

? Addition of integers - once complement we use in comp

- (37)
- (1) add the numbers directly
 - (2) Check for carry out
 - (3) Check the result
 - (4) Determine overflow
 - (5) Interpret the Result

$$A \rightarrow 5 \rightarrow \begin{matrix} 8421 \\ 0101 \end{matrix}$$

$$B \rightarrow -3 \rightarrow 1100$$

$$+ 0101$$

$$1100$$

$$\hline 10001$$

$\rightarrow 5$ (in a 4 bit ones complement system)

(1) 32 bit is sign bit

if num - negative, sign bit 1

if num - positive, sign bit 0

if num = 0, sign bit 0

the rest of bits \rightarrow magnitude

$$\text{Ex(1): } -2^{31} = \text{sign bit magnitude} = 0$$

$$1 \quad 00000000 \dots 0$$

32nd bit

$$\text{Ex(2): } -1 = 1 \quad 11111111 \dots 1 = 1 \quad \text{in ones complement in actual computers}$$

$$\text{sign bit} \quad \text{magnitude}$$

$$-2^{31} + (2^{30} \dots 2^0)$$

$$2^{31} - 1 \Rightarrow -1$$

$$\rightarrow 0001$$

$$1$$

$$\hline 0010 \rightarrow +2$$

$$3^{11} \Rightarrow 11 = (1011)_2 \Rightarrow 3^{11} = 3^8 3^2 3^1$$

$$3^2 = 9$$

$$3^4 = 9^2 = 81$$

$$3^8 = (81)^2 = 6561$$

$$3^{11} = 3^8 \cdot 3^2 \cdot 3^1 = 6561 \cdot 9 \cdot 3 = 177,147$$

(13) for 2's complement expansions

- (1) convert integers to 2's complement
- (2) add 2's complement represent
- (3) handle the carry (if applicable)
- (4) collect final result

$$A = 5 \quad 0101$$

$$B = -3 \text{ in binary (4-bit)} \Rightarrow 1101$$

$$+3 =$$

$$0011$$

$$-3 =$$

$$1100$$

$$+0001$$

$$1101$$

$$0011$$

$$+1101$$

$$0000$$

$$+0101$$

$$1101$$

$$10010 \Rightarrow 2, \text{ so } 5 + (-3) = 2$$

↓

ignore the carry that exceeds the bit width

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