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DM #2

Divide Pair Conquer O2

$$f: \mathbb{Z}^+ * \mathbb{Z}^+ \rightarrow \mathbb{Z}^+$$

$$f(m, n) = \frac{(m+n-2)(m+n-1)}{2} + m$$

$$\text{Solve: } f(x-1, 1) + 1 = f(1, x) \Rightarrow \frac{x(x-1)}{2} + 1$$

$$f(x-1, 1) + 1 = \frac{(\cancel{x-1}+1-2)(\cancel{x-1}+1-1)}{2} + \cancel{x-1}+1 =$$

$$= \frac{(x-2)(x-1)}{2} + x^2 = \frac{x^2 - 3x + 2 + 2x}{2} =$$

$$= \frac{x^2}{2} - \frac{x}{2} + \frac{2}{2} = \frac{x^2 - x}{2} + 1 =$$

$$= \frac{x(x-1)}{2} + 1 \Rightarrow f(1, x)$$