

# Loan Analysis for Lending Club Platform

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For my project I selected the data set that I found on Lending Club's website (<https://www.lendingclub.com>). The data is provided for potential investors. The data set contains information about loans that were issued from 2007 to the third quarter of 2017.

Lending Club is the world's largest peer-to-peer lending platform that enables borrowers to obtain a loan, and investors to purchase notes backed by payments made on loans.

The goals of the project are

1. To find the equation that best predicts the probability of whether the loan will be paid off or not.
2. To understand what might cause the probability to change.
3. Find the classifier that can predict whether the loan will be paid off or not with higher accuracy

An investor earns money when loan is fully paid off and loses money when loan is charged off. If an investor obtains the results generated by the model that classify loans he would be able to make better investment decisions.

While I was reviewing Lending Club's website I found out that investors can see the information such as loan rate, loan term, interest rate, borrower's FICO score, loan amount and loan purpose. Moreover, they have an ability to filter by borrower's employment length and monthly income.

In order to collect the data I downloaded (data source: <https://www.lendingclub.com/info/download-data.action>) and merged 11 files that contain data from 2007 to the third quarter of 2017. To reduce the loading time I implemented the following steps.

*#1. read in a few records of the input file to identify the classes of the input file and assign that class*

```
data_2007_2011 <- read.csv(file="https://cdn-stage.fedweb.org/fed-2/13/LoanStats3a.csv",
                           stringsAsFactors=T, header=T, nrows=5)

data_2012_2013 <- read.csv(file="https://cdn-stage.fedweb.org/fed-2/13/LoanStats3b.csv",
                           stringsAsFactors=T, header=T, nrows=5)

data_2014 <- read.csv("https://cdn-stage.fedweb.org/fed-2/13/LoanStats3c.csv",
                     stringsAsFactors=T, header=T, nrows=5)

data_2015 <- read.csv("https://cdn-stage.fedweb.org/fed-2/13/LoanStats3d.csv",
                     stringsAsFactors=T, header=T, nrows=5)

data_2016_q1 <- read.csv("https://cdn-stage.fedweb.org/fed-2/13/LoanStats_2016Q1.csv",
                        stringsAsFactors=T, header=T, nrows=5)

data_2016_q2 <- read.csv("https://cdn-stage.fedweb.org/fed-2/13/LoanStats_2016Q2.csv",
                        stringsAsFactors=T, header=T, nrows=5)

data_2016_q3 <- read.csv("https://cdn-stage.fedweb.org/fed-2/13/LoanStats_2016Q3.csv",
                        stringsAsFactors=T, header=T, nrows=5)

data_2016_q4 <- read.csv("https://cdn-stage.fedweb.org/fed-2/13/LoanStats_2016Q4.csv",
                        stringsAsFactors=T, header=T, nrows=5)
```

```
data_2017_q1 <- read.csv("https://cdn-stage.fedweb.org/fed-2/13/LoanStats_2017Q1.csv",
  stringsAsFactors=T, header=T, nrows=5)
```

```
data_2017_q2 <- read.csv("https://cdn-stage.fedweb.org/fed-2/13/LoanStats_2017Q2.csv",
  stringsAsFactors=T, header=T, nrows=5)
```

```
data_2017_q3 <- read.csv("https://cdn-stage.fedweb.org/fed-2/13/LoanStats_2017Q3.csv",
  stringsAsFactors=T, header=T, nrows=5)
```

#### *#2. replace all missing values with NAs*

```
data_2007_2011 <- data_2007_2011[is.na(data_2007_2011)]
```

```
data_2012_2013 <- data_2012_2013[is.na(data_2012_2013)]
```

```
data_2014 <- data_2014[is.na(data_2014)]
```

```
data_2015 <- data_2015[is.na(data_2015)]
```

```
data_2016_q1 <- data_2016_q1[is.na(data_2016_q1)]
```

```
data_2016_q2 <- data_2016_q1[is.na(data_2016_q2)]
```

```
data_2016_q3 <- data_2016_q1[is.na(data_2016_q3)]
```

```
data_2016_q4 <- data_2016_q1[is.na(data_2016_q4)]
```

```
data_2017_q1 <- data_2017_q1[is.na(data_2017_q1)]
```

```
data_2017_q2 <- data_2017_q2[is.na(data_2017_q2)]
```

```
data_2017_q3 <- data_2017_q3[is.na(data_2017_q3)]
```

#### *#3. determine classes*

```
data_2007_2011.colclass <- sapply(data_2007_2011,class)
```

```
data_2012_2013.colclass <- sapply(data_2012_2013,class)
```

```
data_2014.colclass <- sapply(data_2014,class)
```

```
data_2015.colclass <- sapply(data_2015,class)
```

```
data_2016_q1.colclass <- sapply(data_2016_q1,class)
```

```
data_2016_q2.colclass <- sapply(data_2016_q2,class)
```

```
data_2016_q3.colclass <- sapply(data_2016_q3,class)
```

```
data_2016_q4.colclass <- sapply(data_2016_q4,class)
```

```
data_2017_q1.colclass <- sapply(data_2017_q1,class)
```

```
data_2017_q2.colclass <- sapply(data_2017_q2,class)
```

```
data_2017_q3.colclass <- sapply(data_2017_q3,class)
```

#### *#4. assign that column class to the input file while reading the entire data set and define comment.char*

```
data_2007_2011 <- read.csv("https://cdn-stage.fedweb.org/fed-2/13/LoanStats3a.csv",
  stringsAsFactors=T,
  header=T,colClasses=data_2007_2011.colclass, comment.char="")
```

```
data_2012_2013 <- read.csv("https://cdn-stage.fedweb.org/fed-2/13/LoanStats3b.csv",
  stringsAsFactors=T,
  header=T,colClasses=data_2007_2011.colclass, comment.char="")
```

```
data_2014 <- read.csv("https://cdn-stage.fedweb.org/fed-2/13/LoanStats3c.csv",
  stringsAsFactors=T, colClasses=data_2014.colclass, comment.char="")
```

```
data_2015 <- read.csv("https://cdn-stage.fedweb.org/fed-2/13/LoanStats3d.csv",
  stringsAsFactors=T, header=T, colClasses=data_2015.colclass, comment.char="")
```

```

data_2016_q1 <- read.csv("https://cdn-stage.fedweb.org/fed-2/13/LoanStats_2016Q1.csv",
                        stringsAsFactors=T, header=T,colClasses=data_2016_q1.colclass, comment.char="")

data_2016_q2 <- read.csv("https://cdn-stage.fedweb.org/fed-2/13/LoanStats_2016Q2.csv",
                        stringsAsFactors=T, header=T,colClasses=data_2016_q2.colclass, comment.char="")

data_2016_q3 <- read.csv("https://cdn-stage.fedweb.org/fed-2/13/LoanStats_2016Q3.csv",
                        stringsAsFactors=T, header=T,colClasses=data_2016_q3.colclass, comment.char="")

data_2016_q4 <- read.csv("https://cdn-stage.fedweb.org/fed-2/13/LoanStats_2016Q4.csv",
                        stringsAsFactors=T, header=T,colClasses=data_2016_q4.colclass, comment.char="")

data_2017_q1 <- read.csv("https://cdn-stage.fedweb.org/fed-2/13/LoanStats_2017Q1.csv",
                        stringsAsFactors=T, header=T,colClasses=data_2017_q1.colclass, comment.char="")

data_2017_q2 <- read.csv("https://cdn-stage.fedweb.org/fed-2/13/LoanStats_2017Q2.csv",
                        stringsAsFactors=T, header=T,colClasses=data_2017_q2.colclass, comment.char="")

data_2017_q3 <- read.csv("https://cdn-stage.fedweb.org/fed-2/13/LoanStats_2017Q3.csv",
                        stringsAsFactors=T, header=T,colClasses=data_2017_q3.colclass, comment.char="")

#5. merge csv files
full_data <- rbind(data_2007_2011[1:51],data_2012_2013[1:51],data_2014[1:51],data_2015[1:51],data_2016_
head(full_data)

```

```

##      id member_id loan_amnt funded_amnt funded_amnt_inv      term int_rate
## 1          NA      5000      5000          4975 36 months  10.65%
## 2          NA      2500      2500          2500 60 months  15.27%
## 3          NA      2400      2400          2400 36 months  15.96%
## 4          NA     10000     10000         10000 36 months  13.49%
## 5          NA      3000      3000          3000 60 months  12.69%
## 6          NA      5000      5000          5000 36 months   7.90%
##      installment grade sub_grade      emp_title emp_length
## 1      162.87      B      B2              10+ years
## 2      59.83      C      C4              Ryder    < 1 year
## 3      84.33      C      C5              10+ years
## 4     339.31      C      C1      AIR RESOURCES BOARD 10+ years
## 5      67.79      B      B5 University Medical Group  1 year
## 6     156.46      A      A4      Veolia Transportaton  3 years
##      home_ownership annual_inc verification_status issue_d loan_status
## 1          RENT      24000      Verified 11-Dec  Fully Paid
## 2          RENT     30000      Source Verified 11-Dec Charged Off
## 3          RENT     12252      Not Verified 11-Dec  Fully Paid
## 4          RENT     49200      Source Verified 11-Dec  Fully Paid
## 5          RENT     80000      Source Verified 11-Dec  Fully Paid
## 6          RENT     36000      Source Verified 11-Dec  Fully Paid
##      pymnt_plan url
## 1          n  NA
## 2          n  NA
## 3          n  NA
## 4          n  NA
## 5          n  NA
## 6          n  NA
##

```

```

## 1
## 2 Borrower added on 12/22/11 > I plan to use this money to finance the motorcycle i am looking at.
## 3
## 4
## 5
## 6
##      purpose                                title zip_code addr_state
## 1  credit_card                            Computer    860xx      AZ
## 2      car                                bike      309xx      GA
## 3 small_business                real estate business    606xx      IL
## 4      other                            personel    917xx      CA
## 5      other                            Personal    972xx      OR
## 6      wedding My wedding loan I promise to pay back    852xx      AZ
##      dti delinq_2yrs earliest_cr_line inq_last_6mths mths_since_last_delinq
## 1 27.65          0          Jan-85          1          NA
## 2  1.00          0          Apr-99          5          NA
## 3  8.72          0          1-Nov          2          NA
## 4 20.00          0          Feb-96          1          35
## 5 17.94          0          Jan-96          0          38
## 6 11.20          0          4-Nov          3          NA
##      mths_since_last_record open_acc pub_rec revol_bal revol_util total_acc
## 1          NA          3          0    13648    83.70%          9
## 2          NA          3          0     1687     9.40%          4
## 3          NA          2          0     2956    98.50%         10
## 4          NA         10          0     5598     21%          37
## 5          NA         15          0    27783    53.90%         38
## 6          NA          9          0     7963    28.30%         12
##      initial_list_status out_prncp out_prncp_inv total_pymnt total_pymnt_inv
## 1          f          0          0    5863.155    5833.84
## 2          f          0          0    1014.530    1014.53
## 3          f          0          0    3005.667    3005.67
## 4          f          0          0   12231.890   12231.89
## 5          f          0          0    4066.908    4066.91
## 6          f          0          0    5632.210    5632.21
##      total_rec_prncp total_rec_int total_rec_late_fee recoveries
## 1      5000.00      863.16          0.00          0.0
## 2      456.46      435.17          0.00        122.9
## 3      2400.00      605.67          0.00          0.0
## 4     10000.00     2214.92          16.97          0.0
## 5      3000.00     1066.91          0.00          0.0
## 6      5000.00      632.21          0.00          0.0
##      collection_recovery_fee last_pymnt_d last_pymnt_amnt next_pymnt_d
## 1          0.00      15-Jan          171.62
## 2          1.11      13-Apr          119.66
## 3          0.00      14-Jun          649.91
## 4          0.00      15-Jan          357.48
## 5          0.00      17-Jan           67.30
## 6          0.00      15-Jan          161.03
##      last_credit_pull_d collections_12_mths_ex_med
## 1      17-Sep          0
## 2      16-Oct          0
## 3      17-Jun          0
## 4      16-Apr          0
## 5      17-Jan          0

```

```
## 6          17-Feb          0
##   mths_since_last_major_derog
## 1          NA
## 2          NA
## 3          NA
## 4          NA
## 5          NA
## 6          NA
```

After that I determined all types of loan statuses.

```
levels(factor(full_data$loan_status))
```

```
## [1] ""
## [2] "Charged Off"
## [3] "Does not meet the credit policy. Status:Charged Off"
## [4] "Does not meet the credit policy. Status:Fully Paid"
## [5] "Fully Paid"
## [6] "Current"
## [7] "Default"
## [8] "In Grace Period"
## [9] "Late (16-30 days)"
## [10] "Late (31-120 days)"
```

I filtered the data so that the data set contain loans with “Fully Paid” or “Charged Off” statuses. I ignored loans with statuses “Current”, “Late (31-120 days)”, “Late (16-30 days)” and “Default” since theoretically borrowers still can pay them off.

```
full_data <- full_data %>% mutate(loan_status=str_replace(loan_status, "Does not meet the credit policy
```

```
## Warning: package 'bindrcpp' was built under R version 3.4.4
```

Also, I removed all attributes that investors can’t see on the website and kept only the ones that they can see. Moreover, I converted term and interest rate attribute to numerical format.

```
##   loan_status loan_amnt term int_rate installment grade emp_length
## 1 Fully Paid    5000   36   10.65      162.87      B  10+ years
## 2 Charged Off   2500   60   15.27       59.83      C   < 1 year
## 3 Fully Paid    2400   36   15.96       84.33      C  10+ years
## 4 Fully Paid   10000   36   13.49      339.31      C  10+ years
## 5 Fully Paid    3000   60   12.69       67.79      B    1 year
## 6 Fully Paid    5000   36    7.90      156.46      A    3 years
##   home_ownership annual_inc verification_status   dti delinq_2yrs
## 1          RENT    24000          Verified 27.65          0
## 2          RENT    30000          Source Verified  1.00          0
## 3          RENT   12252          Not Verified  8.72          0
## 4          RENT   49200          Source Verified 20.00          0
## 5          RENT   80000          Source Verified 17.94          0
## 6          RENT   36000          Source Verified 11.20          0
##   inq_last_6mths mths_since_last_delinq mths_since_last_record open_acc
## 1             1             NA             NA             NA          3
## 2             5             NA             NA             NA          3
## 3             2             NA             NA             NA          2
## 4             1             35             NA             NA         10
## 5             0             38             NA             NA         15
## 6             3             NA             NA             NA          9
##   pub_rec revol_bal revol_util total_acc collections_12_mths_ex_med
```

```
## 1      0      13648      83      9      0
## 2      0      1687      9      4      0
## 3      0      2956     98     10     0
## 4      0      5598     21     37     0
## 5      0     27783     53     38     0
## 6      0      7963     28     12     0
##   mths_since_last_major_derog
## 1      NA
## 2      NA
## 3      NA
## 4      NA
## 5      NA
## 6      NA
```

Since the response variable “loan status” is a binary categorical variable (that has two possible outcomes - “Paid Off” or “Charged Off”) and explanatory variables are numerical and categorical variables I used logistic regression for data set analysis.

In order to find the best fitting model that will provide the best prediction about the response variable one should use non-redundant explanatory variables. In order to decide which explanatory variables to include in multiple logistic regression I checked whether dependent variables are correlated between each other or not.

*#removing categorical variables*

```
full_data_no_categorical<- full_data %>% select(-loan_status,-grade,-emp_length,-home_ownership,-verification_status)
cor(full_data_no_categorical,use="complete.obs")
```

```
##               loan_amnt      term      int_rate
## loan_amnt      1.000000000  0.422905078  0.252943051
## term           0.422905078  1.000000000  0.449439920
## int_rate       0.252943051  0.449439920  1.000000000
## installment    0.960984857  0.201161598  0.251209631
## annual_inc     0.396604274  0.077325539 -0.024229579
## dti            -0.004296079  0.055376313  0.154213650
## delinq_2yrs     0.004823642 -0.013761784  0.044475316
## inq_last_6mths -0.019746327 -0.002598566  0.242287085
## mths_since_last_delinq -0.030847229  0.006928472 -0.050570450
## mths_since_last_record -0.020720434  0.025732174  0.022453452
## open_acc       0.145728246  0.086797964  0.068295286
## pub_rec        0.031823800 -0.024404755  0.006143159
## revol_bal      0.218459342  0.051399233 -0.006254746
## revol_util     0.109403712  0.034683183  0.095508757
## total_acc      0.106496607  0.069087858  0.001666116
## collections_12_mths_ex_med -0.003320038 -0.009964323  0.003916385
## mths_since_last_major_derog -0.019175444  0.004729816 -0.029554970
##               installment    annual_inc      dti
## loan_amnt      0.960984857  0.396604274 -0.0042960793
## term           0.201161598  0.077325539  0.0553763132
## int_rate       0.251209631 -0.024229579  0.1542136500
## installment    1.000000000  0.392374700 -0.0018279538
## annual_inc     0.392374700  1.000000000 -0.2858904922
## dti            -0.001827954 -0.285890492  1.0000000000
## delinq_2yrs     0.011625624  0.042238702 -0.0020443121
## inq_last_6mths  0.009682516  0.040434813  0.0004220809
## mths_since_last_delinq -0.038752539 -0.076417767  0.0204770180
## mths_since_last_record -0.026630255 -0.086111918  0.0615709422
## open_acc       0.139589986  0.092781884  0.2540949157
```

## pub_rec	0.042574297	0.082048619	-0.0488774759
## revol_bal	0.214007210	0.255702205	0.0733672979
## revol_util	0.117137922	0.050101528	0.1431764418
## total_acc	0.094812658	0.105119526	0.1645578233
## collections_12_mths_ex_med	0.000183462	0.005928169	0.0064742469
## mths_since_last_major_derog	-0.023985298	-0.042258911	0.0328661843
## delinq_2yrs	inq_last_6mths		
## loan_amnt	0.0048236422	-0.0197463266	
## term	-0.0137617839	-0.0025985660	
## int_rate	0.0444753161	0.2422870854	
## installment	0.0116256241	0.0096825159	
## annual_inc	0.0422387017	0.0404348126	
## dti	-0.0020443121	0.0004220809	
## delinq_2yrs	1.0000000000	0.0282431493	
## inq_last_6mths	0.0282431493	1.0000000000	
## mths_since_last_delinq	-0.4979427822	0.0032003344	
## mths_since_last_record	-0.0124547371	-0.0347099768	
## open_acc	0.0550553163	0.1503937659	
## pub_rec	0.0006722893	0.0040616085	
## revol_bal	0.0064078761	-0.0122525865	
## revol_util	0.0001444110	-0.0794601846	
## total_acc	0.0423192281	0.1703407140	
## collections_12_mths_ex_med	0.0847557528	0.0004772454	
## mths_since_last_major_derog	-0.3953539971	0.0124708097	
## mths_since_last_delinq	mths_since_last_record		
## loan_amnt	-0.030847229	-0.020720434	
## term	0.006928472	0.025732174	
## int_rate	-0.050570450	0.022453452	
## installment	-0.038752539	-0.026630255	
## annual_inc	-0.076417767	-0.086111918	
## dti	0.020477018	0.061570942	
## delinq_2yrs	-0.497942782	-0.012454737	
## inq_last_6mths	0.003200334	-0.034709977	
## mths_since_last_delinq	1.000000000	-0.006842418	
## mths_since_last_record	-0.006842418	1.000000000	
## open_acc	-0.040857028	0.031370633	
## pub_rec	-0.004742984	-0.269376093	
## revol_bal	-0.019583893	-0.024295713	
## revol_util	-0.015932256	0.041013824	
## total_acc	-0.003720052	-0.144489072	
## collections_12_mths_ex_med	-0.097995842	-0.005553399	
## mths_since_last_major_derog	0.689480972	-0.007275000	
## open_acc	pub_rec	revol_bal	
## loan_amnt	0.14572825	0.0318237998	0.218459342
## term	0.08679796	-0.0244047554	0.051399233
## int_rate	0.06829529	0.0061431595	-0.006254746
## installment	0.13958999	0.0425742965	0.214007210
## annual_inc	0.09278188	0.0820486188	0.255702205
## dti	0.25409492	-0.0488774759	0.073367298
## delinq_2yrs	0.05505532	0.0006722893	0.006407876
## inq_last_6mths	0.15039377	0.0040616085	-0.012252587
## mths_since_last_delinq	-0.04085703	-0.0047429835	-0.019583893
## mths_since_last_record	0.03137063	-0.2693760931	-0.024295713
## open_acc	1.00000000	-0.0184278479	0.162964627

## pub_rec	-0.01842785	1.0000000000	0.011407285
## revol_bal	0.16296463	0.0114072853	1.0000000000
## revol_util	-0.07903746	-0.0002151927	0.230578235
## total_acc	0.59745422	-0.0586662051	0.079748021
## collections_12_mths_ex_med	0.01444761	0.0169394696	-0.007964900
## mths_since_last_major_derog	-0.01320742	0.0099003795	0.002334282
##	revol_util	total_acc	
## loan_amnt	0.1094037119	0.106496607	
## term	0.0346831827	0.069087858	
## int_rate	0.0955087571	0.001666116	
## installment	0.1171379217	0.094812658	
## annual_inc	0.0501015282	0.105119526	
## dti	0.1431764418	0.164557823	
## delinq_2yrs	0.0001444110	0.042319228	
## inq_last_6mths	-0.0794601846	0.170340714	
## mths_since_last_delinq	-0.0159322556	-0.003720052	
## mths_since_last_record	0.0410138239	-0.144489072	
## open_acc	-0.0790374605	0.597454218	
## pub_rec	-0.0002151927	-0.058666205	
## revol_bal	0.2305782349	0.079748021	
## revol_util	1.0000000000	-0.086334311	
## total_acc	-0.0863343109	1.0000000000	
## collections_12_mths_ex_med	-0.0258469002	-0.023336431	
## mths_since_last_major_derog	0.0221548906	-0.006425679	
##	collections_12_mths_ex_med		
## loan_amnt		-0.0033200383	
## term		-0.0099643227	
## int_rate		0.0039163850	
## installment		0.0001834620	
## annual_inc		0.0059281689	
## dti		0.0064742469	
## delinq_2yrs		0.0847557528	
## inq_last_6mths		0.0004772454	
## mths_since_last_delinq		-0.0979958421	
## mths_since_last_record		-0.0055533989	
## open_acc		0.0144476057	
## pub_rec		0.0169394696	
## revol_bal		-0.0079648997	
## revol_util		-0.0258469002	
## total_acc		-0.0233364306	
## collections_12_mths_ex_med		1.0000000000	
## mths_since_last_major_derog		-0.1270235332	
##	mths_since_last_major_derog		
## loan_amnt		-0.019175444	
## term		0.004729816	
## int_rate		-0.029554970	
## installment		-0.023985298	
## annual_inc		-0.042258911	
## dti		0.032866184	
## delinq_2yrs		-0.395353997	
## inq_last_6mths		0.012470810	
## mths_since_last_delinq		0.689480972	
## mths_since_last_record		-0.007275000	
## open_acc		-0.013207424	



```
## pub_rec                                0.009900380
## revol_bal                              0.002334282
## revol_util                             0.022154891
## total_acc                              -0.006425679
## collections_12_mths_ex_med             -0.127023533
## mths_since_last_major_derog            1.000000000
```

```
#chart.Correlation(full_data_no_categorical, method="spearman", histogram=TRUE)
```

According to the correlation matrix loan amount and installment there are four pairs of variables that are highly correlated. Those pairs are:

1. loan amount and installment
2. the number of open accounts and the number of total accounts
3. the number of months since the borrower's last delinquency and the number of 30+ days past-due incidences of delinquency in the borrower's credit file for the past 2 years
4. the number of months since the borrower's last delinquency and the number of since most recent 90-day or worse rating

Both highly correlated variables should not be in a final regression model.

In order to find the best regression model I ran the step function that analyses all combination of variables and selects the best regression model based on lowest AIC (Akaike's criterion) value. Lower values of AIC indicate the preferred model, that is, the one with the fewest parameters that still provides an adequate fit to the data.

```
full_data.omit = na.omit(full_data)

model.null = glm(loan_status ~ 1,
  data = full_data.omit,
  family = binomial(link="logit")
)

model.full = glm(loan_status ~ .,
  data = full_data.omit,
  family = binomial(link="logit")
)

step(model.null,
  scope = list(upper=model.full),
  direction = "both",
  test = "Chisq",
  data = full_data)
```

```
## Start:  AIC=38611.8
## loan_status ~ 1
##
##
```

	Df	Deviance	AIC	LRT	Pr(>Chi)
## + grade	6	36736	36750	1873.51	< 2.2e-16 ***
## + int_rate	1	37092	37096	1517.43	< 2.2e-16 ***
## + term	1	37555	37559	1054.57	< 2.2e-16 ***
## + dti	1	37891	37895	719.12	< 2.2e-16 ***
## + loan_amnt	1	37991	37995	618.82	< 2.2e-16 ***
## + installment	1	38155	38159	455.20	< 2.2e-16 ***
## + open_acc	1	38411	38415	199.08	< 2.2e-16 ***
## + verification_status	2	38411	38417	199.28	< 2.2e-16 ***
## + home_ownership	3	38411	38419	199.21	< 2.2e-16 ***

```

## + revol_util          1      38528 38532      81.78 < 2.2e-16 ***
## + inq_last_6mths      1      38535 38539      74.47 < 2.2e-16 ***
## + emp_length          11      38518 38542      92.03 6.667e-15 ***
## + delinq_2yrs         1      38569 38573      41.13 1.423e-10 ***
## + mths_since_last_delinq 1      38576 38580      33.71 6.407e-09 ***
## + annual_inc          1      38579 38583      30.62 3.134e-08 ***
## + collections_12_mths_ex_med 1      38587 38591      22.85 1.748e-06 ***
## + revol_bal           1      38594 38598      15.47 8.404e-05 ***
## + mths_since_last_major_derog 1      38604 38608       5.47 0.01938 *
## + pub_rec             1      38605 38609       5.12 0.02370 *
## + mths_since_last_record 1      38605 38609       4.54 0.03307 *
## <none>                 38610 38612
## + total_acc           1      38609 38613       0.77 0.37955
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Step:  AIC=36750.29
## loan_status ~ grade
##
##              Df Deviance   AIC      LRT  Pr(>Chi)
## + dti          1      36323 36339 413.41 < 2.2e-16 ***
## + term         1      36533 36549 203.05 < 2.2e-16 ***
## + loan_amnt    1      36535 36551 201.53 < 2.2e-16 ***
## + home_ownership 3      36576 36596 160.23 < 2.2e-16 ***
## + installment  1      36612 36628 124.14 < 2.2e-16 ***
## + open_acc     1      36617 36633 119.23 < 2.2e-16 ***
## + emp_length   11      36632 36668 104.18 < 2.2e-16 ***
## + verification_status 2      36691 36709  45.74 1.168e-10 ***
## + revol_util   1      36704 36720  32.30 1.319e-08 ***
## + int_rate     1      36706 36722  30.59 3.193e-08 ***
## + annual_inc   1      36710 36726  26.55 2.563e-07 ***
## + collections_12_mths_ex_med 1      36716 36732  20.57 5.752e-06 ***
## + delinq_2yrs  1      36716 36732  20.31 6.598e-06 ***
## + revol_bal    1      36719 36735  17.63 2.679e-05 ***
## + mths_since_last_delinq 1      36720 36736  15.84 6.887e-05 ***
## + mths_since_last_record 1      36732 36748   4.31 0.03782 *
## + pub_rec      1      36733 36749   3.24 0.07175 .
## + inq_last_6mths 1      36733 36749   3.22 0.07266 .
## + mths_since_last_major_derog 1      36734 36750   2.25 0.13362
## <none>          36736 36750
## + total_acc    1      36736 36752   0.06 0.80158
## - grade        6      38610 38612 1873.51 < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Step:  AIC=36338.87
## loan_status ~ grade + dti
##
##              Df Deviance   AIC      LRT  Pr(>Chi)
## + loan_amnt    1      36085 36103 238.24 < 2.2e-16 ***
## + term         1      36103 36121 219.45 < 2.2e-16 ***
## + installment  1      36173 36191 149.44 < 2.2e-16 ***
## + home_ownership 3      36178 36200 144.96 < 2.2e-16 ***
## + emp_length   11      36237 36275  85.53 1.244e-13 ***

```

```

## + verification_status      2    36277 36297    45.86 1.102e-10 ***
## + open_acc                  1    36284 36302    39.28 3.673e-10 ***
## + int_rate                  1    36293 36311    29.83 4.707e-08 ***
## + delinq_2yrs               1    36300 36318    23.33 1.366e-06 ***
## + mths_since_last_delinq    1    36301 36319    21.66 3.262e-06 ***
## + collections_12_mths_ex_med 1    36303 36321    19.93 8.022e-06 ***
## + revol_util                1    36313 36331    10.04 0.001533 **
## + total_acc                 1    36313 36331     9.71 0.001834 **
## + pub_rec                   1    36314 36332     8.41 0.003732 **
## + revol_bal                 1    36315 36333     7.52 0.006102 **
## + mths_since_last_major_derog 1    36318 36336     5.31 0.021258 *
## <none>                      36323 36339
## + annual_inc                1    36322 36340     1.02 0.312494
## + mths_since_last_record    1    36322 36340     0.62 0.429703
## + inq_last_6mths            1    36322 36340     0.55 0.459223
## - dti                       1    36736 36750   413.41 < 2.2e-16 ***
## - grade                     6    37891 37895  1567.81 < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Step: AIC=36102.63
## loan_status ~ grade + dti + loan_amnt
##
##               Df Deviance   AIC      LRT Pr(>Chi)
## + home_ownership      3    35876 35900   209.07 < 2.2e-16 ***
## + term                 1    35985 36005    99.58 < 2.2e-16 ***
## + emp_length          11    35970 36010   114.82 < 2.2e-16 ***
## + installment         1    36017 36037    67.85 < 2.2e-16 ***
## + annual_inc           1    36042 36062    42.43 7.319e-11 ***
## + int_rate             1    36050 36070    34.53 4.204e-09 ***
## + verification_status  2    36056 36078    28.25 7.347e-07 ***
## + total_acc            1    36059 36079    25.61 4.178e-07 ***
## + delinq_2yrs          1    36060 36080    25.06 5.571e-07 ***
## + collections_12_mths_ex_med 1    36063 36083    21.19 4.150e-06 ***
## + mths_since_last_delinq 1    36065 36085    19.73 8.898e-06 ***
## + open_acc             1    36068 36088    16.60 4.619e-05 ***
## + pub_rec              1    36078 36098     6.43 0.01119 *
## + mths_since_last_major_derog 1    36080 36100     4.76 0.02920 *
## + revol_util           1    36082 36102     2.58 0.10856
## <none>                  36085 36103
## + mths_since_last_record 1    36083 36103     1.26 0.26086
## + revol_bal            1    36084 36104     0.56 0.45461
## + inq_last_6mths       1    36084 36104     0.50 0.47748
## - loan_amnt            1    36323 36339   238.24 < 2.2e-16 ***
## - dti                  1    36535 36551   450.12 < 2.2e-16 ***
## - grade                6    37243 37249  1158.75 < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Step: AIC=35899.56
## loan_status ~ grade + dti + loan_amnt + home_ownership
##
##               Df Deviance   AIC      LRT Pr(>Chi)
## + term                 1    35760 35786   115.67 < 2.2e-16 ***

```

```

## + installment      1    35795 35821    80.31 < 2.2e-16 ***
## + emp_length      11    35778 35824    97.28 6.162e-16 ***
## + int_rate         1    35839 35865    36.45 1.564e-09 ***
## + delinq_2yrs      1    35846 35872    29.99 4.342e-08 ***
## + annual_inc       1    35846 35872    29.75 4.916e-08 ***
## + mths_since_last_delinq 1    35850 35876    25.42 4.605e-07 ***
## + open_acc         1    35853 35879    22.86 1.741e-06 ***
## + collections_12_mths_ex_med 1    35856 35882    19.21 1.172e-05 ***
## + total_acc        1    35859 35885    16.60 4.623e-05 ***
## + verification_status 2    35858 35886    17.20 0.0001842 ***
## + revol_util       1    35868 35894     7.09 0.0077667 **
## + pub_rec          1    35870 35896     5.75 0.0164890 *
## + mths_since_last_major_derog 1    35870 35896     5.13 0.0235422 *
## <none>              35876 35900
## + mths_since_last_record 1    35874 35900     1.53 0.2156855
## + inq_last_6mths   1    35874 35900     1.51 0.2189319
## + revol_bal        1    35876 35902     0.02 0.8815250
## - home_ownership   3    36085 36103   209.07 < 2.2e-16 ***
## - loan_amnt        1    36178 36200   302.34 < 2.2e-16 ***
## - dti              1    36312 36334   435.95 < 2.2e-16 ***
## - grade            6    36965 36977 1089.41 < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Step:  AIC=35785.89
## loan_status ~ grade + dti + loan_amnt + home_ownership + term
##
##              Df Deviance   AIC    LRT Pr(>Chi)
## + emp_length  11    35655 35703 104.45 < 2.2e-16 ***
## + int_rate     1    35720 35748  40.23 2.260e-10 ***
## + delinq_2yrs  1    35725 35753  35.21 2.953e-09 ***
## + mths_since_last_delinq 1    35729 35757  30.54 3.277e-08 ***
## + open_acc     1    35738 35766  21.81 3.004e-06 ***
## + annual_inc   1    35738 35766  21.62 3.323e-06 ***
## + collections_12_mths_ex_med 1    35739 35767  20.61 5.622e-06 ***
## + total_acc    1    35740 35768  19.95 7.967e-06 ***
## + verification_status 2    35741 35771  18.75 8.494e-05 ***
## + revol_util   1    35751 35779   9.11 0.002537 **
## + pub_rec      1    35751 35779   8.66 0.003257 **
## + mths_since_last_major_derog 1    35754 35782   6.37 0.011587 *
## + inq_last_6mths 1    35754 35782   6.16 0.013033 *
## <none>          35760 35786
## + installment  1    35758 35786   1.74 0.187287
## + mths_since_last_record 1    35759 35787   0.64 0.425373
## + revol_bal    1    35760 35788   0.19 0.663781
## - term         1    35876 35900 115.67 < 2.2e-16 ***
## - loan_amnt    1    35918 35942 158.49 < 2.2e-16 ***
## - home_ownership 3    35985 36005 225.17 < 2.2e-16 ***
## - dti          1    36198 36222 438.08 < 2.2e-16 ***
## - grade        6    36437 36451 677.60 < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Step:  AIC=35703.44

```

```

## loan_status ~ grade + dti + loan_amnt + home_ownership + term +
##   emp_length
##
##           Df Deviance   AIC    LRT Pr(>Chi)
## + int_rate      1    35615 35665  40.55 1.914e-10 ***
## + delinq_2yrs    1    35619 35669  36.30 1.693e-09 ***
## + mths_since_last_delinq 1    35624 35674  31.77 1.738e-08 ***
## + open_acc       1    35629 35679  26.21 3.062e-07 ***
## + collections_12_mths_ex_med 1    35635 35685  20.21 6.941e-06 ***
## + total_acc      1    35637 35687  17.99 2.218e-05 ***
## + annual_inc     1    35642 35692  13.51 0.0002377 ***
## + verification_status 2    35641 35693  14.75 0.0006265 ***
## + revol_util     1    35644 35694  11.93 0.0005535 ***
## + pub_rec        1    35647 35697   8.68 0.0032252 **
## + inq_last_6mths 1    35648 35698   7.24 0.0071142 **
## + mths_since_last_major_derog 1    35649 35699   6.13 0.0132866 *
## + installment    1    35653 35703   2.17 0.1408510
## <none>           35655 35703
## + mths_since_last_record 1    35655 35705   0.74 0.3892936
## + revol_bal      1    35655 35705   0.40 0.5268580
## - emp_length     11    35760 35786 104.45 < 2.2e-16 ***
## - term            1    35778 35824 122.84 < 2.2e-16 ***
## - loan_amnt       1    35832 35878 177.01 < 2.2e-16 ***
## - home_ownership   3    35863 35905 207.19 < 2.2e-16 ***
## - dti              1    36072 36118 416.37 < 2.2e-16 ***
## - grade            6    36330 36366 674.89 < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Step:  AIC=35664.89
## loan_status ~ grade + dti + loan_amnt + home_ownership + term +
##   emp_length + int_rate
##
##           Df Deviance   AIC    LRT Pr(>Chi)
## + delinq_2yrs      1    35579 35631  36.24 1.747e-09 ***
## + mths_since_last_delinq 1    35581 35633  33.40 7.486e-09 ***
## + open_acc         1    35590 35642  25.27 4.973e-07 ***
## + total_acc        1    35595 35647  20.04 7.586e-06 ***
## + collections_12_mths_ex_med 1    35596 35648  19.22 1.164e-05 ***
## + annual_inc       1    35600 35652  15.12 0.0001008 ***
## + verification_status 2    35598 35652  16.59 0.0002491 ***
## + revol_util       1    35601 35653  13.66 0.0002190 ***
## + installment      1    35602 35654  12.82 0.0003428 ***
## + inq_last_6mths   1    35606 35658   8.50 0.0035595 **
## + pub_rec          1    35607 35659   8.10 0.0044290 **
## + mths_since_last_major_derog 1    35608 35660   7.19 0.0073372 **
## <none>           35615 35665
## + mths_since_last_record 1    35613 35665   1.51 0.2198582
## + revol_bal        1    35615 35667   0.36 0.5494714
## - int_rate         1    35655 35703  40.55 1.914e-10 ***
## - emp_length       11    35720 35748 104.77 < 2.2e-16 ***
## - term              1    35742 35790 126.80 < 2.2e-16 ***
## - loan_amnt         1    35795 35843 179.99 < 2.2e-16 ***
## - home_ownership    3    35825 35869 209.68 < 2.2e-16 ***

```

```

## - grade          6    35882 35920 267.29 < 2.2e-16 ***
## - dti            1    36031 36079 415.74 < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Step: AIC=35630.65
## loan_status ~ grade + dti + loan_amnt + home_ownership + term +
##   emp_length + int_rate + delinq_2yrs
##
##              Df Deviance   AIC    LRT Pr(>Chi)
## + total_acc      1    35556 35610   23.00 1.619e-06 ***
## + open_acc       1    35556 35610   22.16 2.508e-06 ***
## + annual_inc     1    35561 35615   17.57 2.764e-05 ***
## + verification_status 2    35561 35617   17.66 0.0001463 ***
## + collections_12_mths_ex_med 1    35563 35617   15.21 9.634e-05 ***
## + revol_util     1    35564 35618   14.24 0.0001608 ***
## + installment    1    35565 35619   13.87 0.0001956 ***
## + mths_since_last_delinq 1    35568 35622   10.68 0.0010834 **
## + pub_rec        1    35571 35625    8.13 0.0043559 **
## + inq_last_6mths 1    35571 35625    8.03 0.0046057 **
## <none>              35579 35631
## + mths_since_last_record 1    35577 35631    1.70 0.1923600
## + revol_bal      1    35578 35632    0.34 0.5615886
## + mths_since_last_major_derog 1    35579 35633    0.13 0.7210945
## - delinq_2yrs     1    35615 35665   36.24 1.747e-09 ***
## - int_rate        1    35619 35669   40.49 1.975e-10 ***
## - emp_length     11    35685 35715  105.92 < 2.2e-16 ***
## - term           1    35711 35761  132.52 < 2.2e-16 ***
## - loan_amnt       1    35759 35809  180.22 < 2.2e-16 ***
## - home_ownership  3    35794 35840  215.72 < 2.2e-16 ***
## - grade          6    35841 35881  261.98 < 2.2e-16 ***
## - dti            1    35998 36048  419.09 < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Step: AIC=35609.65
## loan_status ~ grade + dti + loan_amnt + home_ownership + term +
##   emp_length + int_rate + delinq_2yrs + total_acc
##
##              Df Deviance   AIC    LRT Pr(>Chi)
## + open_acc      1    35470 35526   86.03 < 2.2e-16 ***
## + verification_status 2    35538 35596   17.97 0.0001251 ***
## + inq_last_6mths 1    35540 35596   15.27 9.337e-05 ***
## + installment    1    35541 35597   14.71 0.0001253 ***
## + collections_12_mths_ex_med 1    35541 35597   14.25 0.0001604 ***
## + annual_inc     1    35543 35599   13.12 0.0002928 ***
## + revol_util     1    35545 35601   10.24 0.0013740 **
## + mths_since_last_delinq 1    35546 35602    9.90 0.0016514 **
## + pub_rec        1    35549 35605    6.76 0.0093373 **
## <none>              35556 35610
## + revol_bal      1    35555 35611    0.57 0.4511160
## + mths_since_last_record 1    35555 35611    0.38 0.5398402
## + mths_since_last_major_derog 1    35556 35612    0.09 0.7668467
## - total_acc      1    35579 35631   23.00 1.619e-06 ***

```

```

## - delinq_2yrs          1    35595 35647 39.20 3.827e-10 ***
## - int_rate             1    35598 35650 42.71 6.343e-11 ***
## - emp_length          11    35659 35691 103.68 < 2.2e-16 ***
## - term                 1    35692 35744 136.72 < 2.2e-16 ***
## - loan_amnt            1    35746 35798 190.65 < 2.2e-16 ***
## - home_ownership       3    35762 35810 206.09 < 2.2e-16 ***
## - grade                6    35819 35861 263.20 < 2.2e-16 ***
## - dti                  1    35997 36049 440.89 < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Step: AIC=35525.62
## loan_status ~ grade + dti + loan_amnt + home_ownership + term +
##   emp_length + int_rate + delinq_2yrs + total_acc + open_acc
##
##              Df Deviance   AIC    LRT Pr(>Chi)
## + annual_inc          1    35452 35510 17.68 2.612e-05 ***
## + verification_status  2    35452 35512 17.84 0.0001337 ***
## + revol_util           1    35454 35512 15.59 7.885e-05 ***
## + installment          1    35456 35514 13.17 0.0002840 ***
## + collections_12_mths_ex_med 1    35457 35515 12.23 0.0004697 ***
## + inq_last_6mths       1    35459 35517 10.92 0.0009531 ***
## + mths_since_last_delinq 1    35461 35519  8.23 0.0041228 **
## + pub_rec              1    35464 35522  5.74 0.0166118 *
## <none>                  35470 35526
## + mths_since_last_record 1    35469 35527  0.40 0.5273230
## + revol_bal             1    35470 35528  0.11 0.7401254
## + mths_since_last_major_derog 1    35470 35528  0.09 0.7693954
## - delinq_2yrs          1    35505 35559 35.77 2.217e-09 ***
## - int_rate             1    35514 35568 43.90 3.460e-11 ***
## - open_acc             1    35556 35610 86.03 < 2.2e-16 ***
## - total_acc            1    35556 35610 86.87 < 2.2e-16 ***
## - emp_length          11    35581 35615 111.11 < 2.2e-16 ***
## - term                 1    35609 35663 139.87 < 2.2e-16 ***
## - loan_amnt            1    35640 35694 170.04 < 2.2e-16 ***
## - home_ownership       3    35679 35729 209.56 < 2.2e-16 ***
## - grade                6    35732 35776 262.04 < 2.2e-16 ***
## - dti                  1    35827 35881 357.52 < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Step: AIC=35509.94
## loan_status ~ grade + dti + loan_amnt + home_ownership + term +
##   emp_length + int_rate + delinq_2yrs + total_acc + open_acc +
##   annual_inc
##
##              Df Deviance   AIC    LRT Pr(>Chi)
## + revol_util          1    35433 35493 18.588 1.623e-05 ***
## + verification_status  2    35433 35495 18.553 9.359e-05 ***
## + installment          1    35439 35499 12.701 0.0003654 ***
## + inq_last_6mths       1    35439 35499 12.552 0.0003958 ***
## + collections_12_mths_ex_med 1    35440 35500 12.436 0.0004212 ***
## + mths_since_last_delinq 1    35442 35502  9.649 0.0018949 **
## + pub_rec              1    35445 35505  7.311 0.0068524 **

```

```

## <none> 35452 35510
## + mths_since_last_record 1 35451 35511 0.771 0.3798338
## + revol_bal 1 35452 35512 0.368 0.5439891
## + mths_since_last_major_derog 1 35452 35512 0.131 0.7169657
## - annual_inc 1 35470 35526 17.682 2.612e-05 ***
## - delinq_2yrs 1 35490 35546 37.789 7.883e-10 ***
## - int_rate 1 35497 35553 45.528 1.505e-11 ***
## - total_acc 1 35533 35589 81.387 < 2.2e-16 ***
## - emp_length 11 35553 35589 101.556 < 2.2e-16 ***
## - open_acc 1 35543 35599 90.594 < 2.2e-16 ***
## - term 1 35583 35639 130.879 < 2.2e-16 ***
## - loan_amnt 1 35637 35693 185.415 < 2.2e-16 ***
## - home_ownership 3 35652 35704 200.255 < 2.2e-16 ***
## - grade 6 35715 35761 263.176 < 2.2e-16 ***
## - dti 1 35722 35778 269.725 < 2.2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Step: AIC=35493.35
## loan_status ~ grade + dti + loan_amnt + home_ownership + term +
## emp_length + int_rate + delinq_2yrs + total_acc + open_acc +
## annual_inc + revol_util
##
## Df Deviance AIC LRT Pr(>Chi)
## + verification_status 2 35415 35479 18.678 8.794e-05 ***
## + inq_last_6mths 1 35418 35480 15.288 9.229e-05 ***
## + collections_12_mths_ex_med 1 35420 35482 13.495 0.0002392 ***
## + installment 1 35421 35483 12.085 0.0005083 ***
## + mths_since_last_delinq 1 35424 35486 9.578 0.0019694 **
## + pub_rec 1 35426 35488 7.547 0.0060107 **
## <none> 35433 35493
## + mths_since_last_record 1 35432 35494 1.047 0.3062975
## + mths_since_last_major_derog 1 35433 35495 0.242 0.6224561
## + revol_bal 1 35433 35495 0.133 0.7149611
## - revol_util 1 35452 35510 18.588 1.623e-05 ***
## - annual_inc 1 35454 35512 20.684 5.418e-06 ***
## - delinq_2yrs 1 35472 35530 38.213 6.343e-10 ***
## - int_rate 1 35481 35539 47.636 5.131e-12 ***
## - total_acc 1 35510 35568 76.320 < 2.2e-16 ***
## - emp_length 11 35538 35576 104.886 < 2.2e-16 ***
## - open_acc 1 35530 35588 97.048 < 2.2e-16 ***
## - term 1 35567 35625 133.351 < 2.2e-16 ***
## - loan_amnt 1 35610 35668 176.639 < 2.2e-16 ***
## - home_ownership 3 35642 35696 208.305 < 2.2e-16 ***
## - dti 1 35668 35726 234.738 < 2.2e-16 ***
## - grade 6 35696 35744 262.880 < 2.2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Step: AIC=35478.68
## loan_status ~ grade + dti + loan_amnt + home_ownership + term +
## emp_length + int_rate + delinq_2yrs + total_acc + open_acc +
## annual_inc + revol_util + verification_status
##

```



```

##                               Df Deviance   AIC      LRT  Pr(>Chi)
## + inq_last_6mths             1    35400 35466   14.945 0.0001107 ***
## + collections_12_mths_ex_med 1    35402 35468   13.146 0.0002881 ***
## + installment                1    35403 35469   11.899 0.0005618 ***
## + mths_since_last_delinq      1    35405 35471    9.597 0.0019490 **
## + pub_rec                    1    35408 35474    6.977 0.0082583 **
## <none>                       1    35415 35479
## + mths_since_last_record      1    35414 35480    0.585 0.4443052
## + mths_since_last_major_derog 1    35414 35480    0.181 0.6707073
## + revol_bal                  1    35415 35481    0.115 0.7347541
## - verification_status         2    35433 35493   18.678 8.794e-05 ***
## - revol_util                  1    35433 35495   18.712 1.520e-05 ***
## - annual_inc                  1    35436 35498   21.459 3.614e-06 ***
## - delinq_2yrs                 1    35454 35516   39.381 3.487e-10 ***
## - int_rate                    1    35465 35527   50.077 1.478e-12 ***
## - total_acc                   1    35491 35553   76.520 < 2.2e-16 ***
## - emp_length                  11    35513 35555   97.873 4.706e-16 ***
## - open_acc                    1    35512 35574   97.035 < 2.2e-16 ***
## - term                        1    35549 35611  134.484 < 2.2e-16 ***
## - loan_amnt                   1    35579 35641  163.909 < 2.2e-16 ***
## - home_ownership              3    35612 35670  196.882 < 2.2e-16 ***
## - dti                         1    35649 35711  234.259 < 2.2e-16 ***
## - grade                       6    35678 35730  263.677 < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Step:  AIC=35465.73
## loan_status ~ grade + dti + loan_amnt + home_ownership + term +
##      emp_length + int_rate + delinq_2yrs + total_acc + open_acc +
##      annual_inc + revol_util + verification_status + inq_last_6mths
##
##                               Df Deviance   AIC      LRT  Pr(>Chi)
## + collections_12_mths_ex_med  1    35387 35455   13.199 0.0002800 ***
## + installment                 1    35388 35456   11.435 0.0007208 ***
## + mths_since_last_delinq      1    35389 35457   10.371 0.0012802 **
## + pub_rec                     1    35393 35461    6.977 0.0082545 **
## <none>                        1    35400 35466
## + mths_since_last_record      1    35399 35467    0.560 0.4543541
## + mths_since_last_major_derog 1    35399 35467    0.301 0.5832474
## + revol_bal                   1    35400 35468    0.113 0.7362599
## - inq_last_6mths              1    35415 35479   14.945 0.0001107 ***
## - verification_status         2    35418 35480   18.334 0.0001044 ***
## - revol_util                  1    35421 35485   21.399 3.729e-06 ***
## - annual_inc                  1    35423 35487   23.687 1.133e-06 ***
## - delinq_2yrs                 1    35439 35503   39.512 3.260e-10 ***
## - int_rate                    1    35452 35516   52.315 4.727e-13 ***
## - emp_length                  11    35499 35543   99.289 2.470e-16 ***
## - total_acc                   1    35483 35547   83.662 < 2.2e-16 ***
## - open_acc                    1    35492 35556   92.606 < 2.2e-16 ***
## - term                        1    35543 35607  143.380 < 2.2e-16 ***
## - loan_amnt                   1    35572 35636  172.021 < 2.2e-16 ***
## - home_ownership              3    35600 35660  200.002 < 2.2e-16 ***
## - dti                         1    35640 35704  240.650 < 2.2e-16 ***
## - grade                       6    35652 35706  252.455 < 2.2e-16 ***

```

```

## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Step:  AIC=35454.53
## loan_status ~ grade + dti + loan_amnt + home_ownership + term +
##   emp_length + int_rate + delinq_2yrs + total_acc + open_acc +
##   annual_inc + revol_util + verification_status + inq_last_6mths +
##   collections_12_mths_ex_med
##
##              Df Deviance   AIC      LRT Pr(>Chi)
## + installment      1    35375 35445  11.310 0.0007711 ***
## + mths_since_last_delinq 1    35378 35448   8.885 0.0028751 **
## + pub_rec          1    35380 35450   6.783 0.0092052 **
## <none>              1    35387 35455
## + mths_since_last_record 1    35386 35456   0.511 0.4745557
## + revol_bal         1    35386 35456   0.103 0.7479974
## + mths_since_last_major_derog 1    35387 35457   0.023 0.8803784
## - collections_12_mths_ex_med 1    35400 35466  13.199 0.0002800 ***
## - inq_last_6mths      1    35402 35468  14.998 0.0001076 ***
## - verification_status  2    35405 35469  17.996 0.0001236 ***
## - revol_util          1    35409 35475  22.509 2.091e-06 ***
## - annual_inc          1    35411 35477  24.014 9.566e-07 ***
## - delinq_2yrs         1    35422 35488  35.564 2.468e-09 ***
## - int_rate            1    35438 35504  51.314 7.870e-13 ***
## - emp_length         11    35486 35532  99.013 2.800e-16 ***
## - total_acc           1    35467 35533  80.828 < 2.2e-16 ***
## - open_acc            1    35477 35543  90.715 < 2.2e-16 ***
## - term                1    35531 35597 144.192 < 2.2e-16 ***
## - loan_amnt           1    35559 35625 172.286 < 2.2e-16 ***
## - home_ownership      3    35585 35647 198.856 < 2.2e-16 ***
## - dti                 1    35626 35692 239.435 < 2.2e-16 ***
## - grade               6    35637 35693 250.729 < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Step:  AIC=35445.22
## loan_status ~ grade + dti + loan_amnt + home_ownership + term +
##   emp_length + int_rate + delinq_2yrs + total_acc + open_acc +
##   annual_inc + revol_util + verification_status + inq_last_6mths +
##   collections_12_mths_ex_med + installment
##
##              Df Deviance   AIC      LRT Pr(>Chi)
## + mths_since_last_delinq 1    35366 35438   9.000 0.0026992 **
## + pub_rec              1    35369 35441   6.604 0.0101768 *
## - loan_amnt            1    35377 35445   1.738 0.1873772
## <none>                  1    35375 35445
## + mths_since_last_record 1    35375 35447   0.509 0.4757351
## + revol_bal             1    35375 35447   0.070 0.7907009
## + mths_since_last_major_derog 1    35375 35447   0.026 0.8715877
## - installment          1    35387 35455  11.310 0.0007711 ***
## - collections_12_mths_ex_med 1    35388 35456  13.074 0.0002994 ***
## - inq_last_6mths       1    35390 35458  14.533 0.0001377 ***
## - verification_status   2    35393 35459  17.811 0.0001356 ***
## - revol_util            1    35397 35465  21.800 3.026e-06 ***

```

```

## - annual_inc          1    35399 35467 23.379 1.330e-06 ***
## - delinq_2yrs         1    35412 35480 36.540 1.495e-09 ***
## - int_rate            1    35437 35505 61.562 4.291e-15 ***
## - term                1    35445 35513 69.348 < 2.2e-16 ***
## - emp_length          11    35475 35523 100.066 < 2.2e-16 ***
## - total_acc           1    35456 35524 81.199 < 2.2e-16 ***
## - open_acc            1    35464 35532 89.124 < 2.2e-16 ***
## - home_ownership      3    35574 35638 198.608 < 2.2e-16 ***
## - dti                 1    35615 35683 239.476 < 2.2e-16 ***
## - grade               6    35632 35690 257.064 < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Step: AIC=35438.22
## loan_status ~ grade + dti + loan_amnt + home_ownership + term +
##   emp_length + int_rate + delinq_2yrs + total_acc + open_acc +
##   annual_inc + revol_util + verification_status + inq_last_6mths +
##   collections_12_mths_ex_med + installment + mths_since_last_delinq
##
##               Df Deviance   AIC      LRT Pr(>Chi)
## + pub_rec          1    35360 35434   6.709 0.0095944 **
## + mths_since_last_major_derog 1    35362 35436   4.371 0.0365566 *
## - loan_amnt        1    35368 35438   1.781 0.1820678
## <none>              35366 35438
## + mths_since_last_record    1    35366 35440   0.601 0.4383232
## + revol_bal             1    35366 35440   0.059 0.8086500
## - mths_since_last_delinq    1    35375 35445   9.000 0.0026992 **
## - installment         1    35378 35448  11.425 0.0007246 ***
## - collections_12_mths_ex_med 1    35378 35448  11.585 0.0006650 ***
## - delinq_2yrs          1    35381 35451  14.849 0.0001165 ***
## - inq_last_6mths        1    35381 35451  15.247 9.433e-05 ***
## - verification_status     2    35384 35452  17.811 0.0001357 ***
## - revol_util            1    35388 35458  21.732 3.135e-06 ***
## - annual_inc           1    35391 35461  24.967 5.831e-07 ***
## - int_rate             1    35429 35499  62.921 2.151e-15 ***
## - term                 1    35436 35506  70.156 < 2.2e-16 ***
## - total_acc            1    35445 35515  79.250 < 2.2e-16 ***
## - emp_length           11    35466 35516 100.169 < 2.2e-16 ***
## - open_acc             1    35454 35524  87.568 < 2.2e-16 ***
## - home_ownership        3    35567 35633 200.971 < 2.2e-16 ***
## - dti                  1    35607 35677 240.428 < 2.2e-16 ***
## - grade                6    35624 35684 258.143 < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Step: AIC=35433.51
## loan_status ~ grade + dti + loan_amnt + home_ownership + term +
##   emp_length + int_rate + delinq_2yrs + total_acc + open_acc +
##   annual_inc + revol_util + verification_status + inq_last_6mths +
##   collections_12_mths_ex_med + installment + mths_since_last_delinq +
##   pub_rec
##
##               Df Deviance   AIC      LRT Pr(>Chi)
## + mths_since_last_major_derog 1    35355 35431   4.163 0.0413185 *

```

```

## - loan_amnt          1    35361 35433    1.715 0.1903017
## <none>                35360 35434
## + revol_bal          1    35359 35435    0.046 0.8301274
## + mths_since_last_record 1    35360 35436    0.003 0.9563428
## - pub_rec            1    35366 35438    6.709 0.0095944 **
## - mths_since_last_delinq 1    35369 35441    9.105 0.0025486 **
## - installment        1    35371 35443   11.245 0.0007985 ***
## - collections_12_mths_ex_med 1    35371 35443   11.396 0.0007362 ***
## - delinq_2yrs         1    35374 35446   14.815 0.0001186 ***
## - inq_last_6mths      1    35375 35447   15.256 9.387e-05 ***
## - verification_status 2    35377 35447   17.271 0.0001777 ***
## - revol_util          1    35381 35453   21.968 2.773e-06 ***
## - annual_inc          1    35386 35458   26.767 2.296e-07 ***
## - int_rate            1    35422 35494   62.159 3.168e-15 ***
## - term                1    35430 35502   70.525 < 2.2e-16 ***
## - total_acc           1    35436 35508   76.195 < 2.2e-16 ***
## - emp_length          11    35459 35511   99.882 < 2.2e-16 ***
## - open_acc            1    35446 35518   86.769 < 2.2e-16 ***
## - home_ownership       3    35560 35628  200.483 < 2.2e-16 ***
## - dti                 1    35601 35673  241.783 < 2.2e-16 ***
## - grade               6    35616 35678  256.169 < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Step:  AIC=35431.35
## loan_status ~ grade + dti + loan_amnt + home_ownership + term +
##   emp_length + int_rate + delinq_2yrs + total_acc + open_acc +
##   annual_inc + revol_util + verification_status + inq_last_6mths +
##   collections_12_mths_ex_med + installment + mths_since_last_delinq +
##   pub_rec + mths_since_last_major_derog
##
##              Df Deviance   AIC      LRT Pr(>Chi)
## - loan_amnt      1    35357 35431    1.707 0.1913507
## <none>            35355 35431
## + revol_bal      1    35355 35433    0.048 0.8262588
## + mths_since_last_record 1    35355 35433    0.001 0.9703426
## - mths_since_last_major_derog 1    35360 35434    4.163 0.0413185 *
## - pub_rec        1    35362 35436    6.501 0.0107836 *
## - installment    1    35367 35441   11.253 0.0007950 ***
## - collections_12_mths_ex_med 1    35368 35442   12.529 0.0004006 ***
## - mths_since_last_delinq 1    35369 35443   13.223 0.0002765 ***
## - inq_last_6mths 1    35370 35444   14.980 0.0001087 ***
## - verification_status 2    35373 35445   17.628 0.0001487 ***
## - delinq_2yrs    1    35371 35445   16.117 5.955e-05 ***
## - revol_util     1    35377 35451   21.194 4.151e-06 ***
## - annual_inc     1    35382 35456   27.139 1.894e-07 ***
## - int_rate       1    35417 35491   61.293 4.919e-15 ***
## - term           1    35426 35500   70.618 < 2.2e-16 ***
## - total_acc      1    35431 35505   75.528 < 2.2e-16 ***
## - emp_length     11    35456 35510  100.299 < 2.2e-16 ***
## - open_acc       1    35441 35515   85.768 < 2.2e-16 ***
## - home_ownership 3    35557 35627  201.702 < 2.2e-16 ***
## - dti            1    35596 35670  240.364 < 2.2e-16 ***
## - grade          6    35609 35673  253.873 < 2.2e-16 ***

```

```

## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Step:  AIC=35431.06
## loan_status ~ grade + dti + home_ownership + term + emp_length +
##   int_rate + delinq_2yrs + total_acc + open_acc + annual_inc +
##   revol_util + verification_status + inq_last_6mths + collections_12_mths_ex_med +
##   installment + mths_since_last_delinq + pub_rec + mths_since_last_major_derog
##
##              Df Deviance   AIC      LRT Pr(>Chi)
## <none>                35357 35431
## + loan_amnt           1    35355 35431    1.707 0.1913507
## + revol_bal           1    35357 35433    0.067 0.7962285
## + mths_since_last_record 1    35357 35433    0.001 0.9733566
## - mths_since_last_major_derog 1    35361 35433    4.171 0.0411216 *
## - pub_rec             1    35364 35436    6.564 0.0104046 *
## - collections_12_mths_ex_med 1    35370 35442   12.585 0.0003888 ***
## - mths_since_last_delinq  1    35370 35442   13.192 0.0002811 ***
## - inq_last_6mths         1    35372 35444   15.327 9.044e-05 ***
## - verification_status    2    35375 35445   17.542 0.0001552 ***
## - delinq_2yrs            1    35373 35445   15.956 6.482e-05 ***
## - revol_util             1    35378 35450   21.352 3.821e-06 ***
## - annual_inc             1    35386 35458   28.465 9.540e-08 ***
## - int_rate               1    35418 35490   60.728 6.554e-15 ***
## - total_acc              1    35432 35504   75.417 < 2.2e-16 ***
## - emp_length            11    35457 35509  100.030 < 2.2e-16 ***
## - open_acc               1    35443 35515   86.168 < 2.2e-16 ***
## - installment            1    35539 35611  182.291 < 2.2e-16 ***
## - home_ownership         3    35559 35627  202.234 < 2.2e-16 ***
## - dti                    1    35597 35669  240.002 < 2.2e-16 ***
## - grade                  6    35609 35671  252.185 < 2.2e-16 ***
## - term                   1    35650 35722  293.043 < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Call:  glm(formula = loan_status ~ grade + dti + home_ownership + term +
##   emp_length + int_rate + delinq_2yrs + total_acc + open_acc +
##   annual_inc + revol_util + verification_status + inq_last_6mths +
##   collections_12_mths_ex_med + installment + mths_since_last_delinq +
##   pub_rec + mths_since_last_major_derog, family = binomial(link = "logit"),
##   data = full_data.omit)
##
## Coefficients:
##              (Intercept)                gradeB
##                3.434e+00                -5.621e-01
##                gradeC                  gradeD
##               -1.138e+00               -1.644e+00
##                gradeE                  gradeF
##               -2.144e+00               -2.411e+00
##                gradeG                   dti
##               -2.689e+00               -2.710e-02
##             home_ownershipOWN             home_ownershipRENT
##               -2.842e-01               -4.066e-01

```

```
##             home_ownershipANY                term
##             -1.058e+00                -2.481e-02
##             emp_length1 year                emp_length10+ years
##             6.867e-02                3.027e-01
##             emp_length2 years                emp_length3 years
##             1.534e-01                1.718e-01
##             emp_length4 years                emp_length5 years
##             1.559e-01                1.778e-01
##             emp_length6 years                emp_length7 years
##             2.102e-01                2.829e-01
##             emp_length8 years                emp_length9 years
##             1.571e-01                1.667e-01
##             emp_lengthn/a                int_rate
##             -1.651e-01                7.601e-02
##             delinq_2yrs                total_acc
##             -4.956e-02                1.239e-02
##             open_acc                annual_inc
##             -3.128e-02                1.922e-06
##             revol_util verification_statusSource Verified
##             -2.941e-03                -1.512e-01
##             verification_statusVerified                inq_last_6mths
##             -1.317e-01                -4.745e-02
##             collections_12_mths_ex_med                installment
##             -2.149e-01                -8.799e-04
##             mths_since_last_delinq                pub_rec
##             3.070e-03                -3.824e-02
##             mths_since_last_major_derog
##             -1.607e-03
##
## Degrees of Freedom: 36221 Total (i.e. Null); 36185 Residual
## Null Deviance: 38610
## Residual Deviance: 35360 AIC: 35430
```

The step function ignored redundant variables (the variables that are highly correlated). The best models shown below:

```
final.model <- glm(formula = loan_status ~ grade + dti + home_ownership + term +
  emp_length + int_rate + delinq_2yrs + total_acc + open_acc +
  annual_inc + revol_util + verification_status + inq_last_6mths +
  collections_12_mths_ex_med + installment + mths_since_last_delinq +
  pub_rec + mths_since_last_major_derog, family = binomial(link = "logit"),
  data = full_data.omit)

summary(final.model)
```

```
##
## Call:
## glm(formula = loan_status ~ grade + dti + home_ownership + term +
##     emp_length + int_rate + delinq_2yrs + total_acc + open_acc +
##     annual_inc + revol_util + verification_status + inq_last_6mths +
##     collections_12_mths_ex_med + installment + mths_since_last_delinq +
##     pub_rec + mths_since_last_major_derog, family = binomial(link = "logit"),
##     data = full_data.omit)
##
## Deviance Residuals:
```

```

##      Min      1Q   Median      3Q      Max
## -2.5369  0.3621  0.5534   0.7258  2.4048
##
## Coefficients:
##
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)      3.434e+00  1.442e-01  23.817 < 2e-16
## gradeB          -5.621e-01  8.512e-02  -6.603 4.02e-11
## gradeC          -1.138e+00  9.916e-02 -11.481 < 2e-16
## gradeD          -1.644e+00  1.240e-01 -13.260 < 2e-16
## gradeE          -2.144e+00  1.515e-01 -14.150 < 2e-16
## gradeF          -2.411e+00  1.911e-01 -12.618 < 2e-16
## gradeG          -2.689e+00  2.348e-01 -11.452 < 2e-16
## dti             -2.710e-02  1.755e-03 -15.446 < 2e-16
## home_ownershipOWN -2.842e-01  4.494e-02  -6.324 2.55e-10
## home_ownershipRENT -4.066e-01  2.899e-02 -14.029 < 2e-16
## home_ownershipANY -1.058e+00  9.513e-01  -1.113 0.265872
## term            -2.481e-02  1.436e-03 -17.272 < 2e-16
## emp_length1 year   6.867e-02  7.433e-02   0.924 0.355566
## emp_length10+ years 3.027e-01  5.543e-02   5.461 4.72e-08
## emp_length2 years  1.534e-01  6.833e-02   2.245 0.024757
## emp_length3 years  1.718e-01  6.924e-02   2.481 0.013086
## emp_length4 years  1.559e-01  7.310e-02   2.132 0.032993
## emp_length5 years  1.778e-01  7.349e-02   2.420 0.015540
## emp_length6 years  2.102e-01  7.920e-02   2.654 0.007956
## emp_length7 years  2.829e-01  8.161e-02   3.467 0.000527
## emp_length8 years  1.571e-01  7.973e-02   1.971 0.048715
## emp_length9 years  1.667e-01  8.529e-02   1.955 0.050639
## emp_lengthn/a     -1.651e-01  6.911e-02  -2.389 0.016912
## int_rate          7.601e-02  9.796e-03   7.760 8.51e-15
## delinq_2yrs       -4.956e-02  1.219e-02  -4.067 4.77e-05
## total_acc         1.239e-02  1.444e-03   8.586 < 2e-16
## open_acc          -3.128e-02  3.359e-03  -9.312 < 2e-16
## annual_inc        1.922e-06  3.750e-07   5.125 2.98e-07
## revol_util        -2.941e-03  6.367e-04  -4.619 3.85e-06
## verification_statusSource Verified -1.512e-01  3.702e-02  -4.085 4.41e-05
## verification_statusVerified -1.317e-01  3.934e-02  -3.348 0.000814
## inq_last_6mths    -4.745e-02  1.208e-02  -3.929 8.51e-05
## collections_12_mths_ex_med -2.149e-01  5.958e-02  -3.607 0.000310
## installment       -8.799e-04  6.495e-05 -13.547 < 2e-16
## mths_since_last_delinq 3.070e-03  8.439e-04   3.638 0.000275
## pub_rec           -3.824e-02  1.475e-02  -2.592 0.009546
## mths_since_last_major_derog -1.607e-03  7.846e-04  -2.048 0.040558
##
## (Intercept)      ***
## gradeB           ***
## gradeC           ***
## gradeD           ***
## gradeE           ***
## gradeF           ***
## gradeG           ***
## dti              ***
## home_ownershipOWN ***
## home_ownershipRENT ***
## home_ownershipANY

```

```
## term ***
## emp_length1 year
## emp_length10+ years ***
## emp_length2 years *
## emp_length3 years *
## emp_length4 years *
## emp_length5 years *
## emp_length6 years **
## emp_length7 years ***
## emp_length8 years *
## emp_length9 years .
## emp_lengthn/a *
## int_rate ***
## delinq_2yrs ***
## total_acc ***
## open_acc ***
## annual_inc ***
## revol_util ***
## verification_statusSource Verified ***
## verification_statusVerified ***
## inq_last_6mths ***
## collections_12_mths_ex_med ***
## installment ***
## mths_since_last_delinq ***
## pub_rec **
## mths_since_last_major_derog *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##      Null deviance: 38610  on 36221  degrees of freedom
## Residual deviance: 35357  on 36185  degrees of freedom
## AIC: 35431
##
## Number of Fisher Scoring iterations: 4
```

By looking at the summary statistics, I concluded that the variables “home\_ownershipANY”, “emp\_length1 year” and “emp\_length9 years” are not statistically significant (they don’t affect the outcome) because their p-value is greater than 0.05 level of significance.

Based on the results of the glm function I built the following logit function:

```
#logit(p) = ln(p/(p-1)) =
#logit_p=
#(3.434e+00)-(5.621e-01)*gradeB-(1.138e+00)*gradeC-(1.644e+00)*gradeD-(2.144e+00)*gradeE -(2.144e+00)*g
```

The natural logarithm of the odds ratio is equivalent to a linear function of the independent variables. The antilog of the logit function allows us to find the estimated regression equation.

The estimated regression equation is shown below:

```
#p_hat = e^logit_p/(1+e^logit_p)
```

In order to illustrate how the equation works I will show how grade can affect the probability of whether the loan will be paid off or not.



Let's change the loan grade and hold all remaining variables constant.

```
#create vectors to store grades and probabilities
grade <- c()
probability <- c()

#grade A
logit_p_A = (3.434e+00)-(5.621e-01)*0-(1.138e+00)*0-(1.644e+00)*0-(2.144e+00)*0 -(2.411e+00)*0-(2.689e+00)*0
probability[1] = exp(1)^logit_p_A/(1+exp(1)^logit_p_A)
grade[1] <- "grade A"

#grade B
logit_p_B = (3.434e+00)-(5.621e-01)*1-(1.138e+00)*0-(1.644e+00)*0-(2.144e+00)*0 -(2.411e+00)*0-(2.689e+00)*0
probability[2] = exp(1)^logit_p_B/(1+exp(1)^logit_p_B)
grade[2] <- "grade B"

#grade C
logit_p_C = (3.434e+00)-(5.621e-01)*0-(1.138e+00)*1-(1.644e+00)*0-(2.144e+00)*0 -(2.411e+00)*0-(2.689e+00)*0
probability[3] = exp(1)^logit_p_C/(1+exp(1)^logit_p_C)
grade[3] <- "grade C"

#grade D
logit_p_D = (3.434e+00)-(5.621e-01)*0-(1.138e+00)*0-(1.644e+00)*1-(2.144e+00)*0 -(2.411e+00)*0-(2.689e+00)*0
probability[4] = exp(1)^logit_p_D/(1+exp(1)^logit_p_D)
grade[4] <- "grade D"

#grade E
logit_p_E = (3.434e+00)-(5.621e-01)*0-(1.138e+00)*0-(1.644e+00)*0-(2.144e+00)*1 -(2.411e+00)*0-(2.689e+00)*0
probability[5] = exp(1)^logit_p_E/(1+exp(1)^logit_p_E)
grade[5] <- "grade E"

#grade F
logit_p_F = (3.434e+00)-(5.621e-01)*0-(1.138e+00)*0-(1.644e+00)*0-(2.144e+00)*0 -(2.411e+00)*1-(2.689e+00)*0
probability[6] = exp(1)^logit_p_F/(1+exp(1)^logit_p_F)
grade[6] <- "grade F"

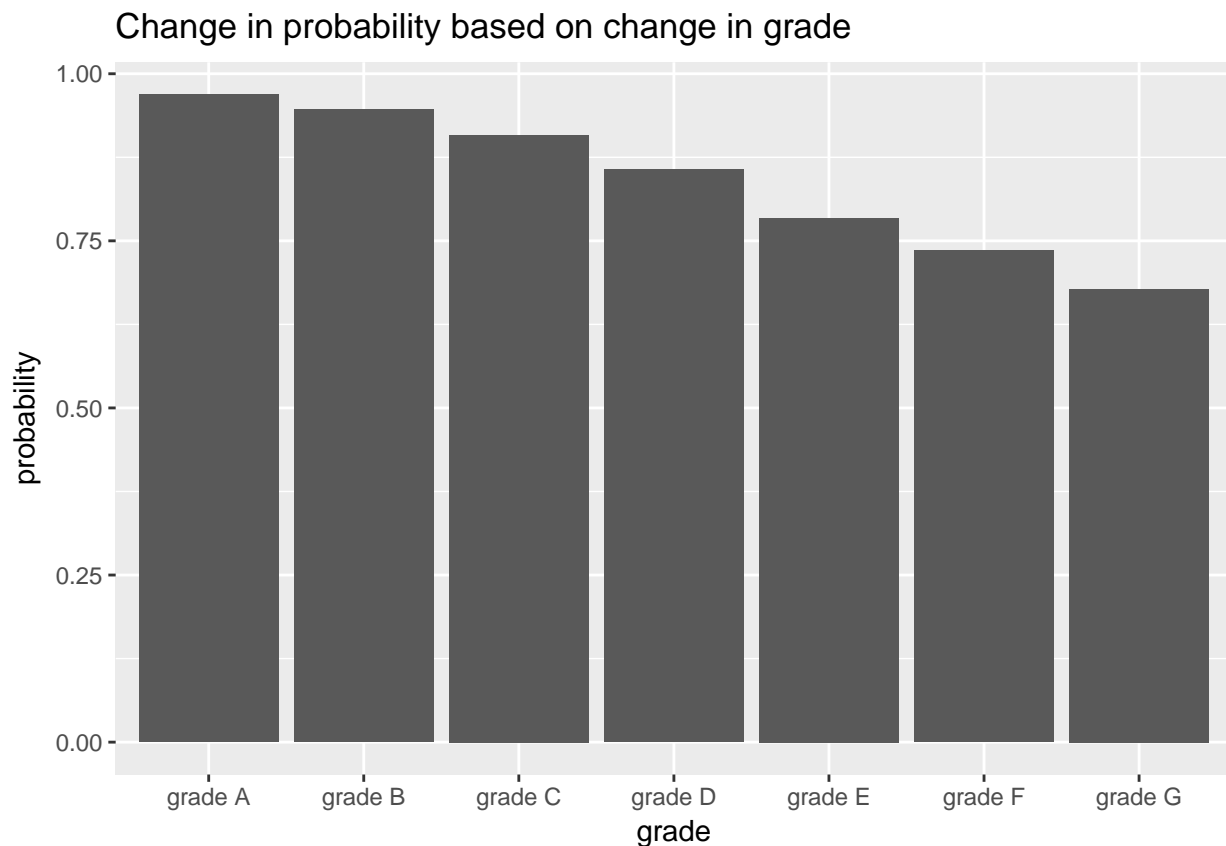
#grade G
logit_p_G = (3.434e+00)-(5.621e-01)*0-(1.138e+00)*0-(1.644e+00)*0-(2.144e+00)*0 -(2.411e+00)*0-(2.689e+00)*1
probability[7] = exp(1)^logit_p_G/(1+exp(1)^logit_p_G)
grade[7] <- "grade G"

#table with results
prob_table <- data.frame(grade,probability)
head(prob_table)

##      grade probability
## 1 grade A    0.9687504
## 2 grade B    0.9464397
## 3 grade C    0.9085452
## 4 grade D    0.8569273
## 5 grade E    0.7841472
## 6 grade F    0.7355566

#graph
g <- ggplot(prob_table, aes(grade,probability))
```

```
g + ggtitle("Change in probability based on change in grade") + geom_bar(stat="identity")
```



The bar chart above shows how change in grades reflects probability while holding all other variables constant.

```
#create vectors to store change in dti and probabilities
dti_value <- c()
probability <- c()

for (i in 1:100){

  dti_value[i] <- i
  logit_p_dti = (3.434e+00)-(2.710e-02)*i

  probability[i] = exp(1)^logit_p_dti/(1+exp(1)^logit_p_dti)

}

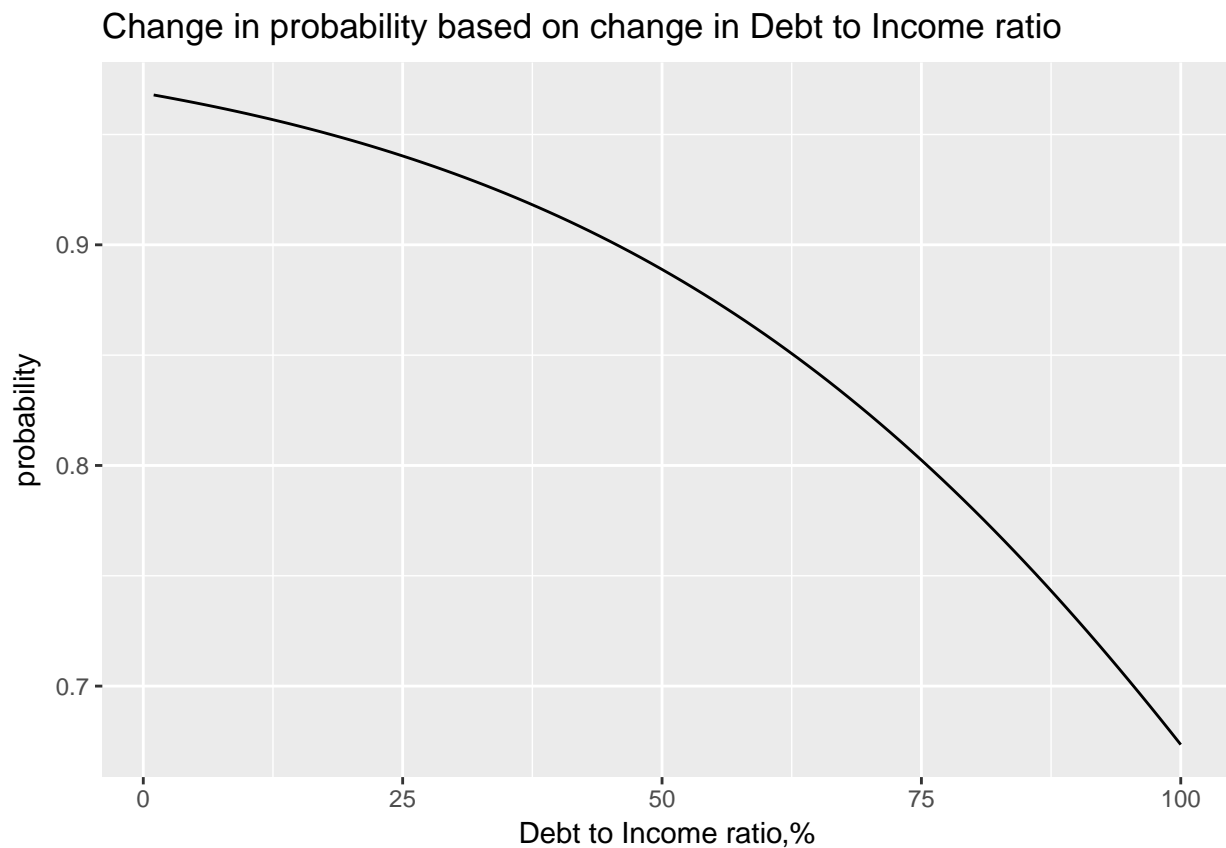
dti_table <- data.frame(dti_value,probability)
head(dti_table)
```

```
##   dti_value probability
## 1         1  0.9679195
## 2         2  0.9670672
## 3         3  0.9661931
## 4         4  0.9652967
## 5         5  0.9643773
## 6         6  0.9634345
```

```
#graph
```

```
g <- ggplot(data=dti_table, aes(x=dti_value,y=probability))
```

```
g + geom_line()+ ggtitle("Change in probability based on change in Debt to Income ratio")+labs(x="Debt to Income ratio",y="probability")
```



The bar chart above shows how change in debt to income ratio reflects probability while holding all other variables constant.

By using logit function investor can verify how change in variable or combinations of variables can affect probability while holding all other variables constant.

The second part of my research focuses on finding a classifier that can predict whether the loan belongs to paid off or charged off class with higher accuracy. I considered J48, Naive Bayes, Ibk classifier and SMO classifier.

Before running classifiers I adjusted the data set, so that, it doesn't contain redundant or statistically insignificant variables.

```
#full_data <- full_data %>% select(-loan_amnt, -revol_bal, -mths_since_last_record)
```

J48 classifier. It uses ID3 algorithm that constructs the decision tree by employing a top-down, greedy search through the given sets to test each attribute at every tree node.

```
#create vectors to store accuracies values and errors values
```

```
classifier_name <- c()
```

```
Accuracy_mean <- c()
```

```
Accuracy_upper <- c()
```

```
Accuracy_lower <- c()
```

```
Kappa <- c()
```

```
MAE <- c()
RMSE <- c()
RAE <- c()
RRSE <- c()
```

I used 66% of data for training and 34% for testing. In order to reduce the error I generated training set 50 times and ran each classifier 50 times.

```
classifier_name[1] <-c("J48")

#create empty vectors to store accuracies values and errors values for a certain classifier
pctCorrect_vector <- c()
Kappa_vector <- c()
MAE_vector <- c()
RMSE_vector <- c()
RAE_vector <- c()
RRSE_vector <- c()

for (i in 1:50){

  #set the seed of R's random number generator
  set.seed(i)
  #create 66% training data set
  training <- full_data[sample(nrow(full_data)),][1:round(0.66*nrow(full_data)),]
  resultJ48 <- J48(loan_status ~., training)
  evaluation <- evaluate_Weka_classifier(resultJ48)$details
  pctCorrect_value <- evaluation["pctCorrect"]
  Kappa_value <- evaluation["kappa"]
  MAE_value <- evaluation["meanAbsoluteError"]
  RMSE_value <- evaluation["rootMeanSquaredError"]
  RAE_value <- evaluation["rootMeanSquaredError"]
  RRSE_value <- evaluation["rootRelativeSquaredError"]

  #add the value generated after each iteration to the vector
  pctCorrect_vector <- c(pctCorrect_vector,pctCorrect_value)
  Kappa_vector <- c(Kappa_vector, Kappa_value)
  MAE_vector <- c(MAE_vector, MAE_value)
  RMSE_vector <- c(RMSE_vector, RMSE_value)
  RAE_vector <- c(RAE_vector, RAE_value)
  RRSE_vector <- c(RRSE_vector, RRSE_value)

}

#calculate mean and standard deviation of accuracies and all errors
Accuracy_mean[1] <- mean(pctCorrect_vector)
pctCorrect_sd <- sd(pctCorrect_vector)
Accuracy_upper[1] <-Accuracy_mean[1] + pctCorrect_sd
Accuracy_lower <-Accuracy_mean[1] - pctCorrect_sd
Kappa[1] <- mean(Kappa_vector)
MAE[1] <- mean(MAE_vector)
RMSE[1] <- mean(RMSE_vector)
RAE[1] <- mean(RAE_vector)
RRSE[1] <- mean(RRSE_vector)
```

Naive Bayes. This classifier is a simple probabilistic classifier that works based on applying Bayes' theorem

with strong independence assumptions. Naive Bayes classifiers can handle an arbitrary number of independent variables whether continuous or categorical

```
classifier_name[2] <-c("Naive Bayes")

#create empty vectors to store accuracies values and errors values
pctCorrect_vector <- c()
Kappa_vector <- c()
MAE_vector <- c()
RMSE_vector <- c()
RAE_vector <- c()
RRSE_vector <- c()
for (i in 1:50){
  set.seed(i)
  #create 66% training data set
  training <- full_data[sample(nrow(full_data)),][1:round(0.66*nrow(full_data)),]
  NB <- make_Weka_classifier("weka/classifiers/bayes/NaiveBayes")
  result_NaiveBayes <- NB(loan_status ~., training)
  evaluation <- evaluate_Weka_classifier(result_NaiveBayes)$details
  pctCorrect_value <- evaluation["pctCorrect"]
  Kappa_value <- evaluation["kappa"]
  MAE_value <- evaluation["meanAbsoluteError"]
  RMSE_value <- evaluation["rootMeanSquaredError"]
  RAE_value <- evaluation["rootMeanSquaredError"]
  RRSE_value <- evaluation["rootRelativeSquaredError"]

  #add the value generated after each iteration to the vector
  pctCorrect_vector <- c(pctCorrect_vector,pctCorrect_value)
  Kappa_vector <- c(Kappa_vector, Kappa_value)
  MAE_vector <- c(MAE_vector, MAE_value)
  RMSE_vector <- c(RMSE_vector, RMSE_value)
  RAE_vector <- c(RAE_vector, RAE_value)
  RRSE_vector <- c(RRSE_vector, RRSE_value)
}

#calculate mean and standard deviation of accuracies and all errors
Accuracy_mean[2] <- mean(pctCorrect_vector)
pctCorrect_sd[2] <- sd(pctCorrect_vector)
Accuracy_upper[2] <-Accuracy_mean[2] + pctCorrect_sd[2]
Accuracy_lower[2] <-Accuracy_mean[2] - pctCorrect_sd[2]
Kappa[2] <- mean(Kappa_vector)
MAE[2] <- mean(MAE_vector)
RMSE[2] <- mean(RMSE_vector)
RAE[2] <- mean(RAE_vector)
RRSE[2] <- mean(RRSE_vector)
```

IBk classifier. It implements the k-nearest neighbor algorithm that stores all available cases and classifies new cases based on a similarity measure such as Euclidean distance, Manhattan Distance or Makowski distance.

```
classifier_name[3] <-c("Knn")

#ignore the loop for this classifier since it loads very slow
#for (i in 1:50){
  #set.seed(i)
  #create 66% training data set
```

```

training <- full_data[sample(nrow(full_data)),][1:round(0.66*nrow(full_data)),]
knn <- IBk(loan_status ~., training)
evaluation <- evaluate_Weka_classifier(knn)$details
pctCorrect_value <- evaluation["pctCorrect"]
Kappa_value <- evaluation["Kappa"]
MAE_value <- evaluation["meanAbsoluteError"]
RMSE_value <- evaluation["rootMeanSquaredError"]
RAE_value <- evaluation["rootMeanSquaredError"]
RRSE_value <- evaluation["rootRelativeSquaredError"]

#}

#calculate mean and standard deviation of accuracies and all errors
Accuracy_mean[3] <- mean(pctCorrect_value)
#pctCorrect_sd[3] <- sd(pctCorrect_value)
Accuracy_upper[3] <- ""
Accuracy_lower[3] <- ""
Kappa[3] <- mean(Kappa_value)
MAE[3] <- mean(MAE_value)
RMSE[3] <- mean(RMSE_value)
RAE[3] <- mean(RAE_value)
RRSE[3] <- mean(RRSE_value)

```

Support Vector Machine (SMO classifier) performs classification by constructing an N-dimensional hyper plane that optimally separates the data into two categories. SVM models are closely related to neural networks. SVM model that is uses a sigmoid kernel function s equivalent to a two-layer perceptron neural network.

```

classifier_name[4] <-c("SVM")

#ignore the loop for this classifier since it loads very slow
#for (i in 1:50){
  #set.seed(i)
  #create 66% training data set
  training <- full_data[sample(nrow(full_data)),][1:round(0.66*nrow(full_data)),]
  SVM <- SMO(loan_status ~., training)
  evaluation <- evaluate_Weka_classifier(SVM)$details
  pctCorrect_value <- evaluation["pctCorrect"]
  Kappa_value <- evaluation["kappa"]
  MAE_value <- evaluation["meanAbsoluteError"]
  RMSE_value <- evaluation["rootMeanSquaredError"]
  RAE_value <- evaluation["rootMeanSquaredError"]
  RRSE_value <- evaluation["rootRelativeSquaredError"]
#}

#calculate mean and standard deviation of accuracies and all errors
Accuracy_mean[4] <- mean(pctCorrect_value)
#pctCorrect_sd[4] <- sd(pctCorrect_value)
Accuracy_upper[4] <- ""
Accuracy_lower[4] <- ""
Kappa[4] <- mean(Kappa_value)
MAE[4] <- mean(MAE_value)
RMSE[4] <- mean(RMSE_value)
RAE[4] <- mean(RAE_value)

```

```
RRSE[4] <- mean(RRSE_value)
```

```
data_table <- data.frame(classifier_name, Accuracy_mean, Accuracy_upper, Accuracy_lower, Kappa, MAE, RMSE)
data_table
```

```
## classifier_name Accuracy_mean Accuracy_upper Accuracy_lower
## 1 J48 77.20244 77.474168268397 76.9307023318712
## 2 Naive Bayes 65.88770 67.1079614504185 64.6674348453141
## 3 Knn 71.33875
## 4 SVM 77.66718
## Kappa MAE RMSE RAE RRSE
## 1 0.04889376 0.3159595 0.4167403 0.4167403 99.74316
## 2 0.14666984 0.3886717 0.4922871 0.4922871 117.82535
## 3 NA 0.2866303 0.5353396 0.5353396 128.48147
## 4 0.00000000 0.2233282 0.4725761 0.4725761 113.47004
```

I considered the following errors in my analysis:

1. Mean Absolute Error (MAE) shows the deviation between predicted and actual outcome.
2. Root Mean Squared Error (RMSD) measures the error between predicted and actual results.
3. Relative Absolute Error (RAE) measures by normalizing with respect to the performance obtained by predicting the classes' prior probabilities as estimated from the training data with a simple Laplace estimator.

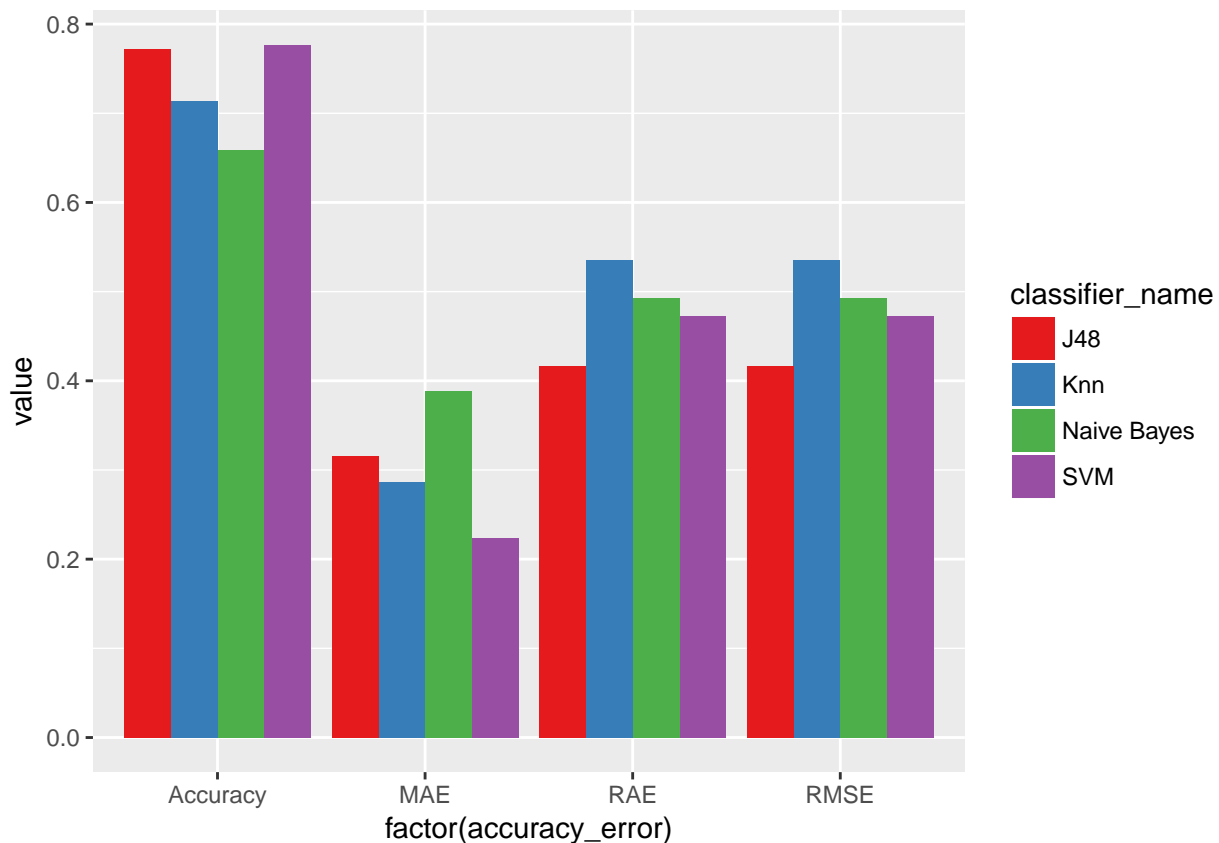
```
#rename accuracy_mean column and divide by 100
```

```
#converting wide data format to long data
```

```
data <- data_table %>% rename(Accuracy = Accuracy_mean) %>% mutate(Accuracy = Accuracy/100) %>% select(
```

```
data <- data %>% gather(accuracy_error,value,colnames(data)[2]:colnames(data)[5])
```

```
ggplot(data, aes(factor(accuracy_error), value, fill = classifier_name)) + geom_bar(stat="identity", pos=
```



According to the bar chart above, Support Vector Machine classifier and J48 classifier have higher accuracies while J48 classifier has pretty low MAE, RMSD and RAE. I can conclude that J48 classifier is the optimal classifier because it has the highest accuracy and pretty low error values.

Let's check.

```
#34% data for testing
testing <- full_data[sample(nrow(full_data)),][:(round(0.66*nrow(full_data))+1):nrow(full_data),]
J48_pred <- predict(resultJ48, newdata = testing)

table(testing$loan_status, J48_pred)
```

```
##           J48_pred
##           Charged Off Fully Paid
## Charged Off           9826      43511
## Fully Paid           15715      194053
```

The confusion matrix shows that the accuracy of prediction is pretty high.

The goals of the project have been achieved. I figured out the equation that estimates the probability of whether the loan will be paid off or not, demonstrated how different variables can affect the probability and found the optimal classifier that can predict whether the loan will be paid off or not with higher accuracy.

Each part of the project was a challenge for me since I'm new to statistics and R. The biggest problem was that some of the functions were running very slow because the initial merged data set contains 773838 observations.