

Усердства, 341

№2

$$-u'' + 10u = 1$$

$$u'(0) = u'(1) = 0$$

$$\text{dom}(A) = U = \{u \mid u \in C^2[0, 1], u'(0) = u'(1) = 0\}$$

$$F = L_2(0, 1)$$

$$F_n = \mathbb{R}^n$$

$$H_A = \{u \mid u'(0) = u'(1) = 0, u' \in L_2(0, 1)\}$$

$$U_n = \langle v_1, \dots, v_n \rangle \subset H_A: u_n = \sum_1^n c_k v_k$$

$$A: U \rightarrow L^2(0, 1); \quad A: u \rightarrow -u'' + 10u$$

$$\varphi_n: H_A \rightarrow U_n; \quad \varphi_n u_n = (c_1, \dots, c_n) = \bar{u}_n$$

$$\bar{\varphi}_n: \mathbb{R}^n \rightarrow L^2(0, 1); \quad \bar{\varphi}_n \bar{u}_n = \sum_1^n c_k v_k$$

$$\psi_n: L^2(0, 1) \rightarrow \mathbb{R}^n$$

$$\psi_n f = ((f, v_1), \dots, (f, v_n))$$

$$A_n: U_n \rightarrow \mathbb{R}^n, \quad A_n \bar{u}_n = \psi_n f, \quad \text{где } A_n = ([v_i, v_j])_{i,j=1}^n$$