfryd1dd1ztdldncqc1cw0000gn/T/ipykernel_78020/2443303117.py:1
8: UserWarning: FixedFormatter should only be used together with FixedLocator
plt.gca().set_xticklabels(['{:,.0f}'.format(x) for x in current_values])



2.1.3 Performance Portability Calculation (Inter Compiler)

for this group we can "calculate" a performance probability by looking at the strong scaling speedup every compiler has when using the max amount of cores. (aka running with 1M entries at max core) (insipred by [1])

example:

```
| achieved | perfect | efficiency | | ------| | GCC(TBB) | 12 | 16 | 12/16=0.75 | | NVC(OMP) | 16 | 16 | 16/16=1 | | NVC(GPU) | 0 | 0 | 0 | | Intel | 14 | 16 | 14/16=0.875 |
```

Performance Portability for `{GCC(TBB), NVC(OMP), NVC(GPU), Intel}` = 0

Performance Portability for `{GCC(TBB), NVC(OMP), Intel}` = 3/((1/0,75)+(1/1)+(1/0,875))`

```
[27]: max_cores :int = 64
     b1_1_data = []
     b1_2_data = []
     b1_4_data = []
     print("GCC")
     # calculate efficiency for gcc on max core for `b1_1_for_each_linear`
     b1_1_for_each_linear_speed_up_64_gcc =
      →== 64].iloc[0]['GCC(TBB)']
     b1_1_data.append(b1_1_for_each_linear_speed_up_64_gcc)
     print("\tb1_1 Speedup(64):", b1_1_for_each_linear_speed_up_64_gcc)
     # calculate efficiency for gcc on max core for `b1_2_for_each_quadratic`
     b1_2_for_each_quadratic_par_par_speed_up_64_gcc = __
      ⇒b1_2_for_each_quadratic_par_par_scaling_parbase_gcc[b1_2_for_each_quadratic_par_par_scaling
      \hookrightarrow== 64].iloc[0]['GCC(TBB)']
     b1_2_data.append(b1_2_for_each_quadratic_par_par_speed_up_64_gcc)
     print("\tb1_2 Speedup(64):", b1_2_for_each_quadratic_par_par_speed_up_64_gcc)
```

calculate efficiency for gcc on max core for `b1_4_for_each_exponential`

```
b1_4_for_each_exponential_speed_up_64_gcc = __
 ⇒b1_4 for each exponential strong scaling parbase gcc[b1_4 for each exponential strong scali
 \Rightarrow== 64].iloc[0]['GCC(TBB)']
b1_4_data.append(b1_4_for_each_exponential_speed_up_64_gcc)
print("\tb1 4 Speedup(64):", b1 4 for each exponential speed up 64 gcc)
print("\nNVC(OMP)")
# calculate efficiency for nuhpc(mc) on max core for `b1_1 for each linear`
b1_1_for_each_linear_speed_up_64_nvc_omp =
 -b1_1_for_each_linear_strong_scaling_parbase_nvc_omp[b1_1_for_each_linear_strong_scaling_par
 ⇒== 64].iloc[0]['NVC(OMP)']
b1_1_data.append(b1_1_for_each_linear_speed_up_64_nvc_omp)
print("\tb1_1 Speedup(64):", b1_1_for_each_linear_speed_up_64_nvc_omp)
# calculate efficiency for nuhpc(mc) on max core for `b1_2_for_each_quadratic`
b1_2_for_each_quadratic_par_par_speed_up_64_nvc_omp = __
 ⇒b1_2_for_each_quadratic_par_par_scaling_parbase_nvc_omp[b1_2_for_each_quadratic_par_par_sca
\hookrightarrow== 64].iloc[0]['NVC(OMP)']
b1_2_data.append(b1_2_for_each_quadratic_par_par_speed_up_64_nvc_omp)
print("\tb1_2 Speedup(64):", __
 ⇒b1_2_for_each_quadratic_par_par_speed_up_64_nvc_omp)
# calculate efficiency for nuhpc(mc) on max core for `b1 4 for each exponential`
b1_4_for_each_exponential_speed_up_64_nvc_omp = __
 →b1_4_for_each_exponential_strong_scaling_parbase_nvc_omp[b1_4_for_each_exponential_strong_s
→== 64].iloc[0]['NVC(OMP)']
b1_4_data.append(b1_4_for_each_exponential_speed_up_64_nvc_omp)
print("\tb1_4 Speedup(64):", b1_4_for_each_exponential_speed_up_64_nvc_omp)
print("\n\n")
# calc
b1_1_perfect = max(b1_1_data)
b1_2_perfect = max(b1_2_data)
b1_4_perfect = max(b1_4_data)
# Performance portability b1_1 inter compiler
b1_1_efficiency = [x / b1_1_perfect for x in b1_1_data]
pp_b1_1 = len(b1_1_efficiency) / (sum([1 / x for x in b1_1_efficiency]))
print("Performance Portability B1_1: " , pp_b1_1)
```

```
# Performance portability b1_2 inter compiler
b1_2_efficiency = [x / b1_2_perfect for x in b1_2_data]
pp_b1_2 = len(b1_2_efficiency) / (sum([1 / x for x in b1_2_efficiency]))
print("Performance Portability B1_2: " , pp_b1_2)

# Performance portability b1_4 inter compiler
b1_4_efficiency = [x / b1_4_perfect for x in b1_4_data]
pp_b1_4 = len(b1_4_efficiency) / (sum([1 / x for x in b1_4_efficiency]))
print("Performance Portability B1_4: " , pp_b1_4)

GCC

b1_1 Speedup(64): 43.03339575922877
b1_2 Speedup(64): 49.50828342574879
b1_4 Speedup(64): 29.887136604756876
```

NVC(OMP)

b1_1 Speedup(64): 51.12460858208368

b1_2 Speedup(64): 32.80705823482036

b1_4 Speedup(64): 1.0332712232351373

Performance Portability B1_1: 0.914067711189745
Performance Portability B1_2: 0.7971067743386567
Performance Portability B1_4: 0.0668342558082125

2.1.4 Findings for H1

b1_1 There is a significant runtime difference between parallel backends (TBB and NVC(OMP)) when we are dealing with quite rudimentary linear homogenous workloads. As you can see in figure of runtime comparisons. The larger the input size gets the worse the performance of GCC(with TBB) gets. On the other side NVC(with OMP backend) seems to scale quite good under linear homogenous workloads.

For strong scaling we can see that calculating the speedup using the parallel implementation with 1 thread and using the sequential implementation, does not make a huge difference. In fact the overhead for this kind of workload seems to be minimal. The backends scale fairly good and the absolute speedup for each number of threads does not have a tremendous difference between the two backends. We only start to notice that the more threads we utilize the larger the speedup between GCC(TBB) and NVC(OMP) gets.

For small number of threads (1-16) we see that the speedup is quite optimal (close to perfect speedup). Only later when utilizing more threads (32+) we start to see a significant performance loss for both GCC(TBB) and NVC(OMP)

Since the performance portability metric used in this hypothesis focuses on the speedup and as

observed above and the difference between speedup is not that huge, we achieve a rather high performance portability of 91%!

Key observations: *Significant runtime differences between GCC(TBB) and NVC(OMP) *Speedup seems to be on same level for backends only for huge number of threads it starts to degrade *Small number of threads nearly perfect speedup for both *Performance portability quite high since backends behave quite good.

b1_2 There is a significant runtime difference between parallel backends (TBB and NVC(OMP)) when we are dealing with nested quadratic parallelism (aka nested loops with each O(n)). As you can see in figure of runtime comparisons. The larger the input size gets the worse the performance of GCC(with TBB) gets. On the other side NVC(with OMP backend) seems to scale quite good under quadratic homogenous workloads.

For this benchmark we only considered the outer parallel and inner parallel with 1thread as base to calculate the speedups. GCC(TBB) seems to have better strong scaling than NVC(OMP). It looks like that NVC(OMP) starts to degrade heavily when having high number of threads and this is also visible when looking at the efficiency.

Since the performance portability metric used in this hypothesis focuses on the speedup and as observed above and the difference between speedup is actually quite huge, we achieve a rather poor portability of 79%!

Key observations: * Significant runtime differences between GCC(TBB) and NVC(OMP). NVC(OMP) faster than GCC(TBB) * Speedup difference becomes bigger with rise of threads. * NVC(OMP) pretty much collapses at 64 threads. * Small number of threads quite good for both backends * Performance portability poor since NVC(OMP) collapses for high number of threads.