

Name: \_\_\_\_\_

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**Assessment 5 Instructions:**

- The AS-5 is 10 problems and is worth 40 points.
- You will have 1 hour to complete AS-5.
- The AS-5 is closed book and closed notes.
- **Calculators are not allowed** on the AS-5.
- Show all your work for full credit and box your final answer.

1. **[4 points]** Use the properties of logarithms to **expand** the following expressions as much as possible.

$$\log \left( \frac{10}{\sqrt{x+y}} \right)$$

2. **[4 points]** Solve the following exponential and logarithmic equations.

a.  $e^{4x} = e^{3x+14}$

b.  $\log_5 x^2 = 3$

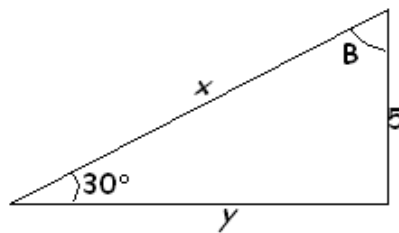
3. [4 points] Convert each of the following angle measures as directed.

a. Express  $\frac{3\pi}{2}$  in degrees.

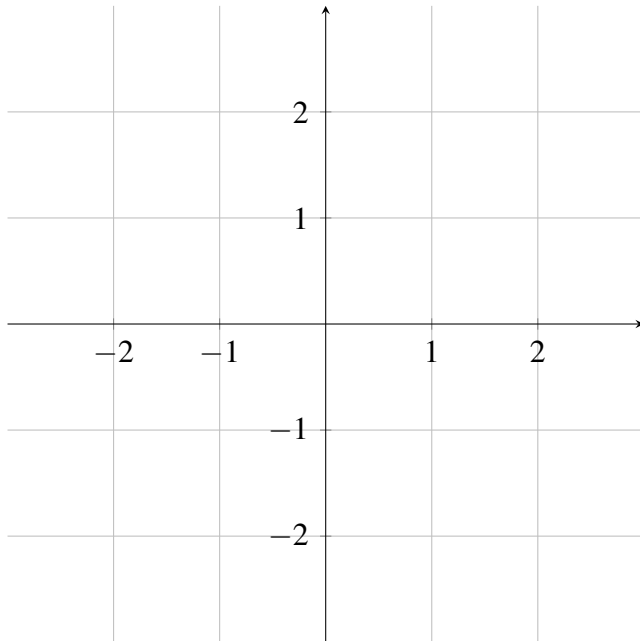
b. Express  $-144^\circ$  in radians.

4. [4 points] Find the area of the sector of a circle of radius 20 ft with a central angle of  $138^\circ$ . (*Hint:*  $A = \frac{r^2\theta}{2}$ )

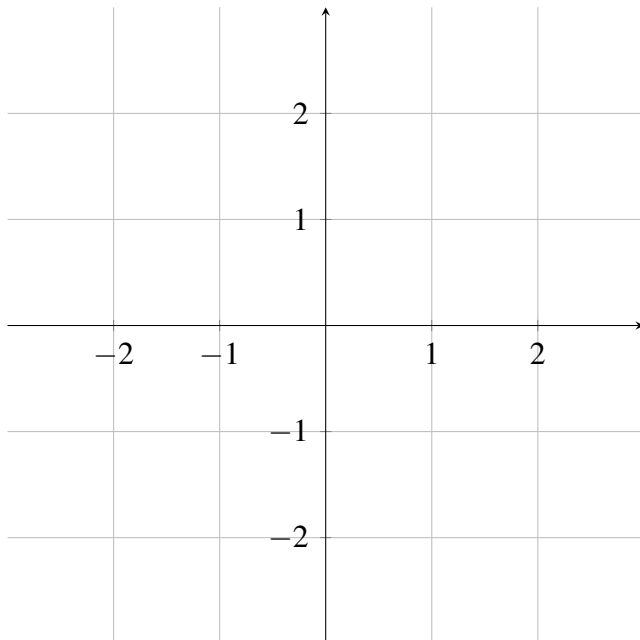
5. [4 points] Use the information contained in the figure to determine the values of the six trigonometric functions of an angle  $B$ .



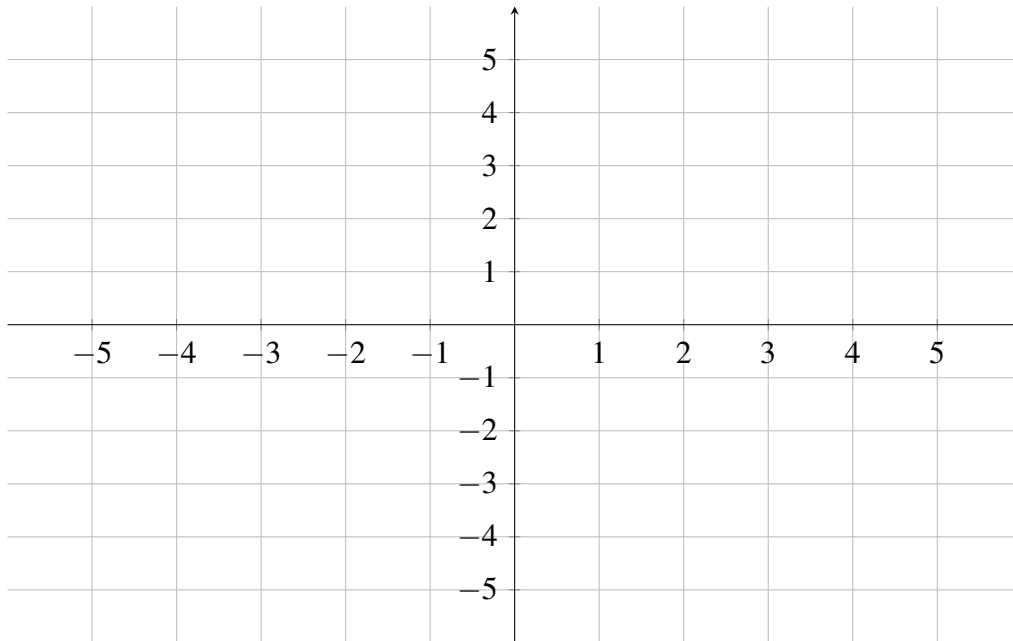
6. [4 points] Determine the point  $(x,y)$  on the unit circle associated with the real number  $s = -\frac{\pi}{4}$ . Sketch the the unit circle and the point  $(x,y)$  on it on the plane below.



7. [4 points] Determine the reference angle associated with the given angle  $\theta = -60^\circ$ . Sketch both angles  $\theta$  and  $\theta'$  on the plane below.



8. [4 points] Sketch the graph of the function  $g(x) = -2\sin(2\pi x)$ . State **precisely** the amplitude, frequency and phase shift for the given function.



9. [4 points] Evaluate the following expressions

a.  $\arccos(-1) =$

b.  $\arctan(-\sqrt{3}) =$

10. [4 points] Use trigonometric identities to simplify the expression

$$\frac{1}{\sec^2 x} + \sin x \cdot \cos\left(\frac{\pi}{2} - x\right)$$