Caliko User Guide

Alastair Lansley / Federation University Australia

a.lansley@federation.edu.au

Contents

Introduction

The Caliko library is a free open-source software (FOSS) implementation of the FABRIK (Forward And Backward Reaching Inverse Kinematics) algorithm created by Aristidou and Lasenby. It is written in the Java programming language.

The inverse kinematics (IK) algorithm is implemented in both 2D and 3D, and incorporates a variety of joint constraints, as well as the ability to connect multiple IK chains together in a hierarchy.

The library allows for the simple creation and solving of multiple IK chains as well as visualisation of these solutions. You can watch a short video outlining the setup and functionality of it here: https://www.youtube.com/watch?v=wEtp4P2ucYk

The Caliko library is licensed under the MIT software license and the source code is freely available for use and modification at: https://github.com/feduni/caliko

Please feel free to report any issues at: https://github.com/feduni/caliko/issues

Further details on the FABRIK algorithm itself can be found in the following paper:

Aristidou, A., & Lasenby, J. (2011). FABRIK: a fast, iterative solver for the inverse kinematics problem. Graphical Models, 73(5), 243-260.

Demo / Quick Start

If you'd like to see what the Caliko library does, then a YouTube demonstration video is available at:

https://www.youtube.com/watch?v=D9-V66m9DVI
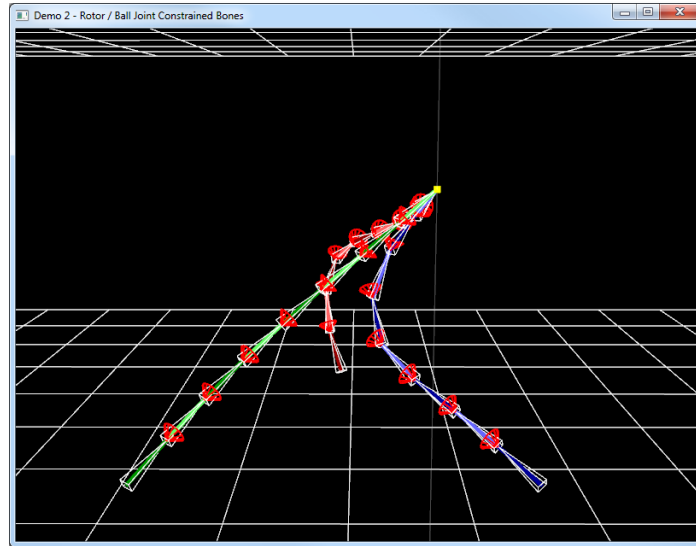
If you'd like to experiment with the demo yourself then you can either download a pre-compiled release from https://github.com/FedUni/caliko/releases or you can use git to clone the Caliko repository at https://github.com/FedUni/caliko and build the library via maven by using the command:

```
mvn package
```

Once you have the library, simply run the demo app from the **caliko/demo** folder either by right-clicking on it and selecting **[Open]** from the pop-up menu (on Windows), or from the command line by issuing the command:

```
java -jar caliko-demo-jar-with-dependencies.jar
```

To run the demo application Java 1.8 and OpenGL 3.3 or newer are required.

In 2D mode, clicking or holding the left mouse button (LMB) updates the target location to be at the location of the cursor. In 3D mode holding the LMB and moving the mouse allows you to look around. The keyboard controls used in the demo are listed below:

Table 1 - Default controls for the Caliko demonstration application.

Input	Action	Input	Action
Up/Down cursor keys	Toggle 2D/3D mode	C	Toggle drawing constraints
Left/Right cursor keys	Previous/Next demo	X	Toggle drawing axes (3D)
W/A/S/D keys	Move camera forward/back/left/right (3D)	M	Toggle drawing models (3D)
P	Toggle orthographic / perspective projection (3D)	L	Toggle drawing lines
F	Toggle fixed-base mode	Space	Toggle pausing moving target (3D)
R	Rotate base locations (3D)	Esc	Exit demo

Download and Structure

The Caliko library is publicly hosted on GitHub at: https://github.com/feduni/caliko

Complete releases may be found at: https://github.com/FedUni/caliko/releases

Releases are provided as a zip archive in the following structure:

```
.
└── caliko
    ├── build.txt
    ├── demo
    │   ├── caliko-demo.jar
    │   └── caliko-demo-jar-with-dependencies.jar
    ├── doc
    │   ├── caliko-user-guide.pdf
    │   └── javadoc.zip
    ├── jar
    │   ├── caliko.jar
    │   └── caliko-visualisation.jar
    └── src.zip

4 directories, 8 files
```
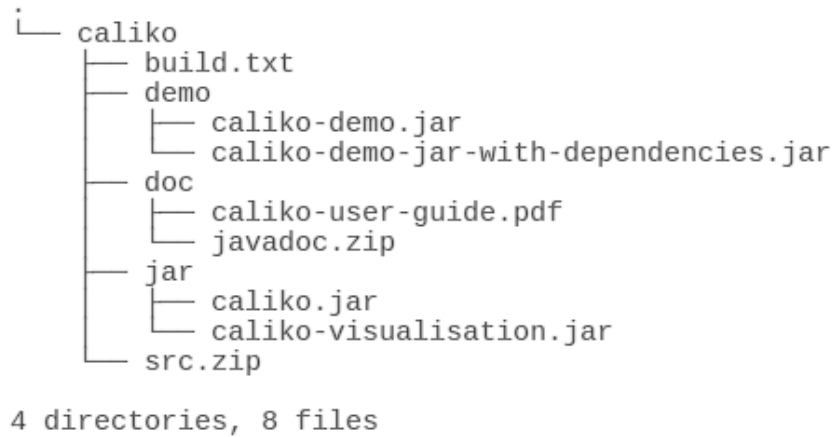
Figure 1 - The Caliko directory structure.

The **build.txt** file identifies the overall version of the Caliko library. This version number may not necessarily match the individual versions of the core and visualisation components which may change independently, however any increment of either component's version number will result in an increment of this overall library version.

The **demo** folder contains the compiled demo source along with a compiled version that includes the LWJGL3 library and native libraries for the Windows, Linux and Mac platforms. As such the 'jar-with-dependencies' is entirely self-contained and ready to be executed.

The **doc** folder contains this user guide and a combined archive of all Javadoc documentation for the library's application programming interface (API).

The **jar** folder contains compiled versions of the core / headless Caliko classes, along with the optional visualisation component.

The **src.zip** file contains all source code for the Caliko library and its visualisation component.

Installation and Setup

If using the jars instead of the source code, then the Caliko library must be added to your build path before it can be used. In an IDE such as Eclipse this is typically achieved by creating a new User Library, and then pointing at the jar file(s), along with the optional source code and Javadoc. For example:
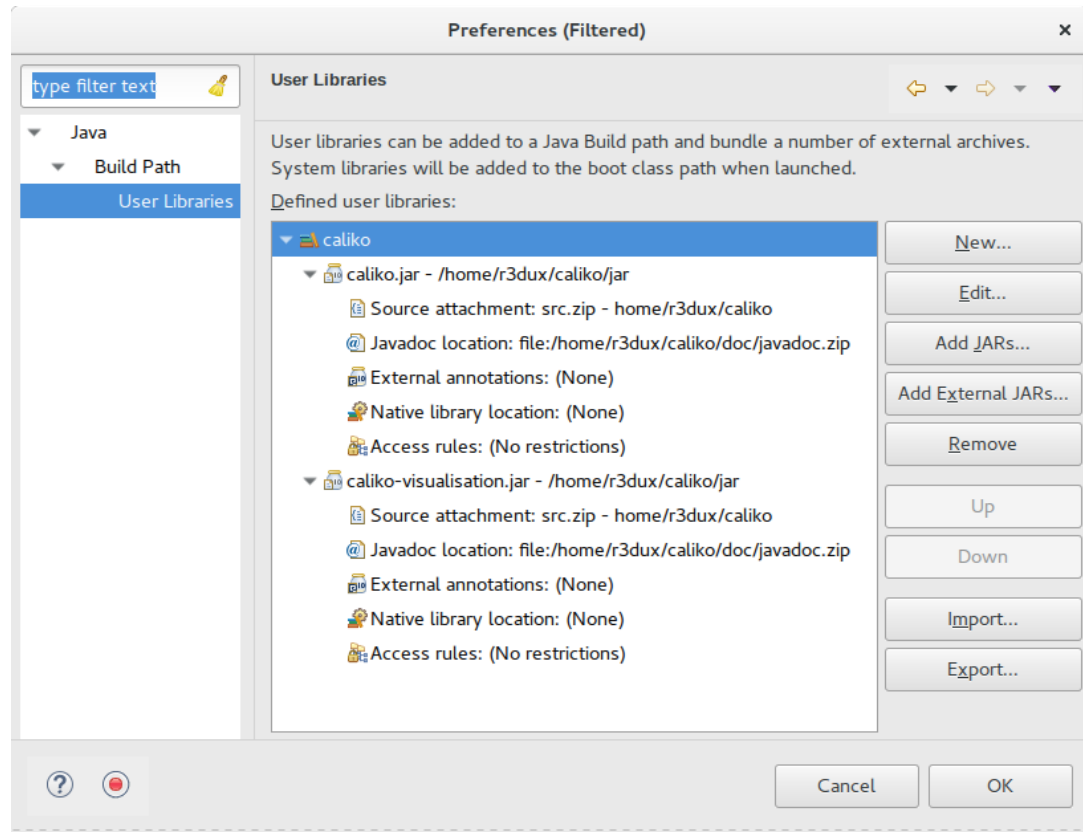

Figure 2 - An example of setting up the Caliko library as a User Library in Eclipse.

To use the visualisation component, which uses the LWJGL3 library, a similar process may be used to create a LWJGL3 user library. For example:
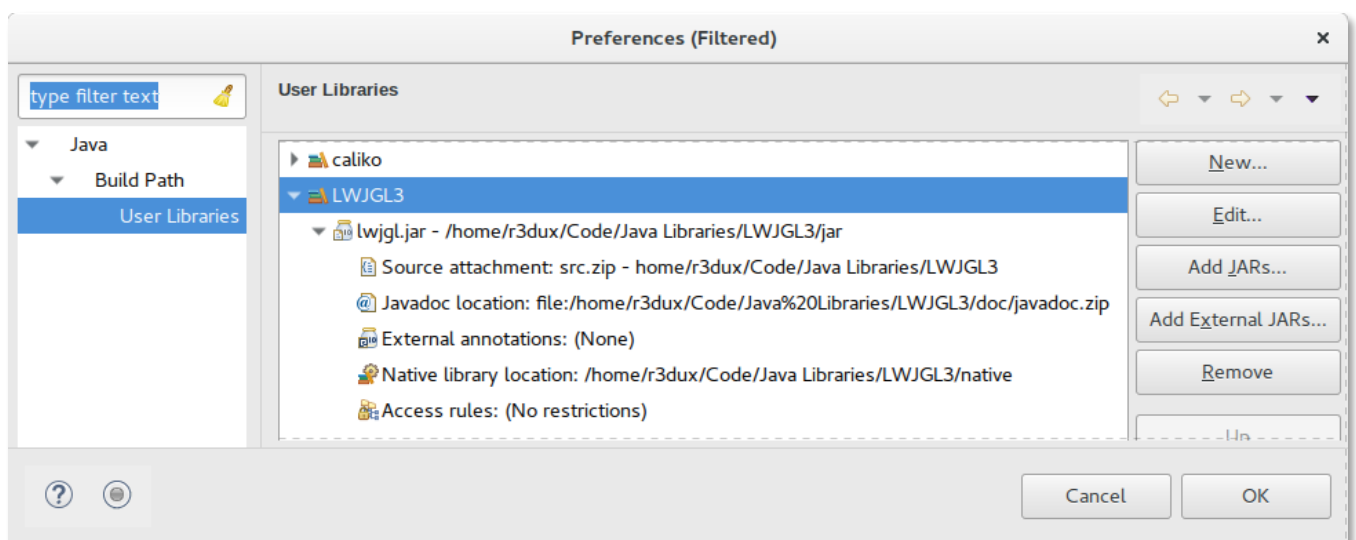

Figure 3 - An example of setting up the LWJGL3 library as a User Library in Eclipse.

Visualisation Setup

The LWJGL3 library guide at https://www.lwjgl.org/guide explains how to create an OpenGL context which can be used for drawing Caliko IK chains. Further, you may look at the Caliko demo app's **au.edu.federation.alansley** package, specifically the **OpenGLWindow** and **Application** classes to see how I've pieced this together.

Potentially the simplest setup you could get away for visualisation of IK chains is similar to the below:

```java
import org.lwjgl.*;
import org.lwjgl.glfw.*;
import org.lwjgl.opengl.*;
import static org.lwjgl.glfw.GLFW.*;
import static org.lwjgl.opengl.GL11.*;
import static org.lwjgl.system.MemoryUtil.*;

import au.edu.federation.caliko.*;
import au.edu.federation.caliko.visualisation.*;
import au.edu.federation.utils.*;

public class HelloCaliko
{
    // We need to strongly reference callback instances.
    private GLFWErrorCallback errorCB;
    private GLFWKeyCallback   keyCB;

    int WIDTH = 800; int HEIGHT = 600; // Window width and height
    private long window;               // Window handle

    FabrikChain2D chain = new FabrikChain2D(); // Create a new 2D chain

    // 2D projection matrix. Params: Left, Right, Top, Bottom, Near, Far
    Mat4f mvpMatrix  = Mat4f.createOrthographicProjectionMatrix(
                         -(float)WIDTH/2.0f,   (float)WIDTH/2.0f,
                          (float)HEIGHT/2.0f, -(float)HEIGHT/2.0f,
                          1.0f,                -1.0f );

    public void run()
    {
        // Create our chain
        FabrikBone2D base = new FabrikBone2D(new Vec2f(), new Vec2f(0.0f, 50.0f));
        chain.addBone(base);
        for (int boneLoop = 0; boneLoop < 5; ++boneLoop)
        {
            chain.addConsecutiveBone(new Vec2f(0.0f, 1.0f), 50.0f);
        }

        try
        {
            init();
            loop();

            // Release window and window callbacks
            glfwDestroyWindow(window);
            keyCallback.release();
        }
        finally
        {
            // Terminate GLFW and release the GLFWErrorCallback
            glfwTerminate();
            errorCallback.release();
        }
    }
```

```java
    private void init()
    {
        // Setup an error callback. The default implementation
        // will print the error message in System.err.
        glfwSetErrorCallback(errorCB = GLFWErrorCallback.createPrint(System.err));

        // Initialize GLFW. Most GLFW functions will not work before doing this.
        if ( glfwInit() != GLFW_TRUE )
            throw new IllegalStateException("Unable to initialize GLFW");
        glfwWindowHint(GLFW_RESIZABLE, GLFW_TRUE); // the window will be resizable

        // Create the window
        window = glfwCreateWindow(WIDTH, HEIGHT, "Hello Caliko!", NULL, NULL);
        if (window == NULL)
            throw new RuntimeException("Failed to create the GLFW window");

        // Setup a key callback
        glfwSetKeyCallback(window, keyCB = new GLFWKeyCallback() {
            @Override
            public void invoke(long window, int key, int scancode, int action, int
mods)
            {
                if ( key == GLFW_KEY_ESCAPE && action == GLFW_RELEASE )
                    glfwSetWindowShouldClose(window, GLFW_TRUE);
            }
        });

        // Get the resolution of the primary monitor
        GLFWVidMode vidmode = glfwGetVideoMode( glfwGetPrimaryMonitor() );

        // Center our window
        glfwSetWindowPos(window, (vidmode.width() - WIDTH) / 2,
                                 (vidmode.height() - HEIGHT) / 2);

        glfwMakeContextCurrent(window); // Make the OpenGL context current
        glfwSwapInterval(1);            // Enable v-sync
        glfwShowWindow(window);         // Make the window visible
    }

    private void loop()
    {
        // This line is critical for LWJGL's interoperation with GLFW's
        // OpenGL context, or any context that is managed externally.
        // LWJGL detects the context that is current in the current thread,
        // creates the GLCapabilities instance and makes the OpenGL
        // bindings available for use.
        GL.createCapabilities();

        // Set the clear color
        glClearColor(0.0f, 0.0f, 0.0f, 0.0f);

        Vec2f offset = new Vec2f(150.0f, 0.0f);
        Vec2f target = new Vec2f(100.0f, 100.0f);

        // Run the rendering loop until the user has attempted to close
        // the window or has pressed the ESCAPE key.
        while ( glfwWindowShouldClose(window) == GLFW_FALSE ) {
            glClear(GL_COLOR_BUFFER_BIT | GL_DEPTH_BUFFER_BIT); // Clear buffers
            chain.solveForTarget( target.plus(offset) );        // Solve the chain
            FabrikLine2D.draw(chain, 3.0f, mvpMatrix);          // Draw the chain
            glfwSwapBuffers(window);                            // Swap colour buf.

            // Rotate the offset 1 degree per frame
            offset = Vec2f.rotateDegs(offset, 1.0f);
```

```
                // Poll for window events. The key callback above will only be
                // invoked during this call.
                glfwPollEvents();
        }
    }

    public static void main(String[] args) { new HelloCaliko().run(); }
}
```

When this code is executed, we'll have a simple 2D chain with six bones (the basebone plus the five we added) which is constantly solved for the given rotating location.
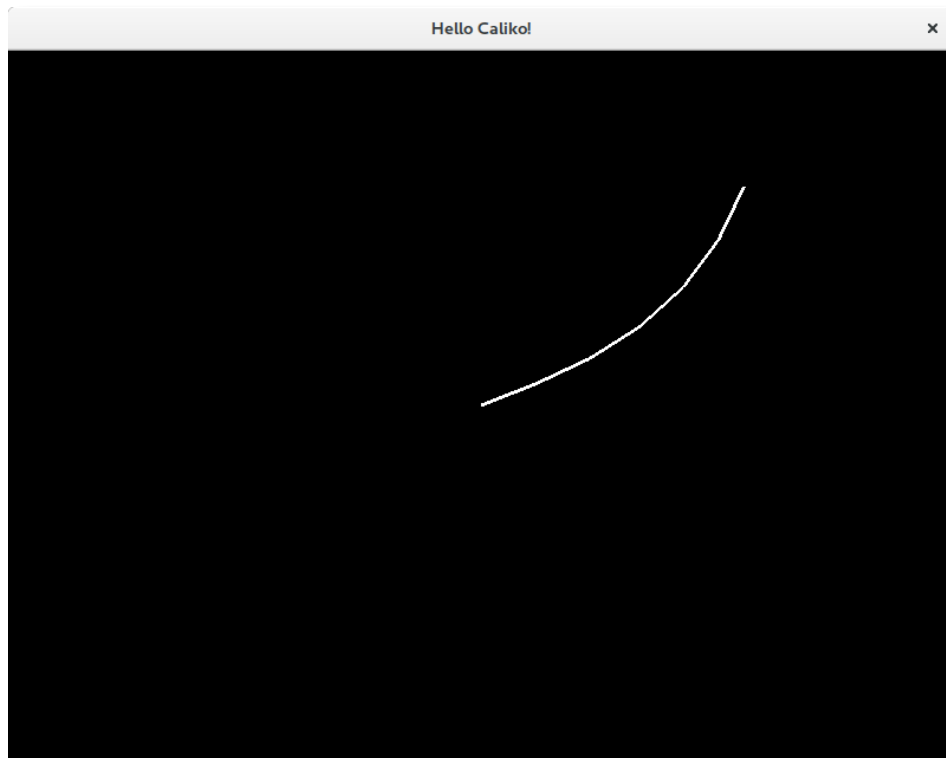

Figure 4 - An example of running the above sample code to create an OpenGL context, and solve and display a simple 2D chain. It's more interesting to look at in motion than via a static screenshot ;-)

IK Terminology and Workflow

An IK **chain** is a collection of IK **bones** which are connected to each other. The very first bone in the chain is called the **basebone**, and the start location of the basebone is called the **base location**.

Each bone has a start location and an end location which, depending on whether we are working in 2D or in 3D, will be defined in either 2D or 3D space. The end location of the final bone in a chain is called the **end-effector**.

Each bone also has a single **joint** which may control the allowable movement of the bone.

The typical workflow of an IK setup is that:
- A chain is created,
- One or more bones are added to this chain, then
- An attempt is made to **solve** the chain for a given target location.

It is during this solve attempt that, in this case, the FABRIK algorithm is executed which may alter the configuration of the chain so that the end-effector is as close to the target location as possible.

During this solve attempt:
- The length of the bones do not change, and
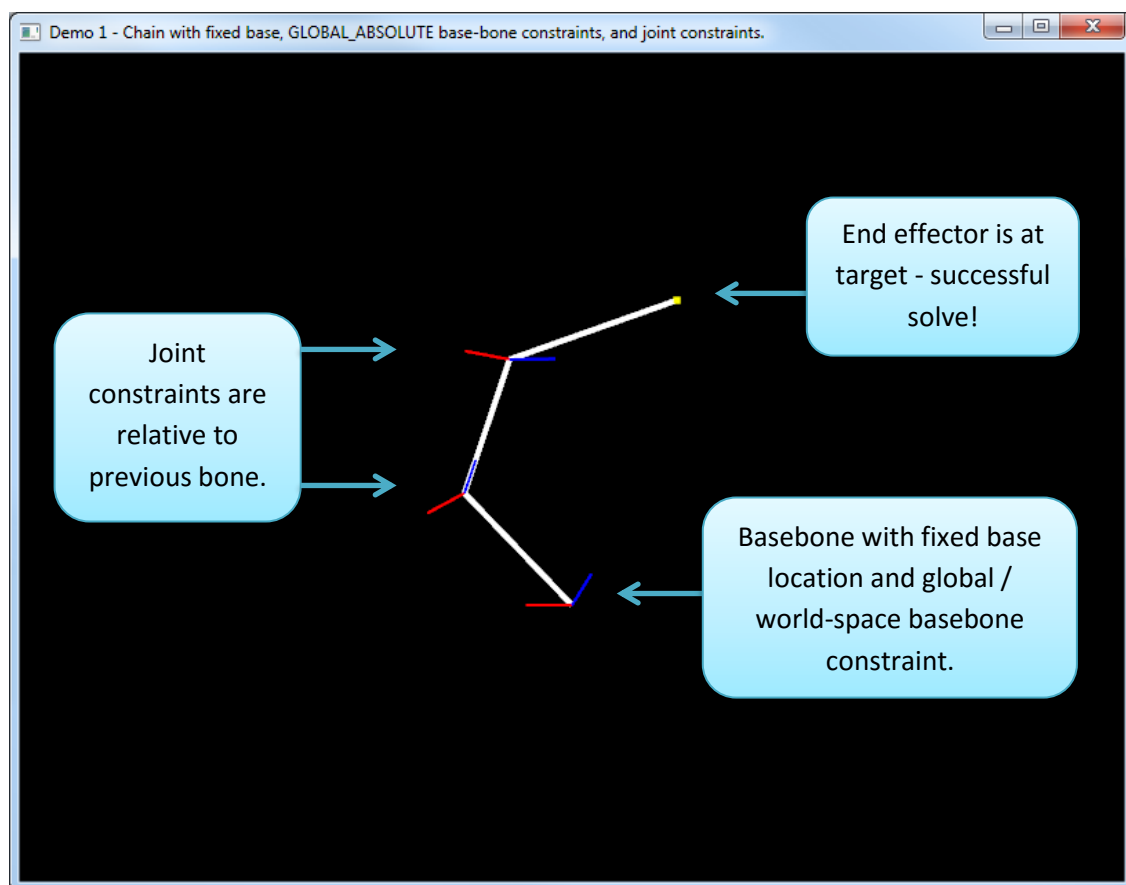- The end location of one bone and the start location of the following bone overlap precisely.

Figure 5 - A simple IK chain in 2D. It contains three bones, has a fixed base location, and has been successfully solved.

Structures

In the Caliko library, multiple IK chains may be connected to each other by placing them into a special 'holder' object called a *structure*. For example, after adding an initial chain to a structure, we might decide to add a second chain to the structure where the basebone of that second chain is connected to the end joint of the third bone in the initial chain (or the start joint of the second bone etc. - it's entirely up to you).

As such, when the first chain moves, the second chain's base location also moves in order to remain attached.

Joints and Restrictions

Each bone in a chain may be configured to allow only a restricted subset of motion. In the Caliko library there are two specific types of restriction:
-   **Basebone restrictions** - which are applied to the *chain*, and
-   **Joint restrictions** - which are applied to individual *bones*.

Depending on whether you are working in 2D or 3D there are a variety of different basebone and standard joint restriction types.

Basebone Restrictions

A basebone restriction is a special-case of standard restriction, and is required because the basebone itself is the very first bone in a chain and as such does not have a previous bone which it may be restricted about.

In 2D, the basebone restriction types are:
-   **NONE**   - No constraint,
-   **GLOBAL_ABSOLUTE**   - Constrained about a global / world-space direction,
-   **LOCAL_RELATIVE**   - Constrained about the direction of the connected bone, and
-   **LOCAL_ABSOLUTE**   - Constrained about a direction relative to that of the connected bone.

The LOCAL_RELATIVE and LOCAL_ABSOLUTE basebone constraint types are only available to be used by chains which are connected to other chains.

In 3D, the basebone restriction types are:
-   **NONE**   - No constraint,
-   **GLOBAL_ROTOR**   - Ball-joint constrained about a global / world-space direction,
-   **LOCAL_ROTOR**   - Ball-joint constrained about the direction of the connected bone,
-   **GLOBAL_HINGE**   - Hinge constrained about a world-space axis, and
-   **LOCAL_HINGE**   - Hinge constrained about an axis relative to that of the connected bone.

As before, the LOCAL_ROTOR and LOCAL_HINGE basebone constraint types are only available to be used by chains which are connected to other chains. In addition, hinge constraints may have an additional *reference axis* constraint which is the direction within the axis of the hinge about which clockwise/anticlockwise movement is allowed.

To put this in perspective - if you think of the front door of your house rotating on its hinges: its reference axis would be when the door is closed, and it can likely rotate zero degrees one way (i.e. it doesn't open outwards) and maybe up to 100 degrees or such the other way to let people in and out.

3D parabolic constraints may be added in a future release, but are not implemented at the present time.

Joint Restrictions

As previously mentioned, each bone has a single joint which can be thought of as being at the start of the bone. In 2D there no specific joint types as the bones may only rotate clockwise and anticlockwise. In 3D, there are three distinct type of joint, which are:

- **BALL**   - A 'rotor' / ball-joint constraint about the previous bone in the chain,
- **GLOBAL_HINGE**   - A world-space hinge constraint, or
- **LOCAL_HINGE**   - A hinge constraint relative to the previous bone in the chain.

The default joint type of a 3D bone is BALL, and the default constraint angle is 180 degrees - which in effect means that no constraint is applied. Ball joints only have a single constraint angle which describes the 'rotor' arc the joint allows, while hinges both have clockwise and anticlockwise constraint angles which may be enforced about a given reference axis that falls within the plane of the hinge.
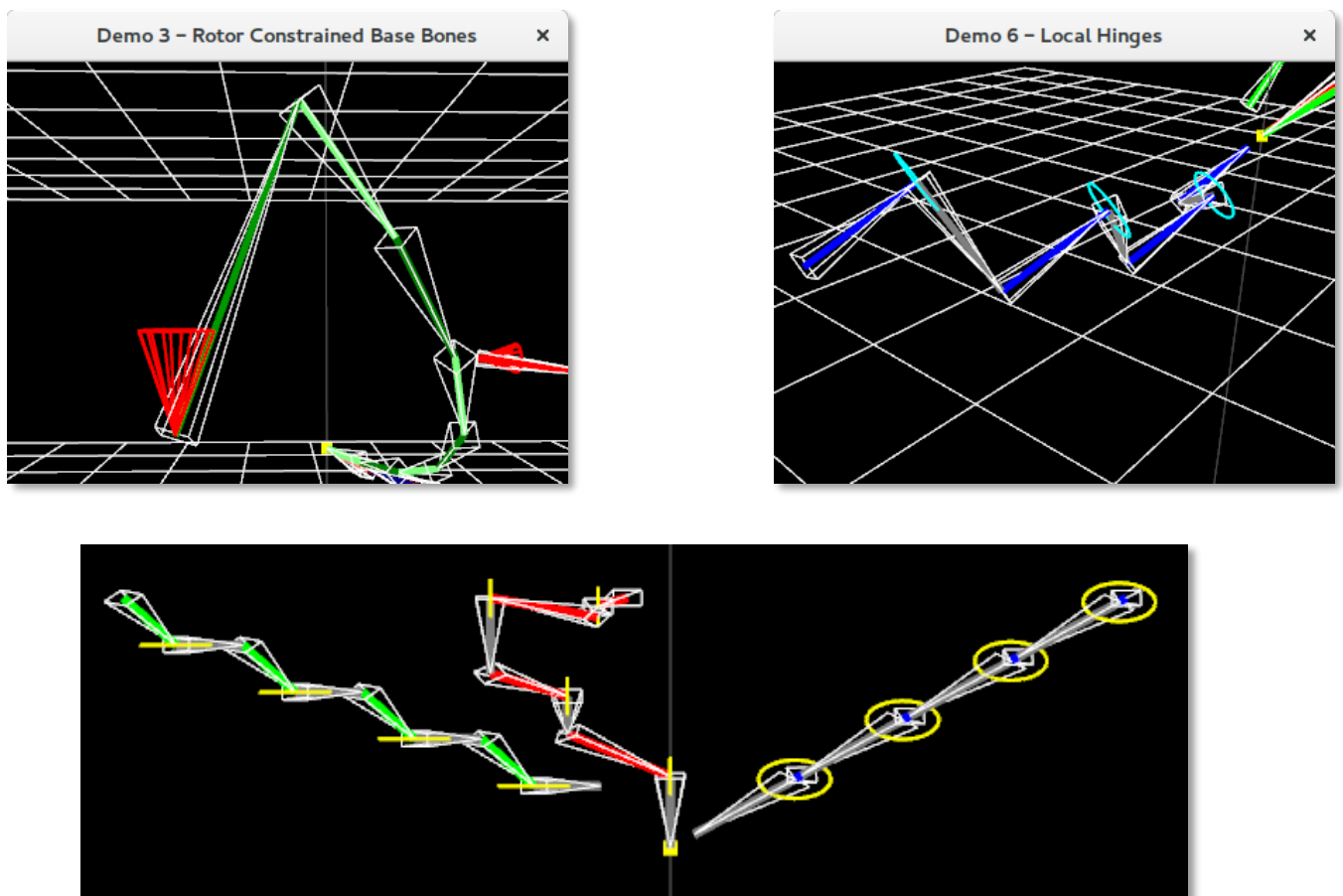

Figure 6 - Rotor / ball-joint constraints (top left) allow movement up to a given angle about the rotor constraint axis, local hinge constraints allow movement about the hinge axis in the coordinate system of the previous bone in the chain, while global hinge constraints (bottom) allow movement about a given world-space axis only.

Solving IK Chains and Structures

Once a chain exists and contains one or more bones, it can be solved by calling the **solveForTarget()** method and providing it a target location to solve the chain for. Targets may be specified as Vec2f or Vec3f objects, or as floats.

If multiple chains exists in a structure, then calling **solveForTarget()** along with a target location results in each chain in the structure being solved in a first-in-first-solved manner for the same target location. However, if a chain in a structure has the **useEmbeddedTarget** mode enabled, then the chain will be solved for its own

embedded target location rather than any provided target. In this manner, a structure may contain a combination of chains which can be solved for the specified target or their own embedded target location with a single call to **solveForTarget()** on the structure. If all chains in a structure use embedded targets then the provided target location is effectively ignored.

Chains that use embedded targets may update their targets via the chain's **updateEmbededTarget()** method, and individual chains may be solved for their embedded targets via a call to **solveForEmbeddedTarget()**.

Vectors and Matrices

The Caliko library uses a series of custom 2D and 3D vector classes (Vec2f, Vec3f) 3x3 and 4x4 matrices (Mat3f, Mat4f). These classes can be found in the **au.edu.federation.utils** package.

Array getters and setters exist to allow you to interact via the vector/matrix classes of your choice - but all Caliko vector and matrix properties are publicly accessible for ease of customisation purposes.

Both orthographic (2D) and perspective (3D) matrices can be created with ease through the provided Mat4f class, and the Vec3f and Vec2f classes offer a wide variety of methods to assist with manipulation of directions and locations. Please see the class source code and provided Javadoc for full API specifications.

Reproducable Sequences

If you'd like to experiment with modifications to the Caliko source code, in particular, the results of solving 3D chains in a reproducible manner - then you can set a fixed seed for the random number generator (which is used by the MovingTarget3D class) by calling:

```
Utils.setSeed(SOME_FIXED_INTEGER);
```

For example:

```
Utils.setSeed(123);
```

Usage Examples

The Caliko demo application provides a number of usage examples which exercise various aspects of the library functionality. The examples below demonstrate how a variety of IK scenarios may be constructed.

In these 2D examples, UP/DOWN/LEFT/RIGHT are defined as the vectors (0.0f, 1.0f) / (0.0f, -1.0f) / (-1.0f, 0.0f) and (1.0f, 0.0f) respectively. In the 3D examples X_AXIS is (1.0f, 0.0f, 0.0f), the Y_AXIS is (0.0f, 1.0f, 0.0f) and Z_AXIS is (0.0f, 0.0f, 1.0f). The Z-axis points directly outwards from the screen.

2D Demo 1 - Chain with GLOBAL_ABSOLUTE basebone constraint and joint constraints

```java
// Instantiate our structure, create a new chain and set it as fixed-base
FabrikStructure2D structure = new FabrikStructure2D();
FabrikChain2D chain = new FabrikChain2D();
chain.setFixedBaseMode(true);

// Default bone length
float boneLength = 40.0f;

// Create the basebone, set constraints and add it to the chain
FabrikBone2D base = new FabrikBone2D(new Vec2f(0.0f, -boneLength), new Vec2f() );
base.setClockwiseConstraintDegs(25.0f);
base.setAnticlockwiseConstraintDegs(90.0f);
chain.addBone(base);

// Fix the basebone and constrain it to the positive Y-axis
chain.setBaseboneConstraintType(BaseboneConstraintType2D.GLOBAL_ABSOLUTE);
chain.setBaseboneConstraintUV(UP);

// Create and add the second bone - 50 clockwise, 90 anticlockwise
chain.addConsecutiveConstrainedBone(UP, boneLength, 50.0f, 90.0f);

// Create and add the third bone - 75 clockwise, 90 anticlockwise
chain.addConsecutiveConstrainedBone(UP, boneLength, 75.0f, 90.0f);

// Finally, add the chain to the structure
structure.addChain(chain);
```
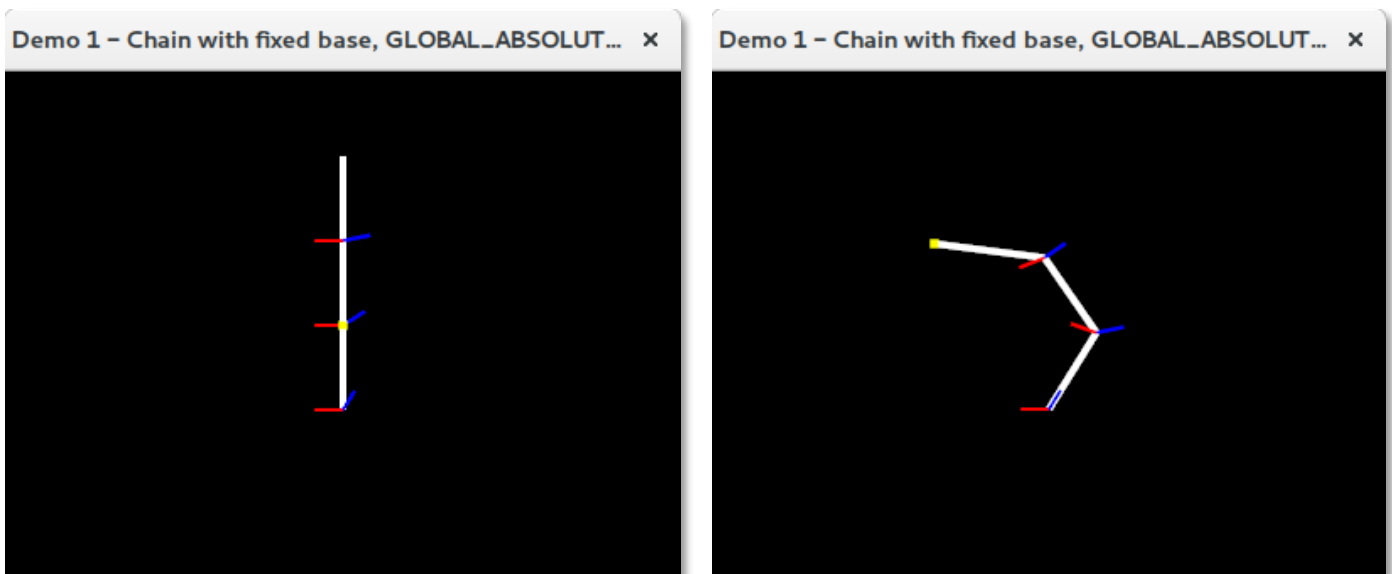

Figure 7 - Chain with GLOBAL_ABSOLUTE basebone constraint and joint constraints (left) original configuration (right) example solve configuration

2D Demo 2 - Chain with fixed base and multiple unconstrained bones

```java
// Instantiate our structure, create a new chain and set it as fixed-base
FabrikStructure2D structure = new FabrikStructure2D();
FabrikChain2D chain = new FabrikChain2D();
chain.setFixedBaseMode(true);

// Create the basebone and add it to the chain.
// Params: Start location, direction, length
FabrikBone2D base = new FabrikBone2D(new Vec2f(), RIGHT, 10.0f);
chain.addBone(base);

// Add a series of additional bones which initially form a circle
float boneLength = 10.0f;
float numBones   = 15;
float rotStep    = 360.0f / numBones;
for (int loop = 0; loop < numBones; loop++){
  // Rotate each bone by 10 degrees and add it to the chain
  Vec2f rotatedUV = Vec2f.rotateDegs(RIGHT, loop * rotStep);
  chain.addConsecutiveBone(rotatedUV, boneLength);
}

// Finally, add the chain to the structure
structure.addChain(chain);
```
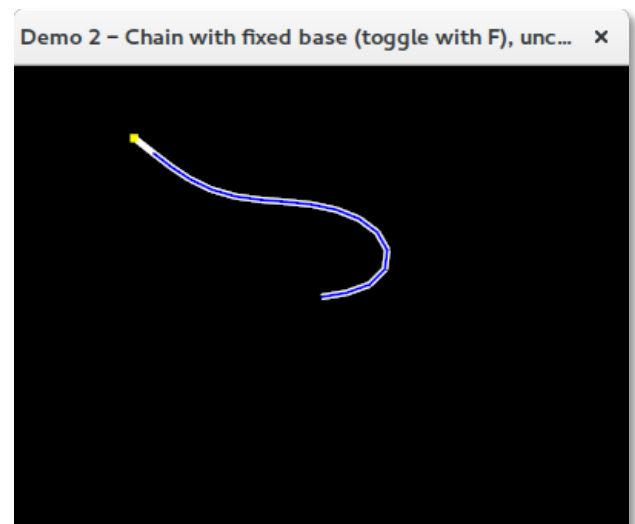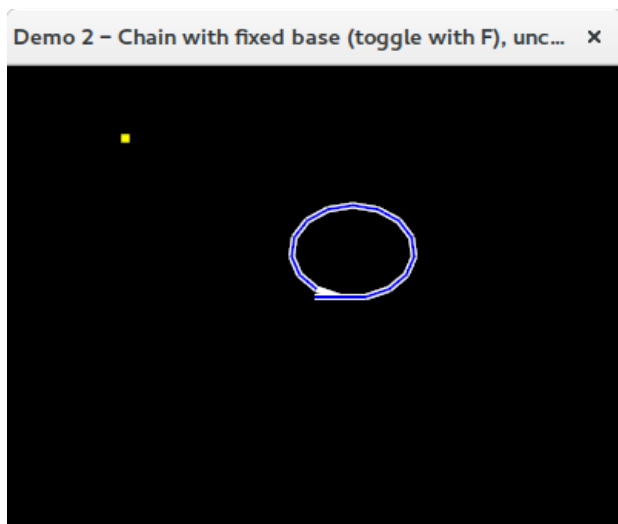

Figure 8 - Unconstrained chain (left) original configuration (right) example solve configuration

2D Demo 3 - Chain with fixed base and multiple constrained bones

```java
// Instantiate our structure, create a new chain and set it as fixed-base
FabrikStructure2D structure = new FabrikStructure2D();
FabrikChain2D chain = new FabrikChain2D();
chain.setFixedBaseMode(true);

// Create the basebone and add it to the chain.
// Params: Start location, direction, length
FabrikBone2D base = new FabrikBone2D(new Vec2f(), RIGHT, 10.0f);
chain.addBone(base);

// Add a series of additional bones which initially form a circle
float boneLength = 10.0f;
float numBones   = 15;
float rotStep    = 360.0f / numBones;
for (int loop = 0; loop < numBones; ++loop) {
```

```
    // Rotate each bone by 10 degrees and add it to the chain with constraint angles
    // Note: Anticlockwise rotation is positive, clockwise rotation is negative.
    Vec2f rotatedUV = Vec2f.rotateDegs(RIGHT, loop * rotStep);
    chain.addConsecutiveConstrainedBone(rotatedUV, boneLength, 60.0f, 60.0f);
}

// Finally, add the chain to the structure
structure.addChain(chain);
```
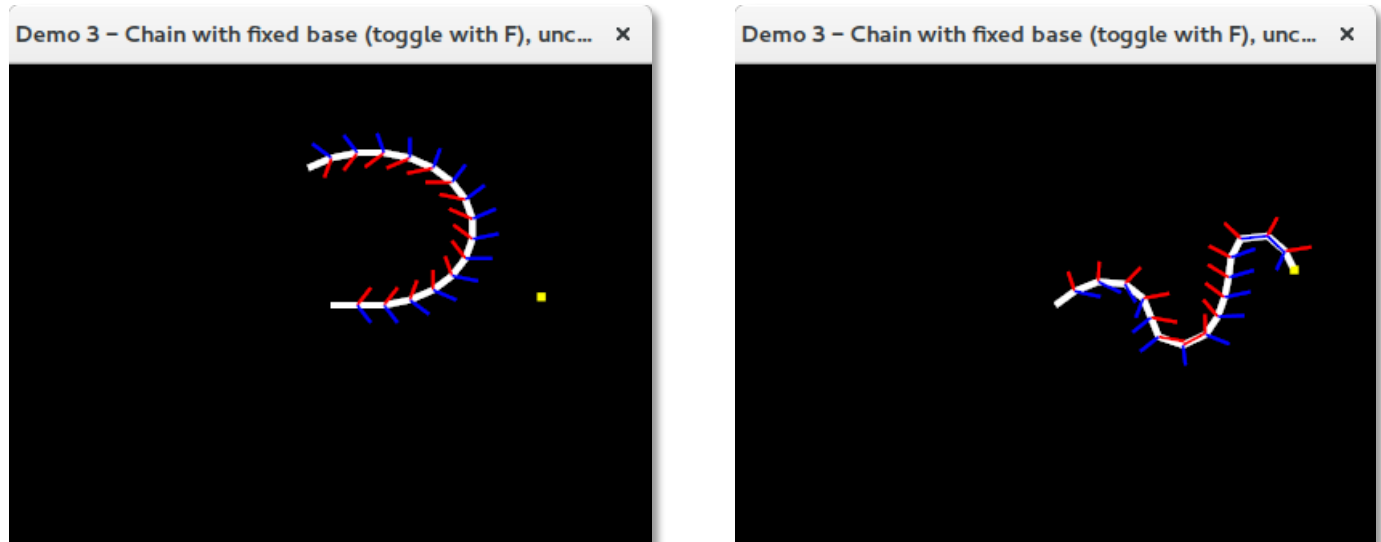

Figure 9 - Constrained chain in (left) original configuration and (right) example solve configuration. No bone may exceed its anticlockwise or clockwise constraint angles, shown in red and blue respectively.

2D Demo 4 - Chain with fixed base and multiple constrained bones

```
// Instantiate our FabrikStructure2D
FabrikStructure2D structure = new FabrikStructure2D();

// ----- Vertical chain -----
float boneLength = 50.0f;
FabrikChain2D verticalChain = new FabrikChain2D();
FabrikBone2D basebone = new FabrikBone2D( new Vec2f(0.0f, -50.0f), UP, boneLength);

// Note: Default basebone constraint type is NONE
verticalChain.addBone(basebone);

// Add two additional consecutive bones
verticalChain.addConsecutiveConstrainedBone(UP,  boneLength, 90.0f, 90.0f);
verticalChain.addConsecutiveConstrainedBone(UP,  boneLength, 90.0f, 90.0f);

// Add our main chain to structure
structure.addChain(verticalChain);

// ----- Left branch chain -----
boneLength = 30.0f;

// Create the base bone and set its colour
basebone = new FabrikBone2D( new Vec2f(), new Vec2f(-boneLength, 0.0f) );
basebone.setColour(Utils.MID_GREEN);

// Create the chain and add the basebone to it
FabrikChain2D leftChain = new FabrikChain2D();
leftChain.addBone(basebone);

// Add consecutive constrained bones
// Note: The base-bone is unconstrained, but these bones ARE constrained
```

```
leftChain.addConsecutiveConstrainedBone(LEFT, boneLength, 90.0f, 90.0f,
Utils.MID_GREEN);
leftChain.addConsecutiveConstrainedBone(LEFT, boneLength, 90.0f, 90.0f,
Utils.MID_GREEN);

// Add the chain to the structure, connecting to the end of bone 0 in chain 0
structure.addConnectedChain(leftChain, 0, 0, BoneConnectionPoint2D.END);

// ----- Right branch chain -----

// Create the base bone
basebone = new FabrikBone2D( new Vec2f(), new Vec2f(boneLength, 0.0f) );
basebone.setColour(Utils.GREY);

// Create the chain and add the basebone to it
FabrikChain2D rightChain = new FabrikChain2D();
rightChain.addBone(basebone);

// Add two consecutive constrained bones to the chain
// Note: The base-bone is unconstrained, but these bones ARE constrained
rightChain.addConsecutiveConstrainedBone(RIGHT, boneLength, 60.0f, 60.0f,
Utils.GREY);
rightChain.addConsecutiveConstrainedBone(RIGHT, boneLength, 60.0f, 60.0f,
Utils.GREY);

// Add the chain to the structure, connecting to the end of bone 1 in chain 0
structure.addConnectedChain(rightChain, 0, 2, BoneConnectionPoint2D.START);
```
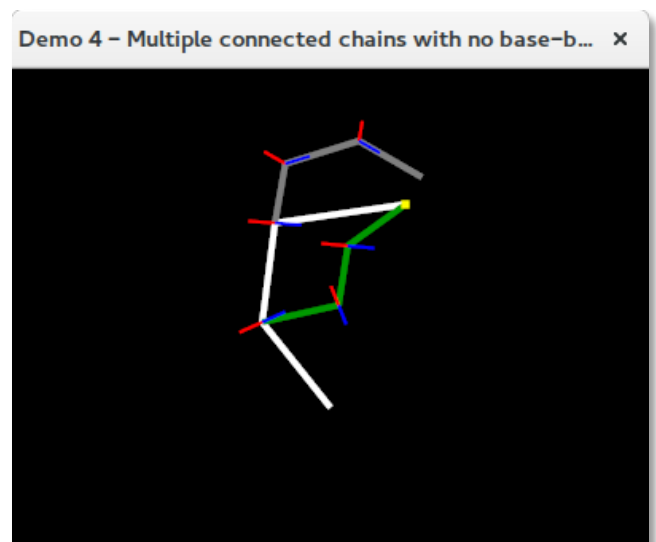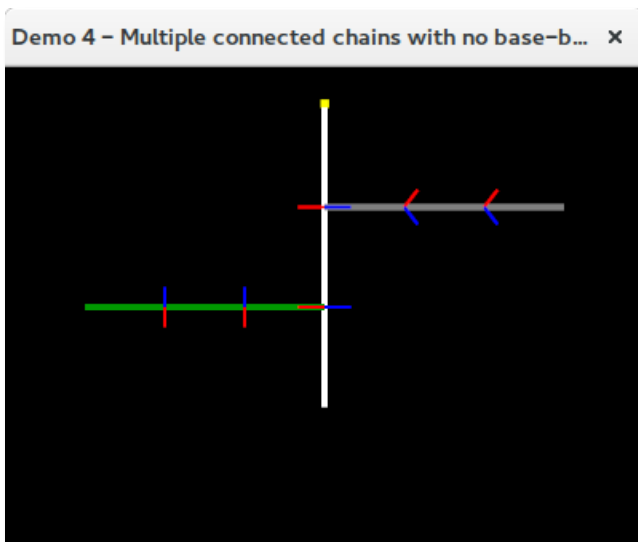

Figure 10 - Connected chains with fixed basebones, joint constraints and no basebone constraints. (left) original configuration (right) example solve configuration. The joint constraints on the grey chain prevent a successful solve in this instance.

2D Demo 5 - Multiple connected chains with LOCAL_RELATIVE basebone constraints

```
FabrikStructure2D structure = new FabrikStructure2D();

// ----- Vertical chain -----
float boneLength = 50.0f;
FabrikChain2D verticalChain = new FabrikChain2D();
FabrikBone2D basebone = new FabrikBone2D( new Vec2f(0.0f, -100.0f), UP,
boneLength);
basebone.setClockwiseConstraintDegs(15.0f);
basebone.setAnticlockwiseConstraintDegs(15.0f);

verticalChain.addBone(basebone);
```

```
verticalChain.addConsecutiveConstrainedBone(UP, boneLength, 30.0f, 30.0f);
verticalChain.addConsecutiveConstrainedBone(UP, boneLength, 30.0f, 30.0f);
verticalChain.setBaseboneConstraintType(BaseboneConstraintType2D.GLOBAL_ABSOLUTE);
verticalChain.setBaseboneConstraintUV(UP);

// Add chain to structure
structure.addChain(verticalChain);

// ----- Left branch chain -----
boneLength = 30.0f;

// Create the base bone
basebone = new FabrikBone2D( new Vec2f(), new Vec2f(-boneLength, 0.0f) );
basebone.setClockwiseConstraintDegs(60.0f);
basebone.setAnticlockwiseConstraintDegs(60.0f);
basebone.setColour(Utils.MID_GREEN);

// Create the chain, add the basebone and enable base bone constraint mode
FabrikChain2D leftChain = new FabrikChain2D();
leftChain.setBaseboneConstraintType(BaseboneConstraintType2D.LOCAL_RELATIVE);
leftChain.addBone(basebone);

// Add consecutive constrained bones
leftChain.addConsecutiveConstrainedBone(LEFT, boneLength, 60.0f, 60.0f,
                                        Utils.MID_GREEN);
leftChain.addConsecutiveConstrainedBone(LEFT, boneLength, 60.0f, 60.0f,
                                        Utils.MID_GREEN);

// Add the chain to the structure, connecting at the end of bone 0 in chain 0
structure.addConnectedChain(leftChain, 0, 0, BoneConnectionPoint2D.END);

// ----- Right branch chain -----
// Create the base bone
basebone = new FabrikBone2D( new Vec2f(), new Vec2f(boneLength, 0.0f) );
basebone.setClockwiseConstraintDegs(30.0f);
basebone.setAnticlockwiseConstraintDegs(30.0f);
basebone.setColour(Utils.GREY);

// Create the chain, add the basebone and enable base bone constraint mode
FabrikChain2D rightChain = new FabrikChain2D();
rightChain.setBaseboneConstraintType(BaseboneConstraintType2D.LOCAL_RELATIVE);
rightChain.addBone(basebone);

// Add two consecutive constrained bones to the chain
rightChain.addConsecutiveConstrainedBone(RIGHT, boneLength, 15.0f, 15.0f,
Utils.GREY);
rightChain.addConsecutiveConstrainedBone(RIGHT, boneLength, 15.0f, 15.0f,
Utils.GREY);

// Add the chain to the structure, connecting at the end of bone 1 in chain 0
structure.addConnectedChain(rightChain, 0, 1, BoneConnectionPoint2D.END);
```
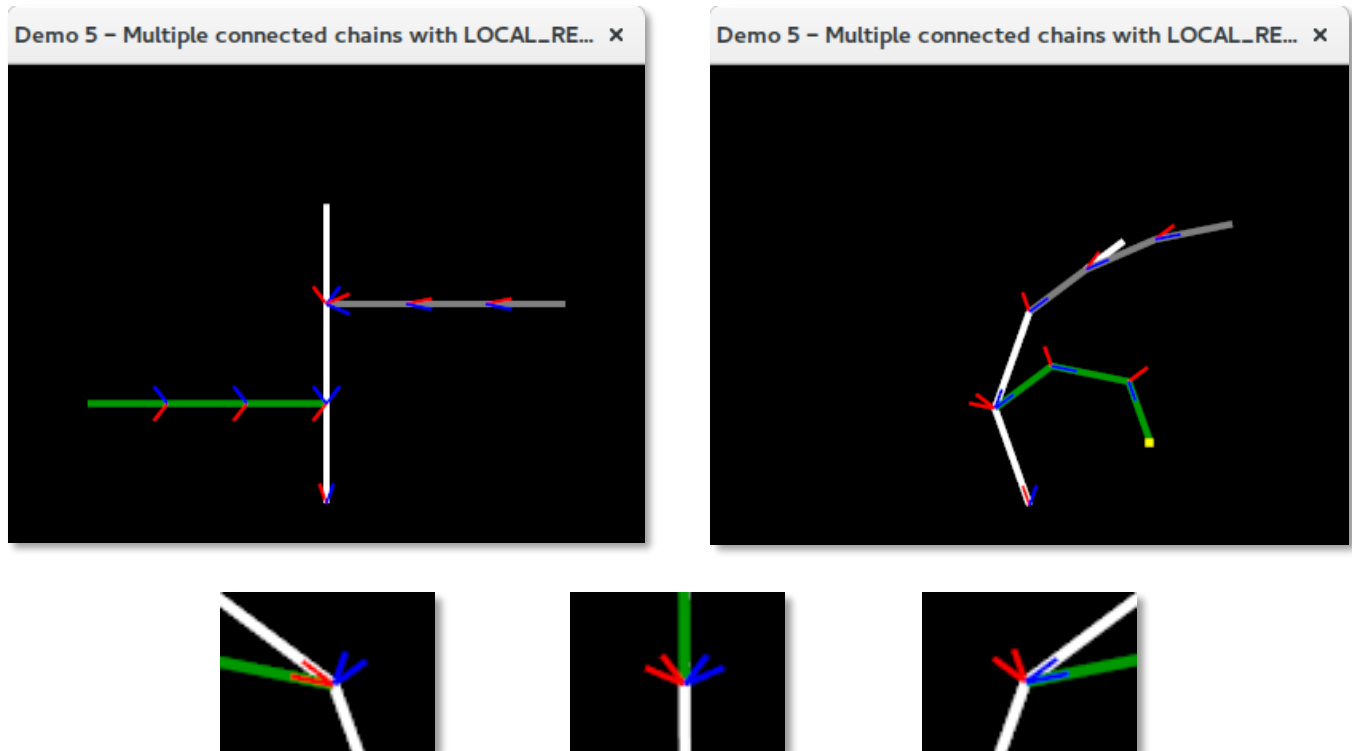
Figure 11 - Connected chains with local relative basebone constraints. (left) original configuration (right) example solved configuration. The white and grey chains are highly constrained in this example. The bottom row shows how the basebone constraints of the green chain move relative to the direction of the first bone in the white chain to which it is attached. Notice that the relative basebone constraints in the original configuration are not being honoured - this is because the structure as a whole has not been solved yet. When a solve attempt is made, all constraints are honoured.

2D Demo 6 - Multiple connected chains with LOCAL_ABSOLUTE basebone constraints

While LOCAL_RELATIVE basebone constraints are applied relative to the direction of the bone a chain is connected to, LOCAL_ABSOLUTE basebone constrains are applied as directions in the local coordinate space of the bone a chain is connected to.

For example, if a basebone constraint is the vector (-1.0f, 0.0f) [i.e. LEFT], then:
- If the bone the chain is connected to is pointing directly upwards, then the 'local' left remains *left*,
- If the bone the chain is connected to is pointing directly left, then 'local' left is now *down*,
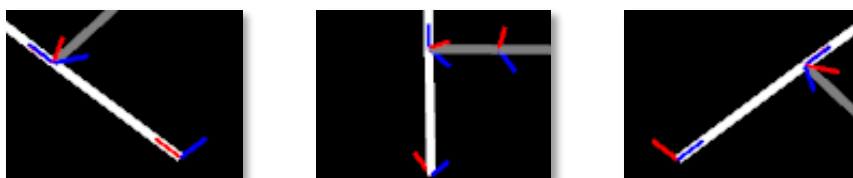- If the bone the chain is connected to is pointing directly right, then 'local' left is now *up*.

Figure 12 - The LOCAL_ABSOLUTE basebone constraint on the grey chain is set to RIGHT, but is maintained in the local space of the white 'host' bone that it's connected to.

LOCAL_ABSOLUTE basebone constraints can be set on a chain by specifying the constraint type **and** a constraint direction unit vector:

```
FabrikChain2D chain = new FabrikChain2D();
chain.setBaseboneConstraintType(BaseboneConstraintType2D.LOCAL_ABSOLUTE);
chain.setBaseboneConstraintUV(RIGHT);
// ...add bones to the chain here...

// If a chain has LOCAL basebone constraints it MUST be connected to another chain!
structure.addConnectedChain(chain, 0, 0, BoneConnectionPoint2D.END);
```

2D Demo 7 – Chains with embedded targets

```
float boneLength = 50.0f;
float startY     = -100.0f;
mStructure = new FabrikStructure2D();

FabrikChain2D chain = new FabrikChain2D();

// ----- Central white chain ------
// Create the first bone, configure it, and add it to the chain
FabrikBone2D basebone;
basebone = new FabrikBone2D(new Vec2f(0.0f, startY), new Vec2f(0.0f, startY +
boneLength) );
basebone.setClockwiseConstraintDegs(65.0f);
basebone.setAnticlockwiseConstraintDegs(65.0f);
chain.addBone(basebone);

// Fix basebone to its current location, and constrain it to the positive Y-axis
chain.setFixedBaseMode(true);
chain.setBaseboneConstraintType(BaseboneConstraintType2D.GLOBAL_ABSOLUTE);
chain.setBaseboneConstraintUV(UP);

// Add second and third bones
chain.addConsecutiveBone(UP, boneLength);
chain.addConsecutiveBone(UP, boneLength);

// Finally, add the chain to the structure
mStructure.addChain(chain);

// ----- Left green chain with embedded target -----
FabrikChain2D leftChain = new FabrikChain2D();
leftChain.setEmbeddedTargetMode(true); // Embedded target loc. set in demo loop
basebone = new FabrikBone2D(new Vec2f(), new Vec2f(-boneLength / 6.0f, 0.0f) );

// Add fifteen bones
leftChain.addBone(basebone);
for (int boneLoop = 0; boneLoop < 14; ++boneLoop)
{
      leftChain.addConsecutiveConstrainedBone(RIGHT, boneLength / 6.0f, 25.0f,
25.0f);
}

// Set chain colour and basebone constraint type
leftChain.setColour(Utils.MID_GREEN);

// Add the left chain to the structure, connected to the start of bone 1 in chain 0
mStructure.addConnectedChain(leftChain, 0, 1, BoneConnectionPoint2D.START);

// ----- Right grey chain with embedded target -----
FabrikChain2D rightChain = new FabrikChain2D();
rightChain.setEmbeddedTargetMode(true); // Embedded target loc. set in demo loop
basebone = new FabrikBone2D(new Vec2f(), new Vec2f(boneLength / 5.0f, 0.0f) );
basebone.setClockwiseConstraintDegs(60.0f);
basebone.setAnticlockwiseConstraintDegs(60.0f);

// Add ten bones
rightChain.addBone(basebone);
for (int boneLoop = 0; boneLoop < 9; ++boneLoop)
{
      rightChain.addConsecutiveBone(RIGHT, boneLength / 5.0f);
}

// Set chain colour and basebone constraint type
rightChain.setColour(Utils.GREY);
rightChain.setBaseboneConstraintType(BaseboneConstraintType2D.LOCAL_ABSOLUTE);
```

```
rightChain.setBaseboneRelativeConstraintUV(RIGHT);

// Add the right chain to the structure, connected to the start of bone 2 in chain 0
mStructure.addConnectedChain(rightChain, 0, 2, BoneConnectionPoint2D.START);
```

Chains that use embedded targets can have those targets updated by calls to the **updateEmbeddedTarget()** method.

Figure 13 - Multiple connected chains with 'fixed' bases. The left and right chains use embedded targets which are updated separately via calls to the chain's updateEmbeddedTarget method.

3D Demo 1 - Unconstrained bones

```
FabrikStructure3D structure  = new FabrikStructure3D();
FabrikChain3D chain          = new FabrikChain3D();
Colour4f colour              = new Colour4f(Utils.GREEN);
float boneLength             = 10.0f;
Vec3f boneDirection          = Z_AXIS.negated(); // i.e. into the screen

// Create a basebone and then add it to the chain
Vec3f start = new Vec3f(0.0f, 0.0f, 40.0f);
Vec3f end   = start.plus( defaultBoneDirection.times(boneLength) );
FabrikBone3D basebone = new FabrikBone3D(start, end);
basebone.setColour(colour);
chain.addBone(basebone);

// Add additional consecutive, unconstrained bones to the chain
for (int boneLoop = 0; boneLoop < 7; boneLoop++) {
    colour = (boneLoop % 2 == 0) ? colour.lighten(0.4f) : colour.darken(0.4f);
    chain.addConsecutiveBone(boneDirection, boneLength, colour);
}

// Finally, add the chain to the structure
structure.addChain(chain);
```
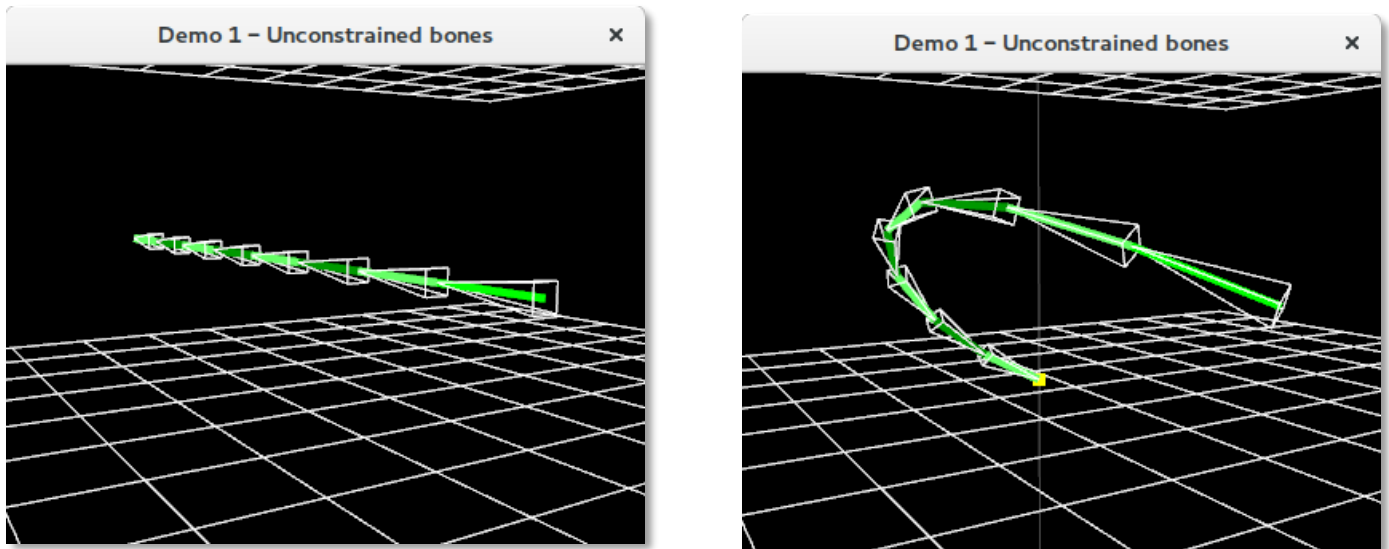
Figure 14 - A 3D chain containing unconstrained bones (left) in their initial and (right) in an example solved state.

3D Demo 2 - Rotor / ball joint constrained bones

```java
FabrikStructure3D structure = new FabrikStructure3D();
int numChains                = 3;
float rotStep                = 360.0f / (float)numChains;
float constraintDegs         = 45.0f;
Colour4f colour              = new Colour4f();
float boneLength             = 10.0f;
Vec3f boneDirection          = Z_AXIS.negated(); // i.e. into the screen

// Create chains and set colours
for (int chainLoop = 0; chainLoop < numChains; ++chainLoop) {
    FabrikChain3D chain = new FabrikChain3D();
    switch (chainLoop % numChains) {
        case 0: boneColour.set(Utils.MID_RED);   break;
        case 1: boneColour.set(Utils.MID_GREEN); break;
        case 2: boneColour.set(Utils.MID_BLUE);  break;
    }

    // Set up the initial base bone location...
    Vec3f startLoc = new Vec3f(0.0f, 0.0f, -40.0f);
    startLoc       = Vec3f.rotateYDegs(startLoc, rotStep * (float)chainLoop);
    Vec3f endLoc   = new Vec3f(startLoc);
    endLoc.z       -= defaultBoneLength;

    // ...then create a base bone, set its colour and add it to the chain.
    FabrikBone3D basebone = new FabrikBone3D(startLoc, endLoc);
    basebone.setColour(colour);
    chain.addBone(basebone);

    // Add additional consecutive rotor constrained bones to the chain
    for (int boneLoop = 0; boneLoop < 7; ++boneLoop) {
        colour = (boneLoop % 2 == 0) ? colour.lighten(0.4f) :
                                       colour.darken(0.4f);

        chain.addConsecutiveRotorConstrainedBone(boneDirection, boneLength,
                                        constraintDegs, colour);
    }
    // Finally, add the chain to the structure
    structure.addChain(chain);
}
```
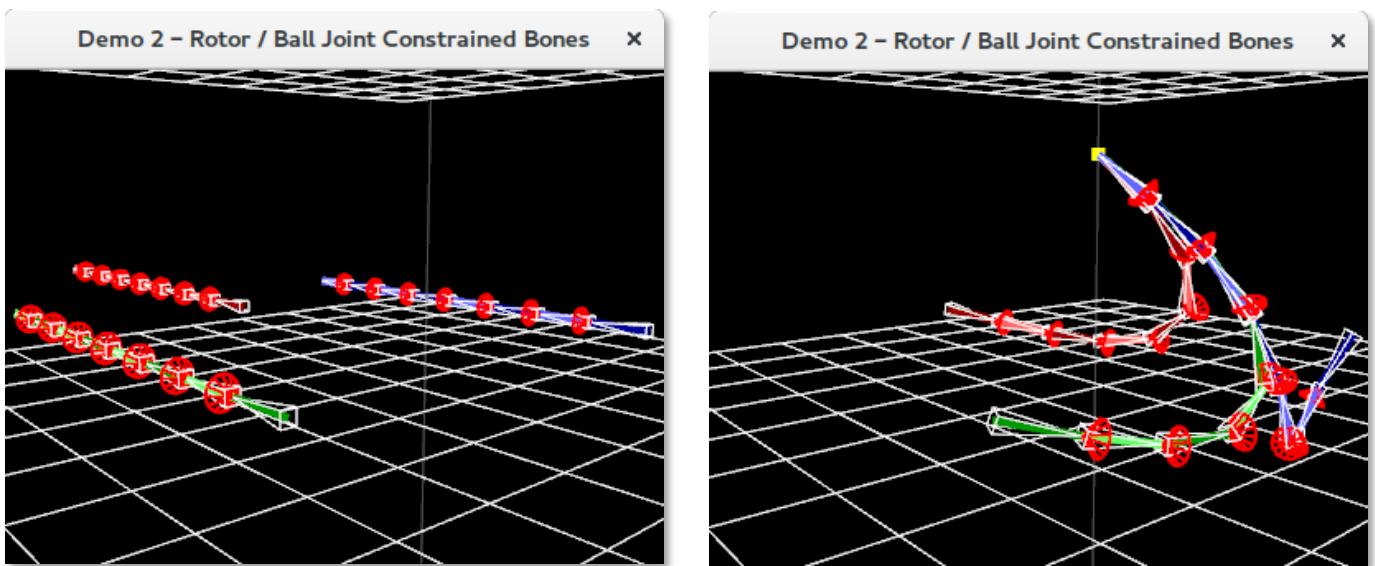
Figure 15 - Chains with 45 degree rotor constrained bones (left) in their initial state and (right) in an example solved state.

3D Demo 3 - Chains with rotor constrained basebones

```java
FabrikStructure3D structure   = new FabrikStructure3D();
int numChains                 = 3;
float rotStep                 = 360.0f / (float)numChains;
Colour4f colour               = new Colour4f();
Colour4f bbColour             = new Colour4f();
Vec3f bbConstraintAxis        = new Vec3f();
float bbConstraintDegs        = 20.0f;

for (int chainLoop = 0; chainLoop < numChains; ++chainLoop) {
    // Set bone colours and basebone constraint axes
    switch (chainLoop % 3) {
        case 0:
                colour.set(Utils.MID_RED);
                bbColour.set(Utils.RED);
                bbConstraintAxis = X_AXIS;
                break;
        case 1:
                colour.set(Utils.MID_GREEN);
                bbColour.set(Utils.MID_GREEN);
                bbConstraintAxis = Y_AXIS;
                break;
        case 2:
                colour.set(Utils.MID_BLUE);
                bbColour.set(Utils.BLUE);
                bbConstraintAxis = Z_AXIS.negated();
                break;
    }

    // Create a new chain and set up the basebone start/end locations
    FabrikChain3D chain = new FabrikChain3D();
    Vec3f start = new Vec3f(0.0f, 0.0f, -40.0f);
    start = Vec3f.rotateYDegs(start, rotStep * (float)chainLoop);
    Vec3f end = start.plus( bbConstraintAxis.times(defaultBoneLength * 2.0f) );

    // ...then create a base bone, set its colour, add it to the chain
    FabrikBone3D basebone = new FabrikBone3D(start, end);
    basebone.setColour(baseBoneColour);
```

```java
        chain.addBone(basebone);

        // EITHER: Set the basebone to be global rotor constrained:
        chain.setRotorBaseboneConstraint(BaseboneConstraintType3D.GLOBAL_ROTOR,
                        baseBoneConstraintAxis, baseBoneConstraintAngleDegs);

        // OR: Freely-rotating global hinge constrained:
        chain.setFreelyRotatingGlobalHingedBasebone(Y_AXIS);

        // OR: Non-freely-rotating global hinge constrained
        // Params: hinge axis, clockwise angle, anticlockwise angle, reference axis
        chain.setGlobalHingeBaseboneConstraint(Y_AXIS, 90.0f, 45.0f, X_AXIS);

        // Add additional consecutive, unconstrained bones to the chain
        for (int boneLoop = 0; boneLoop < 7; ++boneLoop) {
            colour = (boneLoop % 2 == 0) ? colour.lighten(0.5f) :
                                        colour.darken(0.5f);
            chain.addConsecutiveBone(defaultBoneDirection, defaultBoneLength,
                                    colour);
        }
        // Finally, add the chain to the structure
        structure.addChain(chain);
}
```
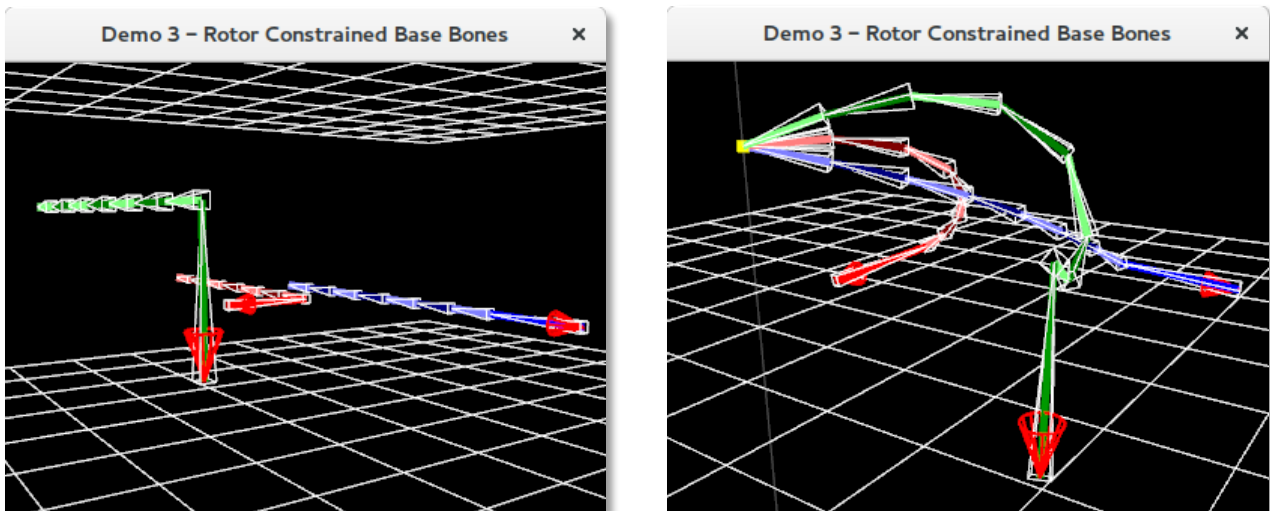

Figure 16 - Chains with rotor constrained basebones (left) in their initial configuration and (right) in an example solved configuration.

3D Demo 4 - Chains with freely rotating global hinges

```java
FabrikStructure3D structure = new FabrikStructure3D();
int numChains           = 3;
float rotStep           = 360.0f / (float)numChains;
Vec3f boneDirection     = Z_AXIS.negated(); // i.e. into the screen
float boneLength        = 10.0f;

// Create a circular arrangement of 3 chains with varying global hinged bones
Vec3f hingeAxis = new Vec3f();
for (int chainLoop = 0; chainLoop < numChains; ++chainLoop) {
    // Set colour and axes
    Colour4f chainColour = new Colour4f();
    switch (chainLoop % numChains) {
        case 0:
            chainColour.set(Utils.RED);   hingeAxis = X_AXIS; break;
        case 1:
            chainColour.set(Utils.GREEN); hingeAxis = Y_AXIS; break;
        case 2:
```

```java
                chainColour.set(Utils.BLUE);  hingeAxis = Z_AXIS; break;
        }

    // Create a new chain and set the start and end locations...
    FabrikChain3D chain = new FabrikChain3D();
    Vec3f start = new Vec3f(0.0f, 0.0f, -40.0f);
    start = Vec3f.rotateYDegs(start, rotStep * (float)chainLoop);
    Vec3f end = startLoc.plus( boneDirection.times(boneLength) );

    // ...then create a base bone, set its colour, and add it to the chain.
    FabrikBone3D basebone = new FabrikBone3D(startLoc, endLoc);
    basebone.setColour(chainColour);
    chain.addBone(basebone);

    // Add alternating global hinge and unconstrained bones to the chain
    for (int boneLoop = 0; boneLoop < 7; ++boneLoop) {
        if (boneLoop % 2 == 0) {
            chain.addConsecutiveFreelyRotatingHingedBone(boneDirection,
                boneLength, JointType.GLOBAL_HINGE, globalHingeAxis, Utils.GREY);
        } else {
            chain.addConsecutiveBone(boneDirection, boneLength, chainColour);
        }
    }
    // Finally, add the chain to the structure
    structure.addChain(chain);
}
```
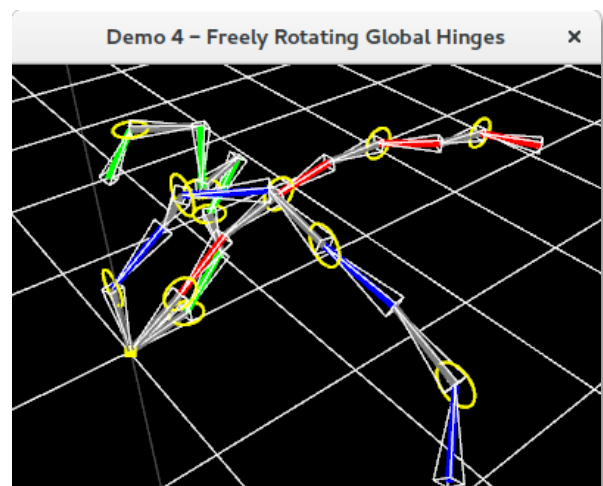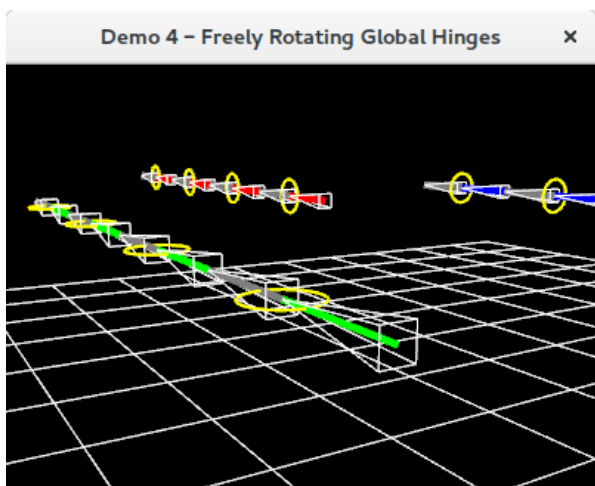

Figure 17 - Chains with global hinged bones (left) in their original and (right) in an example solved configuration.

3D Demo 5 - Global hinges with reference axis constraints

```java
FabrikStructure3D structure = new FabrikStructure3D();
FabrikChain3D chain          = new FabrikChain3D();
Vec3d down                   = Y_Axis.negated();
float boneLength             = 10.0f;

// Set up the initial base bone location...
Vec3f startLoc = new Vec3f(0.0f, 30f, -40.0f);
Vec3f endLoc   = new Vec3f(startLoc);
endLoc.y      -= defaultBoneLength;

// ...then create a base bone, set its colour, and add it to the chain.
FabrikBone3D basebone = new FabrikBone3D(startLoc, endLoc);
basebone.setColour(Utils.YELLOW);
chain.addBone(basebone);

// Add alternating global hinge constrained, and unconstrained bones to the chain
float cwDegs  = 120.0f;
```

```java
float acwDegs = 120.0f;
for (int boneLoop = 0; boneLoop < 8; ++boneLoop) {
    if (boneLoop % 2 == 0) {
        // Params: bone direction, bone length, joint type, hinge rotation
        // axis, clockwise constraint angle, anticlockwise constraint angle,
        // hinge constraint reference axis, colour
        // Note: There is a version of this method where you do not specify the
        // colour - the default is to draw the bone in white.
        chain.addConsecutiveHingedBone(down, boneLength, JointType.GLOBAL_HINGE,
                                    Z_AXIS, cwDegs,acwDegs, down, Utils.GREY);
    } else {
        chain.addConsecutiveBonedown(down, defaultBoneLength, Utils.MID_GREEN);
    }
}

// Finally, add the chain to the structure
structure.addChain(chain);
```
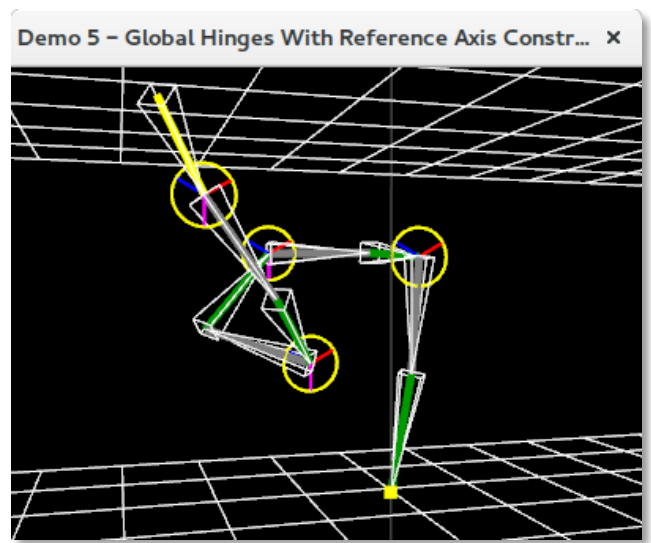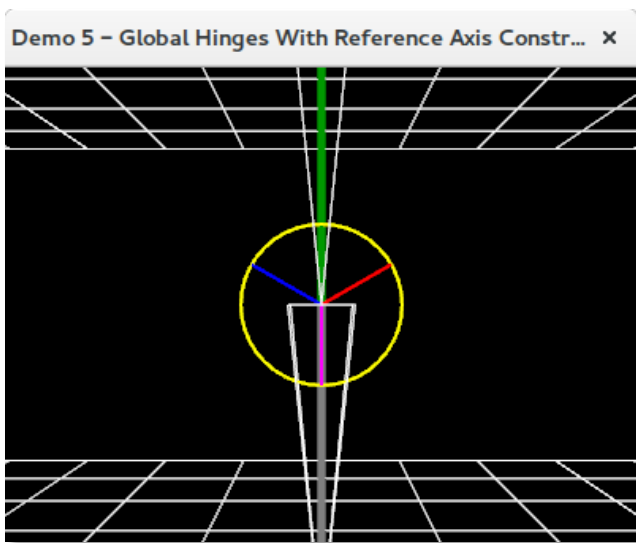

Figure 18 - A chain containing global hinges with reference axes. Anticlockwise (red) and clockwise (blue) constraint angles are measured with respect to the hinge reference axis (cyan). On the left is close-up of a hinge, while the right images show an example solved configuration.

3D Demo 6 - Chains with local hinges

```java
FabrikStructure3D structure = new FabrikStructure3D();
int numChains              = 3;
float rotStep              = 360.0f / (float)numChains;
Vec3f rotationAxis         = new Vec3f();
Vec3f referenceAxis        = new Vec3f();
Vec3f boneDirection        = Z_AXIS.negated(); // i.e. into the screen
float boneLength           = 10.0f;

// We'll create a circular arrangement of 3 chains with alternate bones each
// constrained about different local axes. Note: Local hinge rotation axes are
// relative to the generated rotation matrix of the previous bone in the chain.
for (int chainLoop = 0; chainLoop < numChains; ++chainLoop) {
    // Set colour and axes. Reference axes must be in the plane of hinge axes.
    Colour4f chainColour = new Colour4f();
    switch (loop % numChains) {
        case 0:
                chainColour   = Utils.RED;
                rotationAxis  = new Vec3f(X_AXIS);
                referenceAxis = new Vec3f(Y_AXIS);
                break;
        case 1:
```

```java
                        chainColour   = Utils.GREEN;
                        rotationAxis  = new Vec3f(Y_AXIS);
                        referenceAxis = new Vec3f(X_AXIS);
                        break;
                case 2:
                        chainColour   = Utils.BLUE;
                        rotationAxis  = new Vec3f(Z_AXIS);
                        referenceAxis = new Vec3f(Y_AXIS);
                        break;
        }

        // Create a new chain and set the basebone start and end locations
        FabrikChain3D chain = new FabrikChain3D();
        Vec3f start = new Vec3f(0.0f, 0.0f, -40.0f);
        start       = Vec3f.rotateYDegs(start, rotStep * (float)chainLoop);
        Vec3f end   = start.plus( boneDirection.times(boneLength) );

        // ...then create a base bone, set its colour, and add it to the chain.
        FabrikBone3D basebone = new FabrikBone3D(startLoc, endLoc);
        basebone.setColour(chainColour);
        chain.addBone(basebone);

        // Add alternating local hinge and unconstrained bones to the chain
        float constraintDegs = 90.0f;
        for (int boneLoop = 0; boneLoop < 6; ++boneLoop) {
                if (boneLoop % 2 == 0) {

                        // EITHER: For no reference constraints:
                        chain.addConsecutiveFreelyRotatingHingedBone(boneDirection,
                         boneLength, JointType.LOCAL_HINGE, hingeAxis, Utils.GREY);

                        // OR: To apply reference constraints:
                        chain.addConsecutiveHingedBone(boneDirection, boneLength,
                          JointType.LOCAL_HINGE, rotationAxis, constraintDegs,
                          constraintDegs, referenceAxis, Utils.GREY);
                } else {
                        chain.addConsecutiveBone(boneDirection, boneLength, chainColour);
                }
        }
        // Finally, add the chain to the structure
        structure.addChain(chain);
}
```
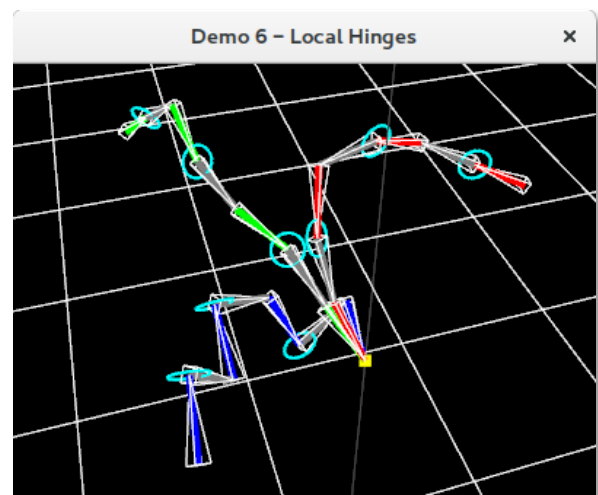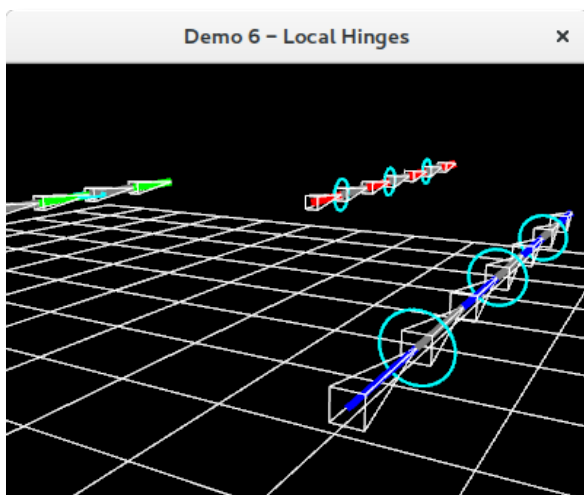

Figure 19 - Chains with local hinges shown (left) in their initial configuration and (right) in an example solved configuration. Each local hinge's rotation axis and reference axis are converted into the coordinate system of the previous bone in the chain before being enforced.

3D Demo 7 - Connecting Chains

```java
FabrikStructure3D structure = new FabrikStructure3D();
FabrikChain3D chain         = new FabrikChain3D();
Colour4f colour             = new Colour4f(Utils.GREEN);
Vec3f boneDirection         = Z_AXIS.negated(); // i.e. into the screen
float boneLength            = 10.0f;

// Create a new chain, set start and end locations then add to chain
Vec3f start = new Vec3f(0.0f, 0.0f, 40.0f);
Vec3f end = start.plus( boneDirection.times(boneLength) );
FabrikBone3D basebone = new FabrikBone3D(start, end);
basebone.setColour(colour);
chain.addBone(basebone);

// Add additional consecutive, unconstrained bones to the chain
for (int boneLoop = 0; boneLoop < 5; boneLoop++) {
    colour = (boneLoop % 2 == 0) ? colour.lighten(0.4f) : colour.darken(0.4f);
    chain.addConsecutiveBone(defaultBoneDirection, defaultBoneLength, colour);
}

// Add the chain to the structure and create a second chain (base location isn't
// particularly important, it'll 'snap' to the connection point on the first chain)
structure.addChain(chain);
FabrikChain3D secondChain = new FabrikChain3D();
FabrikBone3D base = new FabrikBone3D( new Vec3f(100.0f), new Vec3f(110.0f) );
secondChain.addBone(base);

// We may optionally choose to constrain the chain we are connecting to the first
// chain about a global rotor constraint, for example, 45 degrees about the X-axis.
secondChain.setRotorBaseboneConstraint(BaseboneConstraintType3D.GLOBAL_ROTOR,
                                       X_AXIS, 45.0f);
secondChain.addConsecutiveBone(X_AXIS, 20.0f);
secondChain.addConsecutiveBone(Y_AXIS, 20.0f);
secondChain.addConsecutiveBone(Z_AXIS, 20.0f);

// Set the colour of all bones in the chain then connect it to the first chain...
// Params: chain we're connecting, host chain number, host bone number, conn. point
secondChain.setColour(Utils.RED);
structure.connectChain(secondChain, 0, 0, BoneConnectionPoint3D.START);

// We can keep adding the same chain at various points if we like, because the
// chain we connect is actually a clone of the one we provide, and not the
// original 'secondChain' object
secondChain.setColour(Utils.WHITE);

// Basebone constraints may be set on the connecting chain as desired prior to
// connection by using the following methods:
// For GLOBAL_ROTOR:
secondChain.setRotorBaseboneConstraint(BaseboneConstraintType3D.GLOBAL_ROTOR,
X_AXIS, 45.0f);
// LOCAL_ROTOR:
secondChain.setRotorBaseboneConstraint(BaseboneConstraintType3D.LOCAL_ROTOR,
X_AXIS, 45.0f);
// GLOBAL_HINGE:
secondChain.setFreelyRotatingGlobalHingedBasebone(Y_AXIS);
// GLOBAL_HINGE with reference constraints:
secondChain.setGlobalHingeBaseboneConstraint(Y_AXIS, 90.0f, 45.0f, X_AXIS);
// LOCAL_HINGE:
secondChain.setFreelyRotatingLocalHingedBasebone(Y_AXIS);
// LOCAL_HINGE with reference constraints:
secondChain.setLocalHingeBaseboneConstraint(Y_AXIS, 90.0f, 45.0f, X_AXIS);
```

```
// Once any basebone constraints have been applied, we're free to add the chain to
// the structure - in this case we're connecting our secondChain to the end of bone
// 1 in chain 0.
structure.connectChain(secondChain, 0, 1, BoneConnectionPoint3D.END);
```
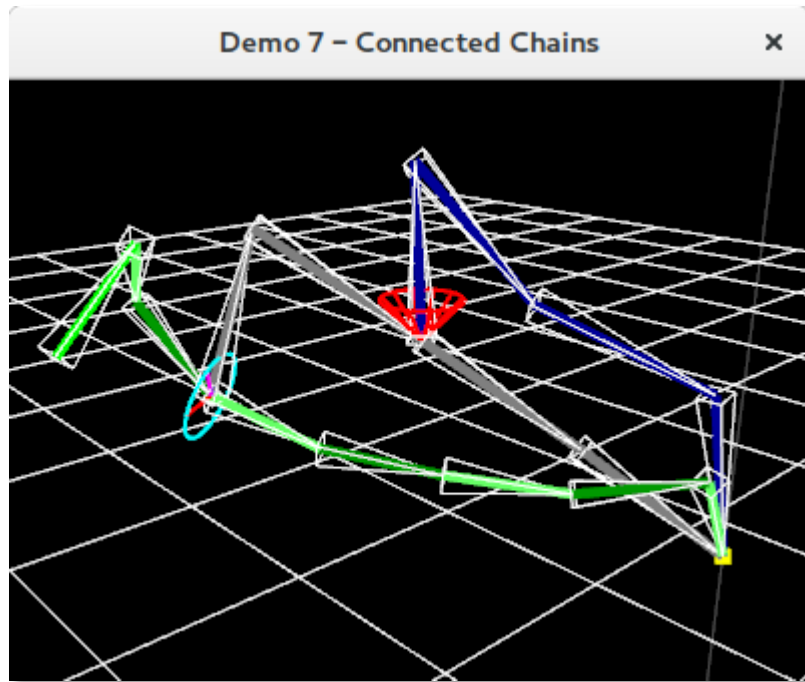

Figure 20 - A chain with a global rotor basebone constraint (in blue) attached to a chain with a local hinge with reference axis basebone constraint (in grey) attached to a chain without any basebone constraint (in green).

3D Demo 12 – Connected chains with embedded targets

Note: We jump from demos 7 to 12 as 8 through 11 show variations on a theme

Just like in 2D, any chain within a structure may have

```
mStructure          = new FabrikStructure3D(demoName);
Colour4f boneColour = new Colour4f(Utils.GREEN);

// Create a new chain...
FabrikChain3D chain = new FabrikChain3D();

// ...then create a basebone, set its draw colour and add it to the chain.
Vec3f startLoc      = new Vec3f(0.0f, 0.0f, 40.0f);
Vec3f endLoc        = startLoc.plus(
defaultBoneDirection.times(defaultBoneLength) );
FabrikBone3D basebone = new FabrikBone3D(startLoc, endLoc);
basebone.setColour(boneColour);
chain.addBone(basebone);

// Add additional consecutive, unconstrained bones to the chain

for (int boneLoop = 0; boneLoop < 7; boneLoop++)
{
    boneColour = (boneLoop % 2 == 0) ? boneColour.lighten(0.4f) :
                                  boneColour.darken(0.4f);
    chain.addConsecutiveBone(defaultBoneDirection, defaultBoneLength,
boneColour);
}

// Finally, add the chain to the structure
```

```
mStructure.addChain(chain);

// Create a second chain which will be connected to the first and will use an
// embedded target (specified in the main loop)
FabrikChain3D secondChain = new FabrikChain3D("Second Chain");
secondChain.setEmbeddedTargetMode(true);
FabrikBone3D base = new FabrikBone3D( new Vec3f(), new Vec3f(15.0f, 0.0f, 0.0f) );
secondChain.addBone(base);

// Set this second chain to have a freely rotating global hinge which rotates about
// the Y axis. Note: We MUST add the basebone to the chain before we can set the
// basebone constraint on it.
secondChain.setHingeBaseboneConstraint(BaseboneConstraintType3D.GLOBAL_HINGE,
Y_AXIS, 90.0f, 45.0f, X_AXIS);

// Add some additional bones
secondChain.addConsecutiveBone(X_AXIS, 20.0f);
secondChain.addConsecutiveBone(X_AXIS, 20.0f);
secondChain.addConsecutiveBone(X_AXIS, 20.0f);
secondChain.setColour(Utils.GREY);

// Connect this second chain to the start point of bone 3 in chain 0 of the struct
mStructure.connectChain(secondChain, 0, 3, BoneConnectionPoint3D.START);
```
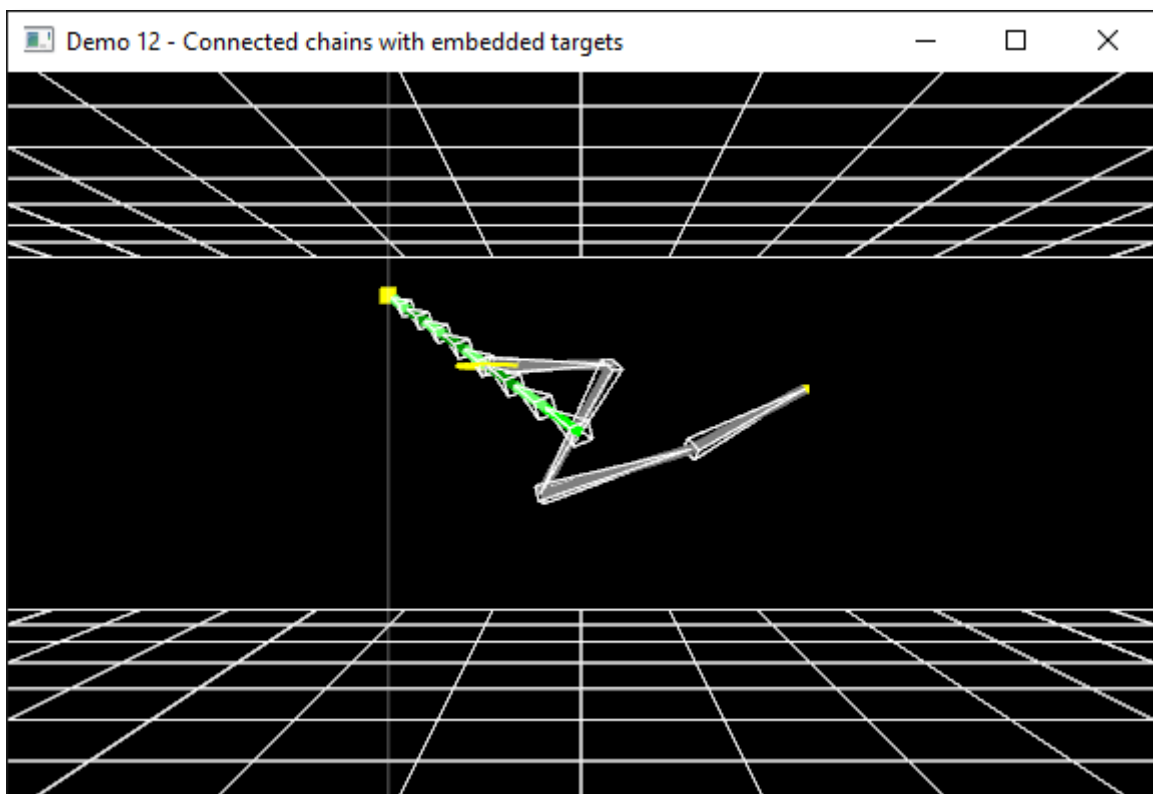

Figure 21 - Connected chains with embedded target locations (i.e. multiple end-effectors in a single structure). When embedded target mode is enabled for a chain then solving that chain uses the embedded target rather than any provided target location.