

Name: _____

Solutions

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No aids (calculator, notes, text, etc.) are permitted. Show all work for full credit and box your final answer.

1. [4 points] Convert the following angles to appropriate measure:

1. convert $\frac{7\pi}{20}$ to degrees

2. convert 132° to radians

$$1. \frac{7\pi}{20} \text{ rad} = \frac{7\pi}{20} \cdot \left(\frac{180}{\pi}\right)^\circ = \frac{7 \cdot 180}{20} = 63^\circ$$

$$2. \quad 132^\circ = 132 \cdot \frac{\pi}{180} \text{ rad} = \frac{66\pi}{90} \text{ rad} = \frac{11\pi}{15} \text{ rad}$$

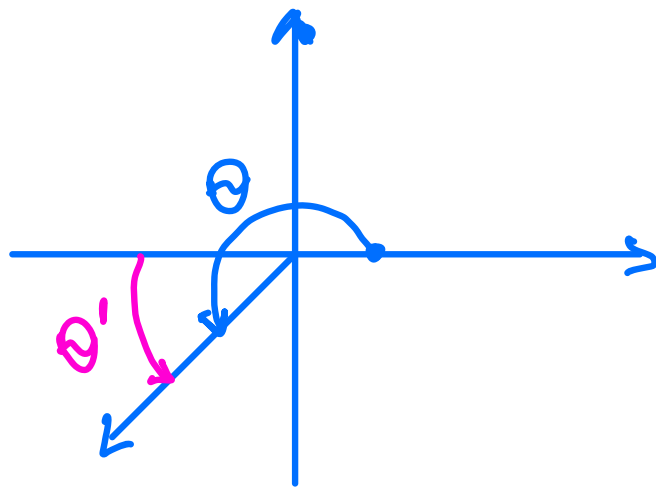
2. [6 points] For the given angle $\theta = \frac{5\pi}{4}$ do the following:

a. find the reference angle θ'

b. calculate $\sin \theta$, $\cos \theta$

c. calculate $\tan \theta'$, $\cot \theta'$

Hint: Sketch the angle θ on the plane.



$$\theta = \frac{5\pi}{4} = \pi + \frac{\pi}{4}$$

(a) $\theta' = \frac{\pi}{4}$

(b) $\sin \theta = -\frac{\sqrt{2}}{2}$, $\cos \theta = -\frac{\sqrt{2}}{2}$

(c) $\tan \theta' = 1$, $\cot \theta' = 1$

3. [2 points] Determine the amplitude, period, frequency, and phase shift for the following trigonometric function (Use appropriate notations for all the terminology above).

$$f(x) = -\frac{1}{2} \cos(8x + 1)$$

$$\begin{aligned} a &= -\frac{1}{2} \\ b &= 8 \\ c &= 1 \end{aligned}$$

Amplitude: $a = -\frac{1}{2}$, $|a| = \boxed{\frac{1}{2}}$

Frequency: $\gamma = \frac{b}{2\pi} = \frac{8}{2\pi} = \boxed{\frac{4}{\pi}}$

Period: $T = \frac{1}{\gamma} = \boxed{\frac{\pi}{4}}$

Phase shift left: $\frac{c}{b} = \boxed{\frac{1}{8}}$