

Sets may be used to represent sequences with no duplicates. Unlike a sequence, a set is not enumerable; but any conceivable representation of a set is. This demands the ability to convert a set into a sequence, for operations where a sequence is more suitable. The following definitions provide support for such an operation.

*take1* takes an arbitrary element out of a set and returns a pair consisting of the element and the remaining set.

$$\begin{array}{c} \text{[ } T \text{]} \\ \hline \text{take1} : \mathbb{P}_1 T \rightarrow T \times \mathbb{P} T \\ \hline \forall ts : \mathbb{P}_1 T \bullet \exists t : ts \bullet \text{take1}(ts) = (t, ts \setminus \{t\}) \\ \hline \end{array}$$

*takeAll* iteratively applies *take1* until the set is empty, and constructs a sequence from the resulting elements.

$$\begin{array}{c} \text{[ } T \text{]} \\ \hline \text{takeAll} : \mathbb{P} T \rightarrow \text{seq } T \\ \hline \forall ts, s : \mathbb{P} T \bullet \forall t : T \bullet \\ (t, s) = \text{take1}(ts) \Rightarrow \text{takeAll}(ts) = \langle t \rangle \frown \text{takeAll}(s) \\ \hline \end{array}$$