

Worksheet Section 3.2: More Product Rule and Quotient Rule
Introduction to Section 3.3

1. For each of the following, compute the derivative using the product or quotient rule, and then compute the derivative without using the product or quotient rule, after the indicated algebraic pre-processing. Do you get the same answer? Which one is easier?

(a) $F(x) = \frac{e^x + 1}{\sqrt{2} + 1} = \frac{1}{\sqrt{2} + 1} (e^x + 1)$

with product/quotient

without product/quotient

(b) $H(s) = \frac{A}{B\sqrt{s}} = \frac{A}{B} s^{-1/2}$

with product/quotient

without product/quotient

(c) $k(t) = \frac{t^3 + 6}{t} = t^2 + 6t^{-1}$

with product/quotient

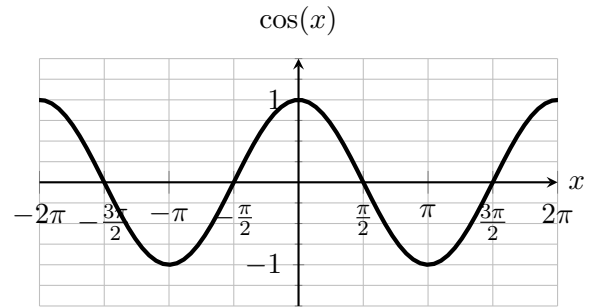
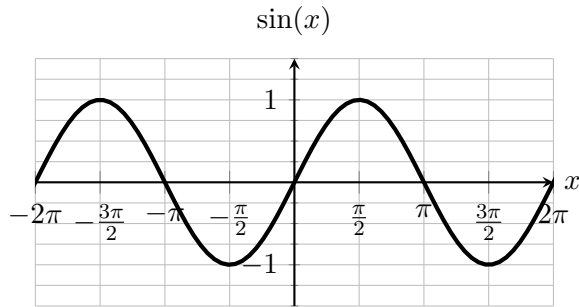
without product/quotient

(d) $y = (x - \pi)e^x = xe^x - \pi e^x$

with product/quotient

without product/quotient

2. Use the graphs of $y = \sin x$ and $y = \cos x$ to sketch a graph of y' (on the same set of axes).



What do you notice?

3. Use the fact that $\frac{d}{dx} \sin(x) = \cos(x)$ and $\frac{d}{dx} \cos(x) = -\sin(x)$ to find the derivative of

$$y = 3x^4 \cos(x).$$

4. Use the fact that $\tan(x) = \frac{\sin(x)}{\cos(x)}$ and the quotient rule to determine the derivative of $y = \tan(x)$. Simplify your answer as much as possible.

5. The equation of motion of a particle is $s(t) = t^3 - 3t$, where s is in meters and t is in seconds. Find:
- the velocity and acceleration as functions of t ,
 - the acceleration after 2 s,
 - the acceleration when the velocity is 0.