

notation is used for  $p_1 \vee p_2 \vee \dots \vee p_n$

(1)  $\bigvee_{j=1}^n p_j$

(2)  $\bigwedge_{j=1}^n p_j$  is used for  $p_1 \wedge p_2 \wedge \dots \wedge p_n$

int res = 0;  $\rightarrow$  when OR 1  
 for (int j = 1; j <= n; j++) {  
   res |= p[j];  
 }

int res = 1;  $\rightarrow$  when and 1  
 for (int j = 1; j <= n; j++) {  
   res &= p[j];  
 }

Sudoku puzzle as satisfiab.  $\rightarrow$  code

1.1

13

(a)  $\neg p$

(b)  $p \wedge \neg q$  but is  $\wedge$

(c)  $p \rightarrow q$  <sup>if you speed you get a ticket</sup> <sup>prep if</sup> implication

(d)  $\neg p \rightarrow \neg q$

(e) same as c  $p \rightarrow q$

(f) ~~conjunction~~ ~~disjunction~~  $q \wedge \neg p$

(g)  $q \rightarrow p$ , whenever is "if"

(33) (a)  $(p \vee q) \rightarrow (p \oplus q)$

$p$	$q$	$p \vee q$	$p \oplus q$	$(p \vee q) \rightarrow (p \oplus q)$	$p \wedge q$	$(p \oplus q) \rightarrow (p \wedge q)$
T	T	T	F	F	T	F
T	F	T	T	T	F	T
F	T	T	T	T	F	T
F	F	F	F	T	F	T

(b)  $(p \oplus q) \rightarrow (p \wedge q)$

(c)  $(p \vee q) \oplus (p \wedge q)$

F (opposite of T)  
T (opposite of F)  
T  
F (opposite of T)

(d)  $(p \leftrightarrow q) \oplus (\neg p \leftrightarrow q)$

$p$	$q$	$\neg p$	$p \leftrightarrow q$	$\neg p \leftrightarrow q$	$(p \leftrightarrow q) \oplus (\neg p \leftrightarrow q)$
T	T	F	T	F	T
T	F	F	F	T	T
F	T	T	F	T	T
F	F	T	T	F	T

(e)  $(p \leftrightarrow q) \oplus (\neg p \leftrightarrow \neg r)$

$p$	$q$	$r$	$p \leftrightarrow q$	$\neg p$	$\neg r$	$\neg p \leftrightarrow \neg r$	$(p \leftrightarrow q) \oplus (\neg p \leftrightarrow \neg r)$
T	T	T	T	F	F	T	F
T	T	F	T	F	T	F	T
T	F	T	F	F	F	T	T
T	F	F	F	F	T	F	T
F	T	T	F	T	F	T	T
F	T	F	F	T	T	F	T
F	F	T	T	T	F	F	T
F	F	F	T	T	T	F	T

\*  
Ash  
Aznet

$$(p \oplus q) \rightarrow (p \oplus \neg q)$$

$p$	$q$	$\neg q$	$p \oplus q$	$p \oplus \neg q$	$(p \oplus q) \rightarrow (p \oplus \neg q)$
T	T	F	F	T	T
T	F	T	T	F	F
F	T	F	T	F	F
F	F	T	F	T	T

(35) (a)  $p \rightarrow \neg q$  (b)  $\neg p \leftrightarrow q$

$p$	$q$	$\neg q$	$p \rightarrow \neg q$	$\neg p$	$\neg p \leftrightarrow q$
T	T	F	F	F	F
T	F	T	T	F	<del>F</del>
F	T	F	T	T	T
F	F	T	T	T	F

(c)  $(p \rightarrow q) \vee (\neg p \rightarrow q)$  (d)  $(p \rightarrow q) \wedge (\neg p \rightarrow q)$

$p$	$q$	$p \rightarrow q$	$\neg p$	$\neg p \rightarrow q$	$(p \rightarrow q) \vee (\neg p \rightarrow q)$	$(p \rightarrow q) \wedge (\neg p \rightarrow q)$
T	T	T	F	T	T	T
T	F	F	F	T	F	F
F	T	T	T	T	T	<del>T</del>
F	F	T	T	F	T	F

(e)  $(p \leftrightarrow q) \vee (\neg p \leftrightarrow q)$  (f)  $(\neg p \leftrightarrow \neg q) \leftrightarrow (p \leftrightarrow q)$

$p$	$q$	$p \leftrightarrow q$	$\neg p \leftrightarrow q$	$(p \leftrightarrow q) \vee (\neg p \leftrightarrow q)$	$(\neg p \leftrightarrow \neg q)$	$(\neg p \leftrightarrow \neg q) \leftrightarrow (p \leftrightarrow q)$
T	T	T	F	T	T	T
T	F	F	T	T	F	F
F	T	F	T	T	F	T
F	F	T	F	T	T	T



41

why  $(p \vee q \vee r) \wedge (\neg p \vee \neg q \vee \neg r) \Rightarrow \text{True}$   
when at least one is T and at least one  
is F, but is F when all var's have  
same truth table?

$(p \vee q \vee r) \Rightarrow T$  if any of  $p, q, r = T$  +

$(\neg p \vee \neg q \vee \neg r) \Rightarrow F$  if any of  $p, q, r = F$  +

Both ~~statements~~ clauses are T,  $\Rightarrow$  entire statement

is T, if only there is at least one T and  
one F among truth values.