

# Milbert Grand Hotel!

(1) Set of all ints is countable:

Watched  
video

$0, 1, -1, 2, -2, 3, -3, 4, -4, \dots$   
 $\downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow$   
 $1 \quad 2 \quad 3 \quad 4 \quad 5 \quad 6 \quad 7 \quad 8 \quad 9 \dots$

(2)  $\frac{1}{1} - \frac{1}{1}$  list all rationals minus  
do zigzag

Watched  
video

$\frac{2}{1} - \frac{2}{1}$   
 $\frac{3}{1} - \frac{3}{1}$

start w/ 0 go to  $\frac{1}{1}$  and do  
zigzag

(35) Power Set of 3 nums: {empty set, {1, 2, 3}}

$\{2\}, \{2, 3\}, \{1\}$   
 $\{1, 3\}, \{1, 2\}, \{2, 3\}$   
 $\{1, 2, 3\}$

subsets

'infinite num of pos. integers:'

$1, 2, 3, 4, 5, \dots$   
 $1 \leftrightarrow N \quad N \quad N$   
 $2 \leftrightarrow Y \quad N \quad N$   
 $3 \leftrightarrow N \quad Y \quad N$   
 $4 \leftrightarrow Y \quad Y \quad N$   
 $5 \leftrightarrow Y \quad N \quad Y$

$6 \leftrightarrow Y \quad N \quad Y$   
 $7 \leftrightarrow N \quad Y \quad Y$   
 $8 \leftrightarrow Y \quad Y \quad Y$

countable  
∞

1, 2, 3, 4, 5, 6, 7, ...

1 → N  
2 → N N N N N  
3 → Y Y Y Y Y Y  
4 → N Y N N Y N  
Y Y N N ...

$|S| < |P(S)| < |P(P(S))|$  there's subset that's not listed  
Power Set of Set is <sup>uncountable</sup> infinite

countably infinite

(1) Hilbert Hotel 1:57 - 3:11

Hotel

B1

B2

B3

B4

1 2 3 4 5 6 ...  
G1 G2 G3 G4 G5 G6 ...  
B1S1 B1S2 B1S3 B1S4 ...  
B2S1 B2S2  
B3S1 B3S2  
B4S1 B4S2  
...

Idea: How to list all of ration or pos rational numbers - zigzag approach

(2) No, you can't fit them - Uncountably infinite

1 → A A A A A ...

2 → A B A B A B ...

3 → A B A A A ...

4 → ...

counters  
diagonalization  
B A A ... - do for all  
another person that's not