Minor corrections to the thesis

Abstract

- 1. "We first present" (was in past tense)
- 2. "we also adapt the criteria for use in blocked experiments" (was in passive voice)

Introduction

- 1. Page 2. ".. all responses are put in an n-dimensional vector \boldsymbol{Y} "
- 2. Page 3. Extra "further" removed

Chapter 2. Background and Related Work

- 1. Page 9. ".. and derived the *DP*-criterion: minimising $(F_{p,d;1-\alpha_{DP}})^p|(\boldsymbol{X'X})^{-1}|$ " (was ν instead of d)
- 2. Page 10. Expanding the explanation of where L-optimality comes from: "If we are interested in the functions of parameters given by $L'\beta$, then the variance-covariance matrix of $L'\hat{\beta}$ is..."
- 3. Page 10. Explaining why Sidak's corrections were used: "Here we shall use Sidak's correction (Šidák, 1967), which is..."
- 4. Page 10. ".. for example, *I*-optimality, that is minimising **average** prediction variance"
- 5. Page 11. Adding a comment regarding the reasons to use the compound criterion approach: "..., and explore how this compromise <...> At the same time the relationships between the components of combined criteria..."
- 6. Page 11. ".. prior knowledge of the **experimenter**" (misprint)
- 7. Page 12. ".. it is sometimes **necessary** to allocate units in blocks"
- 8. Page 12. ".. its $(i, j)^{th}$ element"
- 9. Page 12. ".. and β_B is the vector of block effects"
- 10. Page 13. ".. matrix whose elements indicate the treatments"
- 11. Page 13. ".. the number of replications after subtracting the number of replicates taken for the estimation of block contrasts."
- 12. Page 15. ".. Goos and Vandebroek (2001) considered the three cases when D-optimal designs for split-plot experiments do not depend on the value of η ; in other practical cases an estimate of the variance ratio is to be provided."

- 13. Page 16. "Arnouts and Goos (2012) presented a coordinate-exchange algorithm ... examples of D- and I-optimal designs."
- 14. Page 16. ".. assumed possible values of η_i " (misprint)
- 15. Page 16. ".. in the presence" (misprint)
- 16. Page 17. "In this thesis, due to the primary interest being the quality of inference,.."
- 17. Page 18. Removed "Therefore" in the 4th paragraph.

Chapter 3. Compound criteria. Some amendments

- 1. Page 20. Adding significance levels where they were missed: $F_{n-p-d,d;1-\alpha_{LoF}}$ instead of $F_{n-p-d,d}$, and on Figure 3.1 on page 21.
- 2. Page 21. Expanding interpretation of the plot in Figure 3.1: "Larger numbers of available residual degrees of freedom ..."
- 3. Page 21. "The third component in both criteria corresponds to the DF-efficiency defined in (2.7)."
- 4. Pages 22 and 24. Tables 3.1 and 3.4: added columns with DF-efficiency values
- 5. Page 23. "..therefore, their DF-efficiency values $\frac{n-d}{n}$ are below 75% (i.e. when d > 10)."
- 6. Page 24. "..the design optimal <...> (#12) is also optimal with respect to the criterion with equal weights put on the DF- and LoF-components"
- 7. Page 25. "..except for the point number 18-19 and the point number 36-37"
- 8. Page 25. "..the resulting efficiency values. It also would be sensible.." (breaking the sentence)
- 9. Page 27. Adding extra comment: "This particular parametrisation <...> designs which are more than 50% efficient."
- 10. Page 27. Adding subsection 3.2.2 Optimal designs (no text amendments)
- 11. Pages 28 and 29. Tables 3.6 and 3.7: added columns with DF-efficiency values
- 12. Page 29. Paraphrasing the last paragraph: "It was desired to alter the form of an efficiency's contribution."

Chapter 4. Generalised Compound Criteria

- 1. Page 31. Adding bullet points in the chapter introduction
- 2. Page 32 33. Adding subsections 4.1.1 and 4.1.2
- 3. Page 32. Equation (4.3) ε in the subscripts
- 4. Page 33. "..how large the magnitude of each of the potential terms is assumed to **possibly** be.."
- 5. Page 34. "..we incorporate L-optimality for the primary terms.."
- 6. Pages 35 and 36. "..and (4.11)"
- 7. Page 35. Adding the reference to Section 3.1.1
- 8. Page 37. Adding the reference to DuMouchel and Jones (1994))
- 9. Page 37. Amending the derivation of the formula for the confidence region for β_2 over the posterior distribution (introducing the corresponding F-quantile).
- 10. Page 39. "Henceforth" instead of "Here and further on"
- 11. Page 40. "The results should" instead of "The results would"
- 12. Page 43. Table 4.6, 2nd part, column names: L, LP, LoF(LP) and Bias(L)
- 13. Page 44. Rephrasing: "similar tendency seems to be true"
- 14. Page 49. Paragraph 3. Adding an explanation regarding large LoFefficiencies in case of smaller τ^2 : "Such consistently high performance..."
- 15. Page 53. "..each factor can take five levels.."
- 16. Page 53. "all third and **fourth** order terms are taken as potentially missed terms"
- 17. Page 53. Adding: "Most of the replicates are at corner points..."
- 18. Page 58. Changing the name of Section 4.3 (to "Blocked Experiments") and adding subsection 4.3.1 "Generalised criteria"
- 19. Page 58. Adding " β_B is the vector of fixed block effects,..."
- 20. Page 59. β_B instead of β_0
- 21. Page 59. "Therefore, ..."
- 22. Page 60. "the *D*-optimal design"
- 23. Page 64. Adding a comment regarding ignoring the orthonormalisation: "Ignoring such a requirement would amend the formulae of the bias components, but in general it should not be expected to considerably influence the resulting optimal designs and their performances;

though the orthonormalisation step should not be blindly omitted, especially if the prediction bias is of a particular interest."

Chapter 5. MSE-based Criteria

- 1. Page 66. Adding an explanation of 'pseudo-Bayesian': "..(hence we shall refer to such an approach as "pseudo-Bayesian").."
- 2. Page 67. ".. and \boldsymbol{u} , \boldsymbol{v} are column vectors"
- 3. Page 68. Adding a definition of $\tilde{\boldsymbol{\beta}}_{2i}$ after the equation (5.5): "Here $\tilde{\boldsymbol{\beta}}_{2i}$, i=1..N independent random vectors sampled from $\mathcal{N}(\mathbf{0}, \tau^2 \sigma^2 \boldsymbol{I}_a)$."
- 4. Page 70. Emphasising the computational advantage of the trace-based criterion: "The main advantage is the absence of the necessity of any additional numerical evaluations, and..."
- 5. Page 74. Amending the interpretation: "..the decreased scale of the potentially missed contamination results in an easier achievable compromise between..."
- 6. Page 74. ".. in the corresponding tables"
- 7. Page 74. Rephrasing: "..in the case of MSE(D)-efficient designs with smaller τ^2 ."

Chapter 6. MSE-based Criteria for Blocked Experiments

- 1. Page 78. Equation (6.2): β_B and β_1 instead of $\tilde{\beta}_b$ and $\tilde{\beta}_p$
- 2. Page 82. "in the design #8"
- 3. Page 84. Adding a comment regarding relative efficiencies between the designs optimal w.r.t. the continuous and point-prior-based criteria: "As for the efficiency losses..."
- 4. Page 85. Adding explanation about two centre points requirement: "..two centre points to ensure a good intercept estimate.."
- 5. Page 87. "LoF(DP)-"
- 6. Page 88. Amending the explanation of the "Relative efficiency": "The last column of this table, "Relative Efficiency," is.."
- 7. Page 91. Misprint: "experimenters"

Chapter 7. MSE-based Criteria for Multistratum Experiments

- 1. Page 94. Changing **REML Methodology** from a subsection to section
- 2. Page 96. Changing the title of Section 7.2.2: "Yates' procedure"
- 3. Page 97. " $m_i = ...$ units"

- 4. Page 98. Adding the Construction procedure subsection title (no text amendments)
- 5. Page 103. Expanding the sentence: "Now we need to evaluate the number of degrees of freedom for.."
- 6. Page 103. ".. the factors applied at the current and all higher strata"
- 7. Page 104. Explaining why $\tau^2 = \sqrt{1/q}$ was used: "As this number tends to become.."
- 8. Page 104. "Regarding the **third-order** potential terms.."
- 9. Page 106. "(designs #3)"
- 10. Page 106. ".. designs #5 and #7 provide the worst performance with respect to the MSE(L) and LP-components respectively"
- 11. Page 109. "i.e. designs #6 in Table 7.6"
- 12. Page 111. Adding the **Discussion** subsection title (no text amendments)

Chapter 8. Conclusions and Future Work

1. Page 114. Adding a comment regarding advantages and disadvantages of the Pareto frontier approach: "On one hand, such an algorithm would result in a set of designs..."

References

- Arnouts, H. and Goos, P. (2012) Staggered-level designs for experiments with more than one hard-to-change factor. *Technometrics*, **54**, 355–366.
- DuMouchel, W. and Jones, B. (1994) A simple Bayesian modification of D-optimal designs to reduce dependence on an assumed model. *Technometrics*, **36**, 37–47.
- Goos, P. and Vandebroek, M. (2001) D-optimal response surface designs in the presence of random block effects. *Computational statistics & data analysis*, **37**, 433–453.
- Šidák, Z. (1967) Rectangular confidence regions for the means of multivariate normal distributions. *Journal of the American Statistical Association*, **62**, 626–633.