

Problem 1

Language: Python3

A 2-link manipulator has a revolute joint 1 with the angle and followed by a prismatic joint with the value q . The end effector position is given by

$$x = a \cdot \cos \theta - q \cdot \sin \theta$$

$$y = a \cdot \sin \theta + q \cdot \cos \theta$$

Find the Jacobian matrix of the robot, and determine its singularities.

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In [2]: import sympy as sp
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In [13]: # define symbolic variables
q,t = sp.symbols('q t')

# define forward kinematic equations
x = a*sp.cos(t) - q*sp.sin(t)
y = a*sp.sin(t) + q*sp.cos(t)

# define intermediate diff variables
_x11 = sp.diff(x, t)
_x12 = sp.diff(x, q)
_y21 = sp.diff(y, t)
_y22 = sp.diff(y, q)

# define jacobian matrix
p1_j = sp.simplify(
    sp.Matrix([
        [_x11, _x12],
        [_y21, _y22]
    ])
)
print("jacobian matrix:")
display(p1_j)

# determine singularities
# find determinate of jacobian
p1_j_det = sp.det(p1_j)
print("determinate of jacobian:")
display(p1_j_det)

# solve for singularities
p1_singularities = sp.solve(sp.simplify(p1_j_det), [t, q])
print("singularities:")
display(sp.simplify(p1_singularities))
```

jacobian matrix:

$$\begin{bmatrix} -a \sin(t) - q \cos(t) & -\sin(t) \\ a \cos(t) - q \sin(t) & \cos(t) \end{bmatrix}$$

determinate of jacobian:

$$(-a \sin(t) - q \cos(t)) \cos(t) + (a \cos(t) - q \sin(t)) \sin(t)$$

singularities:

$$[(t, 0)]$$