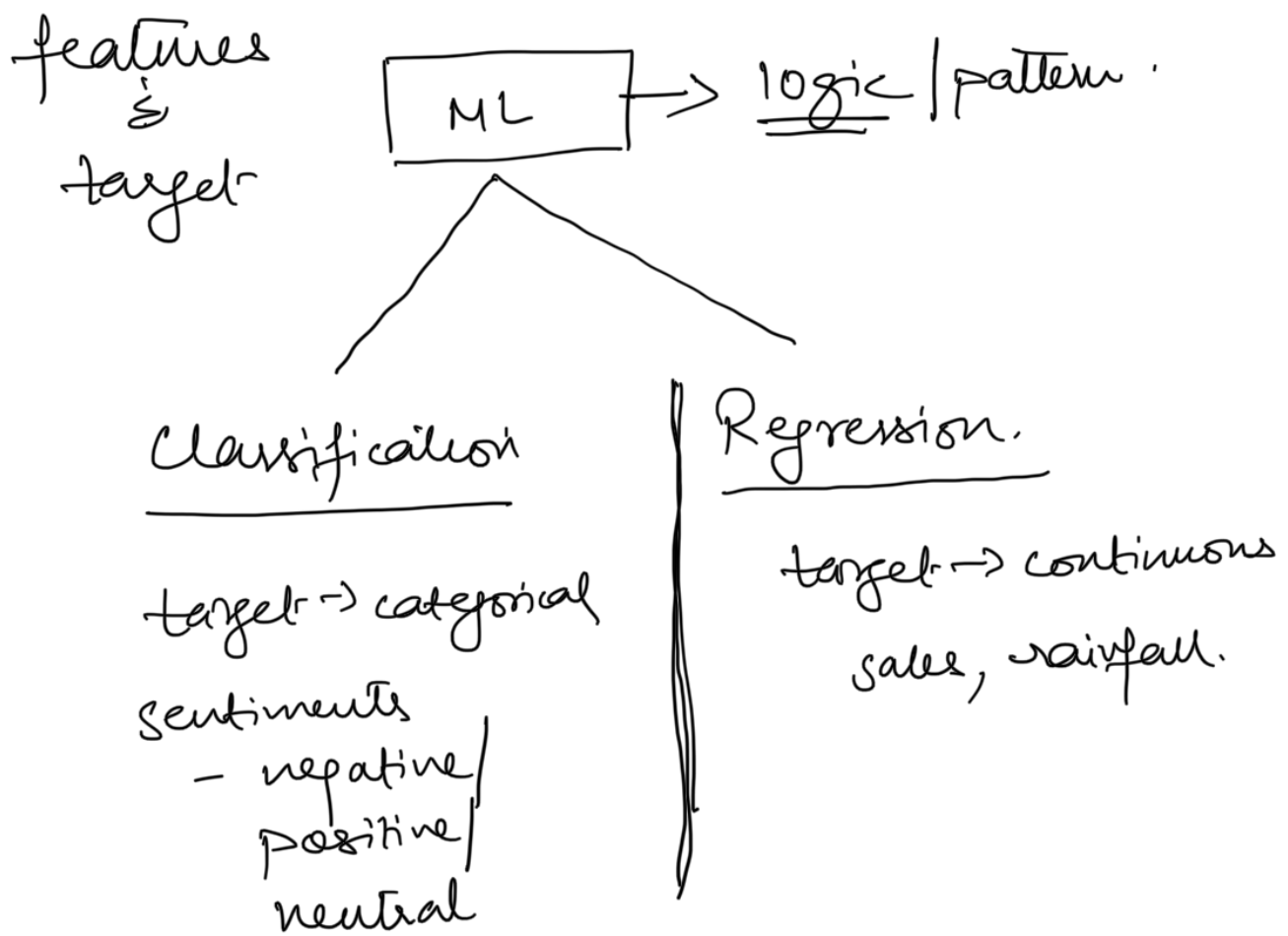
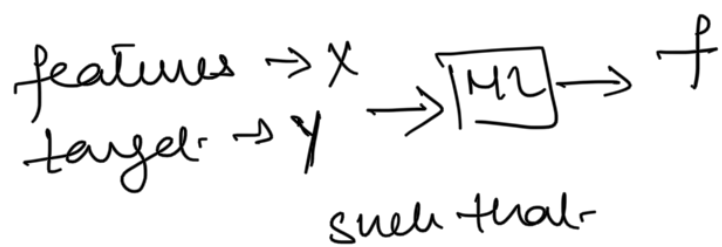


ML model



Regression



$$y = f(x)$$

predicting price of a house.

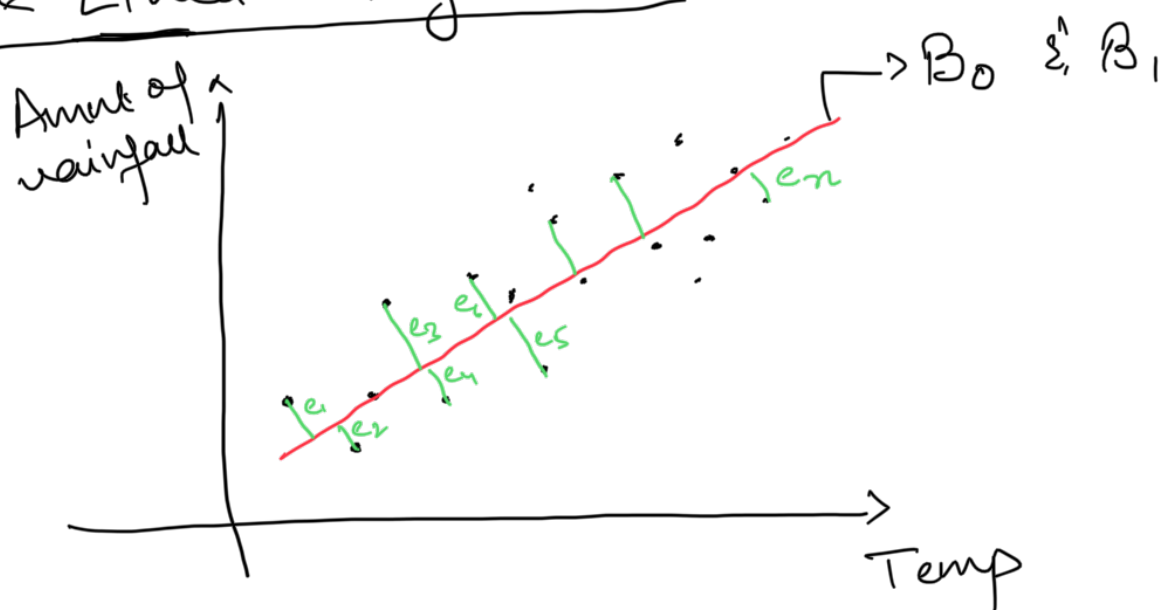
IV \rightarrow carpet area

$$\text{price} = \boxed{f}(\text{carpet area})$$

\hookrightarrow red line

The linear models

① Simple Linear Regression.



$$\frac{e_1^2 + e_2^2 + e_3^2 + e_4^2 + \dots + e_n^2}{n} = \text{MSE} \downarrow$$

General equation of the line.

$$y = B_0 + B_1 x \quad \{ y = mx + c \}$$

Best fit line. How?? By minimize the errors.

Draw a line $L_1 \rightarrow E_1 \rightarrow$
 $L_2 \rightarrow E_2 < E_1$
 $L_3 \rightarrow E_3 < E_2 < E_1$
 \vdots

$B_0 + B_1 x$
 $B_2 + B_3 x$
 $B_4 + B_5 x$
 \vdots
 $B_n + B_{n+1} x$

Objectives In the eqn of line
if you want min error then find
best β_0 and β_1 (parameters)

$$Y = \beta_0 + \beta_1 X$$

$\searrow \quad \swarrow$
 parameters / coefficients

$\beta_0 \rightarrow$ intercept $\beta_1 \rightarrow$ slope

a. Least square method.

$$Y = \beta_0 + \beta_1 X \longrightarrow \text{equation 1}$$

$$Y_i = \beta_0 + \beta_1 X_i + e_i \longrightarrow \text{equation (2)}$$

Y_i = Actual value

\hat{Y}_i = Predicted value.

$$\hat{Y}_i = \hat{\beta}_0 + \hat{\beta}_1 X_i \quad \text{--- (1) } \{i = 1, 2, \dots, n\}$$

$$\underline{Y_i} = \underline{\hat{Y}_i} + \underline{\hat{e}_i} \quad \text{--- (2) } \rightarrow$$

eg $\boxed{\begin{matrix} \uparrow \\ \text{LS} \end{matrix}}$

you have a model (β_0, β_1)

$$\begin{aligned} \hat{Y}_i &= \hat{\beta}_0 + \hat{\beta}_1 (\text{day}) \\ &= 202 \end{aligned}$$

$$Y_i = 205$$

" " " " " "

$$y_i = 202 + 0$$

$$\hat{y}_i + \hat{e}_i$$

$$\begin{array}{l} \hat{y}_1 = \beta_0 + \beta_1 x_1 \quad \hat{y}_2 = \beta_0 + \beta_1 x_2 \quad \dots \quad \hat{y}_n = \beta_0 + \beta_1 x_n \\ y_1 = \hat{y}_1 + \hat{e}_1 \quad y_2 = \hat{y}_2 + \hat{e}_2 \quad \dots \quad y_n = \hat{y}_n + \hat{e}_n \end{array}$$

$$\hat{e}_1^2 + \hat{e}_2^2 + \dots + \hat{e}_n^2 = \sum_{i=1}^n \hat{e}_i^2$$

eg:-

	Actuals	Preds	e	
Monday	202	205	-3	6
Tuesday	203	200	3	

$$RSS = \sum_{i=1}^n e_i^2$$

$$= \sum_{i=1}^n (y_i - \hat{y}_i)^2 \quad \leftarrow y_i = \hat{y}_i + \hat{e}_i$$

$$\downarrow \quad RSS = \sum_{i=1}^n (y_i - \beta_0 - \beta_1 x_i) \quad \hat{y}_i = \beta_0 + \beta_1 x_i$$

Minimize RSS

$$\text{Minimize } \sum_{i=1}^n (y_i - \beta_0 - \beta_1 x_i)$$

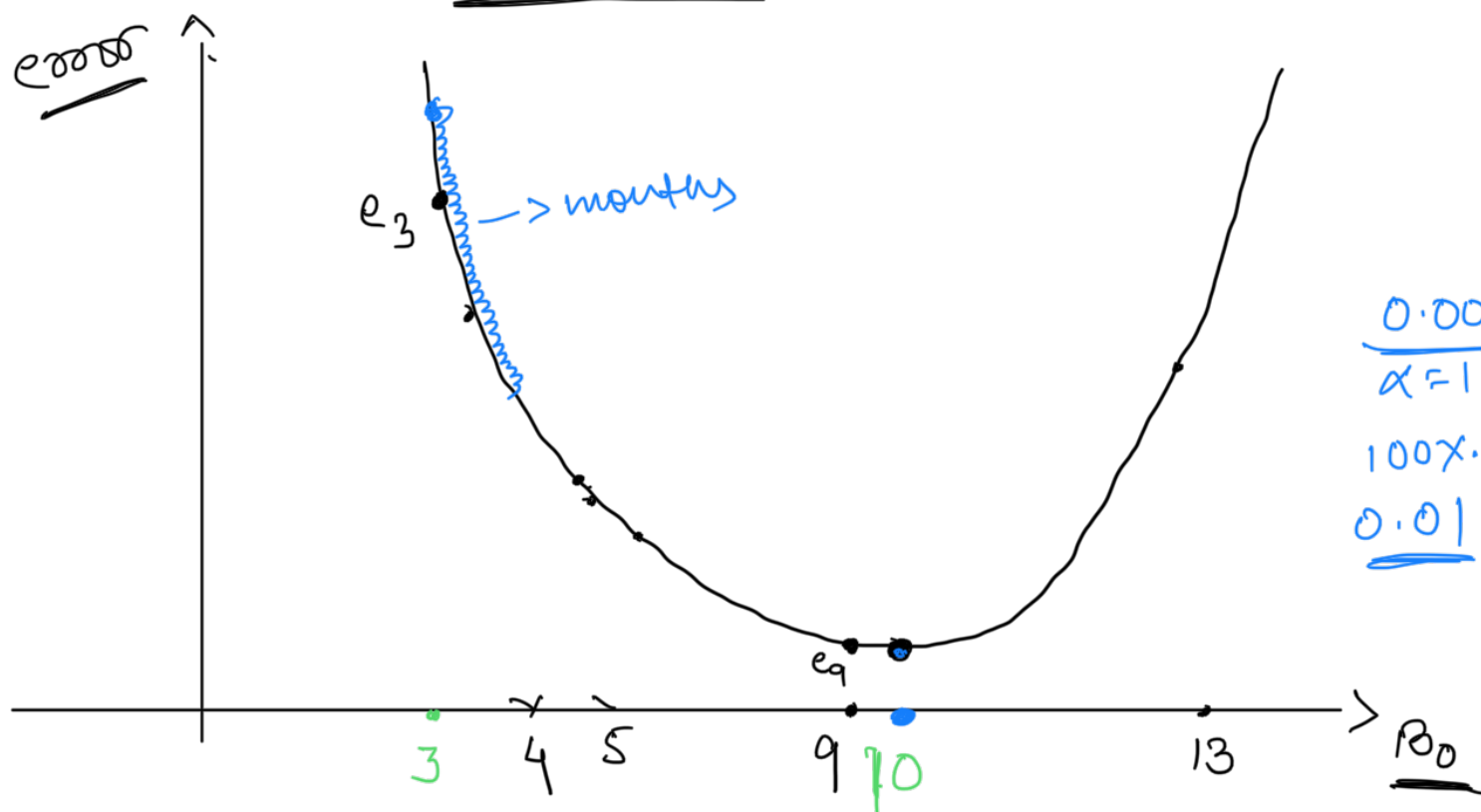
Solve this, β_0 and β_1 which is giving you the least error.

b. Gradient Descent

Obj:- Find β_0 and β_1 such that error is

learn:

β_0 vs Error



$$\boxed{\text{New } \beta_0 = \text{Old } \beta_0 - \text{slope}} \quad \text{sign}$$

$$= \underline{13} - (\underline{+K})$$

$$\text{new } \beta_0 = \underline{13 - K}$$

action \rightarrow move K steps towards left

$$\boxed{\beta_{\text{new}} = \beta_{\text{old}} - \alpha \cdot \frac{dE}{d\beta_0}} \quad \text{--- (1)}$$

$$\boxed{\beta_{\text{new}} = \beta_{\text{old}} - \alpha \cdot \frac{dE}{d\beta_1}} \quad \text{--- (2)}$$

- ✓ ① Where are you starting??
- ✓ ② How much iterations??
- ✓ ③ How much is learning rate??

Model evaluation: —

MAE
MSE
RMSE

Coefficient of determination :- (R^2)

Sales: 2 1 6 5 -3 7

Next value :- $\text{mean}(\quad)$; my

Marketing spend: 10 12 6 2 3 5

Value :- better than my ✓
worse than my.

f1	Target
a	10
b	20
c	30
d	40
e	?? 25 (my)

For e; using mean pred
pred = 25

; use a ML model 1
pred = 30

; use a ML model 2
pred = 32

Actual = 40

When I am assuming the mean pred.
 $\frac{1}{n} \sum_{i=1}^n (\hat{y}_i - y_i)^2$

$$\text{Error} = \sum_{i=1}^n (y_i - \hat{y}_i)$$

$$TSS = \sum_{i=1}^n (y_i - \bar{y})^2$$

using a model $\text{preds} \gg \bar{y}$

$$(y_i - \text{preds}) < (y_i - \bar{y})$$

$$RSS < TSS$$

Quantify how less is RSS to TSS. OR

how much the model is performing better than just mean prediction.

$$R^2 = \frac{TSS - RSS}{TSS}$$

"explained"

$$\text{SLR}(X) \rightarrow Y$$

① $TSS = RSS$

$$\frac{TSS - RSS}{TSS} = 0$$

② $RSS = 0$

$$R^2 = \underline{\underline{1}}$$

③ $0 < R^2 < 1$

$$R^2 = 0.2$$

$$R^2 = 0.9$$

30% of variance of σ_p
" " " " σ_p

90% of variance.