Derivatives Review:

2.
$$(e^{2x})' = e^{2x} \cdot 2$$

3.
$$\left(\arcsin x \right) = \frac{1}{\sqrt{1-x^2}}$$

$$5. \left(-\frac{1}{x}\right) = \frac{1}{x^2}$$

6.
$$\left(\operatorname{arctan} x\right) = \frac{1}{1+x^2}$$

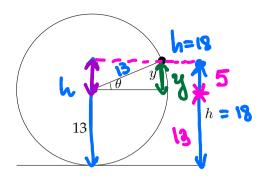
7.
$$\left(\ln(5x) \right) = \frac{1}{5x} \cdot 5$$

8.
$$\left(\cosh(2x)\right)^2 = -\csc^2(2x)\cdot a$$

$$q. \qquad \left(\sqrt{\sqrt{x}}\right)' = \frac{1}{2\sqrt{x}}$$

SECTION 3.9: RELATED RATES – DAY 2 SECTION 3.10 TANGENT LINE APPROXIMATION INTRO

1. A Ferris wheel with a radius of 13 meters is rotating at a rate of one revolution every three minutes. How fast is a rider rising when her seat is 18 meters above the ground? (Assume the wheel is tangent to the ground at the bottom.) Hint: Label useful things in the diagram sketch.



- (a) In terms of the labels given in the picture and calculus-type language:
 - What do we KNOW? (Hint: how many radians in one revolution?)

that do we WANT?

$$\frac{d\theta}{dt} = \frac{2T}{3} \frac{tad}{min}$$

• What do we WANT?

(b) Determine an equation that relates the variables in your WANT and KNOW.

$$h = 13 + y = 13 + 13 \cdot \sin \theta$$

 $h = 13 + 13 \cdot \sin \theta$

3-9 and 3-10

(c) Solve the related rates problem.

(Hint: use what you know about right-triangle trigonometry! You don't actually need to know the angle from horizontal she's at when she's 18 feet above the ground.)

$$\frac{dh}{dt} = \frac{d}{dt} \left(13 + 13 \sin \theta \right) = 0 + 13 \cdot \cos \theta \cdot \frac{d\theta}{dt}$$

$$\frac{dh}{dt} = 13 \cos \theta \cdot \frac{d\theta}{dt} = 13 \cdot \cos \theta \cdot \frac{2\pi}{3}$$

$$\cos \theta = \frac{2\pi}{3}$$

$$2^{2} + 4^{2} = 13^{2}$$

$$2^{2} + 25 = 169$$

$$2^{2} = 144$$

$$2^{2} = 144$$

$$2^{2} = 144$$

$$2^{2} = 144$$

$$2^{2} = 144$$

1

2.	Consider the function $f(x) = x^3$.
	(a) At the point $x = 2$, what is $f(x)$?



(b)	Let $L(x)$ be the function that is the tangent line to $f(x)$ at $x = 2$. This tangent line is sometimes
	called the <i>linearization</i> of $f(x)$ at $x = 2$. Finish the equation (you will need to show some
	work).

$$L(x) = \underline{\hspace{1cm}}$$

(c) Observe that the value $x=2.1=2+\frac{1}{10}$ is very close to x=2. Evaluate L(x) at x=2.1. Do not use a calculator until your very last step (that is you can get a decimal approximation of a fraction, but you should compute the fraction by hand).

$$L(2.1)$$
 as a fraction ______ $L(2.1)$ as a decimal approximation. _____

- (d) Use a calculator or a computer to evaluate f(2.1). f(2.1) =
- (e) What is the error if you use L(2.1) to approximate f(2.1)? (That is, what is the difference between the two quantities?) What is the percent error, calculated as (approx value actual value)/(actual value)?
- (f) Draw a rough sketch of f(x) and L(x), and use the picture and your computations to explain, in a sentence or two, why using L(2.1) to approximate the cube of 2.1 is a reasonable thing to do.