

49 (37)

- (1) (a) $A(x) \rightarrow$ person x that qualifies as elite fl
 (b) $B(x, y) \rightarrow$ person x that flies more than
 y miles in a year
 (c) $C(x, y) \rightarrow$ person x that takes more
 than y flights in a year
 $\ast \forall x (B(x, 25,000) \vee C(x, 25)) \rightarrow A(x)$

- (2) (a) $A(x) \rightarrow$ person x that qualify for manhood
 (b) $B(x) \rightarrow$ person is a Man
 (c) $C(x) \rightarrow$ person is a Woman
 (d) $D(x, y) \rightarrow$ person x has men mar
 in less than y hours
 $\ast \forall x ((B(x) \wedge D(x, 3)) \vee (C(x) \wedge D(x, 35))) \rightarrow A(x)$

- (3) (a) $A(x) \rightarrow$ student
 (b) $B(x) \rightarrow$ master's degree
 (c) $C(x, y) \rightarrow$ student x has to take y courses
 (d) $D(x, y) \rightarrow$ ~~graduate~~ student x has to
 (e) $E(x) \rightarrow$ receive a grade x in y
 $\ast A(x) \rightarrow (C(60) \vee (C(45) \wedge E(x))) \wedge \forall y D(B, y)$
 \ast stud who wrote thesis

- (4) $A(x, y) \rightarrow$ person x who took more than y
 $B(x, z) \rightarrow$ person x who received z credit
 as grade

$$\exists x (A(x, 21) \wedge B(x, 4.0))$$

credits same person all A's

53)

exists a unique

$$(a) \exists! x P(x) \rightarrow \exists x P(x) - \text{True}$$

$$(b) \forall x P(x) \rightarrow \exists! x P(x)$$

more than 1x such that P(x) holds - True

$$(c) \exists! x \neg P(x) \rightarrow \neg \forall x P(x) - \text{True}$$

if there's x such that P(x) is False, then it's not the case that P(x) holds for all x

59)

Let P(x), Q(x) and R(x) be statements

P(x) → x is a professor

Q(x) → x is ignorant

R(x) → x is vain

domain → all people

$$(1) \forall x (P(x) \rightarrow \neg Q(x))$$

$$(2) \forall x (Q(x) \rightarrow R(x))$$

$$(3) \forall x (P(x) \rightarrow \neg R(x))$$

$$(4) \text{No}$$

61)

P(x) → x is a baby

Q(x) → x is logical

R(x) → x is able to manage crocodile

S(x) → x is despised

$$(1) \forall x (P(x) \rightarrow \neg Q(x)) \quad (4) \forall x (P(x) \rightarrow \neg R(x))$$

$$(2) \forall x (R(x) \rightarrow \neg S(x)) \quad (5) \text{No, babies cannot}$$

$$(3) \forall x (Q(x) \rightarrow S(x))$$

manage crocodiles