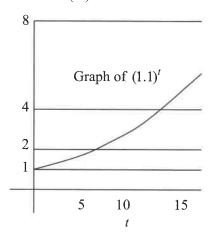
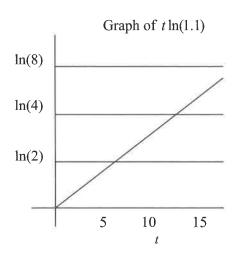
- 1.1.13 We use the following result from calculus: if f and g are differentiable functions such that f(a) = g(a) and f'(x) < g'(x) for a < x < b, then f(b) < g(b).
  - (i) Suppose 0 < t < 1. Let  $f(i) = (1+i)^t$  and  $g(i) = 1+i \cdot t$ . Then f(0) = g(0) = 1. If we can show that f'(i) < g'(i) for any i > 0, then we can use the calculus result above to conclude that f(i) < g(i) for any i > 0. First note that  $f'(i) = t \cdot (1+i)^{t-1}$  and g'(i) = t. Since i > 0, it follows that 1+i > 1, and since t < 1, it follows that t 1 < 0. Then  $(1+i)^{t-1} < 1$ , so f'(i) < g'(i).

This completes the proof of part (i).

- (ii) Suppose that t > 1. Let  $f(i) = 1 + i \cdot t$  and  $g(i) = (1+i)^t$ . Again f(0) = g(0). If we can show that f'(i) < g'(i) for any i > 0, then we can use the calculus result above to conclude that f(i) < g(i) for any i > 0. Since t > 1 and i > 0 it follows that t 1 > 0 and 1 + i > 1. Thus  $(1+i)^{t-1} > 1$ , and it follows that  $f'(i) = t < t \cdot (1+i)^{t-1} = g'(i)$ . This completes the proof of part (ii).
- 1.1.14 Original graph is  $y = (1+i)^t$ . New graph is  $10^y = (1+i)^t$ , or, equivalently,  $y = t \cdot \frac{\ln(1+i)}{\ln(10)}$ , so that y is now a linear function of t.





## SECTIONS 1.2 AND 1.3

1.2.1 Present value is

$$5000 \left[ \frac{1}{1.06} + \frac{1}{(1.06)^2} + \frac{1}{(1.06)^3} + \frac{1}{(1.06)^4} \right] = 17,325.53.$$

1.2.2 Amount now required is

$$25,000[v^{17}+v^{15}+v^{12}]+100,000[v^{20}+v^{18}+v^{15}] \,=\, 75,686$$

1.2.3 
$$28 = 15 + 16.50v \rightarrow v = .78779 \rightarrow i = .2692$$

$$1.2.4 \quad 1000 \cdot v_{06}^3 \cdot v_{07}^4 \cdot v_{09}^3 = 494.62$$

1.2.5 Equation of value on July 1, 2013 is

$$200(1.04) + 300v = 100(1.04)^4 + X \rightarrow X = 379.48.$$