# Package 'rcosmo'

September 3, 2018

<pre>URL https://github.com/VidaliLama/rcosmo</pre>
BugReports https://github.com/VidaliLama/rcosmo/issues
Title R Cosmic Microwave Background Data Analysis
Version 0.0.0.9000
<b>Description</b> Handling and statistical analysis of Cosmic Microwave Background data on a HEALPix grid.
<b>Depends</b> R (>= 3.3.1)
License MIT + file LICENSE
Encoding UTF-8
LazyData true
Imports FITSio (>= 2.1-0), Rcpp (>= 0.12.11), mmap (>= 0.6-17), tibble (>= 1.4.2), rgl (>= 0.99.16), cli (>= 1.0.0)
Suggests knitr, rmarkdown, testthat, R.rsp
LinkingTo Rcpp
RoxygenNote 6.1.0
VignetteBuilder R.rsp
R topics documented:  areCompatibleCMBDFs as.CMBDataFrame assumedConvex cbind.CMBDataFrame CMBDat CMBDataFrame CMBDataFrame CMBDataFrame CMBReadFITS CMBWindow
coords.CMBDataFrame

oords.CMBWindow	11
oords.data.frame	12
oords.HPDataFrame	12
ovCMB	13
ovPwSp	14
ownloadCMBmap	15
ownloadCMBPS	16
nf	17
eoArea.CMBDataFrame	18
eoArea.CMBWindow	19
eoArea.HPDataFrame	19
eoDist	20
eader	21
IPDataFrame	21
CMBDat	22
	23
CMBWindow	23
.HPDataFrame	24
	24
	25
	26
	26
	27
e e e e e e e e e e e e e e e e e e e	28
	28
_ 1	29
	30
	30
· ·	31
•	32
	32
	33
	34
ixelWindow	
lot.CMBDataFrame	
	36
lot.CMBWindow	
	38
	39
	39
	40
	41
	41
	42
1	42
	43
, · · · · · · · · · · · · · · · · · · ·	44
, · · · · · · · · · · · · · · · · · · ·	44
	45
	46
	47
rindow.data.frame	49

3

	window.HPDataFrawinType													
Index														53
areCo	ompatibleCMBDFs	Check con	npatible	ness o	f CN	1BD	atal	Fran	nes					

# Description

Compare attributes to decide if two CMBDataFrames are compatible

# Usage

```
areCompatibleCMBDFs(cmbdf1, cmbdf2, compare.pix = FALSE)
```

# **Arguments**

```
 \begin{array}{ll} \text{cmbdf1} & \text{a CMBDataFrame} \\ \text{cmbdf2} & \text{a CMBDataFrame} \end{array}
```

compare.pix A boolean. If TRUE then cmbdf1 and cmbdf2 must share the same pixel indices

to be considered compatible

#### **Details**

If the CMBDataFrames do not have compatible attributes then a message is printed indicating the attributes that do not match. To suppress this use the suppressMessages function

# **Examples**

```
a <- CMBDataFrame(nside = 2, ordering = "ring", coords = "cartesian")
b <- CMBDataFrame(nside = 1, ordering = "nested", coords = "spherical")
areCompatibleCMBDFs(a,b)
suppressMessages(areCompatibleCMBDFs(a,b))</pre>
```

as.CMBDataFrame

Convert dataframes to CMBDataFrames

# Description

Safely converts a data.frame to a CMBDataFrame. The rows of the data.frame are assumed to be in the HEALPix order given by ordering, and at the HEALPix resolution given by nside. Coordinates, if present, are assumed to correspond to HEALPix pixel centers. The coordinates must be named either x,y,z (cartesian) or theta, phi (spherical colatitude and longitude respectively).

### Usage

```
as.CMBDataFrame(df, ordering, nside, spix)
```

4 assumedConvex

### **Arguments**

df Any data.frame whose rows are in HEALPix order ordering character string that specifies the ordering scheme ("ring" or "nested") nside an integer  $2^k$  that specifies the Nside (resolution) HEALPix parameter spix an integer vector that specifies the HEALPix pixel index corresponding to each

row of df. If spix is left blank and df is a data.frame, then df is assumed to contain data for every pixel at resolution parameter nside (the full sky). In other words, in this case, the number of rows of df must be equal to 12\*nside^2. However, if spix is left blank and df is a CMBDataFrame, then spix is set equal

to pix(df)

#### Value

A CMBDataFrame

### **Examples**

```
## Example 1: Create df with no coords, then create CMBDataFrames cmbdf and
## df2 with spherical coords

df <- data.frame(I=rnorm(12))
    df

cmbdf <- as.CMBDataFrame(df,ordering= "ring", nside=1)
    summary(cmbdf)
    pix(cmbdf)
    coords(cmbdf)

df2 <- coords(cmbdf, new.coords = "spherical")
    df2

## Example 2: Create CMBDataFrames for first 10 Healpix centers

df <- data.frame(I=rnorm(10))
    df
    cmbdf <- as.CMBDataFrame(df,ordering= "ring", nside=2, spix=1:10)
    summary(cmbdf)
    pix(cmbdf)</pre>
```

 $assumed {\tt Convex}$ 

Check if a CMBWindow is assumed convex.

# Description

Initially any CMBWindow is not assumed convex. The assumedConvex attribute can be change for any CMBWindow.

### Usage

```
assumedConvex(win, assume.convex)
```

cbind.CMBDataFrame 5

# **Arguments**

```
win a CMBWindow object
assume.convex optionally change the assumedConvex attribute to TRUE or FALSE
```

# **Examples**

```
win1 <- CMBWindow(theta = c(0,pi/2,pi/2), phi = c(0,0,pi/2)) assumedConvex(win1) win2 <- assumedConvex(win1, assume.convex = TRUE) assumedConvex(win2) assumedConvex(win1) <- TRUE assumedConvex(win1)
```

cbind.CMBDataFrame

cbind for CMBDataFrames

# Description

Add a new column or columns (vector, matrix or data.frame) to a CMBDataFrame. Note that method dispatch occurs on the first argument. So, the CMBDataFrame must be the first argument

# Usage

```
## S3 method for class 'CMBDataFrame'
cbind(..., deparse.level = 1)
```

# **Details**

See the documentation for cbind

```
cmbdf <- CMBDataFrame(nside = 1, ordering = "nested", coords = "spherical")
cmbdf2 <- cbind(cmbdf, myData = rep(1, 12))
cmbdf2</pre>
```

6 CMBDataFrame

CMBDat class.

#### **Description**

The function CMBReadFITS creates objects of class CMBDat. These are lists containing header information and other metadata as well as an element called data, whose columns may include, for example, the intensity (I), polarisation (Q, U), PMASK and TMASK. It also may contain an mmap object that points to the CMB map data table in the FITS file.

# **Arguments**

filename The path to the fits file.

mmap A boolean indicating whether to use memory mapping.

spix The sample pixels (rows) to read from the FITS file binary data table (optional)

#### Value

A list containing header information and other metadata as well as an element called data where: If mmap = FALSE then a data. frame is included, named data, whose columns may include, for example, the intensity (I), polarisation (Q, U), PMASK and TMASK. If mmap = TRUE then a mmap object is returned that points to the CMB map data table in the FITS file.

# **Examples**

```
cmbdat <- CMBReadFITS("CMB_map_smica1024.fits", mmap = TRUE)
class(cmbdat)
str(cmbdat)

# View metadata
dat$header1
dat$header2
dat$resoln
dat$method
dat$coordsys
dat$nside
dat$hdr</pre>
```

 ${\it CMBDataFrame}$ 

CMBDataFrame class

# Description

The function CMBDataFrame creates objects of class CMBDataFrame. These are a special type of data.frame that carry metadata about, e.g., the HEALPix ordering scheme, coordinate system, and nside parameter.

CMBDataFrame 7

#### Usage

```
CMBDataFrame(CMBData, coords, win, include.polar = FALSE,
include.masks = FALSE, spix, sample.size, nside, ordering, I, ...)
```

#### **Arguments**

CMBData Can be a string location of FITS file, another CMBDataFrame, a CMBDat object,

or unspecified.

coords Can be "spherical," "cartesian", or unspecified (HEALPix only).

win optional CMBWindow object that specifies a spherical polygon within which to

subset the full sky CMB data.

include.polar TRUE if polarisation data is required, otherwise FALSE.

include.masks TRUE if TMASK and PMASK are required, otherwise FALSE.

spix Optional vector of sample pixel indices, or a path to a file containing comma

delimited sample pixel indices. The ordering scheme is given by ordering. If ordering is unspecified then CMBData must be either a CMBDataFrame or a FITS file and the ordering scheme is then assumed to match that of CMBData.

sample.size If a positive integer is given, a simple random sample of size equal to sample.size

will be taken from CMBData. If spix is specified then sample.size must be

unspecified.

nside Optionally specify the nside parameter manually nside= $2^k$  (usually 1024 or

2048).

ordering Specifies the desired HEALPix ordering scheme ("ring" or "nested") for the

output CMBDataFrame. If ordering is unspecified then the ordering scheme will be taken from the CMBData object, which must then be either a CMBDataFrame or a path to a FITS file. This parameter also specifies the ordering

scheme of spix.

I A vector of intensities to be included if CMBData is unspecified. Note that

length(I) must equal  $12 * nside^2$  if either spix or sample.size are unspeci-

fied.

... Optional names data columns of length nrow(CMBData) to add to the CMB-

DataFrame.

#### Value

A CMBDataFrame whose row.names attribute contains HEALPix indices.

```
## Method 1: Read the data while constructing the CMBDataFrame
df <- CMBDataFrame("CMB_map_smica1024.fits")

# Specify a sample size for a random sample
df.sample <- CMBDataFrame(df, sample.size = 800000)
plot(df.sample)

# Specify a vector of pixel indices using spix
df.subset <- CMBDataFrame(df, spix = c(2,4,6))

# Take a look at the summary</pre>
```

8 CMBReadFITS

```
summary(df)

# Access HEALPix pixel indices using pix function
# (these are stored in the row.names attribute)
pix(df.subset)
```

**CMBReadFITS** 

Read CMB data from a FITS file.

### **Description**

CMBReadFITS is adapted from the readFITS function in package FITSio. CMBReadFITS is in development stage and will only work with 'CMB\_map\_smica1024.fits'. When it works, CMBReadFITS is much faster than readFITS. However, readFITS is more general and so is more likely to work.

# Usage

```
CMBReadFITS(filename, mmap = FALSE, spix)
```

### **Arguments**

filename The path to the fits file.

mmap A boolean indicating whether to use memory mapping.

spix The sample pixels (rows) to read from the FITS file binary data table (optional)

#### **Details**

The function CMBReadFITS creates objects of class CMBDat. These are lists containing header information and other metadata as well as an element called data, whose columns may include, for example, the intensity (I), polarisation (Q, U), PMASK and TMASK. It also may contain an mmap object that points to the CMB map data table in the FITS file.

#### Value

A list containing header information and other metadata as well as an element called data where: If mmap = FALSE then a data. frame is included, named data, whose columns may include, for example, the intensity (I), polarisation (Q, U), PMASK and TMASK. If mmap = TRUE then a mmap object is returned that points to the CMB map data table in the FITS file.

```
cmbdat <- CMBReadFITS("CMB_map_smica1024.fits", mmap = TRUE)
class(cmbdat)
str(cmbdat)

# View metadata
dat$header1
dat$header2
dat$resoln</pre>
```

CMBWindow 9

dat\$method
dat\$coordsys
dat\$nside
dat\$hdr

CMBWindow

CMBWindow class.

# **Description**

The function CMBWindow creates objects of class CMBWindow. It is either a polygon or a disc type.

### Usage

```
CMBWindow(..., r, set.minus = FALSE, assume.convex = FALSE)
```

#### **Arguments**

these arguments are compulsory and must be labelled either x, y, z (cartesian) or theta, phi (spherical, colatitude and longitude respectively). Alternatively, a single data.frame may be passed in with columns labelled x, y, z or theta, phi.

r if a disc type window is required then this specifies the radius of the disc when TRUE the window will be the unit sphere minus the window specified when TRUE the window is assumed to be convex resulting in a faster computation time when the window is used with functions such as subWindow. This argument

is irrelevant when the window is not a polygon

#### **Details**

If r is unspecified then the rows of . . . correspond to counter-clockwise ordered vertices defining a spherical polygon lying entirely within one open hemisphere on the unit sphere. Counter-clockwise is understood from the perspective outside the sphere, facing the hemisphere that contains the polygon, looking toward the origin. Note that there must be at least 3 rows (vertices) to define a polygon (we exlude bygons). On the other hand, if r is specified then . . . must specify just one row, and this row is taken to be the center of a disc of radius r

```
win <- CMBWindow(theta = c(pi/2,pi/2,pi/3, pi/3), phi = c(0,pi/3,pi/3,0))
plot(win)

## Create a disc type window
win1<- CMBWindow(x=0,y=3/5,z=4/5,r=0.8, set.minus =TRUE)
plot(win1)

## Apply a disc type window to CMBDataFrame
cmbdf <- CMBDataFrame(nside = 64, coords = "cartesian", ordering = "nested")
window(cmbdf) <- CMBWindow(x=0,y=3/5,z=4/5,r=0.8, set.minus =TRUE)
plot(cmbdf)</pre>
```

10 coords.CMBDataFrame

coords.CMBDataFrame

 ${\it Coordinate\ system\ from\ a\ {\it CMBDataFrame}}$ 

### **Description**

If new.coords is unspecified then this function returns the coordinate system used in the CMB-DataFrame cmbdf. The coordinate system is either "cartesian" or "spherical". If a new coordinate system is specified, using e.g. new.coords = "spherical", then this function instead returns a new CMBDataFrame whose coordinates are of the specified type. The original CMBDataFrame, cmbdf, is unaffected. If you would like to change cmbdf without creating a new variable, then use coords<-.CMBDataFrame (see examples below).

# Usage

```
## S3 method for class 'CMBDataFrame'
coords(cmbdf, new.coords)
```

#### **Arguments**

cmbdf A CMBDataFrame.

new.coords Specifies the new coordinate system ("spherical" or "cartesian") if a change of

coordinate system is desired.

### Value

If new.coords is unspecified, then the name of the coordinate system of cmbdf is returned. Otherwise a new CMBDataFrame is returned equivalent to cmbdf but having the desired change of coordinates

```
## Create df with no coords, then create df2 with cartesian coords
df <- CMBDataFrame(nside = 16)
df
coords(df)
df2 <- coords(df, new.coords = "cartesian")
coords(df2)

## Change the coords of df directly (to spherical)
coords(df) <- "spherical"
coords(df)</pre>
```

coords.CMBWindow 11

coords.CMBWindow

Coordinate system from a CMBWindow

# Description

This function returns the coordinate system used in a CMBWindow. The coordinate system is either "cartesian" or "spherical"

# Usage

```
## S3 method for class 'CMBWindow'
coords(win, new.coords)
```

# **Arguments**

new.coords specifies the new coordinate system ("spherical" or "cartesian") if a change of

coordinate system is desired

cmbdf a CMBWindow.

#### **Details**

If a new coordinate system is specified, using e.g. new.coords = "spherical", the coordinate system of the CMBWindow will be converted

# Value

If new.coords is unspecified, then the name of the coordinate system of win is returned. Otherwise a new CMBWindow is returned equivalent to win but having the desired change of coordinates

```
## Create win with sperical coords, then change it to win1 with cartesian coords
win <- CMBWindow(theta = c(0,pi/2,pi/2), phi = c(0,0,pi/2))
coords(win)
win1 <- coords(win, new.coords = "cartesian")
coords(win1)
## Change back to spherical coordinates

coords(win1) <- "spherical"
coords(win1)</pre>
```

12 coords.HPDataFrame

coords.data.frame

Create a new data.frame with a given coordinate system

# **Description**

This does not affect the original object unless new coordinate system is directly assigned.

#### Usage

```
## S3 method for class 'data.frame'
coords(df, new.coords)
```

# **Arguments**

df a data.frame with columns labelled x, y, z (for cartesian) or theta, phi (for spher-

ical colatitude and longitude respectively)

new.coords specifies the new coordinate system ("spherical" or "cartesian").

#### Value

A new data.frame whose coordinates are as specified by new.coords

# **Examples**

```
## Create df with no coords, then create df2 with spherical coords df <- data.frame(x = c(1,0,0), y = c(0,1,0), z = c(0,0,1)) df  df2 <- coords(df, new.coords = "spherical") \\ df2 
## The function coords does not affect the original object. ## To change the coords assign a new value ("spherical or "cartesian")  coords(df, new.coords = "spherical") \\ df \\ coords(df) <- "spherical" \\ df
```

coords.HPDataFrame

Coordinate system from a HPDataFrame

# Description

Add or change coordinates in a HPDataFrame. This does not affect the argument object hpdf. Instead it returns a new HPDataFrame with the desired coordinates. To change hpdf directly see coords<-.HPDataFrame.

covCMB 13

#### **Usage**

```
## S3 method for class 'HPDataFrame'
coords(hpdf, new.coords, healpix.only = FALSE)
```

#### **Arguments**

hpdf a HPDataFrame.

new.coords specifies the new coordinate system ("spherical" or "cartesian")

healpix.only boolean. If TRUE then columns x,y,z or theta, phi will be ignored and removed

if present. This forces the coordinates to be found from HEALPix pixel indices

only

### **Details**

If columns exist labelled x,y,z (cartesian) or theta, phi (colatitude and longitude respectively), then these will be treated as the coordinates of hpdf and converted accordingly. If columns x,y,z or theta,phi are not present then the healpix pixel indices as given by pix(hpdf) are used for assigning coordinates.

#### Value

A HPDataFrame with columns x,y,z (cartesian) or theta, phi (colatitude and longitude respectively)

# **Examples**

covCMB

Sample covariance for CMB

# **Description**

This function provides an empirical covariance estimate for data in a CMBDataFrame or data.frame. It places data into bins.

14 covPwSp

#### **Usage**

```
covCMB(cmbdf, num.bins = 10, sample.size, max.dist = pi, breaks,
  equiareal = TRUE, calc.max.dist = FALSE)
```

#### **Arguments**

cmbdf is a CMBDataFrame or data.frame num.bins specifies the number of bins sample.size optionally specify the size of a simple random sample to take before calculating covariance. This may be useful if the full covariance computation is too slow. max.dist an optional number between 0 and pi specifying the maximum geodesic distance to use for calculating covariance. Only used if breaks is unspecified. breaks optionally specify the breaks manually using a vector giving the break points between cells. This vector has length num.bins since the last break point is taken as max.dist. If equiareal = TRUE then these breaks should be  $cos(r_i)$ where  $r_i$  are radii. If equiareal = FALSE then these breaks should be  $r_i$ . equiareal if TRUE then the bins have equal spherical area. If false then the bins have equal annular widths. Default is TRUE. calc.max.dist if TRUE then the max.dist will be calculated from the locations in cmbdf. Otherwise either max. dist must be specified or max. dist will default to pi.

#### Value

An object of class CMBCovariance consisting of a data.frame containing sample covariance values, bin centers, and number n of data point pairs whose distance falls in the corresponding bin. The first row of this data.frame corresponds to the sample variance. The attribute "breaks" contains the break points used. The returned data.frame has num.bins + 1 rows since the first row, the sample variance, is not counted as a bin.

covPwSp	Covariance estimate via power spectra	

# **Description**

This function provides a covariance estimate using the values of the estimated power spectra.

# Usage

```
covPwSp(PowerSpectra, Ns)
```

# Arguments

PowerSpectra a data frame which first column lists values of multipole moments and the second column gives the corresponding values of CMB power spectra.

N a number of points in which the covariance estimate is computed on the interval [-1,1]

downloadCMBmap 15

#### Value

A data frame which first column is 1-d grid starting at -1+1/Ns and finishing at 1 with the step 2/Ns. The second column is the values of estimated covariances on this grid.

#### References

Formula (2.1) in Baran A., Terdik G. Power spectrum estimation of spherical random fields based on covariances. Annales Mathematicae et Informaticae 44 (2015) pp. 15–22.

Power Spectra data are from Planck Legacy Archive http://pla.esac.esa.int/pla/#cosmology

# **Examples**

```
N <- 20000
COM_PowerSpectra <- downloadCMBPS(link=1)

Cov_est <- covPwSp(COM_PowerSpectra[,1:2], N)
plot(Cov_est, type="1")

## Plot the covariance estimate as a function of angular distances
plot(acos(Cov_est[,1]), Cov_est[,2], type ="1", xlab ="angular distance", ylab ="Estimated Covariance")</pre>
```

download CMB map

Download CMB Maps from Planck Public Data Release.

# Description

The function downloadCMBmap downloads CMB maps from http://irsa.ipac.caltech.edu/data/Planck/release\_2/all-sky-maps/matrix\_cmb.html.

# Usage

```
downloadCMBmap(link = 1, destfile)
```

### **Arguments**

link A character string naming the URL of a resource to be downloaded.

destfile A character string with the file name for the downloaded file to be saved. Tilde-

expansion is performed.

### **Details**

CMB maps have been produced by the COMMANDER, NILC, SEVEM, and SMICA pipelines, respectively.

For each pipeline, the intensity maps are provided at Nside = 2048, at 5 arcmin resolution, and the polarization maps are provided at Nside = 1024 at 10 arcmin resolution.

link = 1: CMB Maps produced by Commander with Nside=1024;

link = 2: CMB Maps produced by NILC with Nside=1024;

link = 3: CMB Maps produced by SEVEM with Nside=1024;

link = 4: CMB Maps produced by SMICA with Nside=1024;

16 downloadCMBPS

```
link = 5: CMB Maps produced by Commander with Nside=2048;
link = 6: CMB Maps produced by NILC with Nside=2048;
link = 7: CMB Maps produced by SEVEM with Nside=2048;
link = 8: CMB Maps produced by SMICA with Nside=2048;
```

#### Value

CMB Map Fits File

#### References

```
Planck Public Data Release 2 Maps http://irsa.ipac.caltech.edu/data/Planck/release_ 2/all-sky-maps/matrix_cmb.html
```

Other fits maps can also be downloaded using the general command download.file.

#### **Examples**

```
## Download Commander with Nside=1024 and save in the default folder
## as "../rcosmo/CMB_map_commander1024.fits"
downloadCMBmap(link=1)
## Download SMICA with Nside=2048 and save in the default folder
## as "../rcosmo/CMB_map_smica2048.fits"
downloadCMBmap(link=8)
## Download SMICA with Nside=1024 and save in the specified folder,
## fpr example, "C:/CMB_map_smica1024.fits"
downloadCMBmap(link=8, destfile="C:/CMB_map_smica1024.fits")
```

downloadCMBPS

Download CMB Power Spectra from Planck Legacy Archive.

# **Description**

The function downloadCMBPS downloads CMB power spectra components from http://pla.esac.esa.int/pla/#cosmology.

# Usage

```
downloadCMBPS(link = 1, destfile)
```

#### **Arguments**

link The URL to download the file

destfile A character string with the file name for the downloaded file to be saved. Tilde-

expansion is performed.

fmf 17

#### **Details**

```
link = 1: Best-fit LCDM CMB power spectra from the baseline Planck TT, TE, EE+lowE+lensing (2 <= ell <= 2508).

link = 2: Baseline high-ell Planck TT power spectra (2 <= ell <= 2508).

link = 3: Baseline high-ell Planck EE power spectra (2 <= ell <= 1996).

link = 4: Baseline high-ell Planck TE power spectra (2 <= ell <= 1996).

link = 5: Low-ell Planck EB power spectra (2 <= ell <= 29).

link = 6: Low-ell Planck BB power spectra (2 <= ell <= 29).
```

#### Value

The Data Frame with CMB Power Spectra and a txt file in destfile

#### References

```
Planck Legacy Archive http://pla.esac.esa.int/pla/#cosmology
```

#### **Examples**

fmf

First Minkowski functional

# Description

This function returns an area of the spherical region where measured values are above of the specified threshold level alpha.

### Usage

```
fmf(cmbdf, alpha, var)
```

# **Arguments**

```
cmbdf a CMB Data Frame.

var an index of CMBDataFrame column with measured values 
alpha a threshold level
```

#### Value

The area of the exceedance region

#### References

Leonenko N., Olenko A. (2014) Sojourn measures of Student and Fisher-Snedecor random fields. Bernoulli, 20:1454-1483.

# **Examples**

```
n <- 64  
cmbdf <- CMBDataFrame(nside=n, I = rnorm(12*n^2), coords = "cartesian", ordering = "nested")  
fmf(cmbdf, 0, 4)  
fmf(cmbdf, 2, 4)  
win <- CMBWindow(theta = c(0,pi/2,pi/2), phi = c(0,0,pi/2))  
cmbdf.win <- window(cmbdf, new.window = win)  
fmf(cmbdf.win, 0, 4)
```

 ${\tt geoArea.CMBDataFrame}$   ${\tt Geodesic\ area\ covered\ by\ a\ {\tt CMBDataFrame}}$ 

### **Description**

Gives the surface on the unit sphere that is encompassed by all pixels in cmbdf

# Usage

```
## S3 method for class 'CMBDataFrame'
geoArea(cmbdf)
```

# Arguments

cmbdf

a CMBDataFrame

# Value

the sum of the areas of all pixels (rows) in cmbdf

```
## At low resolution, a few data points can
## occupy a large pixel area, e.g.:
cmbdf <- CMBDataFrame(nside = 1, spix = c(1,2,3))
pix(cmbdf)
## The total number of Healpix points at nside=1 equals 12. As cmbdf has 3 Helpix
## it occupies pi = 1/4*(surface area of unit sphere)</pre>
```

geoArea.CMBWindow 19

```
geoArea(cmbdf)
plot(cmbdf, size = 5, hp.boundaries = 1)
```

geoArea.CMBWindow

Geodesic area of a CMBWindow

# Description

Geodesic area of a CMBWindow

# Usage

```
## S3 method for class 'CMBWindow'
geoArea(win)
```

# **Arguments**

win

a CMBWindow

#### Value

Tthe spherical area inside win

# **Examples**

```
## A window that covers 1/8 of the unit sphere is constructed and its area is ## pi/2 = 1/8*(surface area of unit sphere)
win <- CMBWindow(theta = c(0,pi/2,pi/2), phi = c(0,0,pi/2))
geoArea(win)
```

 ${\tt geoArea.HPDataFrame}$ 

Geodesic area covered by a HPDataFrame

# **Description**

Gives the surface on the unit sphere that is encompassed by all pixels in hpdf

# Usage

```
## S3 method for class 'HPDataFrame'
geoArea(hpdf)
```

# **Arguments**

hpdf

a HPDataFrame

20 geoDist

#### Value

the sum of the areas of all pixels (rows) in hpdf

#### **Examples**

```
## Generate random I for HPDataFrame
hp1 <- HPDataFrame(I=rnorm(5), nside = 1, spix = c(1,1,2,2,3))
pix(hp1)

## The total number of Healpix points at nside=1 equals 12. As hp1 has five
## I values at 3 Helpix points, then the occupied area is
## pi = 1/4*(surface area of unit sphere)

geoArea(hp1)
plot(hp1, size = 5, hp.boundaries = 1)</pre>
```

geoDist

Geodesic distance on the unit sphere

# **Description**

Get geodesic distance between points on the unit sphere

# Usage

```
geoDist(p1, p2, include.names = FALSE)
```

# **Arguments**

p1 A data. frame with rows specifying numeric points located on the unit sphere.

It should have columns labelled x,y,z for Cartesian or theta, phi for spherical

colatitude and longitude respectively.

p2 Same as p1.

include.names Boolean. If TRUE then the row and column names of the returned matrix will

be taken from the points in p1 and p2 (see examples below).

### Value

Let n denote the number of rows of p1 and let m denote the number of rows of p2. Then the returned object is an n by m matrix whose entry in position ij is the geodesic distance from the ith row of p1 to the jth row of p2.

```
p1 <- data.frame(diag(3))
colnames(p1) <- c("x", "y", "z")
p1
p2 <- data.frame(x=c(1,0), y=c(0,3/5), z=c(0,4/5))
p2
geoDist(p1, p2, include.names = FALSE)</pre>
```

header 21

header

Get the FITS headers from a CMBDataFrame

# **Description**

Get the FITS headers from a CMBDataFrame

# Usage

```
header(cmbdf)
```

# **Arguments**

cmbdf

a CMBDataFrame.

#### Value

The FITS headers belonging to the FITS file from which cmbdf data was imported

# **Examples**

```
df <- CMBDataFrame("CMB_map_smica1024.fits")
df.sample <- CMBDataFrame(df, sample.size = 10000)
header(df.sample)</pre>
```

**HPDataFrame** 

HPDataFrame class

# **Description**

HPDataFrames are a type of data.frame designed to carry data located on the unit sphere. Each row of a HPDataFrame is associated with a HEALPix pixel index. The HPDataFrame also holds an attribute called nside which stores the HEALPix Nside parameter (i.e., the resolution of the HEALPix grid that is being used). Unlike CMBDataFrame, HPDataFrames may have repeated pixel indices. They are made this way so that multiple data points falling within a given pixel can be stored in different rows of any given HPDataFrame.

#### Usage

```
HPDataFrame(..., nside, ordering = "nested", auto.spix = FALSE, spix)
```

# **Arguments**

```
... data, can be named vectors or a data.frame
```

nside integer number  $2^k$ , the nside parameter, i.e, resolution ordering the HEALPix ordering scheme ("ring" or "nested")

is.CMBDat

auto.spix boolean. If TRUE then spix will be found from the coordinates provided in the

data. That is, each row of data will be assigned the pixel index of its closest HEALPix pixel center. There must be columns x,y,z for cartesian or theta, phi

for spherical colatitude and longitude respectively

spix a vector of HEALPix pixel indices indicating the pixel locations of the data.

Note that spix is ignored if auto.spix = TRUE

# **Examples**

```
hp1 <- HPDataFrame(I=rnorm(5), nside = 1, spix = c(1,1,2,2,3)) pix(hp1) coords(hp1, new.coords = "cartesian") class(hp1)
```

is.CMBDat

Check if an object is of class CMBDat

# Description

Check if an object is of class CMBDat

# Usage

```
is.CMBDat(cmbdf)
```

# Arguments

cmbdf

Any R object

# Value

TRUE if cmbdf is a CMBDat object, otherwise FALSE

```
cmbdat <- CMBReadFITS("CMB_map_smica1024.fits", mmap = TRUE)
class(cmbdat)
is.CMBDat(cmbdat)</pre>
```

is.CMBDataFrame 23

is.CMBDataFrame

Check if an object is of class CMBDataFrame

# Description

Check if an object is of class CMBDataFrame

# Usage

```
is.CMBDataFrame(cmbdf)
```

# Arguments

 ${\sf cmbdf}$ 

Any R object

# Value

TRUE if cmbdf is a CMBDataFrame, otherwise FALSE

# **Examples**

```
df <- CMBDataFrame(nside = 16)
is.CMBDataFrame(df)
df2 <- coords(df, new.coords = "cartesian")
is.CMBDataFrame(df2)</pre>
```

is.CMBWindow

Check if an object is a CMBWindow

# Description

Check if an object is a CMBWindow

# Usage

```
is.CMBWindow(win)
```

# Arguments

win

any object

# Value

TRUE or FALSE depending if win is a CMBWindow

24 jacobiPol

# **Examples**

```
win <- CMBWindow(x=0,y=3/5,z=4/5,r=0.8, set.minus = TRUE) is.CMBWindow(win)
```

is.HPDataFrame

 $Check\ if\ an\ object\ is\ of\ class\ {\tt HPDataFrame}$ 

# Description

Check if an object is of class HPDataFrame

# Usage

```
is.HPDataFrame(hpdf)
```

#### **Arguments**

hpdf

Any R object

# Value

TRUE if hpdf is a HPDataFrame, otherwise FALSE

# **Examples**

```
df <- CMBDataFrame(nside = 16)
is.HPDataFrame(df)

df <- HPDataFrame(I = rep(0,12), nside = 1)
is.HPDataFrame(df)</pre>
```

jacobiPol

Calculate Jacobi polynomial values

# Description

Calculate Jacobi polynomial values of degree L at given point T in [-1,1].

# Usage

```
jacobiPol(a, b, L, T)
```

# **Arguments**

L The degree of Jacobi polynomial

T Given point in [-1,1].

(a, b) The parameters of Jacobi polynomial

maxDist.CMBDataFrame 25

#### Value

Jacobi polynomial values

#### **Source**

```
http://dlmf.nist.gov/18.9
```

# **Examples**

```
jacobiPol(0,0,5,0)
jacobiPol(2,-5,2,-1)
jacobiPol(1,2,4,0.5)
```

maxDist.CMBDataFrame

Get the maximum distance between all points in a CMBDataFrame

# Description

Get the maximum distance between all points in a CMBDataFrame

# Usage

```
## S3 method for class 'CMBDataFrame'
maxDist(cmbdf)
```

# **Arguments**

cmbdf

a CMBDataFrame object

# Value

maximum distance between all points

```
## For CMBDataFrame with all Healpix ponts included it must be pi
cmbdf <- CMBDataFrame(nside = 4)
pix(cmbdf)
maxDist(cmbdf)

## Example for CMBDataFrame with Healpix only ponts 1 and 2 included

cmbdf <- CMBDataFrame(nside = 4, spix =c(1,2))
pix(cmbdf)
maxDist(cmbdf)</pre>
```

26 minDist

maxDist.CMBWindow

Get the maximum distance between all points in a CMBWindow

### **Description**

Get the maximum distance between all points in a CMBWindow

#### Usage

```
## S3 method for class 'CMBWindow'
maxDist(win)
```

# **Arguments**

win

a CMBWindow object

# Value

the maximum distance between window's points

# **Examples**

```
## win is a equilateral spherical triangle which sides are pi/2 win <- CMBWindow(theta = c(0,pi/2,pi/2), phi = c(0,0,pi/2)) maxDist(win)
```

minDist

Get the minimum distance between points

# **Description**

Get the minimum distance between a point and points in a data frame

# Usage

```
minDist(df, point)
```

# **Arguments**

df

A data. frame with columns x,y,z for cartesian or theta, phi for spherical colatitude and longitude respectively. The rows must correspond to points on the unit sphere. If this is a  ${\tt HPDataFrame}$  or  ${\tt CMBDataFrame}$  and coordinate columns are missing, then coordinates will be assigned based on  ${\tt HEALPix}$  pixel indices.

point

A point on the unit sphere in cartesian coordinates.

# Value

the shortest distance from point to the points specified by the rows of df

nest2ring 27

#### **Examples**

```
## Using a CMBDataFrame with HEALPix coordinates only
cmbdf <- CMBDataFrame(nside = 1, spix = c(1,5,12), ordering = "ring")
plot(cmbdf, hp.boundaries = 1, col = "blue", size = 5)
p < -c(0,0,1)
minDist(cmbdf, p) # no need to have coordinates
\hbox{\it \#\# Using a HPDataFrame with HEALPix coordinates only}\\
hp <- HPDataFrame(nside = 1, I = rep(0,3), spix = c(1,5,12))
minDist(hp, p) # notice no need to have coordinates
## Using a data.frame with cartesian coordinates
coords(hp) <- "cartesian"</pre>
df \leftarrow data.frame(x = hp$x, y = hp$y, z = hp$z)
minDist(df, p)
## Using a data.frame with spherical coordinates
coords(hp) <- "spherical"</pre>
df <- data.frame(theta = hp$theta, phi = hp$phi)</pre>
minDist(df, p)
```

nest2ring

Convert nest to ring ordering

# **Description**

Convert from "nested" to "ring" ordering

nest2ring computes the HEALPix pixel index in the "ring" ordering scheme from the pixel index in the "nested" ordering scheme.

### Usage

```
nest2ring(nside, pix)
```

# **Arguments**

nside is the HEALPix nside parameter.

pix is the set or subset of pixel indices at nside. If pix is left blank then all pixels are

converted.

# Value

the output is the corresponding set of pixel in the ring ordering scheme.

```
# compute HEALPix indices in the ring ordering scheme
nside <- 8
pix <-c(1,2,23)
nest2ring(nside,pix)</pre>
```

28 nestSearch\_step

### **Description**

Finds the closest HEALPix pixel center to a given target point, specified in Cartesian coordinates, using an efficient nested search algorithm. HEALPix indices are all assumed to be in the "nested" ordering scheme.

# Usage

```
nestSearch(target, nside, index.only = FALSE, j = 0:log2(nside),
  demo.plot = FALSE)
```

### **Arguments**

target is a vector of Cartesian coordinates for the target point on  $S^2$  nside is an integer number  $2^k$  for which the HEALPix points are searched

pixel at each step in red

#### Value

if index.only = TRUE then the output will be a HEALPix index. If index.only FALSE then the output is the list containing the HEALPix index and Cartesian coordinate vector of the HEALPix point closest to target.

# **Examples**

```
# Find the pix index and Cartesian coordinates of the HEALPix point # at nside closest to the target point c(0,0,1) h <- nestSearch(c(0,0,1), nside=1024) cat("Closest HEALPix point to (0,0,1) at nside = 1024 is (",h$xyz,")")
```

```
nestSearch_step nestSearch_step
```

# Description

Search for the closest HEALPix pixel to a target point, where the search is restricted to within HEALPix pixel, pix.j1, at resolution j1. The returned value is a HEALPix pixel (and, optionally, the cartesian coordinates of its center) at resolution j2, where j2 > j1. All pixels are assumed to be in nested ordering scheme.

# Usage

```
nestSearch_step(target, j1 = j2, j2, pix.j1 = 0, demo.plot = FALSE)
```

nside.CMBDataFrame 29

### **Arguments**

target	is the target point on S^2 in spherical coordinates.
j1	is the lower resolution, with $j1 < j2$ .
j2	is the upper resolution.
pix.j1	is the initial pix index at resolution j1, i.e., the j1-level pixel to search in. If $pix.j1 = 0$ then all pixels will be searched (slow).
demo.plot	If TRUE then a plot will be produced with target pixel in yellow and closest pixel in red

#### **Details**

```
j1 and j2 are HEALPix resolution parameters, i.e., nside = 2^{j}.
```

nestSearch\_step(target, j2, j1, pix.j1) searches within the subregion pix.j1, where pix.j1 is a HEALPix pixel index at resolution j1. The return value is the HEALPix point closest to target, at resolution j2.

Setting pix.j1 = 0 (the default) searches for the HEALPix point closest to target at resolution j2, among all HEALPix points at resolution j1.

# Value

A list containing the Cartesian coordinates, xyz, and the HEALPix pixel index, pix, of the closest HEALPix pixel center to the target point, target, at resolution j2

# Examples

```
# search for the HEALPix pixel center closest to North pole # (0,0,1) at level 3 nestSearch_step(target = c(0,0,1), j2 = 3, j1 = -1, demo.plot = TRUE )
```

nside.CMBDataFrame

HEALPix Nside parameter from a CMBDataFrame

#### **Description**

This function returns the HEALPix Nside parameter of a CMBDataFrame

### Usage

```
## S3 method for class 'CMBDataFrame'
nside(cmbdf)
```

# **Arguments**

cmbdf a CMB Data Frame.

### Value

The HEALPix Nside parameter

# **Examples**

```
df <- CMBDataFrame(nside = 16)
nside(df)</pre>
```

nside.HPDataFrame

HEALPix Nside parameter from a HPDataFrame

# Description

This function returns the HEALPix Nside parameter of a HPDataFrame

# Usage

```
## S3 method for class 'HPDataFrame'
nside(hpdf)
```

# **Arguments**

hpdf

a HPDataFrame.

#### Value

The HEALPix Nside parameter

# **Examples**

```
df <- HPDataFrame(I = rep(0,12), nside = 1) nside(df)
```

 $ordering. {\tt CMBDataFrame} \ \ \textit{HEALPix ordering scheme from a CMBDataFrame}$ 

# Description

This function returns the HEALPix ordering scheme from a CMBDataFrame. The ordering scheme is either "ring" or "nested".

# Usage

```
## S3 method for class 'CMBDataFrame'
ordering(cmbdf, new.ordering)
```

# Arguments

cmbdf a CMB Data Frame.

new.ordering specifies the new ordering ("ring" or "nest") if a change of ordering scheme is

desired.

ordering.HPDataFrame

#### **Details**

If a new ordering is specified, using e.g. new.ordering = "ring", the ordering scheme of the CMB-DataFrame will be converted.

#### Value

The name of the HEALPix ordering scheme that is used in the CMBDataFrame cmbdf

# **Examples**

```
df <- CMBDataFrame(nside = 1, ordering = "nested")
ordering(df)
df1 <- ordering(df, new.ordering = "ring")
ordering(df1)</pre>
```

ordering.HPDataFrame

HEALPix ordering scheme from a HPDataFrame

# **Description**

This function returns the HEALPix ordering scheme from a HPDataFrame. The ordering scheme is either "ring" or "nested". If a new ordering is specified, using e.g. new.ordering = "ring", the ordering scheme of the HPDataFrame will be converted.

#### Usage

```
## S3 method for class 'HPDataFrame'
ordering(hpdf, new.ordering)
```

# **Arguments**

hpdf a HPDataFrame.

new.ordering specifies the new ordering ("ring" or "nest") if a change of ordering scheme is

desired.

### Value

The name of the HEALPix ordering scheme that is used in the HPDataFrame hpdf, or a new hpdf with the desired new.ordering

```
df <- HPDataFrame(I = rep(0,12), nside = 1, ordering = "nested")
ordering(df)
df1 <- ordering(df, new.ordering = "ring")
ordering(df1)</pre>
```

32 pix.HPDataFrame

pix.CMBDataFrame

HEALPix pixel indices from CMBDataFrame

### **Description**

If new.pix is unspecified then this function returns the vector of HEALPix pixel indices from a CMBDataFrame. If new.pix is specified then this function returns a new CMBDataFrame with the same number of rows as cmbdf, but with pix attribute new.pix. Thus, new.pix must have length equal to nrow(cmbdf).

#### Usage

```
## S3 method for class 'CMBDataFrame'
pix(cmbdf, new.pix)
```

#### **Arguments**

cmbdf a CMBDataFrame.

new.pix optional vector of pixel indices with length equal to nrow(cmbdf)

#### Value

The vector of HEALPix pixel indices or, if new.pix is specified, a new CMBDataFrame.

# **Examples**

```
df <- CMBDataFrame("CMB_map_smica1024.fits", sample.size = 800000)
pix(df)</pre>
```

pix.HPDataFrame

HEALPix pixel indices from HPDataFrame

# Description

If new.pix is unspecified then this function returns the vector of HEALPix pixel indices from a HPDataFrame. If new.pix is specified then this function returns a new HPDataFrame with the same number of rows as hpdf, but with pix attribute new.pix. Thus, new.pix must have length equal to nrow(hpdf).

# Usage

```
## S3 method for class 'HPDataFrame'
pix(hpdf, new.pix)
```

#### **Arguments**

hpdf a HPDataFrame.

new.pix optional vector of pixel indices with length equal to nrow(hpdf)

pix2coords 33

#### Value

The vector of HEALPix pixel indices (integers) or, if new.pix is specified, a new HPDataFrame.

# **Examples**

```
df <- HPDataFrame(I = rep(0,12), nside = 1) pix(df)
```

pix2coords

Convert pixel indices to cartesian/spherical coordinates

# Description

Convert HEALPix pixel indices to cartesian or spherical coordinates

# Usage

```
pix2coords(nside, coords = "cartesian", ordering = "nested", spix)
```

# Arguments

nside the nside parameter (integer number  $2^k$ ) coords 'cartesian' or 'spherical' coordinates

ordering 'ring' or 'nested' ordering

spix optional integer or vector of sample pixel indices

### Value

```
a data.frame with columns 'x', 'y', 'z' (cartesian) or 'theta', 'phi' (spherical)
```

```
pix2coords(nside=1, spix=c(2,5))
pix2coords(nside=1, coords = "spherical", spix=c(2,5))
```

34 pixelWindow

pixelArea

Area of a HEALPix pixel

# **Description**

Get the area of a single HEALPix pixel

#### Usage

```
pixelArea(cmbdf)
```

### **Arguments**

cmbdf

 $a \; {\tt CMBDataFrame}$ 

#### Value

the area of a single HEALPix pixel at the nside resolution of cmbdf

### **Examples**

```
df <- CMBDataFrame("CMB_map_smica1024.fits")
pixelArea(df)

df1 <- CMBDataFrame(nside = 64, coords = "cartesian", ordering = "nested")
pixelArea(df1)</pre>
```

pixelWindow

Find high resolution pixels falling in a lower resolution window

# Description

Find all pixels in a higher resolution that fall within the specified pixel area at a lower resolution. All pixels are assumed to be in nested ordering.

# Usage

```
pixelWindow(j1, j2, pix.j1)
```

### **Arguments**

<u>.</u> 1	A :	The 1		:41- :	1 -	:0
31	An integer.	The lower	resolution,	with	1 =<	14.

j2 An integer. The upper resolution.

pix.j1 An integer. The pixel index at resolution j1 within which all pixels from resolu-

tion j2 will be returned. pix. j1 can also be a vector of non-zero pixel indices.

# Value

All pixels in resolution j2 that fall within the pixel pix.j1 specified at resolution j1

plot.CMBDataFrame 35

# **Examples**

```
pixelWindow(3, 3, 2)
pixelWindow(3, 4, 2)
pixelWindow(3, 5, 2)
```

plot.CMBDataFrame

Plot CMB Data

# **Description**

This function produces a plot from a CMBDataFrame.

# Usage

```
## S3 method for class 'CMBDataFrame'
plot(cmbdf, intensities = "I", add = FALSE,
  sample.size, type = "p", size = 1, box = FALSE, axes = FALSE,
  aspect = FALSE, col, back.col = "black", labels, hp.boundaries = 0,
  hpb.col = "gray", ...)
```

# **Arguments**

. . .

cmbdf	A CMBDataFrame.
intensities	The name of a column that specifies CMB intensities. This is only used if col is unspecified.
add	If TRUE then this plot will be added to any existing plot. Note that if back.col (see below) is specified then a new plot window will be opened and add = TRUE will have no effect.
sample.size	Optionally specifies the size of a simple random sample to take before plotting. This can make the plot less computationally intensive.
type	A single character indicating the type of item to plot. Supported types are: 'p' for points, 's' for spheres, 'l' for lines, 'h' for line segments from $z=0$ , and 'n' for nothing.
size	The size of plotted points.
box	Whether to draw a box.
axes	Whether to draw axes.
aspect	Either a logical indicating whether to adjust the aspect ratio, or a new ratio.
col	Specify the colour(s) of the plotted points.
back.col	Optionally specifies the background colour of the plot. This argument is passed to rgl::bg3d.
labels	Optionally specify a vector of labels to plot, such as words or vertex indices. If this is specified then rgl::text3d is used instead of rgl::plot3d. Then length(labels) must equal nrow(cmbdf).
hp.boundaries	Integer. If greater than 0 then HEALPix pixel boundaries at nside = hp.boundaries will be added to the plot.
hpb.col	Colour for the hp.boundaries.

Arguments passed to rgl::plot3d.

36 plot.CMBWindow

#### Value

A plot of the CMB data

# **Examples**

```
filename <- "CMB_map_smica1024.fits"
sky <- CMBDataFrame(filename)
plot(sky, sample.size = 800000)</pre>
```

plot.CMBWindow

Visualise a CMBWindow

# **Description**

Visualise a CMBWindow

# Usage

```
## S3 method for class 'CMBWindow'
plot(win, add = TRUE, type = "1", col = "red",
    size = 2, box = FALSE, axes = FALSE, aspect = FALSE, back.col,
    ...)
```

# **Arguments**

win	a CMBWindow
add	if TRUE then this plot will be added to any existing plot. Note that if back.col (see below) is specified then a new plot window will be opened and add = TRUE will have no effect
type	a single character indicating the type of item to plot. Supported types are: 'p' for points, 's' for spheres, 'l' for lines, 'h' for line segments from $z=0$ , and 'n' for nothing.
col	specify the colour(s) of the plotted points
size	the size of plotted points
box	whether to draw a box
axes	whether to draw axes
aspect	either a logical indicating whether to adjust the aspect ratio, or a new ratio.
back.col	specifies the background colour of the plot. This argument is passed to rgl::bg3d.
	arguments passed to rgl::plot3d
eps	the geodesic distance between consecutive points to draw on the window boundary

```
win1 <- CMBWindow(theta = c(0,pi/2,pi/2), phi = c(0,0,pi/2))
win2 <- CMBWindow(theta = c(2*pi/3,3*pi/4,3*pi/4,2*pi/3), phi = c(pi/4,pi/4,pi/3,pi/3))
plot(win1)
plot(win2)
```

plot.HPDataFrame 37

# Description

This function produces a plot from a HPDataFrame. If columns x,y,z (cartesian) or theta,phi (colatitude and longitude respectively) are present in hpdf, then these will be used as coordinates for plotting. Otherwise, the HEALPix indices as in pix(hpdf) will be used. If HEALPix indices are used and multiple rows correspond to a single pixel index, then beware that values may be obfuscated in the plot, and all locations are pixel centers.

# Usage

```
## S3 method for class 'HPDataFrame'
plot(hpdf, intensities = "I", add = FALSE,
  sample.size, type = "p", size = 1, box = FALSE, axes = FALSE,
  aspect = FALSE, col = "blue", back.col = "black", labels,
  hp.boundaries = 0, hpb.col = "gray", ...)
```

# **Arguments**

hpdf	a HPDataFrame.
add	if TRUE then this plot will be added to any existing plot. Note that if back.col (see below) is specified then a new plot window will be opened and add = TRUE will have no effect
sample.size	optionally specifies the size of a simple random sample to take before plotting. This can make the plot less computationally intensive
type	a single character indicating the type of item to plot. Supported types are: 'p' for points, 's' for spheres, 'l' for lines, 'h' for line segments from $z=0$ , and 'n' for nothing.
size	the size of plotted points
box	whether to draw a box
axes	whether to draw axes
aspect	either a logical indicating whether to adjust the aspect ratio, or a new ratio.
col	specify the colour(s) of the plotted points
back.col	optionally specifies the background colour of the plot. This argument is passed to rgl::bg3d.
labels	optionally specify a vector of labels to plot, such as words or vertex indices. If this is specified then rgl::text3d is used instead of rgl::plot3d. Then length(labels) must equal nrow(hpdf)
hp.boundaries	integer. If greater than 0 then HEALPix pixel boundaries at $nside = hp.boundaries$ will be added to the plot
hpb.col	colour for the hp.boundaries
	arguments passed to rgl::plot3d

## Value

A plot of the data locations according to coordinate columns or HEALPix index

38 plotHPBoundaries

## **Examples**

plotHPBoundaries

Plot HEALPix pixel boundaries

# Description

Plot the HEALPix pixel boundaries at nside

# Usage

```
plotHPBoundaries(nside, eps = pi/90, col = "gray", lwd = 1, ordering,
  incl.labels = 1:(12 * nside^2), nums.col = col, nums.size = 1,
  font = 2, ...)
```

# Arguments

nside	the HEALPix nside parameter (integer number $2^{\kappa}$ )
eps	controls the smoothness of the plot, smaller eps implies more samples
col	the colour of plotted boundary lines
lwd	the thickness of the plotted boundary lines
ordering	optionally specify an ordering scheme from which to plot HEALPix pixel numbers. Can be either "ring" or "nested"
incl.labels	If ordering is specified then this parameter sets the pixel indices that will be displayed (default is all indices at nside)
nums.col	specifies the colour of pixel numbers if ordering is specified
nums.size	specifies the size of pixel numbers if ordering is specified
font	A numeric font number from 1 to 5, used if ordering is specified
	arguments passed to rgl::plot3d

## Value

produces a plot of the HEALPix pixel boundaries

```
plotHPBoundaries(1, eps = pi/90, col = "red")
plotHPBoundaries(2, eps = pi/90, col = "green")
```

print.CMBDataFrame 39

# Description

This function neatly prints the contents of a CMB Data Frame.

# Usage

```
## S3 method for class 'CMBDataFrame'
print(cmbdf, ...)
```

# **Arguments**

```
cmbdf a CMB Data Frame.
... arguments passed to print.tbl_df
```

# Value

Prints contents of the CMB data frame to the console.

# **Examples**

```
df <- CMBDataFrame("CMB_map_smica1024.fits", sample.size = 800000)
print(df)
df</pre>
```

print.HPDataFrame

Print a HPDataFrame

# Description

This function neatly prints the contents of a HPDataFrame.

# Usage

```
## S3 method for class 'HPDataFrame'
print(hpdf, ...)
```

# Arguments

```
hpdf a HPDataFrame.
... arguments passed to print.tbl_df
```

# Value

Prints contents of the HPDataFrame to the console.

40 rbind.CMBDataFrame

#### **Examples**

```
\label{eq:df} \begin{split} &\text{df} <\text{- HPDataFrame}(I = rep(0,12), \ nside = 1, \ ordering = "nested") \\ &\text{print}(df) \\ &\text{df} \end{split}
```

rbind.CMBDataFrame

rbind for CMBDataFrames

#### **Description**

Add a new row or rows to a CMBDataFrame. All arguments passed to . . . must be CMBDataFrames. If the CMBDataFrame arguments have overlapping pixel indices then all but one of the non-unique rows will be deleted unless unsafe = TRUE. If unsafe = TRUE then a HPDataFrame will be returned instead of a CMBDataFrame.

## Usage

```
## S3 method for class 'CMBDataFrame'
rbind(..., deparse.level = 1, unsafe = FALSE)
```

#### Arguments

... A number of CMBDataFrames

unsafe

A boolean. If the CMBDataFrame arguments have overlapping pixel indices then all but one of the non-unique rows will be deleted unless unsafe = TRUE. If unsafe = TRUE then a HPDataFrame will be returned instead of a CMBDataFrame.

#### See Also

See the documentation for rbind

```
df <- CMBDataFrame(nside = 1, I = 1:12)

df.123 <- CMBDataFrame(df, spix = c(1,2,3))
 df.123
 df.234 <- CMBDataFrame(df, spix = c(2,3,4))
 df.234

df.1234 <- rbind(df.123, df.234)
 df.1234
 class(df.1234) # A CMBDataFrame
 pix(df.1234)

df.123234 <- rbind(df.123, df.234, unsafe = TRUE)
 df.123234
 class(df.123234) # A HPDataFrame
 pix(df.123234)</pre>
```

rcosmo 41

rcosmo

rcosmo - This Documentation is a place holder.

## **Description**

To be completed

## Section1

To be completed

# Section2

To be completed

# **Section 3**

To be completed

# **Dependencies**

To be completed

# Author(s)

Daniel Fryer <d.fryer@latrobe.edu.au>

resolution

 $\textit{Get the arcmin resolution from a $\tt CMBDataFrame}$ 

# Description

Get the arcmin resolution from a CMBDataFrame

# Usage

```
resolution(cmbdf)
```

## **Arguments**

cmbdf

a CMBDataFrame.

## Value

The arcmin resolution as specified by the FITS file where the data was sourced

```
df <- CMBDataFrame("CMB_map_smica1024.fits")
resolution(df)</pre>
```

42 sampleCMB

ring2nest

Convert ring to nest ordering.

## **Description**

ring2nest converts HEALPix pixel indices in the 'ring' ordering scheme to HEALPix pixel indices in the 'nested' ordering scheme.

#### Usage

```
ring2nest(nside, pix)
```

## **Arguments**

nside is the HEALPix nside parameter (integer number  $2^k$ )

pix is a vector of HEALPix pixel indices, in the 'ring' ordering scheme.

#### Value

the output is a vector of HEALPix pixel indices in the 'nested' ordering scheme.

# **Examples**

```
# compute HEALPix indices in the ring order of the set pix given in the nest order at nside nside <- 8 pix <-c(1,2,23) ring2nest(nside,pix)
```

sampleCMB

Take a simple random sample from a CMBDataFrame

## **Description**

This function returns a CMBDataFrame with size sample.size, whose rows comprise a simple random sample of the rows from the input CMBDataFrame.

# Usage

```
sampleCMB(cmbdf, sample.size)
```

## **Arguments**

cmbdf a CMB Data Frame. sample.size the desired sample size.

## Value

A CMBDataFrame with size sample.size, whose rows comprise a simple random sample of the rows from the input CMBDataFrame.

sphericalharmonics 43

## **Examples**

```
df <- CMBDataFrame("CMB_map_smica1024.fits")
plot(sampleCMB(df, sample.size = 800000))</pre>
```

sphericalharmonics

Compute spherical harmonic values at given points on the sphere.

## **Description**

The function spherical harmonics computes the spherical harmonic values for the given 3D Cartesian coordinates.

## Usage

```
sphericalharmonics(L, m, xyz)
```

#### **Arguments**

L The degree of spherical harmonic (L=0,1,2,...)

m The order number of the degree-L spherical harmonic (m=-L,-L+1,...,L-1,L)

xyz Dataframe for given points in 3D cartesian coordinates

## Value

values of spherical harmonics

#### References

See https://en.wikipedia.org/wiki/Table\_of\_spherical\_harmonics

It uses equation (7) in Hesse, K., Sloan, I. H., & Womersley, R. S. (2010). Numerical integration on the sphere. In Handbook of Geomathematics (pp. 1185-1219). Springer Berlin Heidelberg,

but instead of the order k=1,...,2L+1 in the book we use m=k-L-1.

```
## Calculate spherical harmonic value at the point (0,1,0) with L=5, m=2
point<-data.frame(x=0,y=1,z=0)
sphericalharmonics(5,2,point)
## Calculate spherical harmonic values at the point (1,0,0), (0,1,0), (0,0,1) with L=5, m=2
points<-data.frame(diag(3))
sphericalharmonics(5,2,points)</pre>
```

summary.CMBDataFrame Summarise a CMBDataFrame

## **Description**

This function produces a summary from a CMBDataFrame.

#### Usage

```
## S3 method for class 'CMBDataFrame'
summary(cmbdf, intensities = "I")
```

## **Arguments**

cmbdf a CMBDataFrame.

intensities the name of a column specifying CMB intensities (or potentially another nu-

meric quantity of interest)

#### Value

A summary includes window's type and area, total area covered by observations, and main statistics for intensity values

## **Examples**

```
df <- CMBDataFrame("CMB_map_smica1024.fits")
df.sample <- CMBDataFrame(df, sample.size = 800000)
summary(df.sample)
win1<- CMBWindow(x=0,y=3/5,z=4/5,r=0.8)
df.sample1 <- window(df.sample, new.window = win1)
summary(df.sample1)</pre>
```

summary.CMBWindow

Summarise a CMBWindow

# Description

This function produces a summary from a CMBWindow

# Usage

```
## S3 method for class 'CMBWindow'
summary(win)
```

#### **Arguments**

cmbdf a CMBWindow

triangulate 45

#### Value

A summary includes window's type and area

#### **Examples**

```
win <- CMBWindow(theta = c(0,pi/2,pi/2), phi = c(0,0,pi/2)) summary(win) win1<- CMBWindow(x=0,y=3/5,z=4/5,r=0.8, set.minus = TRUE) summary(win1)
```

triangulate

Triangulate a polygonal CMBWindow

#### **Description**

Triangulate a polygonal CMBWindow

## Usage

```
triangulate(win)
```

## **Arguments**

win

a CMBWindow object

## Value

a list of CMBWindow polygons or minus.polygons, each having 3 vertices and representing a triangle. If winType of win does not include "minus" then these triangles have pairwise disjoint interiors and their union is equal to the original polygon, win. Otherwise, if winType of win does include "minus" the triangles are the same as for the non-minus type above, but have "minus" types.

```
## Example 1
win <- CMBWindow(theta = c(2*pi/3,3*pi/4,3*pi/4, 2*pi/3), phi = c(pi/4,pi/4,pi/3,pi/3))
win
plot(win)
win1 <- triangulate(win)
win1
summary(win1[[1]])
plot(win1[[1]], add= FALSE, col="green")
plot(win1[[2]], col="blue")
## Example 2: triangilation minus-type polygon
win <- CMBWindow(theta = c(pi/5,pi/3,pi/4, pi/3, pi/5), phi = c(pi/5,pi/5, pi/4, pi/3,pi/3), set.minus =TRUE)</pre>
```

46 window.CMBDat

```
win
plot(win)
summary(win)
win1 <- triangulate(win)
win1
plot(win1[[1]], add= FALSE, col="green")
plot(win1[[2]], col="blue")
plot(win1[[3]], col="yellow")
summary(win1[[1]])
summary(win1[[2]])
summary(win1[[2]])</pre>
```

window.CMBDat

Get a sub window from a CMBDat object

## **Description**

This function returns a data.frame containing the data in cmbdat restricted to the CMBWindow new.window

#### Usage

```
## S3 method for class 'CMBDat'
window(cmbdat, new.window, intersect = TRUE)
```

## Arguments

cmbdat a CMBDat object.

new.window A single CMBWindow object or a list of them.

intersect A boolean that determines the behaviour when win is a list containing BOTH

regular type and "minus" type windows together (see details).

## **Details**

Windows that are tagged with set.minus (see CMBWindow) are treated differently from other windows.

If the argument is a list of CMBWindows, then interious of all windows whose winType does not include "minus" are united (let A be their union) and exteriors of all windows whose winType does include "minus" are intersected, (let B be their intersection). Then, provided that intersect = TRUE (the default), the returned data.frame will be the points of cmbdat\$data in the the intersection of A and B. Otherwise, if intersect = FALSE, the returned data.frame consists of the points of cmbdat\$data in the union of A and B.

Note that if A (resp. B) is empty then the returned data.frame will be the points of cmbdat in B (resp. A).

# Value

A CMBDataFrame containing the data in cmbdat restricted to the CMBWindow new.window

window.CMBDataFrame 47

#### **Examples**

```
win1 <- CMBWindow(theta = c(0,pi/2,pi/2), phi = c(0,0,pi/2)) cmbdat <- CMBReadFITS("CMB_map_smica1024.fits", mmap = TRUE) class(cmbdat) cmbdat.win <- window(cmbdat, new.window = win1) class(cmbdat.win)
```

window.CMBDataFrame

 $Get\ a\ sub\ window\ from\ {\tt CMBDataFrame}$ 

## **Description**

When new.window or in.pixels is unspecified this function returns the CMBWindow attribute of a CMBDataFrame. The return value is NULL if the window is full sky. When new.window is specified this function instead returns a new CMBDataFrame whose CMBWindow attribute is new.window

## Usage

```
## $3 method for class 'CMBDataFrame'
window(cmbdf, new.window, intersect = TRUE,
   in.pixels, in.pixels.res = 0)
```

#### Arguments

cmbdf	a CMBDataFrame.
new.window	optionally specify a new window in which case a new CMBDataFrame is returned whose CMBWindow is new.window. new.window may also be a list (see details section and examples).
intersect	A boolean that determines the behaviour when win is a list containing BOTH regular type and "minus" type windows together (see details).
in.pixels	A vector of pixels at resolution in.pixels.res whose union contains the window(s) win entirely, or if new.window is unspecified then this whole pixel is returned.
in.pixels.res	An integer. Resolution (i.e., $j$ such that nside = 2 <sup>j</sup> ) at which the in.pixels parameter is specified

#### **Details**

Windows that are tagged with set.minus (see CMBWindow) are treated differently from other windows.

If the argument is a list of CMBWindows, then interious of all windows whose winType does not include "minus" are united (let A be their union) and exteriors of all windows whose winType does include "minus" are intersected, (let B be their intersection). Then, provided that intersect = TRUE (the default), the returned CMBDataFrame will be the points of cmbdf in the the intersection of A and B. Otherwise, if intersect = FALSE, the returned CMBDataFrame consists of the points of cmbdf in the union of A and B.

Note that if A (resp. B) is empty then the returned CMBDataFrame will be the points of cmbdf in B (resp. A).

48 window.CMBDataFrame

#### Value

The window attribute of cmbdf or, if new.window/in.pixels is specified, a new CMBDataFrame.

```
## Example 1: Create a new CMBDataFrame with a window
cmbdf <- CMBDataFrame(nside = 64, coords = "cartesian", ordering = "nested")</pre>
win <- CMBWindow(theta = c(0,pi/2,pi/2), phi = c(0,0,pi/2))
cmbdf.win <- window(cmbdf, new.window = win)</pre>
plot(cmbdf.win)
window(cmbdf.win)
## Example 2: Change the window of an existing CMBDataFrame
cmbdf <- CMBDataFrame(nside = 64, coords = "cartesian", ordering = "nested")</pre>
\label{eq:cmbdf} window(cmbdf) <- win2 <- CMBWindow(theta = c(pi/6,pi/3,pi/3, pi/6),
                                    phi = c(0,0,pi/6,pi/6))
plot(cmbdf)
## Example 3: union of windows
## Create 2 windows
win1 <- CMBWindow(theta = c(0,pi/2,pi/2), phi = c(0,0,pi/2))
win2 <- CMBWindow(theta = c(2*pi/3,3*pi/4,3*pi/4, 2*pi/3),
                             phi = c(pi/4, pi/4, pi/3, pi/3))
plot(win1)
plot(win2)
## Create CMBDataFrame with points in the union of win1 and win2
cmbdf <- CMBDataFrame(nside = 64, coords = "cartesian", ordering = "nested")</pre>
cmbdf.win <- window(cmbdf, new.window = list(win1, win2), intersect = TRUE)</pre>
plot(cmbdf.win)
#' ## Example 4: intersection of windows
## Create 2 windows
win1 <- CMBWindow(theta = c(0,pi/2,pi/2), phi = c(0,0,pi/2))
win2 <- CMBWindow(theta = c(pi/4,pi/3,pi/3, pi/4),
                  phi = c(pi/4, pi/4, pi/3, pi/3))
plot(win1)
plot(win2)
## Create CMBDataFrame with points in the intersection of win1 and win2
cmbdf <- CMBDataFrame(nside = 64, coords = "cartesian", ordering = "nested")</pre>
cmbdf.win1 <- window(cmbdf, new.window = win1)</pre>
cmbdf.win12 <- window(cmbdf.win1, new.window = win2)</pre>
plot(cmbdf.win12)
plot(win1)
plot(win2)
```

window.data.frame 49

```
## Example 5: intersection of windows with "minus" type
## Create 2 windows with "minus" type
win1 <- CMBWindow(theta = c(0,pi/2,pi/2), phi = c(0,0,pi/2), set.minus =TRUE)
win2 <- CMBWindow(theta = c(pi/4,pi/3,pi/3, pi/4),
                  phi = c(pi/4, pi/4, pi/3, pi/3),
                  set.minus =TRUE)
plot(win1)
plot(win2)
## Create CMBDataFrame with points in the intersection of win1 and win2
cmbdf <- CMBDataFrame(nside = 64, coords = "cartesian", ordering = "nested")</pre>
cmbdf.win <- window(cmbdf, new.window = list(win1, win2))</pre>
plot(cmbdf.win)
## Example 6: intersection of windows with different types
##Create 2 windows, one with "minus" type
win1 <- CMBWindow(theta = c(0,pi/2,pi/2), phi = c(0,0,pi/2))
win2 <- CMBWindow(theta = c(pi/4,pi/3,pi/3,pi/4),
                  phi = c(pi/4, pi/4, pi/3, pi/3),
                  set.minus =TRUE)
plot(win1)
plot(win2)
## Create CMBDataFrame with points in the intersection of win1 and win2
cmbdf <- CMBDataFrame(nside = 64, coords = "cartesian", ordering = "nested")</pre>
cmbdf.win <- window(cmbdf, new.window = list(win1, win2), intersect = TRUE)</pre>
plot(cmbdf.win)
## Example 7: union of windows with different types
win1 <- CMBWindow(theta = c(0,pi/2,pi/2), phi = c(0,0,pi/2), set.minus =TRUE)
win2 <- CMBWindow(theta = c(pi/4,pi/3,pi/3, pi/4), phi = c(pi/4,pi/4,pi/3,pi/3))
plot(win1)
plot(win2)
## Create CMBDataFrame with points in the union of win1 and win2
cmbdf <- CMBDataFrame(nside = 64, coords = "cartesian", ordering = "nested")</pre>
cmbdf.win <- window(cmbdf, new.window = list(win1, win2), intersect = FALSE)</pre>
plot(cmbdf.win)
```

window.data.frame

Get a sub window from a data.frame

#### **Description**

This function returns a data frame containing the data in df restricted to the CMB Window new.window

50 window.HPDataFrame

#### Usage

```
## S3 method for class 'data.frame'
window(df, new.window, intersect = TRUE)
```

#### **Arguments**

df a data.frame. Must have columns labelled x,y,z specifying cartesian coordinates,

or columns labelled theta, phi specifying colatitude and longitude respectively.

new.window A single CMBWindow object or a list of them.

intersect A boolean that determines the behaviour when win is a list containing BOTH

regular type and "minus" type windows together (see details).

#### **Details**

Windows that are tagged with set.minus (see CMBWindow) are treated differently from other windows.

If the argument is a list of CMBWindows, then interiors of all windows whose winType does not include "minus" are united (let A be their union) and exteriors of all windows whose winType does include "minus" are intersected, (let B be their intersection). Then, provided that intersect = TRUE (the default), the returned data.frame will be the points of df in the the intersection of A and B. Otherwise, if intersect = FALSE, the returned data.frame consists of the points of df in the union of A and B.

Note that if A (resp. B) is empty then the returned data.frame will be the points of df in B (resp. A).

#### Value

A data.frame containing the data in df restricted to the CMBWindow new.window

# **Examples**

```
win1 <- CMBWindow(theta = c(0,pi/2,pi/2), phi = c(0,0,pi/2))

cmbdf <- CMBDataFrame(nside = 4)

df2 <- coords(cmbdf, new.coords = "cartesian")

df <- as.data.frame(df2[,1:3])

df

df.win <- window(df, new.window = win1)

df.win
```

window.HPDataFrame

Get a sub window from a HPDataFrame

# Description

This function returns a HPDataFrame containing the data in hpdf restricted to the CMBWindow new.window. If the HPDataFrame has columns x,y,z or theta, phi then these will be used to determine locations with priority over the HEALPix indices in pix(hpdf) unless healpix.only = TRUE is given. Note that if healpix.only = TRUE then columns x,y,z or theta, phi will be discarded and replaced with pixel center locations.

window.HPDataFrame 51

#### Usage

```
## S3 method for class 'HPDataFrame'
window(hpdf, new.window, intersect = TRUE,
   healpix.only = FALSE)
```

#### **Arguments**

hpdf A HPDataFrame.

new.window A single CMBWindow object or a list of them.

intersect A boolean that determines the behaviour when win is a list containing BOTH

regular type and "minus" type windows together (see details).

healpix.only A boolean. If the HPDataFrame has columns x,y,z or theta, phi then these

will be used to determine locations with priority over the HEALPix indices in pix(hpdf) unless healpix.only = TRUE is given. Note that if healpix.only = TRUE then columns x,y,z or theta, phi will be discarded and replaced with pixel center

locations.

#### **Details**

Windows that are tagged with set.minus (see CMBWindow) are treated differently from other windows.

If the argument is a list of CMBWindows, then interiors of all windows whose winType does not include "minus" are united (let A be their union) and exteriors of all windows whose winType does include "minus" are intersected, (let B be their intersection). Then, provided that intersect = TRUE (the default), the returned data.frame will be the points of df in the the intersection of A and B. Otherwise, if intersect = FALSE, the returned data.frame consists of the points of df in the union of A and B.

Note that if A (resp. B) is empty then the returned data.frame will be the points of df in B (resp. A).

# Value

A HPDataFrame containing the data in hpdf restricted to the CMBWindow new.window

```
ns <- 16
hpdf <- HPDataFrame(nside = ns, I = 1:(12*ns^2))
hpdf
win1 <- CMBWindow(theta = c(0,pi/2,pi/2), phi = c(0,0,pi/2))
plot(hpdf); plot(win1)
hpdf.win <- window(hpdf, new.window = win1)
plot(hpdf.win, col = "yellow", size = 4, add = TRUE)
attributes(hpdf.win)
hpdf.win</pre>
```

52 winType

winType

Get/change winType

# **Description**

Get/change the winType (polygon or disk) of a CMBWindow. If new.type is missing then the winType of win is returned. Otherwise, a new window is returned with winType equal to new.type. If you want to change the winType of win directly, then use winType<-.

#### Usage

```
winType(win, new.type)
```

## **Arguments**

win a CMBWindow object or a list of such

new.type optionally specify a new type. Use this to change between "polygon" and "mi-

nus.polygon" or to change between "disc" and "minus.disc"

#### Value

If new. type is missing then the winType of win is returned. Otherwise a new window is returned with winType equal to new. type

```
win <- CMBWindow(theta = c(pi/2,pi/2,pi/3, pi/3), phi = c(0,pi/3,pi/3,0))
winType(win)

win1 <- CMBWindow(x=0,y=3/5,z=4/5,r=0.8)
winType(win1)
cmbdf <- CMBDataFrame(nside = 64, coords = "cartesian", ordering = "nested")
cmbdf.win1 <- window(cmbdf, new.window = win1)
plot(cmbdf.win1)

winType(win1)
cmbdf <- CMBDataFrame(nside = 64, coords = "cartesian", ordering = "nested")
cmbdf <- CMBDataFrame(nside = 64, coords = "cartesian", ordering = "nested")
cmbdf.win1 <- window(cmbdf, new.window = win1)
plot(cmbdf.win1)</pre>
```

# Index

*Topic <b>CMB</b>	goodroo CMPWindow 10
downloadCMBmap, 15	geoArea.CMBWindow, 19 geoArea.HPDataFrame, 19
downloadCMBPS, 16	· ·
*Topic Jacobi,Orthogonal	geoDist, 20
jacobiPol, 24	header, 21
*Topic Maps	HPDataFrame, 12, 13, 19, 21, 24, 26, 30–32,
- ·	37, 39, 40, 50
downloadCMBmap, 15 *Topic <b>Power</b>	37, 39, 10, 30
downloadCMBPS, 16	is.CMBDat, 22
*Topic <b>Spectra</b>	is.CMBDataFrame, 23
downloadCMBPS, 16	is.CMBWindow, 23
*Topic harmonic	is.HPDataFrame, 24
sphericalharmonics, 43	,
*Topic <b>polynomials.</b>	jacobiPol, 24
jacobiPol, 24	maxDist.CMBDataFrame, 25
*Topic <b>spherical</b>	maxDist.CMBWindow, 26
sphericalharmonics, 43	minDist, 26
areCompatibleCMBDFs, 3	mmap, 6, 8
as.CMBDataFrame, 3	
assumedConvex, 4	nest2ring, 27
assumed soft ex, 1	nestSearch, 28
cbind, 5	nestSearch_step, 28
cbind.CMBDataFrame, 5	nside.CMBDataFrame, 29
CMBDat, 6, 46	nside.HPDataFrame, 30
CMBDataFrame, 3, 5, 6, 10, 14, 18, 21, 25, 26,	
32, 34, 35, 40, 41, 44, 47	ordering.CMBDataFrame, 30
CMBReadFITS, 8	ordering.HPDataFrame, 31
CMBWindow, 4, 7, 9, 11, 19, 26, 36, 44–47,	niv CMDDataEnama 22
50–52	pix.CMBDataFrame, 32
coords.CMBDataFrame, 10	pix.HPDataFrame, 32
coords.CMBWindow, 11	pix2coords, 33
coords.data.frame, 12	pixelArea, 34
coords.HPDataFrame, 12	pixelWindow, 34 plot.CMBDataFrame, 35
covCMB, 13	•
covPwSp, 14	plot.CMBWindow, 36
	plot.HPDataFrame, 37
data.frame, $3, 6, 14, 20$	plotHPBoundaries, 38
download.file, <i>16</i>	print.CMBDataFrame, 39
downloadCMBmap, 15	print.HPDataFrame, 39
downloadCMBPS, 16	print.tbl_df,39
fmf, 17	rbind, 40
	rbind.CMBDataFrame, 40
geoArea.CMBDataFrame, 18	Rcosmo (rcosmo), 41

54 INDEX

```
rCosmo (rcosmo), 41
rcosmo, 41
rcosmo-package (rcosmo), 41
readFITS, 8
resolution, 41
ring2nest, 42
sampleCMB, 42
{\it spherical harmonics}, 43
\operatorname{subWindow}, 9
\verb|summary.CMBDataFrame|, 44|
summary.CMBWindow,44
suppressMessages, 3
triangulate, 45
window.CMBDat, 46
window.CMBDataFrame, 47
window.data.frame, 49
window.HPDataFrame, 50
winType, 52
```