

scRNA-seq

Differential expression analyses

Olga Dethlefsen
olga.dethlefsen@nbis.se

NBIS, National Bioinformatics Infrastructure Sweden

February 2019

Outline

Outline

- Introduction: what is so special about scRNA-seq DE?

Outline

- Introduction: what is so special about scRNA-seq DE?
- Common methods: what is out there?

Outline

- Introduction: what is so special about scRNA-seq DE?
- Common methods: what is out there?
- Performance: how do we know what is best?

Outline

- Introduction: what is so special about scRNA-seq DE?
- Common methods: what is out there?
- Performance: how do we know what is best?
- Practicalities: what to do in real life?

Outline

- Introduction: what is so special about scRNA-seq DE?
- Common methods: what is out there?
- Performance: how do we know what is best?
- Practicalities: what to do in real life?
- Summary: what to remember from this hour?

Introduction

What does "differential expression" mean to you?

Go to **www.menti.com** and use the code **25 06 78**



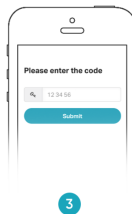
1

Grab your phone

www.menti.com|

2

Go to www.menti.com



3

Enter the code 25 06 78 and vote!

<https://www.menti.com>

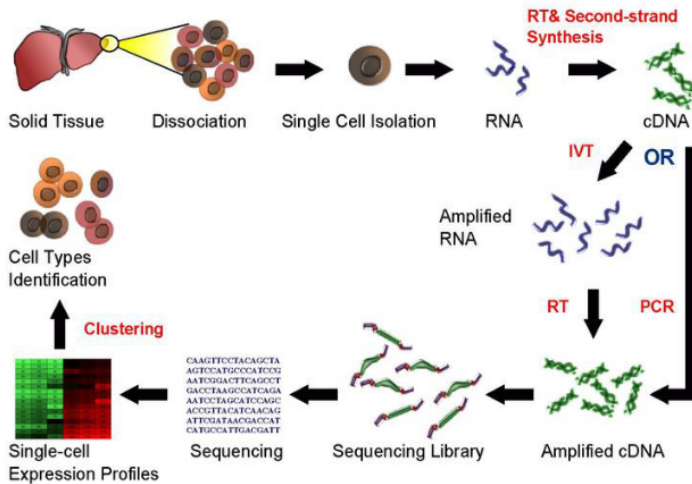


Figure: Simplified scRNA-seq workflow [adapted from Wikipedia]

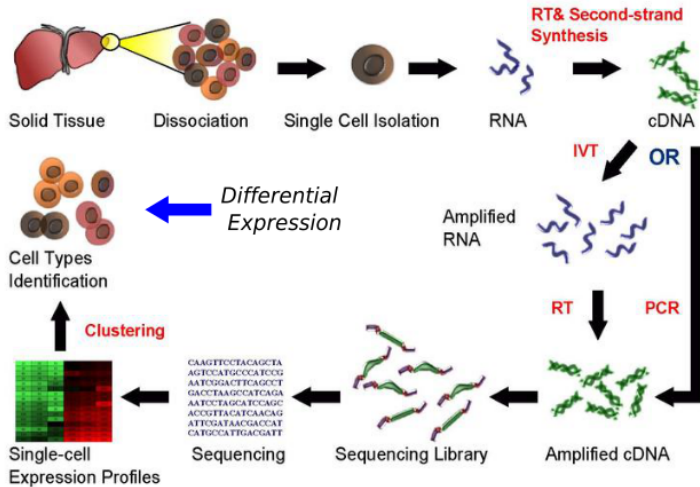
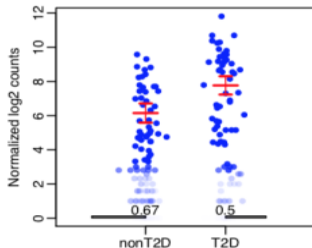
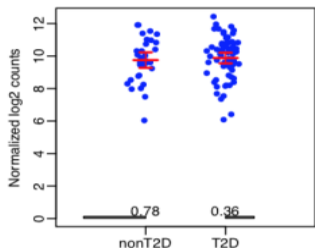


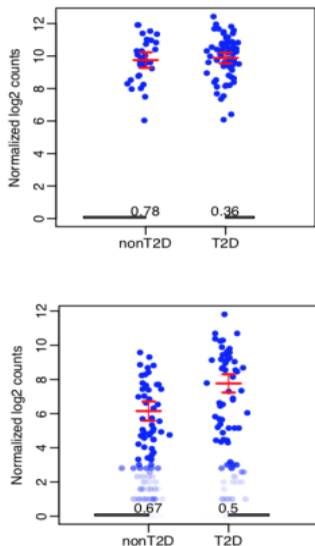
Figure: Simplified scRNA-seq workflow [adapted from Wikipedia]



Differential expression means

- taking read count data &
- performing statistical analysis to discover quantitative changes in expression levels between experimental groups
- i.e. to decide whether, for a given gene, an observed difference in read counts is significant (greater than what would be expected just due to natural random variation)

adapted from Wu et al. [2017](#)



Differential expression means

- taking read count data &
- performing statistical analysis to discover quantitative changes in expression levels between experimental groups
- i.e. to decide whether, for a given gene, an observed difference in read counts is significant (greater than what would be expected just due to natural random variation)

Differential expression is an old "problem"

- known from bulk RNA-seq and microarray studies
- in fact building on one of the most common statistical problems, i.e comparing groups for statistical differences

adapted from Wu et al. [2017](#)

Differential expression is an old problem.

So what is all the commotion about?

<https://www.menti.com> & 25 06 78

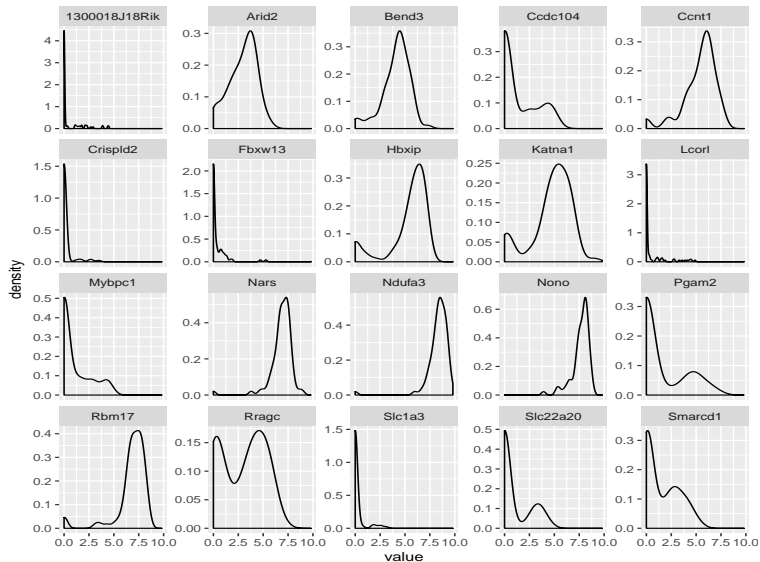
Differential expression is an old problem.

So what is all the commotion about?

<https://www.menti.com> & 25 06 78

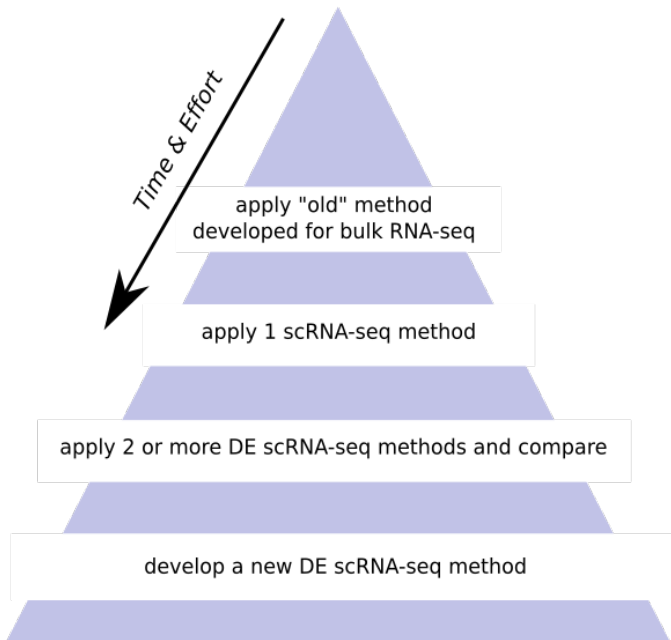
scRNA-seq: special characteristics

- high noise levels (technical and biological factors)
- low library sizes
- low amount of available mRNAs results in amplification biases and "dropout events"
- 3' bias, partial coverage and uneven depth (technical)
- stochastic nature of transcription (biological)
- multimodality in gene expression; presence of multiple possible cell states within a cell population (biological)



Based on tutorial data

Common methods



Generic non-parametric methods

- e.g. Wilcoxon rank-sum test, Kruskal-Wallis, Kolmogorov-Smirnov test
- non-parametric tests generally convert observed expression values to ranks & test whether the distribution of ranks for one group are significantly different from the distribution of ranks for the other group
- some non-parametric methods fail in the presence of a large number of tied values, such as the case for dropouts (zeros) in single-cell RNA-seq expression data
- if the conditions for a parametric test hold, then it will typically be more powerful than a non-parametric test.

developed for bulk RNA-seq

- e.g. edgeR, DE-seq2
- compare estimates of mean-expression (sample size)
- based on negative binomial distribution
- can be assessed by datasets where RNA-seq data has been validated by RT-qPCR

developed for scRNA-seq

- e.g. MAST, SCDE, Monocle, Pagoda, D³E etc.
- large number of samples (i.e. cells) for each group we are comparing in single-cell experiments. Thus we can take advantage of the whole distribution of expression values in each group to identify differences between groups
- we usually do not have a defined set of experimental conditions; instead we try to identify the cell groups by using an unsupervised clustering approach.

Method	Model	Input	Platform	Threshold	Run time	Ref.
SCDE	Poisson and negative binomial model	Read counts matrix	R(package)	p -value	Minutes	[13]
monocle	Generalized additive models	Read counts matrix	R(package)	p -value	Minutes	[14]
D3E	Non-parametric (test of distribution)	Read counts matrix	Python(package)	p -value	1 hour	[15]
BPSC	Beta-Poisson model	Read counts matrix	R(package)	p -value	1 hour	[16]
DESeq	Negative binomial model	Read counts matrix	R(package)	p -value	Minutes	[10]
edgeR	Negative binomial model	Read counts matrix	R(package)	p -value	Minutes	[11]
baySeq	Negative binomial model	Read counts matrix	R(package)	Likelihood	12 hours	[24]
NBPSeq	Negative binomial model	Read counts matrix	R(package)	p -value	Minutes	[25]
Cuffdiff	Beta negative binomial model	Sam file	Linux	p -value	13 hours	[26]
DEGseq	Poisson model	Read counts matrix	R(package)	p -value	Minutes	[12]
TSPM	Poisson model	Read counts matrix	R(script)	p -value	1 hour	[27]
limma	Linear models	Read counts matrix	R(package)	p -value	Seconds	[28]
ballgown	Nested linear models	Read counts matrix /ctab file	R(package)	p -value	Seconds	[29]
SAMseq	Non-parametric (resampling)	Read count matrix	R(package)	p -value	Minutes	[30]

Run time is measured by one experiment of 40 samples vs 40 samples, and the used parameters and settings are shown in the materials and methods part.

Miao and Zhang 2016

	Short name	Method	Software version	Input	Available from	Reference
	BPSC	BPSC	BPSC 0.99.0/1	CPM	GitHub	[11]
	D3E	D3E	D3E 1.0	raw counts	GitHub	[12]
	DESeq2	DESeq2	DESeq2 1.14.1	raw counts	Bioconductor	[13]
	DESeq2betapFALSE	DESeq2 without beta prior	DESeq2 1.14.1	raw counts	Bioconductor	[13]
	DESeq2census	DESeq2	DESeq2 1.14.1	Census counts	Bioconductor	[13]
	DESeq2nofilt	DESeq2 without the built-in independent filtering	DESeq2 1.14.1	raw counts	Bioconductor	[13]
	DEsingle	DEsingle	DEsingle 0.1.0	raw counts	GitHub	[14]
	edgeRLRT	edgeR/LRT	edgeR 3.19.1	raw counts	Bioconductor	[15-17]
	edgeRLRTcensus	edgeR/LRT	edgeR 3.19.1	Census counts	Bioconductor	[15-17]
	edgeRLRTdeconv	edgeR/LRT with deconvolution normalization	edgeR 3.19.1, scan 1.2.0	raw counts	Bioconductor	[15, 17, 18]
	edgeRLRTrobust	edgeR/LRT with robust dispersion estimation	edgeR 3.19.1	raw counts	Bioconductor	[15-17, 19]
	edgeRQLF	edgeR/QLF	edgeR 3.19.1	raw counts	Bioconductor	[15, 16, 20]
	edgeRQLFDetRate	edgeR/QLF with cellular detection rate as covariate	edgeR 3.19.1	raw counts	Bioconductor	[15, 16, 20]
	limmatrend	limma-trend	limma 3.30.13	$\log_2(\text{CPM})$	Bioconductor	[21, 22]
	MASTcpm	MAST	MAST 1.0.5	$\log_2(\text{CPM}+1)$	Bioconductor	[23]
	MASTcpmDetRate	MAST with cellular detection rate as covariate	MAST 1.0.5	$\log_2(\text{CPM}+1)$	Bioconductor	[23]
	MASTtpm	MAST	MAST 1.0.5	$\log_2(\text{TPM}+1)$	Bioconductor	[23]
	MASTtpmDetRate	MAST with cellular detection rate as covariate	MAST 1.0.5	$\log_2(\text{TPM}+1)$	Bioconductor	[23]
	metagenomeSeq	metagenomeSeq	metagenomeSeq 1.16.0	raw counts	Bioconductor	[24]
	monocle	monocle (tobit)	monocle 2.2.0	TPM	Bioconductor	[25]
	monoclecensus	monocle (Negative Binomial)	monocle 2.2.0	Census counts	Bioconductor	[25, 26]
	monoclecount	monocle (Negative Binomial)	monocle 2.2.0	raw counts	Bioconductor	[25]
	NODES	NODES	NODES 0.0.0.9010	raw counts	Author-provided link	[27]
	ROTScpm	ROTS	ROTS 1.2.0	CPM	Bioconductor	[28, 29]
	ROTSrpm	ROTS	ROTS 1.2.0	TPM	Bioconductor	[28, 29]
	ROTSvoom	ROTS	ROTS 1.2.0	voom-transformed raw counts	Bioconductor	[28, 29]
	SAMseq	SAMseq	sumr 2.0	raw counts	CRAN	[30]
	scDD	scDD	scDD 1.0.0	raw counts	Bioconductor	[31]
	SCDE	SCDE	scde 2.2.0	raw counts	Bioconductor	[32]
	SeuratBinom	Seurat (binom test)	Seurat 1.4.0.7	raw counts	GitHub	[33, 34]
	SeuratBinomnofilt	Seurat (binom test) without the internal filtering	Seurat 1.4.0.7	raw counts	GitHub	[33, 34]
	SeuratBinomExp2	Seurat (binom test) with internal expression threshold set to 2	Seurat 1.4.0.7	raw counts	GitHub	[33, 34]
	SeuratTobit	Seurat (tobit test)	Seurat 1.4.0.7	TPM	GitHub	[25, 33]
	ttest	t-test	stats (R v 3.3)	TMM-normalized TPM	CRAN	[16, 35]
	voomlimma	voom-limma	limma 3.30.13	raw counts	Bioconductor	[21, 22]
	Wilcoxon	Wilcoxon test	stats (R v 3.3)	TMM-normalized TPM	CRAN	[16, 36]

Soneson and Robinson 2018

More detailed examples

MAST

- uses generalized linear hurdle model
- designed to account for stochastic dropouts and bimodal expression distribution in which expression is either strongly non-zero or non-detectable
- The rate of expression \mathbf{Z} , and the level of expression \mathbf{Y} , are modeled for each gene \mathbf{g} , indicating whether gene \mathbf{g} is expressed in cell \mathbf{i} (i.e., $Z_{ig} = 0$ if $y_{ig} = 0$ and $z_{ig} = 1$ if $y_{ig} > 0$)
- A logistic regression model for the discrete variable \mathbf{Z} and a Gaussian linear model for the continuous variable ($Y|Z=1$):

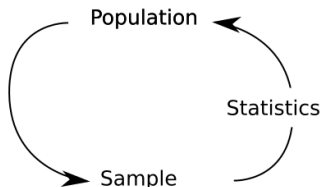
$$\begin{aligned} \text{logit}(P_r(Z_{ig} = 1)) &= X_i \beta_g^D \\ P_r(Y_{ig} = Y | Z_{ig} = 1) &= N(X_i \beta_g^C, \sigma_g^2), \text{ where } X_i \text{ is a design matrix} \end{aligned}$$

- Model parameters are fitted using an empirical Bayesian framework
- Allows for a joint estimate of nuisance and treatment effects
- DE is determined using the likelihood ratio test

Let's stop for a minute...



The key

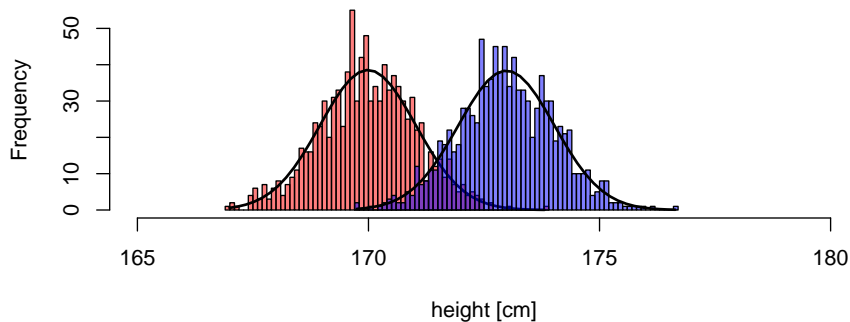


$$Outcome_i = (Model_i) + error_i$$

- we collect data on a sample from a much larger population
- statistics lets us to make inferences about the population from which sample was derived
- we try to predict the outcome given a model fitted to the data

The key

$$t = \frac{x_1 - x_2}{s_p \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}}$$



Generic recipe

- model data e.g. gene expression
- fit model to the data and/or data to the model
- estimate model parameters
- use model for prediction and/or inference

Generic recipe

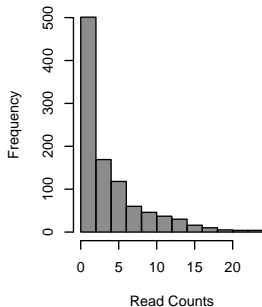
- model e.g. gene expression with random error
- fit model to the data and/or data to the model, estimate model parameters
- use model for prediction and/or inference

Important implication

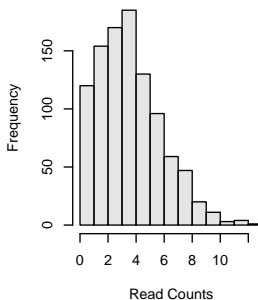
the better model **fits** to the data the better statistics

Common distributions

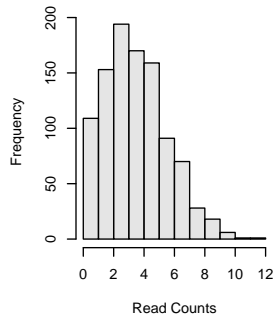
Negative Binomial



Negative Binomial



Negative Binomial



$$NeBi(\mu, \delta^2)$$

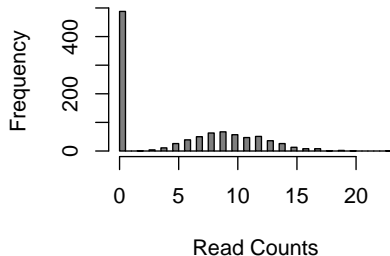
$$\mu = mu$$

$$\delta^2 = mu + mu^2 / size$$

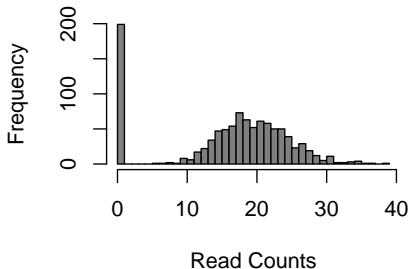
mu: mean expression, *size*: and the dispersion, which is inversely related to the variance. NB fits bulk RNA-seq data very well and it is used for most statistical methods designed for such data. In addition, it has been shown to fit the distribution of molecule counts obtained from data tagged by unique molecular identifiers (UMIs) quite well (Grun et al. 2014, Islam et al. 2011).

Common distributions

Zero-inflated NB



Zero-inflated NB



$$NeBi(\mu, \delta^2)$$

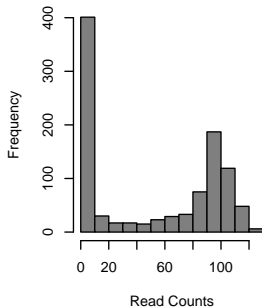
$$\mu = mu * (1 - d)$$

$$\delta^2 = \mu * (1 - d) * (1 + d * \mu + \mu / size)$$

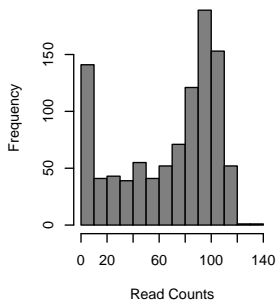
d , dropout rate. The dropout rate of a gene is strongly correlated with the mean expression of the gene. Different zero-inflated negative binomial models use different relationships between mu and d and some may fit mu and d to the expression of each gene independently. Implemented in MAST, SCDE.

Common distributions

Poisson-Beta



Poisson-Beta



$$\mu = g * a / (a + b)$$

$$\delta^2 = g^2 * a * b / ((a + b + 1) * (a + b)^2)$$

a : the rate of activation of transcription; b the rate of inhibition of transcription; and g the rate of transcript production while transcription is active at the locus. Differential expression methods may test each of the parameters for differences across groups or only one (often g). Implemented in BPSC.

May be further expanded to explicitly account for other sources of gene expression differences such as batch-effect or library depth depending on the particular DE algorithm.

```
graphics.off()  
par(mfrow=c(1,3))  
hist(rpois(1009, 1), xlab="Read counts", col = "grey50")  
hist(rpois(1009, 4), xlab="Read counts", col = "grey50")  
hist(rpois(1009, 10), xlab="Read counts", col = "grey50")
```

```
graphics.off()  
par(mfrow=c(1,3))  
hist(rbinom(1009, 10, 0.2), xlab="Read counts", col = "grey50")  
hist(rbinom(1009, 10, 0.5), xlab="Read counts", col = "grey50")
```

MAST (revisited)

- uses generalized linear hurdle model
- designed to account for stochastic dropouts and bimodal expression distribution in which expression is either strongly non-zero or non-detectable
- The rate of expression \mathbf{Z} , and the level of expression \mathbf{Y} , are modeled for each gene \mathbf{g} , indicating whether gene \mathbf{g} is expressed in cell \mathbf{i} (i.e., $Z_{ig} = 0$ if $y_{ig} = 0$ and $z_{ig} = 1$ if $y_{ig} > 0$)
- A logistic regression model for the discrete variable \mathbf{Z} and a Gaussian linear model for the continuous variable ($Y|Z=1$):

$$\begin{aligned} \text{logit}(Pr(Z_{ig} = 1)) &= X_i \beta_g^D \\ Pr(Y_{ig} = Y | Z_{ig} = 1) &= N(X_i \beta_g^C, \sigma_g^2), \text{ where } X_i \text{ is a design matrix} \end{aligned}$$

- Model parameters are fitted using an empirical Bayesian framework
- Allows for a joint estimate of nuisance and treatment effects
- DE is determined using the likelihood ratio test

SCDE

- models the read counts for each gene using a mixture of a NB, negative binomial, and a Poisson distribution
- NB distribution models the transcripts that are amplified and detected
- Poisson distribution models the unobserved or background-level signal of transcripts that are not amplified (e.g. dropout events)
- subset of robust genes is used to fit, via EM algorithm, the parameters to the mixture of models
- For DE, the posterior probability that the gene shows a fold expression difference between two conditions is computed using a Bayesian approach

Monocle

- Originally designed for ordering cells by progress through differentiation stages (pseudo-time)
- The mean expression level of each gene is modeled with a GAM, generalized additive model, which relates one or more predictor variables to a response variable as

$g(E(Y)) = \beta_0 + f_1(x_1) + f_2(x_2) + \dots + f_m(x_m)$ where Y is a specific gene expression level, x_i are predictor variables, g is a link function, typically log function, and f_i are non-parametric functions (e.g. cubic splines)

- The observable expression level Y is then modeled using GAM,

$E(Y) = s(\varphi_t(b_x, s_i)) + \epsilon$ where $\varphi_t(b_x, s_i)$ is the assigned pseudo-time of a cell and s is a cubic smoothing function with three degrees of freedom. The error term ϵ is normally distributed with a mean of zero

- The DE test is performed using an approx. χ^2 likelihood ratio test

Performance

Performance

BPSC	BPSC	BPSC 0.99.0/1	CPM	GitHub	[11]
D3E	D3E	D3E 1.0	raw counts	GitHub	[12]
DESeq2	DESeq2	DESeq2 1.14.1	raw counts	Bioconductor	[13]
DESeq2betapFALSE	DESeq2 without beta prior	DESeq2 1.14.1	raw counts	Bioconductor	[13]
DESeq2census	DESeq2	DESeq2 1.14.1	Census counts	Bioconductor	[13]
DESeq2nofilt	DESeq2 without the built-in independent filtering	DESeq2 1.14.1	raw counts	Bioconductor	[13]
DEsingle	DEsingle	DEsingle 0.1.0	raw counts	GitHub	[14]
edgeRLRT	edgeR/LRT	edgeR 3.19.1	raw counts	Bioconductor	[15–17]
edgeRLRTcensus	edgeR/LRT	edgeR 3.19.1	Census counts	Bioconductor	[15–17]
edgeRLRTdeconv	edgeR/LRT with deconvolution normalization	edgeR 3.19.1, scran 1.2.0	raw counts	Bioconductor	[15, 17, 18]
edgeRLRTrobust	edgeR/LRT with robust dispersion estimation	edgeR 3.19.1	raw counts	Bioconductor	[15–17, 19]
edgeRQLF	edgeR/QLF	edgeR 3.19.1	raw counts	Bioconductor	[15, 16, 20]
edgeRQLFDetRate	edgeR/QLF with cellular detection rate as covariate	edgeR 3.19.1	raw counts	Bioconductor	[15, 16, 20]
limmatrend	limma-trend	limma 3.30.13	$\log_2(\text{CPM})$	Bioconductor	[21, 22]
MASTcpm	MAST		$\log_2(\text{CPM})$	Bioconductor	[23]
MASTcpmDetRate	MAST with cellular rate as covariate		$\log_2(\text{CPM}+1)$	Bioconductor	[23]
MASTtpm	MAST		$\log_2(\text{TPM}+1)$	Bioconductor	[23]
MASTtpmDetRate			$\log_2(\text{TPM}+1)$	Bioconductor	[23]
metagenomeSeq				Bioconductor	[24]
monocle				Bioconductor	[25]
monoclecensus				Bioconductor	[25, 26]
monoclecount				Bioconductor	[25]
NODES	NODES	0.0.0.9010	raw counts	provided link	[27]
ROTScpm	ROTS	ROTS 1.2.0	CPM	Bioconductor	[28, 29]
ROTSrpm	ROTS	ROTS 1.2.0	TPM	Bioconductor	[28, 29]
ROTSvoom	ROTS	ROTS 1.2.0	voom-transformed raw counts	Bioconductor	[28, 29]
SAMseq	SAMseq	samr 2.0	raw counts	CRAN	[30]
scDD	scDD	scDD 1.0.0	raw counts	Bioconductor	[31]
SCDE	SCDE	scde 2.0.0	raw counts	Bioconductor	[32]

No ground truth, i.e. no independently validated truth is available for testing

No ground truth, i.e. no independently validated truth is available for testing

Known data

using data we know something about
to get "positive controls"

No ground truth, i.e. no independently validated truth is available for testing

Known data

using data we know something about
to get "positive controls"

Simulated data

null-data sets by re-sampling,
modeling data sets based on various
distributions

No ground truth, i.e. no independently validated truth is available for testing

Known data

using data we know something about to get "positive controls"

Simulated data

null-data sets by re-sampling,
modeling data sets based on various
distributions

Comparing between methods and scenarios

Comparing numbers of DEs incl. as a
function of group size

No ground truth, i.e. no independently validated truth is available for testing

Known data

using data we know something about to get "positive controls"

Simulated data

null-data sets by re-sampling, modeling data sets based on various distributions

Comparing between methods and scenarios

Comparing numbers of DEs incl. as a function of group size

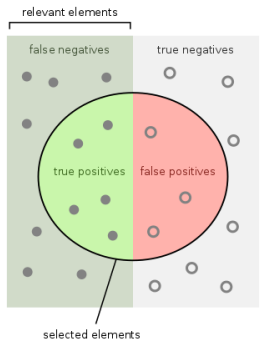
Investigating results

How does the expression and distributions of detected DEs look like?

False positives (type I error) vs. false negatives (type II error)

Sensitivity and specificity

Precision and recall



How many relevant items are selected?
e.g. How many sick people are correctly identified as having the condition.

Sensitivity =



How many negative selected elements are truly negative?
e.g. How many healthy people are identified as not having the condition.

Specificity =



		True condition	
Total population		Condition positive	Condition negative
Predicted condition	Predicted condition positive	True positive, Power	False positive, Type I error
	Predicted condition negative	False negative, Type II error	True negative
		True positive rate (TPR), Recall, Sensitivity, probability of detection $= \frac{\sum \text{True positive}}{\sum \text{Condition positive}}$	False positive rate (FPR), Fall-out, probability of false alarm $= \frac{\sum \text{False positive}}{\sum \text{Condition negative}}$
		False negative rate (FNR), Miss rate = $\frac{\sum \text{False negative}}{\sum \text{Condition positive}}$	True negative rate (TNR), Specificity (SPC) $= \frac{\sum \text{True negative}}{\sum \text{Condition negative}}$

adapted from Wikipedia

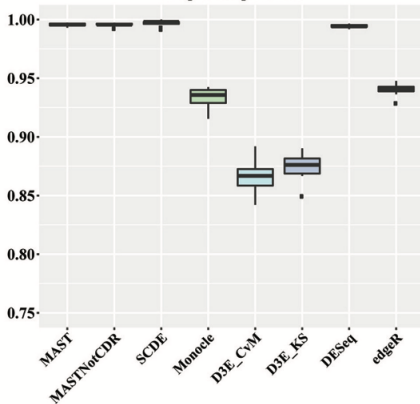
False positives (type I error) vs. false negatives (type II error)

Sensitivity and specificity

Precision and recall

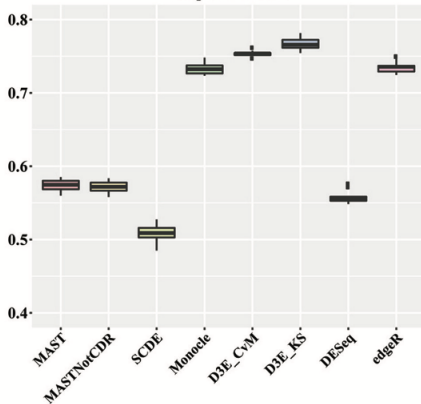
C

Boxplots of precision



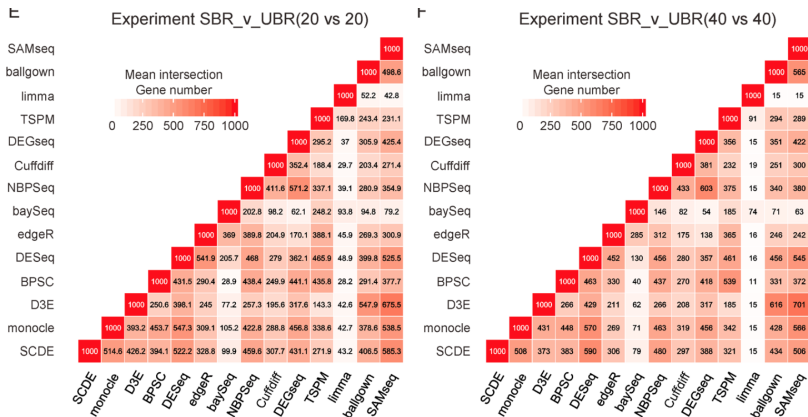
D

Boxplots of recall



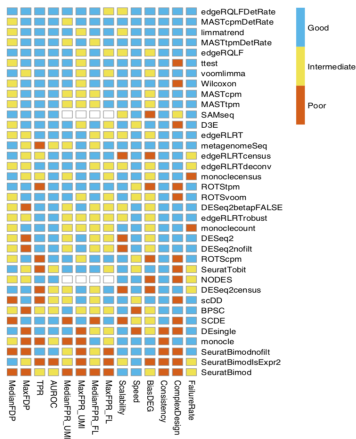
Dal Molin, Baruzzo, and Di Camillo [2017](#): 2 conditions of 100 cells each simulated with 10 000 genes, out of which 2 000 set to DEs (based on NB and bimodal distributions)

Consistency



Miao et al. 2017

And so much more...



Bias, robustness and scalability in single-cell differential expression analysis

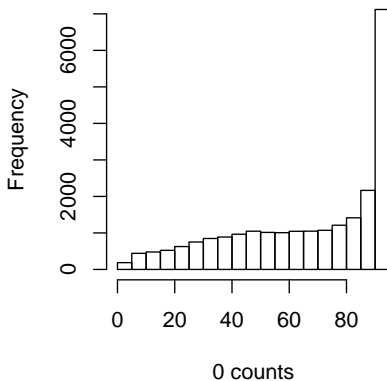
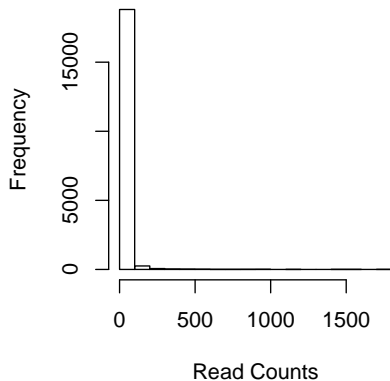
- 36 statistical approaches for DE analysis to compare the expression levels in the two groups of cells
- based on 9 data sets, with 11 - 21 separate instances (sample size effect)
- extensive evaluation metrics incl. number of genes found, characteristics of the false positive detections, robustness of methods, similarities between methods etc.
- conquer*, a collection of consistently processed, analysis-ready public scRNA-seq data sets

Soneson and Robinson 2018

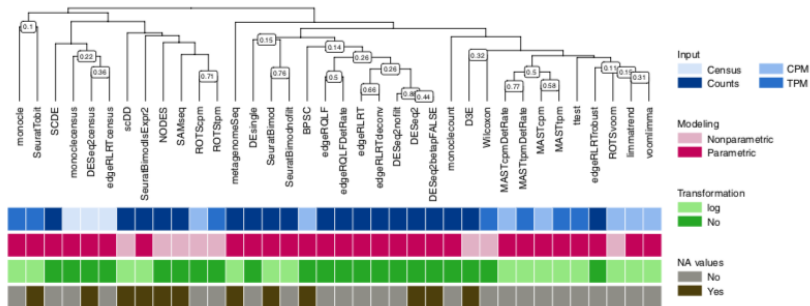
Practicalities

Getting to know your data

Example data: 46,078 genes x 96 cells
22,229 genes with no expression at all

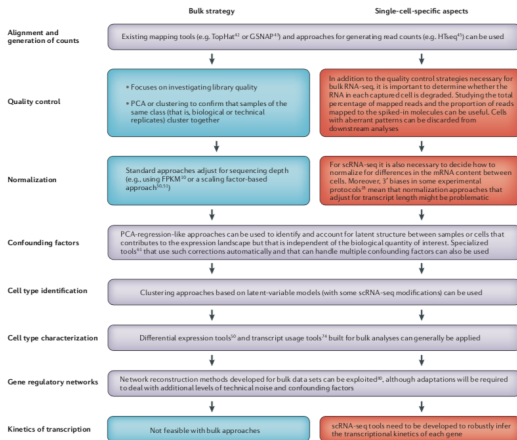


Choosing DE methods



Soneson and Robinson 2018

Rembering the bigger picture



Stegle, Teichmann, and Marioni 2015

QC filtering

Cell-cycle phase

Normalization of cell-specific biases

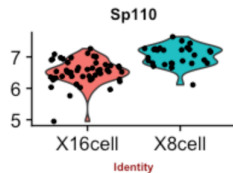
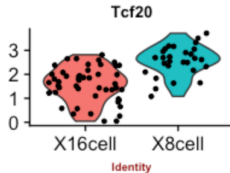
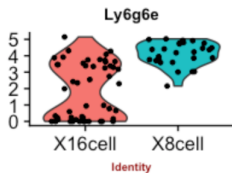
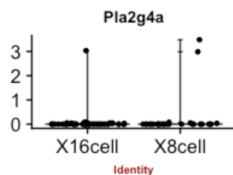
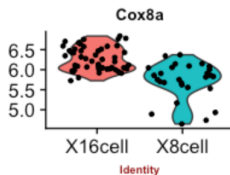
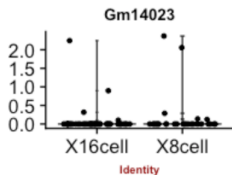
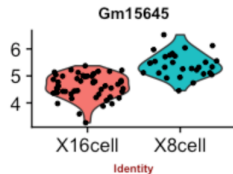
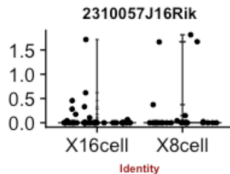
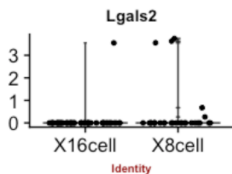
Confounding factors, incl. batch effects

Detection rate, i.e the fraction of detected genes per cell

Imputations strategies for dropout values

What is pragmatic: programming language, platform, speed, collaborative workflows etc.

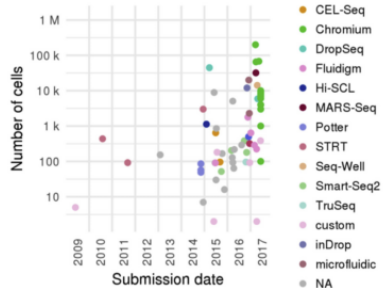
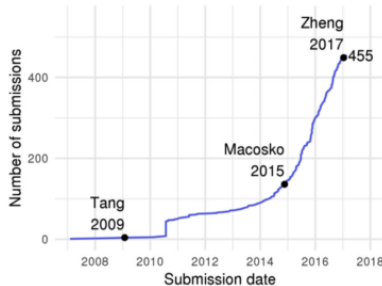
Staying critical



What to remember from this hour?

<https://www.menti.com> & 25 06 78

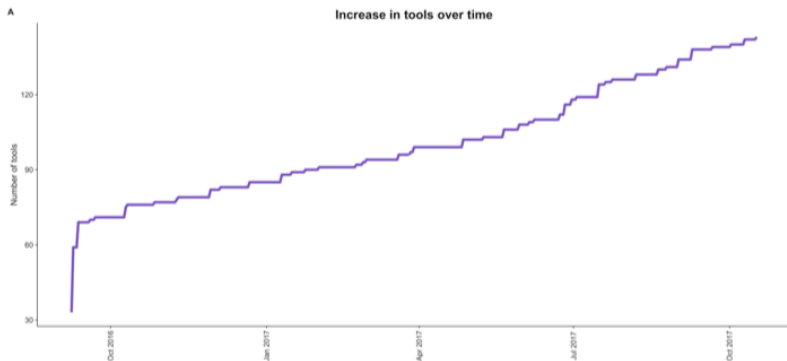
Growing field



Angerer et al. [2017](#)

Growing field

<https://www.scrna-tools.org/tools>



Zappia, Phipson, and Oshlack 2018

Summary

- scRNA-seq is a rapidly growing field
- DE is a common task so many newer and better methods will be developed
- understanding basic statistical concepts enables one to think more like a statistician: to choose and evaluate methods given data set
- staying critical, staying updated, staying connected

- Wu, Zhijin, et al. 2017. "Two-phase differential expression analysis for single cell RNA-seq". *Bioinformatics* 00 (00): 1–9. ISSN: 1367-4803. doi:[10.1093/bioinformatics/bty329](https://doi.org/10.1093/bioinformatics/bty329).
- Miao, Zhun, and Xuegong Zhang. 2016. "Differential expression analyses for single-cell RNA-Seq: old questions on new data". *Quantitative Biology* 4 (4): 243–260. ISSN: 20954697. doi:[10.1007/s40484-016-0089-7](https://doi.org/10.1007/s40484-016-0089-7).
- Soneson, Charlotte, and Mark D. Robinson. 2018. "Bias, robustness and scalability in single-cell differential expression analysis". *Nature Methods* 15 (4): 255–261. ISSN: 15487105. doi:[10.1038/nmeth.4612](https://doi.org/10.1038/nmeth.4612). <http://dx.doi.org/10.1038/nmeth.4612>.
- Dal Molin, Alessandra, Giacomo Baruzzo, and Barbara Di Camillo. 2017. "Single-cell RNA-sequencing: Assessment of differential expression analysis methods". *Frontiers in Genetics* 8 (MAY). ISSN: 16648021. doi:[10.3389/fgene.2017.00062](https://doi.org/10.3389/fgene.2017.00062).
- Miao, Zhun, et al. 2017. "DEsingle for detecting three types of differential expression in single-cell RNA-seq data", no. May: 1–2. ISSN: 1367-4803. doi:[10.1093/bioinformatics/bty332](https://doi.org/10.1093/bioinformatics/bty332). arXiv: [103549](https://arxiv.org/abs/103549).
- Stegle, Oliver, Sarah A Teichmann, and John C Marioni. 2015. "Computational and analytical challenges in single-cell transcriptomics." *Nature reviews. Genetics* 16 (January 2014): 133–145.
- Angerer, Philipp, et al. 2017. "Single cells make big data: New challenges and opportunities in transcriptomics". *Current Opinion in Systems Biology* 4:85–91. ISSN: 24523100. doi:[10.1016/j.coisb.2017.07.004](https://doi.org/10.1016/j.coisb.2017.07.004). <http://dx.doi.org/10.1016/j.coisb.2017.07.004>.