

# Introduction to Probabilistic Models for Information Retrieval

Victor Lavrenko  
University of Edinburgh

Copyright 2010, Victor Lavrenko

## Objectives

- Highlight influential work on probabilistic models for IR
- Provide a working understanding of the probabilistic techniques through a set of common implementation tricks
- Establish relationships between the popular approaches: stress common ideas, explain differences
- Outline issues in extending the models to interactive, cross-language, multi-media

Copyright 2010, Victor Lavrenko

# Outline

- Recap of probability theory
- Probability ranking principle
- Classical probabilistic model
  - Binary Independence Model
  - 2-Poisson model and BM25
  - feedback methods
- Language modeling approach
  - overview and design decisions
  - estimation techniques
  - synonymy and CLIR

Copyright 2010, Victor Lavrenko

## Recap of Probability Theory

- Random variables and event spaces
  - sample space, events, and probability axioms
  - random variables and probability distributions
- Conditional probabilities and Bayes rule
- Independence and conditional independence
- Dealing with data sparseness
  - pairwise and mutual independence
  - dimensionality reduction and its perils
  - symmetry and exchangeability

Copyright 2010, Victor Lavrenko

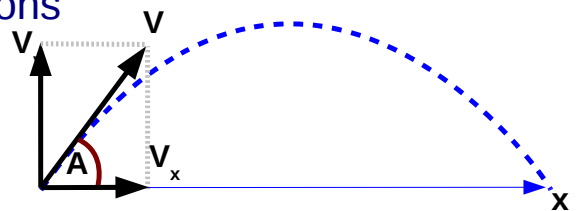
# What's a probability?

- Means many things to many people
  - inherent physical property of a system
    - ... a coin toss comes up heads
  - (asymptotic) frequency of something happening
    - ... Red Sox win against Yankees
  - subjective belief that something will happen
    - ... the sun will rise tomorrow
- Laplace: “*common sense reduced to numbers*”
  - a very good substitute for scientific laws, when your scientific method can't handle the complexity

Copyright 2010, Victor Lavrenko

## Coin-tossing example

- Toss a coin, determine how far it will land?
  - Newtonian physics: solve equations
    - $\text{Force} \cdot dt / \text{Mass} \rightarrow \text{velocity } V$
    - $2 \cdot G / (V \cdot \sin(\text{Angle})) \rightarrow \text{time } T$
    - $T \cdot V \cdot \cos(\text{Angle}) \rightarrow \text{distance } X$
  - Probability / statistics: count coincidences
    - a gazillion throws, varying angle  $A$ , distance  $X$
    - count how often we see  $X$  for a given  $A$  ,, conditional  $P(X|A)$
  - Why would we ever do that?
    - lazy, expensive, don't **really** understand what's going on...
    - can capture hidden factors that are difficult to account for
      - air resistance, effect of coin turning, wind, nearby particle accelerator...



Copyright 2010, Victor Lavrenko

# Outcomes and Events

- Sample and Event Spaces:
  - sample space: all possible **outcomes** of some experiment
  - event space: all possible **sets** of outcomes (power-set<sup>\*\*</sup>)
- Examples:
  - toss a coin, measure how far it lands
    - outcome: e.g. coin lands at exactly 12.34567m (uncountably many)
    - event: range of numbers, coin landed between 12m and 13m
  - toss a coin twice, record heads / tails on each toss
    - sample space: {HH, HT, TH, TT} – only four possible outcomes
    - event space: { $\{\}$ , {HH}, {HT}, ..., {HH,HT}, {HH,TH}, ..., {HH,HT,TH}, ..., }
    - {HH,HT} = event that a head occurred on the first toss
    - {HH,HT,TH} = event that a head occurred on at least one of the tosses

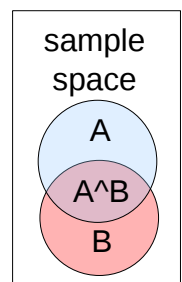
Copyright 2010, Victor Lavrenko

# Probabilities

- Probability = how frequently we expect an event
  - e.g. fair coin  $\rightarrow P(H) = P(T) = \frac{1}{2}$
  - assigned to **events**, not **outcomes**:
    - i.e.  $P(H)$  really means  $P(\{H\})$ , but notation  $\{\}$  frequently dropped

- Probabilities must obey rules:

- for any event:  $0 \leq P(\text{event}) \leq 1$
- $P(\text{sample space}) = 1$  ... some outcome must occur
- for any events A,B:  $P(A \cup B) = P(A) + P(B) - P(A \cap B)$ 
  - $P(A \cup B) = P(A) + P(B)$  if events don't overlap (e.g. {HH, HT}+{TT})
  - $\sum_{\text{outcome}} P(\{\text{outcome}\}) = 1$  ... additivity over sample space



Copyright 2010, Victor Lavrenko

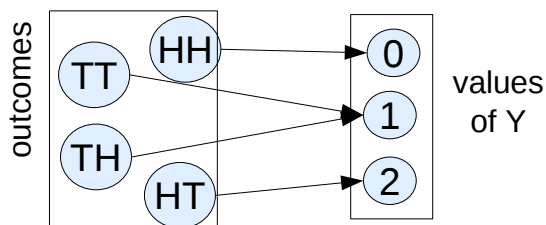
# Random Variables

- RV = a function defined over sample space
  - compute some property / feature of an outcome, e.g.:
    - X: coin toss distance, truncated to nearest imperial unit
      - $X(0.023) = \text{"inch"}$ ,  $X(0.8) = \text{"yard"}$ ,  $X(1500.1) = \text{"mile"}$ , ...
    - Y: number of heads observed during two coin tosses
      - $Y(HH) = 2$ ,  $Y(HT) = Y(TH) = 1$ ,  $Y(TT) = 0$
  - RVs ... capital letters, their values ... lowercase
- Central notion in probabilistic approaches:
  - very flexible and convenient to work with:
    - can map discrete outcomes to numeric, and back
    - often describe everything in terms of RVs (forget sample space)

Copyright 2010, Victor Lavrenko

## Random Variables and Probabilities

- RVs usually deterministic (counting, rounding)
- What they operate on (outcomes) is probabilistic
  - probability RV takes a particular value is defined by the probabilities of outcomes that lead to that value:
    - $P(Y=2) = P(\text{two heads in two tosses}) = P(\{HH\})$
    - $P(Y=1) = P(\text{exactly one head}) = P(\{HT\}) + P(\{TH\})$
    - $P(X=\text{"foot"}) = P(\text{distance rounds to "foot"}) = P(0.1 < \text{distance} < 0.5)$
- In general:  $P(X=x) = \sum_{\text{outcome} : X(\text{outcome}) = x} P(\{\text{outcome}\})$



Copyright 2010, Victor Lavrenko

# Random Variables Confusion

- Full RV notation is tedious
  - frequently shortened to list just variables, or just values:
    - $P(X_1 = x_1, X_2 = x_2, Y = y) \rightarrow P(X_1, X_2, Y)$
    - $P(X_1 = \text{yard}, W_2 = \text{mile}) \rightarrow P(\text{yard}, \text{mile})$
- Fine, as long as clear what RVs mean:
  - for 2 coin-tosses  $P(\text{"head"})$  can mean:
    - $P(\text{head on the first toss}) = P(\{HH\}) + P(\{HT\})$
    - $P(\text{a head was observed}) = P(\{HH\}) + P(\{HT\}) + P(\{TH\})$
    - $P(\text{exactly one head observed}) = P(\{HT\}) + P(\{TH\})$
  - these mean different things, can't be interchanged
- In general: clearly define the domain for each RV.

Copyright 2010, Victor Lavrenko

## Types of Random Variables

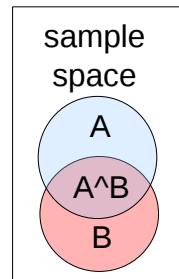
- Completely determined by domain (types of output)
- Discrete: RV values = finite or countable
  - ex: coin tossing, dice-rolling, counts, words in a language
  - additivity:  $\sum_x P(x) = 1$ 
    - $P(X = x)$  is a sensible concept
- Continuous: RV values are real numbers
  - ex: distances, times, parameter values for IR models
  - additivity:  $\int_x p(x) dx = 1$ 
    - $P(X = x)$  is always zero,  $p(x)$  is a "density" function
- Singular RVs ... never see them in IR

Copyright 2010, Victor Lavrenko

# Conditional Probabilities

- $P(A | B)$  ... probability of event A happening assuming we know B happened

$$P(A|B) = \frac{P(A \cap B)}{P(B)}$$



- Example:
  - population size: 10,000,000
  - number of scientists: 10,000
  - Nobel prize winners: 10 (1 is an engineer)
  - $P(\text{scientist}) = 0.001$
  - $P(\text{scientist} | \text{Nobel prize}) = 0.9$

Copyright 2010, Victor Lavrenko

## Bayes Rule

- A way to “flip” conditional probabilities:

$$P(A|B) = \frac{P(B|A)P(A)}{P(B)}$$

- Example:
  - $P(\text{scientist} | \text{Nobel prize}) = 0.9$
  - $P(\text{Nobel prize}) = 10^{-6}$ ,  $P(\text{scientist}) = 10^{-3}$
  - $P(\text{Nobel prize} | \text{scientist}) = 0.9 * 10^{-6} / 10^{-3} = 0.0009$
- Easy to derive (definition of conditional probabilities):

$$P(A|B) = \frac{P(A \cap B)}{P(B)} = \frac{P(A \cap B)}{P(A)} \times \frac{P(A)}{P(B)} = \frac{P(B|A)P(A)}{P(B)}$$

Copyright 2010, Victor Lavrenko

# Chain Rule and Independence

- Chain Rule: a way to decompose joint probabilities

- directly from definition of conditionals
- exact, no assumptions are involved

$$P(X_1 \dots X_n) = P(X_1 | X_2 \dots X_n) P(X_2 | X_3 \dots X_n) \dots P(X_n)$$

- Independence:

- X and Y are independent (don't influence each other)
- coin example: distance travelled and whether it's H or T
  - probably doesn't hold for very short distances
- mutual independence: multiply probabilities (cf. Chain rule):

$$P(X_1 \dots X_n) = \prod_{i=1}^n P(X_i)$$

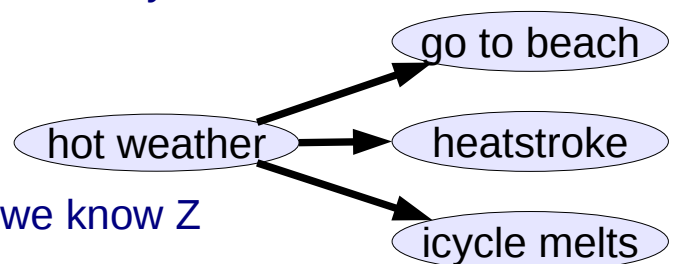
Copyright 2010, Victor Lavrenko

## Conditional Independence

- Variables X and Y may be dependent

- but all influence can be explained by another variable Z

- X: you go to the beach
- Y: you get a heatstroke
- Z: the weather is hot



- X and Y are independent if we know Z

- if weather is hot, heatstroke irrespective of beach

$$P(X, Y | Z) = P(X | Z) P(Y | Z)$$

- if Z is unknown, X and Y are dependent

$$P(X, Y) = \sum_z P(X | Z = z) P(Y | Z = z) P(Z = z)$$

- Don't mix conditional and mutual independence

Copyright 2010, Victor Lavrenko



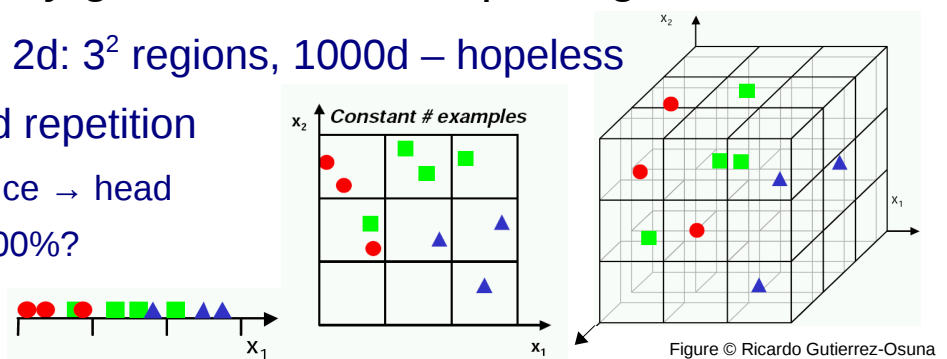
# Curse of dimensionality

- Why do we need to assume independence?
- Probabilistic models based on counting
  - count observations (documents)
  - of different classes (relevant / non-relevant)
  - along different regions of space (words)
- As dimensionality grows, fewer dots per region

- 1d: 3 regions, 2d:  $3^2$  regions, 1000d – hopeless

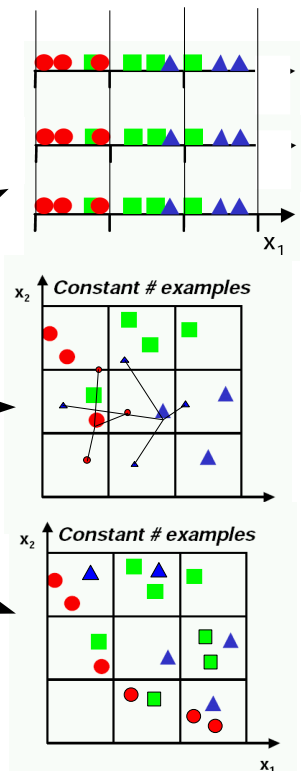
- statistics need repetition

- flip a coin once → head
- $P(\text{head}) = 100\%$ ?



## Dealing with high dimensionality

- Use domain knowledge
  - feature engineering: doesn't really work for IR
- Make assumption about dimensions
  - independence
    - count along each dimension separately, combine
  - smoothness
    - propagate class counts to neighbouring regions
  - symmetry
    - e.g. invariance to order of dimensions:  $x_1 \leftrightarrow x_2$
- Reduce the dimensionality of the data
  - create a new set of dimensions (variables)



# Outline

- Recap of probability theory
- Probability ranking principle
- Classical probabilistic model
  - Binary Independence Model
  - 2-Poisson model and BM25
  - feedback methods
- Language modeling approach
  - overview and design decisions
  - estimation techniques
  - synonymy and feedback

Copyright 2010, Victor Lavrenko

## Models in Information Retrieval

- Mathematical formalism for processes:
  - formulation: information need → query
  - indexing: documents → index terms
  - **retrieval: query + corpus → search results**
- Over the following variables
  - documents (D), queries (Q), relevance (R)
  - user, task, context, search history, click rate, ...
- Usually involve abstract analogy
  - document is an urn containing words
  - query is a logical formula that needs to be “proved”
  - user is a greedy memory-less random process

Copyright 2010, Victor Lavrenko

# Probability Ranking Principle

- Robertson (1977)
  - “If a reference retrieval system’s response to each request is a **ranking** of the documents in the collection in order of decreasing **probability of relevance** to the user who submitted the request,
  - where the **probabilities** are **estimated** as **accurately** as possible on the basis of whatever data have been made available to the system for this purpose,
  - the overall **effectiveness** of the system to its user **will be** the **best** that is obtainable on the basis of those data.”
- Basis for most probabilistic approaches to IR

Copyright 2010, Victor Lavrenko

## Let's dissect the PRP

- rank documents ... by probability of relevance
  - $P(\text{relevant} \mid \text{document})$
- estimated as accurately as possible
  - $P_{\text{est}}(\text{relevant} \mid \text{document}) \rightarrow P_{\text{true}}(\text{rel} \mid \text{doc})$  in some way
- based on whatever data is available to system
  - $P_{\text{est}}(\text{relevant} \mid \text{document, query, context, user profile, ...})$
- best possible accuracy one can achieve with that data
  - recipe for a perfect IR system: just need  $P_{\text{est}}(\text{relevant} \mid \dots)$
  - strong stuff, can this really be true?

Copyright 2010, Victor Lavrenko

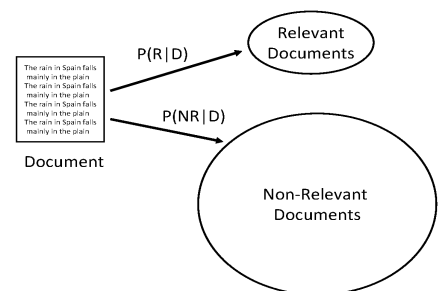
# Probability of relevance

- What is:  $P_{\text{true}}(\text{relevant} \mid \text{doc}, \text{qry}, \text{user}, \text{context})$  ?
  - isn't relevance just the user's opinion?
    - user decides relevant or not, what's the “probability” thing?
- “user” does not mean the human being
  - doc, qry, user, context ... *representations*
    - parts of the real thing that are available to the system
  - typical case:  $P_{\text{true}}(\text{relevant} \mid \text{document}, \text{query})$ 
    - query: 2-3 keywords, user profile unknown, context not available
    - whether document is relevant is uncertain
      - depends on the factors which are not *available to our system*
    - think of  $P_{\text{true}}(\text{rel} \mid \text{doc}, \text{qry})$  as proportion of all unseen users/contexts/... for which the document would have been judged relevant

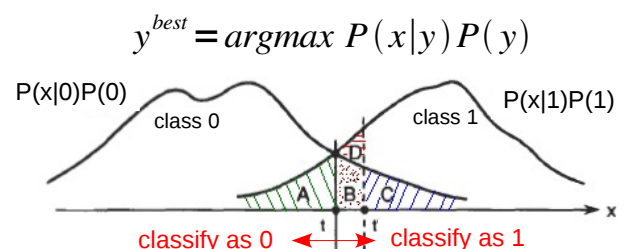
Copyright 2010, Victor Lavrenko

## IR as classification

- For a given query, documents fall into two classes
  - relevant ( $R=1$ ) and non-relevant ( $R=0$ )
  - compute  $P(R=1 \mid D)$  and  $P(R=0 \mid D)$ 
    - retrieve if  $P(R=1 \mid D) > P(R=0 \mid D)$
- Related to Bayes error rate



- if  $P(x|0)P(0) > P(x|1)P(1)$   
then class 0 otherwise 1
- $\text{error}_{\text{Bayes}} = A + (B + C)$   
 $\leq A + B + C + D$   
 $= \text{error}_{\text{any other classifier}}$



- no way to do better than Bayes given input  $x$ 
  - input  $x$  does not allow us to determine class any better

Copyright 2010, Victor Lavrenko

# Optimality of PRP

- Retrieving a set of documents:
  - PRP equivalent to Bayes error criterion
  - optimal wrt. classification error
- Ranking a set of documents: optimal wrt:
  - precision / recall at a given rank
  - average precision, etc.
- Need to estimate  $P(\text{relevant} \mid \text{document, query})$ 
  - many different attempts to do that
  - Classical Probabilistic Model (Robertson, Sparck-Jones)
    - also known as Binary Independence model, Okapi model
    - very influential, successful in TREC (BM25 ranking formula)

Copyright 2010, Victor Lavrenko

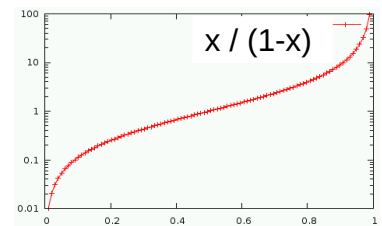
## Outline

- Recap of probability theory
- Probability ranking principle
- Classical probabilistic model
  - Binary Independence Model
  - 2-Poisson model and BM25
  - feedback methods
- Language modeling approach
  - overview and design decisions
  - estimation techniques
  - synonymy and feedback

Copyright 2010, Victor Lavrenko

# Classical probabilistic model

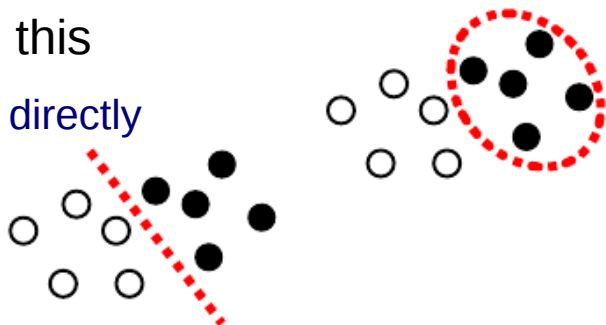
- Assumption A0:
  - relevance of  $D$  doesn't depend on any other document
    - made by almost every retrieval model (exception: cluster-based)
- Rank documents by  $P(R=1|D)$ 
  - $R = \{0,1\}$  ... Bernoulli RV indicating relevance
  - $D$  ... represents content of the document
- Rank-equivalent:
 
$$P(R=1|D) \stackrel{rank}{=} \frac{P(R=1|D)}{P(R=0|D)} = \frac{P(D|R=1)P(R=1)}{P(D|R=0)P(R=0)}$$
- Why Bayes? Want a generative model.
  - $P(\text{observation} | \text{class})$  sometimes easier with limited data
  - note:  $P(R=1)$  and  $P(R=0)$  don't affect the ranking



Copyright 2010, Victor Lavrenko

## Generative and Discriminative

- A complete probability distribution over documents
  - defines likelihood for any possible document  $d$  (observation)
  - $P(\text{relevant})$  via  $P(\text{document})$ :  $P(R|d) \propto P(d|R)P(R)$
  - can “generate” synthetic documents
    - will share some properties of the original collection
- Not all retrieval models do this
  - possible to estimate  $P(R|d)$  directly
  - e.g. log-linear model



$$P(R|d) = \frac{1}{z_R} \exp \left( \sum_i \lambda_i g_i(R, d) \right)$$

Copyright 2010, Victor Lavrenko

# Probabilistic model: assumptions

- Want  $P(D|R=1)$  and  $P(D|R=0)$
- Assumptions:
  - A1:  $D = \{D_w\}$  ... one RV for every word  $w$ 
    - Bernoulli: values 0,1 (word either present or absent in a document)
  - A2:  $D_w$  ... are mutually independent given  $R$ 
    - blatantly false: presence of “Barack” tells you nothing about “Obama”
    - but must assume something:  $D$  represents subsets of vocabulary
      - without assumptions:  $10^6!$  possible events
  - allows us to write:
 
$$P(R=1|D) \stackrel{rank}{=} \frac{P(D|R=1)}{P(D|R=0)} = \frac{\prod_w P(D_w|R=1)}{\prod_w P(D_w|R=0)}$$
- Observe: identical to the Naïve Bayes classifier

Copyright 2010, Victor Lavrenko

# Probabilistic model: assumptions

- Define:  $p_w = P(D_w=1|R=1)$  and  $q_w = P(D_w=1|R=0)$
- Assumption A3 :  $P(\vec{0}|R=1) = P(\vec{0}|R=0)$ 
  - empty document (all words absent) is equally likely to be observed in relevant and non-relevant classes
- Result:
 
$$P(R=1|D) \stackrel{rank}{=} \prod_{w \in D} \left( \frac{p_w}{q_w} \right) \prod_{w \notin D} \left( \frac{1-p_w}{1-q_w} \right) / \underbrace{\prod_w \left( \frac{1-p_w}{1-q_w} \right)}_{\frac{P(\vec{0}|R=1)}{P(\vec{0}|R=0)} = 1} = \prod_{w \in D} \frac{p_w(1-q_w)}{q_w(1-p_w)}$$
  - dividing by 1: no effect
  - provides “natural zero”
  - practical reason: final product only over words present in  $D$ 
    - fast: small % of total vocabulary + allows term-at-a-time execution

Copyright 2010, Victor Lavrenko

# Estimation (with relevance)

- Suppose we have (partial) relevance judgments:
  - $N_1 \dots$  relevant,  $N_0 \dots$  non-relevant documents marked
  - word  $w$  observed in  $N_1(w)$ ,  $N_0(w)$  docs
  - $P(w)$  = % of docs that contain at least one mention of  $w$ 
    - includes crude smoothing: avoids zeros, reduces variance

$$p_w = \frac{N_1(w) + 0.5}{N_1 + 1.0} \quad q_w = \frac{N_0(w) + 0.5}{N_0 + 1.0}$$

- What if we don't have relevance information?
  - no way to count words for relevant / non-relevant classes
  - things get messy...

Copyright 2010, Victor Lavrenko

## Example (with relevance)

- relevant docs:  $D_1 = \text{"a b c b d"}\text{"}$ ,  $D_2 = \text{"a b e f b"}\text{"}$
- non-relevant:  $D_3 = \text{"b g c d"}\text{"}$ ,  $D_4 = \text{"b d e"}\text{"}$ ,  $D_5 = \text{"a b e g"}\text{"}$
- word:
 

	a	b	c	d	e	f	g	h	
$N_1(w)$ :	2	2	1	1	1	1	0	0	$N_1 = 2$
$N_0(w)$ :	1	3	1	2	2	0	2	0	$N_0 = 3$
$p_w$ :	$\frac{2.5}{3}$	$\frac{2.5}{3}$	$\frac{1.5}{3}$	$\frac{1.5}{3}$	$\frac{1.5}{3}$	$\frac{1.5}{3}$	$\frac{0.5}{3}$	$\frac{0.5}{3}$	
$q_w$ :	$\frac{1.5}{4}$	$\frac{3.5}{4}$	$\frac{1.5}{4}$	$\frac{2.5}{4}$	$\frac{2.5}{4}$	$\frac{0.5}{4}$	$\frac{2.5}{4}$	$\frac{0.5}{4}$	
- new document  $D_6 = \text{"b g h"}\text{"}$ :

$$P(R=1|D_6) \stackrel{\text{rank}}{=} \prod_{\substack{w \in D_6 \\ \text{only words} \\ \text{present in } D_6}} \frac{p_w(1-q_w)}{q_w(1-p_w)} = \frac{\frac{2.5}{3} \cdot (1 - \frac{3.5}{4}) \cdot \frac{0.5}{3} \cdot (1 - \frac{2.5}{4}) \cdot \frac{0.5}{3} \cdot (1 - \frac{0.5}{4})}{\frac{3.5}{4} \cdot (1 - \frac{2.5}{3}) \cdot \frac{2.5}{4} \cdot (1 - \frac{0.5}{3}) \cdot \frac{0.5}{4} \cdot (1 - \frac{0.5}{3})} = \frac{1.64}{13.67}$$

Copyright 2010, Victor Lavrenko



# Estimation (no relevance)

- Assumption A4:  $p_w = q_w$  if  $w \notin Q$ 
  - if the word is not in the query, it is equally likely to occur in relevant and non-relevant populations
  - practical reason: restrict product to query – document overlap
- Assumption A5:  $p_w = 0.5$  if  $w \in Q$ 
  - a query word is equally likely to be present and absent in a randomly-picked relevant document (usually  $p_w \ll 0.5$ )
  - practical reason:  $p_w$  and  $(1-p_w)$  cancel out
- Assumption A6:  $q_w \approx N_w / N$ 
  - non-relevant set approximated by collection as a whole
  - very reasonable: most documents are non-relevant

Result:  $P(R=1|D)^{rank} = \prod_{w \in D} \frac{p_w(1-q_w)}{q_w(1-p_w)} = \prod_{w \in D \cap Q} \frac{1-q_w}{q_w} = \prod_{w \in D \cap Q} \frac{N - N_w + 0.5}{N_w + 0.5}$

Copyright 2010, Victor Lavrenko

## Example (no relevance)

- documents:  $D_1 = \text{"a b c b d"} , D_2 = \text{"b e f b"} , D_3 = \text{"b g c d"} , D_4 = \text{"b d e"} , D_5 = \text{"a b e g"} , D_6 = \text{"b g h"}$

word:	a	b	c	d	e	f	g	h	
N(w):	2	6	2	3	3	1	3	1	N = 6
$\frac{N-N_w}{N_w}$ :	$\frac{4.5}{2.5}$	$\frac{0.5}{6.5}$	$\frac{4.5}{2.5}$	$\frac{3.5}{3.5}$	$\frac{3.5}{3.5}$	$\frac{5.5}{1.5}$	$\frac{3.5}{3.5}$	$\frac{5.5}{1.5}$	

- query:  $Q = \text{"a c h"}$

$$P(R=1|D_1)^{rank} = \prod_{w \in Q \cap D_1} \frac{N - N_w + 0.5}{N_w + 0.5} = \frac{4.5}{2.5} \cdot \frac{4.5}{2.5}$$

only words present in both D & Q

$$P(R=1|D_2)^{rank} = 1$$

$$P(R=1|D_3)^{rank} = \frac{4.5}{2.5}$$

$$P(R=1|D_4)^{rank} = 1$$

$$P(R=1|D_5)^{rank} = \frac{4.5}{2.5}$$

$$P(R=1|D_6)^{rank} = \frac{5.5}{1.5}$$

Ranking:

$D_6$   
 $D_1$   
 $D_3$   
 $D_5$   
 $D_2$   
 $D_4$

Copyright 2010, Victor Lavrenko

# Probabilistic model (review)

- Probability Ranking Principle: best possible ranking

- Assumptions: 
$$P(R=1|D) \stackrel{rank}{=} \prod_{w \in D} \frac{p_w}{q_w} \prod_{w \notin D} \frac{1-p_w}{1-q_w} = \prod_{w \in D \cap Q} \frac{N - N_v}{N_v}$$

- A0: relevance for document in isolation
  - A1: words absent or present (can't model frequency)
  - A2: all words mutually independent (given relevance)
  - A3: empty document equally likely for R=0,1
  - A4: non-query words cancel out
  - A5: query words: relevant class doesn't matter
  - A6: non-relevant class ~ collection as a whole
- } efficiency
- } estimate  $p_w, q_w$   
w/out relevance  
observations

- How can we improve the model?

Copyright 2010, Victor Lavrenko

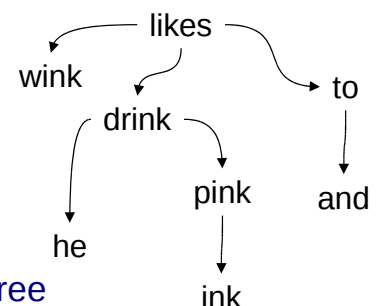
## Modeling word dependence

- Classical model assumes all words independent
  - blatantly false, made by almost all retrieval models
  - the most widely criticized assumption behind IR models
    - should be able to do better, right?

- Word dependence models

- details in part II of the tutorial
- preview: (van Rijsbergen, 1977)

- structure dependencies as maximum spanning tree
- each word depends on its parent (and R)



$$\begin{aligned}
 &P(\text{"he likes to wink and drink pink ink"}) \\
 &= P(\text{likes}) * P(\text{to}|\text{likes}) * P(\text{wink}|\text{likes}) * P(\text{and}|\text{to}) \\
 &\quad * P(\text{drink}|\text{likes}) * P(\text{he}|\text{drink}) * P(\text{pink}|\text{drink}) * P(\text{ink}|\text{pink})
 \end{aligned}$$

Copyright 2010, Victor Lavrenko

# Why dependency models fail

- Word independence constantly criticized
  - blatantly wrong assumption about language
  - numerous attempts to model dependency
  - never a consistent improvement
- Language Modeling Framework
  - dependency models address wrong problem
    - focus on surface form of the string
  - we are dealing with already well-formed strings
- Classical Probabilistic Framework
  - does not in fact assume word independence

Copyright 2010, Victor Lavrenko

## BIR **doesn't** assume independence

$$\frac{P_{R=1}(\vec{d})}{P_{R=0}(\vec{d})} = \underbrace{\prod_v \frac{P_1(d_v)}{P_0(d_v)}}_{\text{independence}} \times \underbrace{\prod_v \frac{k_1(v)}{k_0(v)}}_{\text{will not affect ranking if}} = \underbrace{\prod_v \frac{P_1(d_v | d_{\pi(v)})}{P_0(d_v | d_{\pi(v)})}}_{\text{1st order dependence}}$$

$k_r(v) = \frac{P_r(d_v, d_{\pi(v)})}{P_r(d_v) P_r(d_{\pi(v)})}$

$$\underbrace{\sum_v \log \frac{P_1(d_v, d_{\pi(v)})}{P_1(d_v) P_1(d_{\pi(v)})}}_{\substack{\text{aggregate dependence} \\ \text{between word and parent} \\ \text{in the relevant class}}} \sim \underbrace{\sum_v \log \frac{P_0(d_v, d_{\pi(v)})}{P_0(d_v) P_0(d_{\pi(v)})}}_{\substack{\text{aggregate dependence} \\ \text{in the non-relevant class}}}$$

- Sufficient condition: **proportional interdependence**

*the **total** amount of interdependence among **all** words in a document is approximately the same under  $R=1$  and  $R=0$*

Copyright 2010, Victor Lavrenko

# Meaning of Independence

- Independence:
  - seeing “subprime” doesn't affect chances of seeing “loan”
- Linked Dependence:
  - seeing “subprime” increases chance of seeing “loan”
  - by the same amount under  $R=1$  and  $R=0$ 
    - reasonable... unless topic is financial crisis
- Proportional Interdependence:
  - “subprime” increases chance of “loan”
  - can be more co-dependent in relevant class
  - as long as offset by other word sets under  $R=0$ 
    - “world cup” more co-dependent in non-relevant class

Copyright 2010, Victor Lavrenko

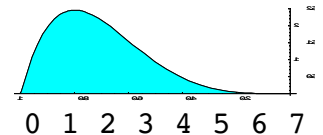
## Probabilistic model (review)

- Probability Ranking Principle: best possible ranking
  - Assumptions:
$$P(R=1|D) \stackrel{rank}{=} \prod_{w \in D} \frac{p_w}{q_w} \prod_{w \notin D} \frac{1-p_w}{1-q_w} = \prod_{w \in D \cap Q} \frac{N - N_v}{N_v}$$
    - A0: relevance for document in isolation
    - A1: words absent or present (can't model frequency)
    - A2: all words mutually independent (given relevance)
    - A3: empty document equally likely for  $R=0,1$
    - A4: non-query words cancel out
    - A5: query words: relevant class doesn't matter
    - A6: non-relevant class ~ collection as a whole
- } efficiency
- } estimate  $p_w, q_w$  w/out relevance observations
- How can we improve the model?

Copyright 2010, Victor Lavrenko

# Modeling word frequencies

- Want to model TF (empirically useful)  $P(R=1|D) \stackrel{\text{rank}}{=} \prod_{w \in D} \frac{P(d_w|R=1)}{P(d_w|R=0)}$ 
  - A1': assume  $D_w = d_w \dots$  # times word  $w$  occurs in document  $D$
  - estimate  $P(d_w|R)$ : e.g. “obama” occurs 5 times in a rel. doc
  - naive: separate prob. for every outcome:  $p_{w,1}, p_{w,2}, p_{w,3}, \dots$ 
    - many outcomes  $\rightarrow$  many parameters (BIR had only one  $p_w$ )
    - “smoothness” in the outcomes:  $d_w=5$  similar to  $d_w=6$ , but not  $d_w=1$
  - parametric model: assume  $d_w \sim \text{Poisson}$ 
    - single parameter  $m_w \dots$  expected frequency
  - problem: Poisson a poor fit to observations
    - does not capture bursty nature of words



$$P(d_w) = \frac{e^{-\mu_w} \mu_w^{d_w}}{d_w!}$$

Copyright 2010, Victor Lavrenko

## Two-Poisson model [Harter]

- Idea: words generated by a mixture of two Poissons
  - “elite” words for a document: occur unusually frequently
  - “non-elite” words – occur as expected by chance
  - document is a mixture:  $P(d_w) = P(E=1) \frac{\exp^{-\mu_{1,w}} \mu_{1,w}^{d_w}}{d_w!} + P(E=0) \frac{\exp^{-\mu_{0,w}} \mu_{0,w}^{d_w}}{d_w!}$ 
    - estimate  $m_{0,w}, m_{1,w}, P(E=1)$  by fitting to data (max. likelihood)
- Problem: need probabilities conditioned on relevance
  - “eliteness” not the same as relevance
  - Robertson and Sparck Jones: condition eliteness on  $R=0, R=1$ 
    - final form has too many parameters, and no data to fit them...
    - same problem that plagued BIR
- BM25: an “approximation” to conditioned 2-Poisson
 
$$\frac{p_w(d_w) q_w(0)}{q_w(d_w) p_w(0)} \approx \exp \left( \frac{d_w \cdot (1+k)}{d_w + k \cdot ((1-b) + b \cdot n_d / n_{avg})} \times \log \frac{N}{N_w} \right)$$

Copyright 2010, Victor Lavrenko

# BM25: an intuitive view

Repetitions of query words  $\rightarrow$  good

Common words less important

$$\log \frac{p(d|R=1)}{p(d|R=0)} \approx \sum_w \left( \frac{d_w \cdot (1+k)}{d_w + k \cdot ((1-b) + b \cdot n_d / n_{avg})} \times \log \frac{N}{N_w} \right)$$

More words in common with the query  $\rightarrow$  good

Repetitions less important than different query words

But more important if document is relatively long (wrt. average)

Copyright 2010, Victor Lavrenko

## Example (BM25)

- documents:  $D_1 = \text{"a b c b d"}$ ,  $D_2 = \text{"b e f b"}$ ,  $D_3 = \text{"b g c d"}$ ,  
 $D_4 = \text{"b d e"}$ ,  $D_5 = \text{"a b e g"}$ ,  $D_6 = \text{"b g h h"}$

- query:  $Q = \text{"a c h"}$ , assume  $k = 1$ ,  $b = 0.5$

word:	a	b	c	d	e	f	g	h	
$N(w)$ :	2	6	2	3	3	1	3	1	$N = 6$
$\frac{N-Nw}{Nw}$ :	$\frac{4.5}{2.5}$	$\frac{0.5}{6.5}$	$\frac{4.5}{2.5}$	$\frac{3.5}{3.5}$	$\frac{3.5}{3.5}$	$\frac{5.5}{1.5}$	$\frac{3.5}{3.5}$	$\frac{5.5}{1.5}$	

$$\log \frac{p(D_1|R=1)}{p(D_1|R=0)} \approx 2 \times \left( \frac{1 \cdot (1+1)}{1 + 1 \cdot (0.5 + 0.5 \cdot 5/4)} \times \log \frac{6+1}{2+0.5} \right)$$

$$\log \frac{p(D_6|R=1)}{p(D_6|R=0)} \approx \left( \frac{2 \cdot (1+1)}{2 + 1 \cdot (0.5 + 0.5 \cdot 4/4)} \times \log \frac{6+1}{1+0.5} \right)$$

# Summary: probabilistic model

- Probability Ranking Principle
  - ranking by  $P(R=1|D)$  is optimal
- Classical probabilistic model
  - words: binary events (relaxed in the 2-Poisson model)
  - words assumed independent (not accurate)
    - numerous attempts to model dependence, all without success
- Formal, interpretable model
  - explicit, elegant model of relevance (if observable)
  - very problematic if relevance not observable
    - authors resort to heuristics, develop BM25

Copyright 2010, Victor Lavrenko

## Outline

- Recap of probability theory
- Probability ranking principle
- Classical probabilistic model
  - Binary Independence Model
  - 2-Poisson model and BM25
  - feedback methods
- Language modeling approach
  - overview and design decisions
  - estimation techniques
  - synonymy and feedback

Copyright 2010, Victor Lavrenko

# What is a Language Model?

- Probability distribution over strings of text
  - how likely is a given string (observation) in a given “language”
  - for example, consider probability for the following four strings
  - English:  $p_1 > p_2 > p_3 > p_4$ 
    - $P_1 = P(\text{“a quick brown dog”})$
    - $P_2 = P(\text{“dog quick a brown”})$
    - $P_3 = P(\text{“un chien quick brown”})$
    - $P_4 = P(\text{“un chien brun rapide”})$
  - ... depends on what “language” we are modeling
  - in most of IR we will have  $p_1 \approx p_2$
  - for some applications we will want  $p_3$  to be highly probable

Copyright 2010, Victor Lavrenko

## Language Modeling Notation

- Make explicit what we are modeling:
  - M ... represents the language we're trying to model
  - s ... “observation” (strings of tokens / words)
  - $P(s|M)$  ... probability of observing “s” in language M
- M can be thought of as a “source” or a generator
  - a mechanism that can produce strings that are legal in M
  - $P(s|M)$  ... probability of getting “s” during repeated random sampling from M

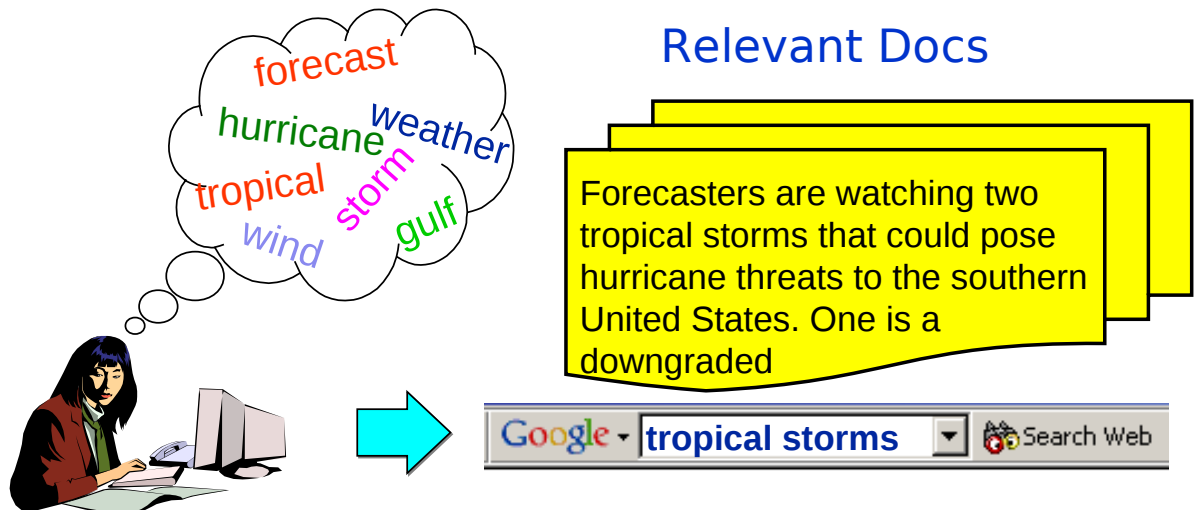
Copyright 2010, Victor Lavrenko



# How can we use LMs in IR?

Use LMs to model the process of query generation:

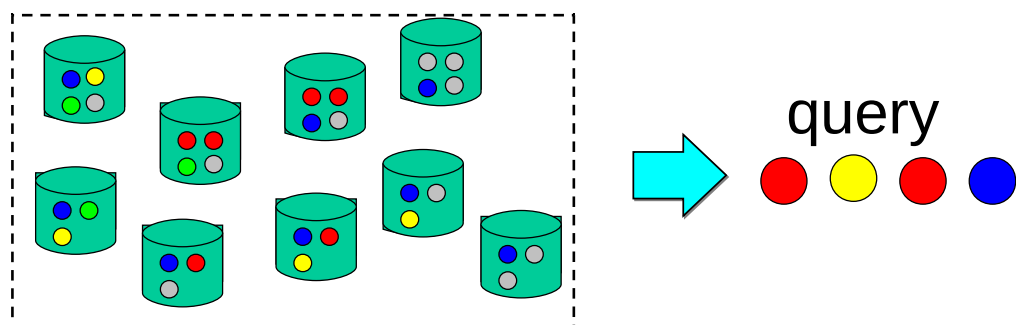
- user thinks of some relevant document
- picks some keywords to use as the query



Copyright 2010, Victor Lavrenko

## Retrieval with Language Models

- Each document  $D$  in a collection defines a “language”
  - all possible sentences the author of  $D$  could have written
  - $P(s|M_D)$  ... probability that author would write string “s”
    - intuition: write a billion variants of  $D$ , count how many times we get “s”
    - language model of what the author of  $D$  was trying to say
- Retrieval: rank documents by  $P(q|M_D)$ 
  - probability that the author would write “q” while creating  $D$



Copyright 2010, Victor Lavrenko

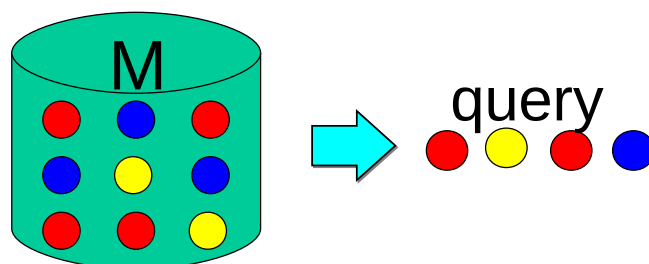
# Major issues in applying LMs

- What kind of language model should we use?
  - Unigram or higher-order models?
  - Multinomial or multiple-Bernoulli?
- How can we estimate model parameters?
  - maximum likelihood and zero frequency problem
  - discounting methods: Laplace, Lindstone and Good-Turing estimates
  - interpolation methods: Jelinek-Mercer, Dirichlet prior, Witten-Bell
  - leave-one-out method
- Ranking methods
  - query likelihood / document likelihood / model comparison

Copyright 2010, Victor Lavrenko

## Unigram Language Models

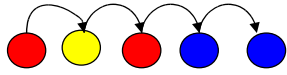
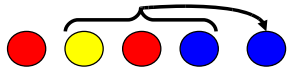
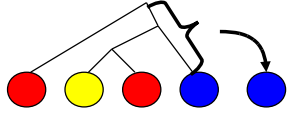
- words are “sampled” independently of each other
  - metaphor: randomly pulling out words from an urn (w. replacement)
  - joint probability decomposes into a product of marginals
  - estimation of probabilities: simple counting



$$\begin{aligned} P(\text{red } \text{yellow } \text{red } \text{blue}) &= P(\text{red}) P(\text{yellow}) P(\text{red}) P(\text{blue}) \\ &= 4/9 * 2/9 * 4/9 * 3/9 \end{aligned}$$

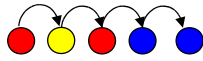
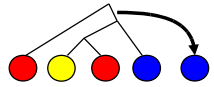
Copyright 2010, Victor Lavrenko

# Higher-order Models

- Unigram model assumes word independence
  - cannot capture surface form:  $P(\text{"brown dog"}) \neq P(\text{"dog brown"})$
- Higher-order models
  - n-gram: condition on preceding words: 
  - cache: condition on a window (cache): 
  - grammar: condition on parse tree 
- Are they useful?
  - no improvements from n-gram, grammar-based models
  - some research on cache-like models (proximity, passages, etc.)
  - parameter estimation is prohibitively expensive

Copyright 2010, Victor Lavrenko

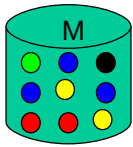
## Why unigram models?

- Higher-order LMs useful in other areas
  - n-gram models: critical in speech recognition 
  - grammar-based models: successful in machine translation 
- IR experiments: no improvement over unigram
  - unigram assumes word independence, intuitively wrong
  - no conclusive reason, still subject of debate
- Possible explanation: solving a non-existent problem
  - higher-order language models focus on surface form of text
  - ASR / MT engines must produce well-formed, grammatical utterances
  - in IR all utterances (documents, queries) are already grammatical
- What about phrases?
  - bi-gram:  $O(v^2)$  parameters, there are better ways

Copyright 2010, Victor Lavrenko

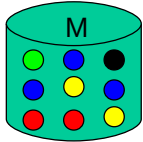
# Multinomial or multiple-Bernoulli?

- Most popular model is the multinomial:
  - fundamental event: *what word is in the  $i$ 'th position in the sample?*
  - observation is a sequence of events, one for each token in the sample



$$P(q_1 \dots q_k | M) = \prod_{i=1}^k P(q_i | M)$$

- Original model is multiple-Bernoulli:
  - fundamental event: *does the word  $w$  occur in the sample?*
  - observation is a set of binary events, one for each possible word



$$P(q_1 \dots q_k | M) = \prod_{w \in q_1 \dots q_k} P(w | M) \prod_{w \notin q_1 \dots q_k} [1 - P(w | M)]$$

Copyright 2010, Victor Lavrenko

# Multinomial or multiple-Bernoulli?

- Two models are fundamentally different
  - entirely different event spaces (“word” means different things)
  - both assume word independence (though it has different meanings)
  - have different estimation methods (though appear very similar)

- Multinomial

- accounts for multiple word occurrences in the query (primitive)
- well understood: lots of research in related fields (and now in IR)
- possibility for integration with ASR/MT/NLP (same event space)

- Multiple-Bernoulli

- arguably better suited to IR (directly checks presence of query terms)
- provisions for explicit negation of query terms (“A but not B”)
- no issues with observation length

Copyright 2010, Victor Lavrenko

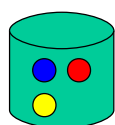
# Outline

- Recap of probability theory
- Probability ranking principle
- Classical probabilistic model
  - Binary Independence Model
  - 2-Poisson model and BM25
  - feedback methods
- Language modeling approach
  - overview and design decisions
  - estimation techniques
  - synonymy and feedback

Copyright 2010, Victor Lavrenko

## Estimation of Language Models

- Usually we don't know the model  $M$ 
  - but have a sample of text representative of that model
  - estimate a language model from that sample
- Maximum likelihood estimator:
  - count relative frequency of each word



$$P(\text{blue}) = 1/3$$

$$P(\text{red}) = 1/3$$

$$P(\text{yellow}) = 1/3$$

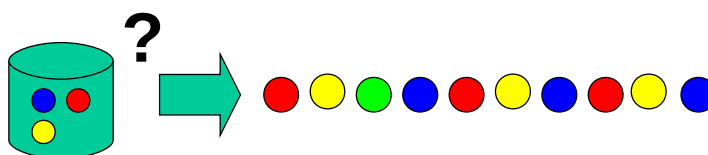
$$P(\text{green}) = 0$$

$$P(\text{grey}) = 0$$

Copyright 2010, Victor Lavrenko

# The Zero-frequency Problem

- Suppose some event (word) not in our sample D
  - model will assign zero probability to that event
  - and to any set of events involving the unseen event
- Happens very frequently with language (Zipf)
- It is incorrect to infer zero probabilities
  - especially when dealing with incomplete samples



Copyright 2010, Victor Lavrenko

## Counts vs. Probabilities

- Have a biased coin:  $P(\text{"heads"} = p)$ 
  - flip a coin several times → get sequence of heads / tails
  - try to recover  $p$  from these observations



0 / 0,  $p = ???$

4 / 5,  $p = 0.80$

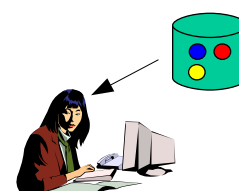
1 / 1,  $p = 1.00$

17 / 20,  $p = 0.85$

2 / 2,  $p = 1.00$

72 / 100,  $p = 0.72$

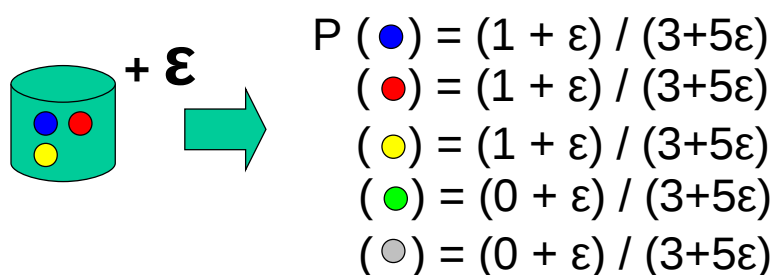
- Same problem with language-models ( $n$ -faced coins)
  - document is an observation (word counts)
  - “sampled” from urn with unknown frequencies
    - i.e. contents of the author's mind while writing



Copyright 2010, Victor Lavrenko

# Simple Discounting Methods

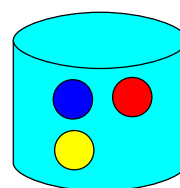
- Laplace correction:
  - add 1 to every count, normalize
  - problematic for large vocabularies
- Lindstone correction:
  - add a small constant  $\epsilon$  to every count, re-normalize
- Absolute Discounting
  - subtract a constant  $\epsilon$ , re-distribute the probability mass



Copyright 2010, Victor Lavrenko

## Good-Turing Estimation

- Leave-one-out discounting
  - remove some word, compute  $P(D|M_D)$
  - repeat for every word in the document
  - iteratively adjusting  $\epsilon$  to maximize  $P(D|M_D)$ 
    - increase if word occurs once, decrease if more than once
- Good-Turing estimate
  - derived from leave-one-out discounting, but closed-form
  - if a word occurred  $n$  times, its “adjusted” frequency is:
 
$$n^* = (n+1) E \{ \#_{n+1} \} / E \{ \#_n \}$$
    - probability of that word is:  $n^* / N^*$
    - $E \{ \#_n \}$  is the “expected” number of words with  $n$  occurrences
    - $E \{ \#_n \}$  very unreliable for high values of  $n$



Copyright 2010, Victor Lavrenko

# Interpolation Methods

- Problem with all discounting methods:
  - discounting treats unseen words equally (add or subtract  $\epsilon$ )
  - some words are more frequent than others
- Idea: use background probabilities
  - “interpolate” ML estimates with General English expectations
  - reflects expected frequency of words in “average” document
  - in IR applications, plays the role of IDF
- 2-state HMM analogy

$$\lambda \underbrace{\text{cylinder with 4 colored dots}}_{tf_{w,D}/|D|} + (1-\lambda) \underbrace{\text{cylinder with 16 colored dots}}_{cf_w/|C|}$$

Copyright 2010, Victor Lavrenko

63

## “Jelinek-Mercer” Smoothing

- Correctly setting  $\lambda$  is very important
- Start simple:
  - set  $\lambda$  to be a constant, independent of document, query
- Tune to optimize retrieval performance
  - optimal value of  $\lambda$  varies with different databases, queries, etc.

$$\lambda \text{ (small cylinder)} + (1-\lambda) \text{ (large cylinder)}$$

Copyright 2010, Victor Lavrenko



# “Dirichlet” Smoothing

- Problem with Jelinek-Mercer:
  - longer documents provide better estimates
  - could get by with less smoothing
- Make smoothing depend on sample size
- Formal derivation from Bayesian (Dirichlet) prior on LMs
- Currently best out-of-the-box choice for short queries
  - parameter tuned to optimize MAP, needs some relevance judgments

$$\underbrace{N / (N + \mu)}_{\lambda} \quad \text{[small cylinder with 4 colored balls]} + \underbrace{\mu / (N + \mu)}_{(1-\lambda)} \quad \text{[large cylinder with 16 colored balls]}$$

65

Copyright 2010, Victor Lavrenko

## Leave-one-out Smoothing

- Re-visit leave-one-out idea:
  - Randomly remove some word from the example
  - Compute the likelihood for the original example, based on  $\lambda$
  - Repeat for every word in the sample
  - Adjust  $\lambda$  to maximize the likelihood
- Performs as well as well-tuned Dirichlet smoothing
  - does not require relevance judgments for tuning the parameter

$$\lambda \quad \text{[small cylinder with 4 colored balls]} + (1-\lambda) \quad \text{[large cylinder with 16 colored balls]}$$

Copyright 2010, Victor Lavrenko

# IDF-like role of smoothing

$$\lambda \underbrace{tf_{w,D}}_{\text{document}} + (1-\lambda) \underbrace{cf_w}_{\text{query}}$$

document query

$Q \cap D$   $Q - D$

$$P(Q|D) = \prod_{w \in Q} P(w|D)$$

$$= \prod_{w \in Q \cap D} \left[ \lambda \frac{tf_{w,D}}{|D|} + (1-\lambda) \frac{cf_w}{|C|} \right] \prod_{w \in Q - D} \left[ (1-\lambda) \frac{cf_w}{|C|} \right]$$

$$= \prod_{w \in Q \cap D} \frac{\lambda \frac{tf_{w,D}}{|D|} + (1-\lambda) \frac{cf_w}{|C|}}{(1-\lambda) \frac{cf_w}{|C|}} = \prod_{w \in Q \cap D} \left[ 1 + \frac{\lambda}{1-\lambda} \frac{tf_{w,D}}{|D|} \frac{|C|}{cf_w} \right]$$

rank

67

Copyright 2010, Victor Lavrenko

## LMs: an intuitive view

Repetitions of query words  $\rightarrow$  good

Common words less important

$$\log P(Q|D) = \sum_{w \in Q \cap D} \log \left( 1 + \frac{\lambda_D}{1-\lambda_D} \cdot \frac{tf_{w,D}}{|D|} \cdot \frac{|C|}{cf_w} \right)$$

More words in common with the query  $\rightarrow$  good

Repetitions less important than different query words

$\log(1 + tf_w)$

Copyright 2010, Victor Lavrenko

# Variations of the LM Framework

- Query-likelihood:  $P(Q|M_D)$ 
  - probability of observing query from the document model  $M_D$
  - difficult to incorporate relevance feedback, expansion, operators
- Document-likelihood:  $P(D|M_Q)$ 
  - estimate relevance model  $M_q$  using text in the query
  - compute likelihood of observing document as a random sample
  - strong connections to classical probabilistic models:  $P(D|R)$
  - ability to incorporate relevance, interaction, query expansion
- Model comparison:  $D (M_Q || M_D)$ 
  - estimate both document and query models
  - measure “divergence” between the two models
  - best of both worlds, but loses pure probabilistic interpretation

Copyright 2010, Victor Lavrenko

## Language Models and PRP

- Relevance not explicitly part of LM approach
- [Lafferty & Zhai, 2003]: it's *implicitly* there:

- **PRP:** 
$$P(R=1|D, Q) \stackrel{rank}{=} \frac{P(R=1|D, Q)}{P(R=0|D, Q)} = \frac{P(D, Q|R=1) P(R=1)}{P(D, Q|R=0) P(R=0)}$$
- **Bayes' rule, then chain rule:** 
$$= \frac{P(Q|D, R=1) P(D|R=1) P(R=1)}{P(Q|D, R=0) P(D|R=0) P(R=0)}$$
- **Bayes' rule again:** 
$$= \frac{P(Q|D, R=1)}{P(Q|D, R=0)} \cdot \frac{P(R=1|D)}{P(R=0|D)}$$
- **Assumption:** 
$$= \frac{P(Q|D, R=1)}{P(Q|R=0)} \cdot \frac{P(R=1|D)}{P(R=0|D)}$$
  - $R=1$ :  $Q$  drawn from  $D$  (LM)
  - $R=0$ :  $Q$  independent of  $D$
  - odds ratio assumed to be 1
$$\stackrel{rank}{=} P(Q|D) \cdot \frac{P(R=1|D)}{P(R=0|D)}$$

Copyright 2010, Victor Lavrenko

# Summary: Language Modeling

- Formal mathematical model of retrieval
  - based on simple process: sampling query from a document urn
  - assumes word independence, higher-order LMs unsuccessful
  - **cleverly avoids pitfall of the classical probabilistic model**
- At a cost: no notion of relevance in the model
  - relevance feedback / query expansion unnatural
    - “augment the sample” rather than “re-estimate model”
  - can’t accommodate phrases, passages, Boolean operators
  - extensions to LM overcome many of these problems
    - query feedback, risk minimization framework, LM+BeliefNet, MRF
- Active area of research

Copyright 2010, Victor Lavrenko

## Outline

- Recap of probability theory
- Probability ranking principle
- Classical probabilistic model
  - Binary Independence Model
  - 2-Poisson model and BM25
  - feedback methods
- Language modeling approach
  - overview and design decisions
  - estimation techniques
  - **synonymy and cross-language**

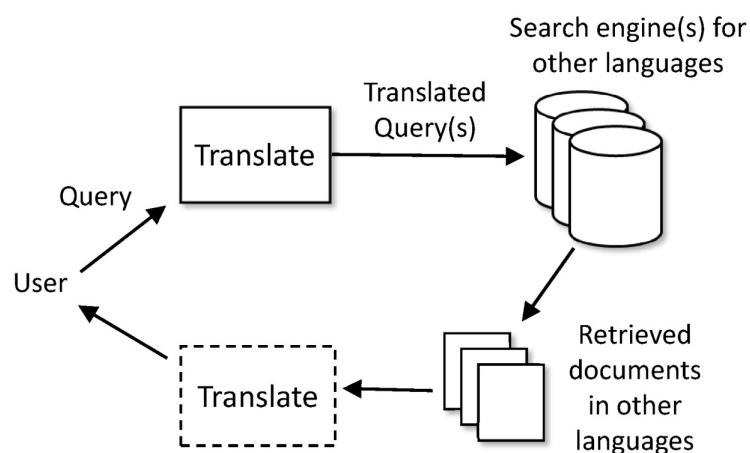
Copyright 2010, Victor Lavrenko

# Cross-language IR

- Cross-language Information Retrieval (CLIR)
  - accept queries / questions in one language (English)
  - find relevant information in a variety of other languages
- Why is this useful?
  - Ex1: research central banks' response to financial crisis
    - dozens of languages, would like to formulate a single query
    - can translate retrieved web-pages into English
  - Ex2: Topic Detection and Tracking (TDT)
    - identify new events (e.g. “5.9 earthquake in El-Salvador on Nov.15”)
    - group together all stories discussing the event, regardless of language
    - note: no query to start with
- Good domain to show slightly advanced LMs

Copyright 2010, Victor Lavrenko

## Typical CLIR architecture



Copyright 2010, Victor Lavrenko

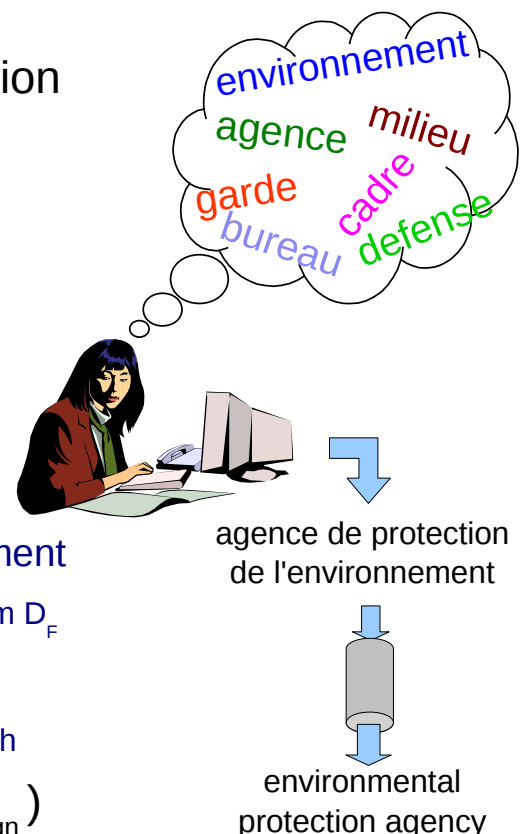
# Translating the queries

- Translating documents usually infeasible
- Query translation: ambiguous process
  - query as a sentence: may produce odd results
    - not a well-formed utterance, ok for “phrase” queries
  - word-for-word: multiple candidate translations
    - **environment** → environnement, milieu, atmosphere, cadre, conditions
    - **protection** → garde, protection, preservation, defense, racket
    - **agency** → agence, action, organisme, bureau
- How to combine translations?
  - single bag of words: bad idea
  - combinations / hypotheses
    - How many? How to assign weights?

Copyright 2010, Victor Lavrenko

## Language modeling view of CLIR

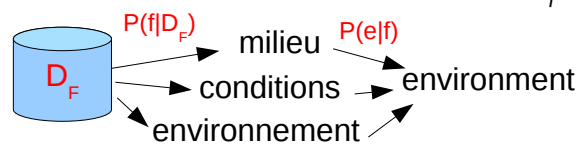
- Don't translate, model query generation
- Metaphor: user is really foreign
  - contemplates relevant documents
  - writes query in the foreign language
  - sends it over a noisy channel
    - query arrives “garbled” into English
- Using metaphor for retrieval:
  - language model for every foreign document
    - what foreign queries could be generated from  $D_F$
  - translation model for the noisy channel
    - how foreign queries are “garbled” into English
- Rank documents by  $P(Q_{\text{English}} | D_{\text{Foreign}})$



Copyright 2010, Victor Lavrenko

# Language modeling approach

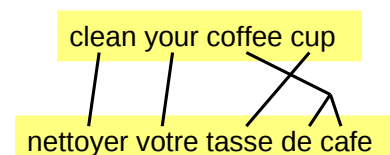
- Translation model: set of probabilities  $P(e|f)$ 
  - probability that French word “f” translates to English word “e”
    - e.g.  $P(\text{“environment”} | \text{“milieu”}) = 1/4$ ,  $P(\text{“agency”} | \text{“agence”}) = 1/2$ , etc.
- Language model of a French document:  $P(f|D_F)$ 
  - probability of observing “f”:  $P(\text{milieu}|D_F) = \frac{tf_{\text{milieu}, D_F}}{|D_F|}$
- Combine into noisy-channel model:
  - prob. of sampling f and translating to e:  $P(e, f|D_F) = P(e|f)P(f|D_F)$
  - many different foreign words can translate to e
  - total probability of observing e:  $P(e|D_F) = \sum_f P(e|f)P(f|D_F)$



Copyright 2010, Victor Lavrenko

## Translation probabilities

- How to estimate  $P(e|f)$ ?
- $f \rightarrow e$  dictionary: assign equal likelihoods to all translations
  - $\text{agence} \rightarrow \text{agency}:1/5, \text{bureau}:1/5, \text{branch}:1/5, \text{office}:1/5, \text{service}:1/5$
- $e \rightarrow f$  dictionary: use Bayes rule, collection frequency
  - $\text{agency} \rightarrow \text{agence}:1/4, \text{action}:1/4, \text{organisme}:1/4, \text{bureau}:1/4$
  - $P(\text{agency}|\text{agence}) = P(\text{agence}|\text{agency}) * P(\text{agency}) / P(\text{agence})$
- parallel corpus:
  - set of parallel sentences  $\{E, F\}$  such that E is a translation of F
  - simple co-occurrence: how many times e, f co-occur:  $P(e|f) = \frac{|(E, F): e \in E \wedge f \in F|}{|F: f \in F|}$
  - IBM translation model 1:
    - alignment: links between English, French words
    - count how many times e, f are aligned
    - iterative (EM) solution



Copyright 2010, Victor Lavrenko

# CLIR: putting it all together

- Rank documents by

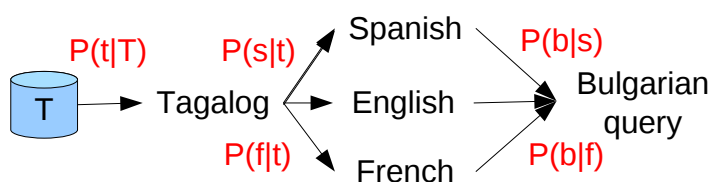
$$P(e_{1...k}|D_F) = \prod_{i=1}^k \left( \underbrace{\lambda_D \sum_f \overbrace{P(e_i|f)}^{\text{channel}} \overbrace{P(f|D_F)}^{\text{source}}}_{\text{probability of seeing query word } e_i \text{ during random sampling from } D_F} + \overbrace{(1 - \lambda_D) P(e_i)}^{\text{smoothing}} \right)$$

- Important issues:
  - translation probabilities ignore context
    - one solution: treat phrases as units, but there's a better way
  - vocabulary coverage extremely important
    - use as many dictionaries / lexicons / corpora as possible
  - morphological analysis crucial for Arabic, Slavic, etc.
  - no coverage for proper names → *transliterate*:
    - Qadafi, Kaddafi, Qathafi, Gadafi, Qaddafi, Quadhaffi, al-Qaddafi, ..

Copyright 2010, Victor Lavrenko

## Triangulated translation

- Translation models need bilingual resources
  - dictionaries / parallel corpora
  - not available for every language pair (Bulgarian ↔ Tagalog)
- Idea: use resource-rich languages as interlingua:
  - map Tagalog → Spanish, then Spanish → Bulgarian
  - use multiple intermediate languages, assign weights
- Results slightly exceed direct bilingual resource



Copyright 2010, Victor Lavrenko



# Summary: CLIR

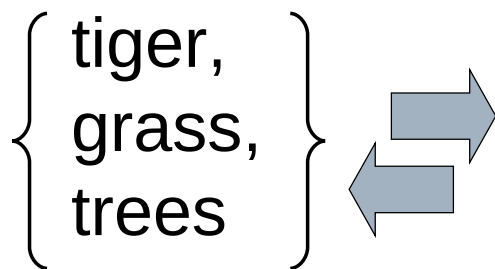
- Queries in one language, documents in another
  - real task, at least for intelligence analysts
  - translate query to foreign language, retrieve, translate results
- Language modelling approach:
  - probabilistic way to deal with uncertainty in translations
  - effective: 75-95% of mono-lingual performance
  - translation probabilities: based on dictionary, parallel corpus
- Triangulated translation for resource-poor languages
- Translation model: very general idea
  - synonyms: English → English translation

Copyright 2010, Victor Lavrenko

# Content-based Image Search

# Image Annotation / Retrieval Task

- Given a collection of **un-labeled** images
  - **annotation:** assign relevant keywords to images
  - **retrieval:** find images relevant to a given query
- Learn to associate sets of words with pictures



## Annotation vs. Retrieval

- NOTE: related but not equivalent problems
  - can have good retrieval with bad annotation
    - half the words assigned to each image are wrong
    - 80% of queries (all but “city”) will have perfect precision



city, tiger



city, iguana



city, bear

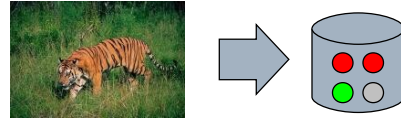


city, zebra

# Language-modeling Approach

- Query is a bag of words: {tiger,grass,trees}

- Convert every image to a bag of word-like units



- Reduces to cross-language retrieval problem
  - given a query in English: “tiger grass”
  - match documents written in foreign (visual) “words”
- Main issues:
  - how do we define / compute these visual words?
  - is the cross-language retrieval model sufficient?

## Converting Image to “Words”

- Convert into a set of discrete “features”

- break image into a set of patches

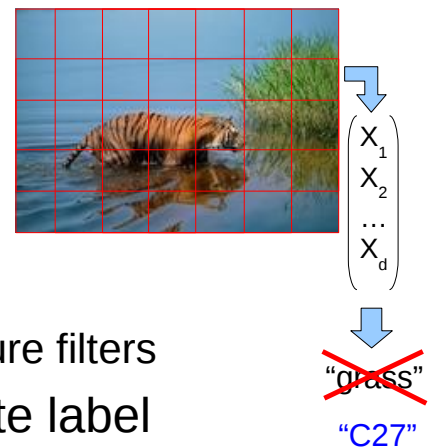
- “grassy”, “watery”, “tigery” patches
- captures different objects in image

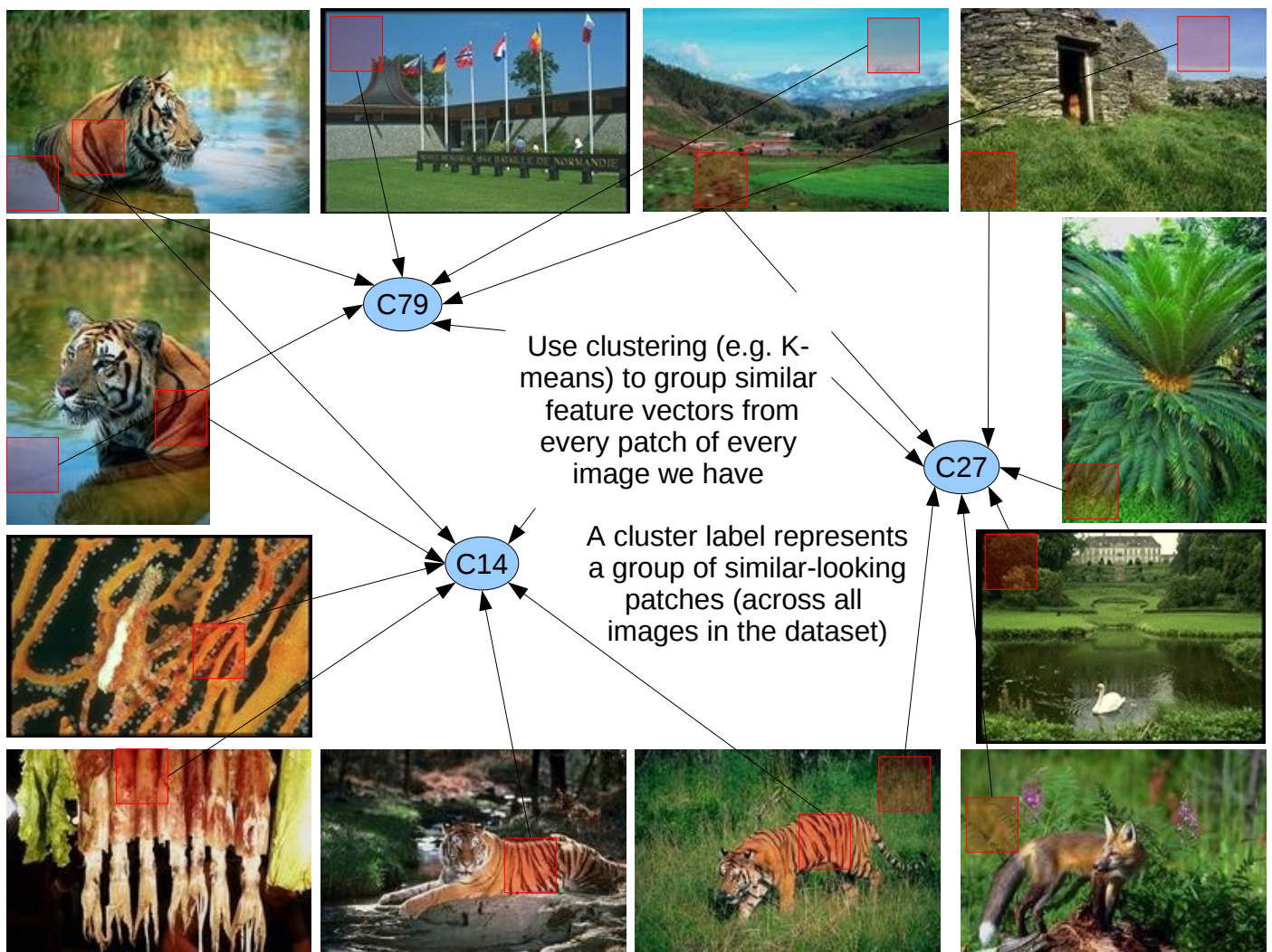
- extract features for each patch

- reflect visual appearance of a patch
- relative position, color histogram, texture filters

- replace feature vector with a discrete label

- meaningful label (e.g. “grass”) needs human annotations
- clustering: group feature vector with other, similar vectors

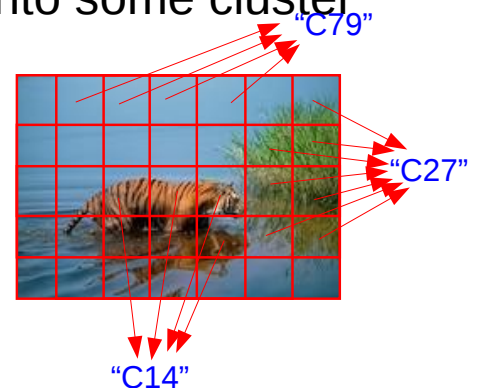




## Cluster Numbers as Visual “Words”

- After clustering:
  - every patch of every image falls into some cluster

- all similar-looking patches fall into the same cluster
- cluster id says something about patches that fall into it
  - “C27” → green, vertically-textured




- Use cluster ids as “words”

- $D = \{ 4 \times \text{“C14”}, 7 \times \text{“C27”}, 24 \times \text{“C79”}, 0 \times \text{everything else} \}$

- similar to controlled vocabulary / category codes
  - discrete, content-bearing, Zipfian distribution
  - sometimes called “vis-terms” or “visual words”

# Retrieving Images


- Converted:   $\Rightarrow \{4 \times \text{"C14"}, 7 \times \text{"C27"}, 24 \times \text{"C79"}\}$
- Want to query with *"tiger"*, not *"C14"*
  - use LMs to "translate" English queries into vis-terms
  - rank images by probability they "generate" query:

$$P(e_{1...k}|I) = \prod_{i=1}^k \left( \lambda_I \underbrace{\sum_v \overbrace{P(e_i|v) P(v|I)}^{\text{translate to English}}}_{\text{probability that one of the visterms present in the image "translates" to query word } e_i} + \underbrace{(1 - \lambda_I) P(e_i)}_{\text{Smoothing (IDF)}} \right)$$

draw a visterm

- need two components:
  - $P(v|I)$  ... document model based on counts of vis-terms
  - $P(q|v)$  ... model for associating words  $q$  with visterms  $v$

## Translating Visterms to Words

- No dictionaries
- Parallel corpora (manually-tagged images)
  - e.g.: Corel, Pascal VOC, TRECVID, LabelMe
  - pre-process  $\rightarrow$  get paired sets:  $\{\underbrace{v_1 \dots v_n}_{\text{visterms}}, \underbrace{e_1 \dots e_m}_{\text{tags}}\}$
  - extract translation pairs  $P(e|v)$ 
    - co-occurrence model (direct count):  $P(e|v) = \frac{|I: e \in E_I, v \in V_I|}{|I: v \in V_I|}$ 
      - problem: will associate "tiger" with C14 **and** C27 **and** C79
    - IBM translation model 1
      - uses EM to align "tiger"  $\rightarrow$  C14, "grass"  $\rightarrow$  C27, etc.
  - problem: visterms don't map to words 1-1
    -  in isolation does not "translate" to anything



# Set-to-Set Translation

- Visterms  $\leftrightarrow$  tags is a set-to-set mapping
  - don't try to break it into pairs: model holistically
  - joint probability of a set of tags w. a set of visterms
    - cross-media relevance model:

$$P(e_1 \dots e_m, v_1 \dots v_n) = \sum_{E, V} \prod_i P(e_i | E) \cdot \prod_j P(v_j | V) \cdot P(E, V)$$

query or candidate label
unlabeled testing image
training images
 $e_1 \dots e_m$  observed in a training image
 $v_1 \dots v_n$  observed in the same training image
prior

- note: can't just count:  $\{e_1 \dots e_m, v_1 \dots v_n\}$
- Annotate with set of tags:  $\arg \max_{e_1 \dots e_m} P(e_1 \dots e_m, v_1 \dots v_n)$
- Rank images by:  $P(e_1 \dots e_m | v_1 \dots v_n) = \frac{P(e_1 \dots e_m, v_1 \dots v_n)}{P(v_1 \dots v_n)}$

## Summary: CBIR

- Task: associate image content with keywords
  - **annotate** new images with tags automatically
  - **retrieve** unlabeled images using keyword queries
- Convert image to vis-terms
  - segment into patches, group into clusters
  - cluster id = “word” reflecting visual appearance
- Use language models as in CLIR:  $P(e_{1..m} | v_{1..n})$ 
  - translation pairs  $P(e|v)$  ... co-occurrence, EM
  - better way: joint probabilities (relevance model)

# Practical Suggestions

## Use a Toolkit

- Lemur (C++): [www.lemurproject.org](http://www.lemurproject.org)
  - use the Indri engine
- Terrier (Java): [www.terrier.org](http://www.terrier.org)
- Zettair (C): [www.seg.rmit.edu.au/zettair](http://www.seg.rmit.edu.au/zettair)
- Parallel (experimental):
  - Galago (Java): [www.galagosearch.org](http://www.galagosearch.org)
    - uses TupleFlow, used in Croft's new textbook
  - Ivory (Java): [www.umiacs.umd.edu/~jimmylin/ivory](http://www.umiacs.umd.edu/~jimmylin/ivory)
    - uses Hadoop/Cloud, new project
- Lucene, Xapian, etc.: production, not research

# Compute Everything in Log-Space

- IR models have lots of variables (words, docs)
  - independence => products of 1000s of probabilities
    - probabilities are very small numbers (must add up to 1)
  - easy to “overflow” floating point precision:
    - smallest non-zero value:  $10^{-38}$  (single),  $10^{-308}$  (double)
    - overflows after ~1000 words, storing lots of zeroes
  - ratios won't save you:  $\frac{P(\vec{d}|R=1)}{P(\vec{d}|R=0)} = \prod_v \underbrace{\frac{P(d_v|R=1)}{P(d_v|R=0)}}_{>10^3}$  <1 for most v
- Take log of everything
  - turns  $10^{-38}$  into -38

$$\log P(\vec{d}|R=1) = \log \prod_v P(d_v|R=1) = \sum_v \log P(d_v|R=1)$$

## Log-sum-exp Trick

- Your model has a product inside a summation
  - applies to most mixture models
  - how to compute in log-space?

$$\log \left[ \sum_a \prod_b P_{a,b} \right] = \log \left[ \sum_a \exp \left( \log \prod_b P_{a,b} \right) \right]$$

$$= \log \left[ \sum_a \exp \left( \sum_b \log P_{a,b} \right) \right]$$

$A$  ... sufficiently large constant

$$= \log \left[ \sum_a \exp \left( \sum_b \log P_{a,b} + A - A \right) \right]$$

$A = -\max_a \left[ \sum_b \log P_{a,b} \right]$  preserves top “ranks”

$$= \log \left[ \sum_a \exp \left( \sum_b \log P_{a,b} + A \right) e^{-A} \right]$$

$A = -\frac{1}{n_a} \sum_a \sum_b \log P_{a,b}$  preserves “average”

$$= \log \left[ \sum_a \exp \left( \sum_b \log P_{a,b} + A \right) \right] - A$$



# Compute over the D-Q Overlap

- Models often involve entire doc /qry/vocabulary
  - BIR:  $P(\vec{d}|R=1) = \prod_v P(d_v|R=1) = \underbrace{\prod_{v \in d} r_v \prod_{v \notin d} (1-r_v)}_{\text{all words in vocabulary}}$
  - LM:  $P(q|d) = \underbrace{\prod_{v \in q} P(v|d)}_{\text{words in qry}}$
- Very expensive to compute for every document
- Doesn't fit the way most toolkits work
  - don't call *Similarity(Q,D)* for every *D* in the corpus
  - retrieval scores computed from inverted indices
  - will pass only terms that occur **both** in *D* and in *Q*

## Retrieval with Inverted Indices

- Initialize array to hold all partial scores
- For each query term
  - fetch inverted list from disk
  - update partial score of each document
- Extract result set (non-zero)

					partial scores				
$10 * \#(\text{thing}) + 2 * \#(\text{pink}) + \#(\text{ink})$					D1	D2	D3	D4	D5
pink →		4 : 1	5 : 1	• 2	0	0	0	2	2
ink →	3 : 1	4 : 1	5 : 1		0	0	1	3	3
thing →	3 : 1			• 10	0	0	11	3	3

# Computing over D-Q Overlap

- Re-work to go over overlapping terms

$$\begin{aligned}
 P(\vec{d}|R=1) &= \prod_{v \in d} r_v \times \prod_{v \notin d} (1-r_v) \times \overbrace{\prod_{v \in d} \frac{1-r_v}{1-r_v}}^{=1} \\
 &= \prod_{v \in d} r_v \times \prod_v (1-r_v) / \prod_{v \in d} (1-r_v) \\
 &= \prod_{v \in d} \frac{r_v}{1-r_v} \times \prod_v (1-r_v)
 \end{aligned}$$

- Log:  $\log P(\vec{d}|R=1) = \sum_{v \in d} \log \frac{r_v}{1-r_v} + \sum_v \log(1-r_v)$

- inner product of doc and model
- constants can be pre-computed

$$\begin{aligned}
 &= \underbrace{\vec{d} \cdot \vec{\rho}}_{\text{dot product}} + \underbrace{\sum_v \log(1-r_v)}_{\text{constant: doesn't depend on } d, \text{ doesn't affect ranking}} \\
 &\quad \text{document} \quad \text{"model" vector}
 \end{aligned}$$

- Note for MapReduce:

- some constants will be hard to fit into framework

$$\rho_v = \log \frac{r_v}{1-r_v}$$

## Inconsistent Assumptions

- Common situation: estimate  $P(R|D,Q)$ 
  - want to condition  $R$  on two sources of evidence ( $D,Q$ )
    - $R,D,Q$ : relevance/doc/query, from/to/title, video/speech/tag...
  - don't want to condition on "complex" events ( $D,Q$ )
  - assume independence whenever convenient

$$\begin{aligned}
 P(R|D,Q) &= \frac{P(D,Q|R)P(R)}{P(D,Q)} \\
 &= \frac{P(D|R) \cdot P(Q|R) \cdot P(R)}{P(D) \cdot P(Q)} \\
 &= \frac{P(R|D)}{P(R)} \cdot \frac{P(R|Q)}{P(R)} \cdot P(R) \\
 &= \frac{P(R|D)P(R|Q)}{P(R)}
 \end{aligned}$$

apply Bayes' rule

assume  $D$  and  $Q$  are independent

Bayes' again:  $P(D|R) = \frac{P(R|D)P(D)}{P(R)}$

easy to work with

# Data Inconsistency

- Case: users pick doc, query, judge relevance:

- $d$  ... one of 10 possible documents  $P(q)=P(d)=P(r)=0.1$
- $q$  ... one of 10 possible queries  $P(r|q)=P(r|d)=0.5$
- relevance observed in 10% of all trials
- ... but in 50% of trials with  $d$ , or with  $q$

- Joint events under assumptions:  $Q \perp D$  and  $Q \perp D|R$

$P(d, q \text{ picked and judged relevant}) = P(d, q, r) = P(d, q|r) P(r)$

$$Q \perp D|R \Rightarrow P(d|r) P(q|r) P(r)$$

$P(d, q \text{ picked in the same trial})$ :

$$P(d, q) = P(d) P(q)$$

$$Q \perp D \Rightarrow = 0.1 \times 0.1$$

$$= 0.010$$

absurdity

$$P(d, q) < P(d, q, r)$$

$$= \frac{P(r|d) P(d)}{P(r)} \frac{P(r|q) P(q)}{P(r)} P(r)$$

$$= 0.5 \times 0.1 \times 0.5 \times 0.1 / 0.1$$

$$= 0.025$$

Did we pick bad estimates?

## Inconsistent Assumptions

- Are the estimates to blame?
  - did we just pick inconsistent  $P(q)$ ,  $P(d)$ ,  $P(r)$ ?
    - no, this is achievable in practice
- Assumed both  $Q \perp D$  and  $Q \perp D \text{ given } R$ 
  - this means either  $R$  is independent of  $D$ 
    - ... or  $R$  is independent of  $Q$
  - probably not what you intended
    - defeats the purpose of using both  $Q, D$  as evidence

# Proof: $Q \perp D$ and $Q \perp D | R \Rightarrow Q \perp R$ or $D \perp R$

Let  $Q$  ... query

$D$  ... document

$R$  ... relevance ( $r$  or  $n$ )

Define:  $r_d = P(d|R=r)$ ,  $r_q = P(q|R=r)$ ,  $p_r = P(R=r)$

$n_d = P(d|R=n)$ ,  $n_q = P(q|R=n)$ ,  $p_n = P(R=n)$

Assume:  $Q \perp D$  conditioned on  $R$  and  $Q \perp D$

$$P(d|r)P(q|r)p_r + P(d|n)P(q|n)p_n = P(d, q) = P(d)P(q)$$

$$r_d r_q p_r + n_d n_q p_n = (r_d p_r + n_d p_n)(r_q p_r + n_q p_n)$$

$$r_d r_q p_r + n_d n_q p_n = r_d^2 p_r^2 + n_d^2 p_n^2 + n_d r_q p_n p_r + r_d n_q p_r p_n$$

$$r_d r_q p_r (1 - p_r) + n_d n_q p_n (1 - p_n) = (n_d r_q + r_d n_q) p_n p_r$$

$$r_d r_q + n_d n_q = n_d r_q + r_d n_q$$

absurdity

Holds for any values of  $D, Q$   
Can extend beyond binary  $R$

$$r_d(r_q - n_q) = n_d(r_q - n_q)$$

$$\begin{aligned} & \text{or } r_q = n_q \Rightarrow R \perp Q \\ & \text{or } r_d = n_d \Rightarrow R \perp D \end{aligned}$$

## Proof (easy version)

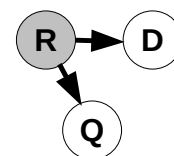
- Assumed both  $Q \perp D$  and  $Q \perp D$  given  $R$

- Look at dependence diagrams:

- conditional independence:

$$P(Q, D | R) = P(Q | R) P(D | R)$$

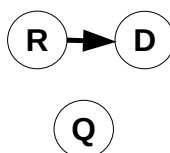
path between  $Q, D$  goes through  $R$



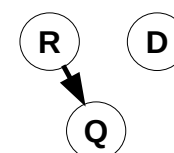
- mutual independence:

$$P(Q, D) = P(Q) P(D)$$

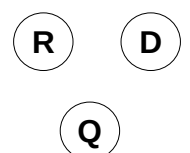
no path between  $Q, D$



or



or



– either no path between  $R, Q$

... or no path between  $R, D$

- Assuming both breaks dependence on  $R$

# What does it mean?

- Can't assume independence left and right
  - make sure assumptions don't contradict each other
- Isn't independence false anyway?
- Yes, but there's a difference:
  - false assumptions:
    - your model poorly fits observed data
  - inconsistent assumptions:
    - you don't have a model at all
      - model violates axioms of probability theory

## Checking your Model

- Inconsistency is just one of modelling errors
- Which independence assumptions made
  - do they contradict each other?
- What event spaces are you using
  - are they compatible?
  - what are the possible values of each RV?
- Does the model respect probability axioms?
  - do the marginals add up to 1 over all words / docs?
  - if can't figure out – likely to be a problem

# Summary: Practical Suggestions

- Use a toolkit
- Compute everything in log-space
- Log-sum-exp trick
- Compute over document-query overlap
- Check for inconsistencies in the model

## References

### Probabilistic Relevance Model

- [1] S. Robertson. *The probability ranking principle in IR*. Journal of Documentation, 33(4):294-303, 1977.
- [2] K. Sparck Jones, S. Walker and S. E. Robertson. *A probabilistic model of information retrieval: development and comparative experiments*. Information Processing and Management, pages 779-840, 2000.
- [3] W. B. Croft and D. Harper. *Using probabilistic models of information retrieval without relevance information*. Journal of Documentation, 35(4):285-295, 1979.
- [4] V. Lavrenko and W. B. Croft. *Relevance-based language models*. In Proc. 24th Ann. Intl. ACM SIGIR Conf. on Research and Development in Information Retrieval, pages 120-127, 2001.
- [5] J. Teevan and D. R. Karger. *Empirical development of an exponential probabilistic model for text retrieval: using textual analysis to build a better model*. In SIGIR '03: Proceedings of the 26th annual international ACM SIGIR conference on Research and development in information retrieval, pages 18-25, New York, NY, USA, 2003. ACM.
- [6] S. Robertson. *Understanding inverse document frequency: on theoretical arguments for IDF*. Journal of Documentation, 60(5):503-520, 2004.
- [7] S. Robertson and S. Walker. *Some simple effective approximations to the 2-poisson model for probabilistic weighted retrieval*. In Proc. 17th Ann. Intl. ACM SIGIR Conf. on Research and Development in Information Retrieval, pages 232-241, 1994.
- [8] S. E. Robertson and S. Walker. *On relevance weights with little relevance information*. In Proc. 20th Ann. Intl. ACM SIGIR Conf. on Research and Development in Information Retrieval, pages 16-24, 1997.
- [9] S. E. Robertson and K. Sparck Jones. *Relevance weighting of search terms*. Journal of the American Society for Information Science, 27(3):129-146, 1976.
- [10] C. J. van Rijsbergen. *A theoretical basis for the use of cooccurrence data in information retrieval*. Journal of Documentation, 33(2):106-119, 1977.
- [11] W. S. Cooper. *Some inconsistencies and misnomers in probabilistic information retrieval*. In Proc. 14th Ann. Intl. ACM SIGIR Conf. on Research and Development in Information Retrieval, pages 57-61, 1991.
- [12] P. Domingos and M. Pazzani. *Beyond Independence: Conditions for the Optimality of the Simple Bayesian Classifier*. Machine Learning, pages 105-112, Morgan Kaufmann, 1996.
- [13] V. Lavrenko. *A Generative Theory of Relevance*. Pages 23-26, Springer-Verlag, 2009.

# References

## Language Modeling Approach

- [14] J. Ponte and W. B. Croft. *A language modeling approach to information retrieval*. In Proc. 21st Ann. Intl. ACM SIGIR Conf. on Research and Development in Information Retrieval, pages 275-281, 1998.
- [15] D. H. Miller, T. Leek, and R. Schwartz. *A hidden markov model information retrieval system*. In Proc. 22nd Ann. Intl. ACM SIGIR Conf. on Research and Development in Information Retrieval, pages 214-221, 1999.
- [16] C. Zhai and J. Lafferty. *A study of smoothing methods for language models applied to ad hoc information retrieval*. In Proc. 24th Ann. Intl. ACM SIGIR Conf. on Research and Development in Information Retrieval, pages 334-342, 2001.
- [17] D. Hiemstra. *Using language models for information retrieval*. PhD thesis, University of Twente, Amsterdam, NL, 2001.
- [18] J. Lafferty and C. Zhai. *Probabilistic relevance models based on document and query generation*, pages 1-10. Kluwer Academic Publishers, Dordrecht, The Netherlands, 2003.
- [19] J. Lafferty and C. Zhai. *Document language models, query models, and risk minimization for information retrieval*. In Proc. 24th Ann. Intl. ACM SIGIR Conf. on Research and Development in Information Retrieval, pages 111-119, 2001.
- [20] C. Zhai and J. Lafferty. *Two-stage language models for information retrieval*. In Proc. 25th Ann. Intl. ACM SIGIR Conf. on Research and Development in Information Retrieval, pages 49-56, 2002.
- [21] D. Metzler, V. Lavrenko, and W. B. Croft. *Formal multiple bernoulli models for language modeling*. In Proc. 27th Ann. Intl. ACM SIGIR Conf. on Research and Development in Information Retrieval, pages 540-541, 2004.
- [22] H. Zaragoza, D. Hiemstra, and M. Tipping. *Bayesian extension to the language model for ad-hoc information retrieval*. In the proceedings of the 26th International ACM SIGIR Conference on Research and Development in Information Retrieval, pages 4-9, Toronto, Canada, July 2003.
- [23] T. Tao, X. Wang, Q. Mei, and C. Zhai. *Language model information retrieval with document expansion*. In Proc. of HLT/NAACL, pages 407-414, 2006.
- [24] C. Zhai and J. Lafferty. *Model-based feedback in the language modeling approach to information retrieval*. In Proc. 10th Intl. Conf. on Information and Knowledge Management, pages 403-410, 2001.
- [25] K. Collins-Thompson and J. Callan. *Query expansion using random walk models*. In Proc. 14th Intl. Conf. on Information and Knowledge Management, pages 704-711, 2005.

# References

## Language Models (cont)

- [27] J. Gao, J. Nie, G. Wu, and G. Cao. *Dependence language model for information retrieval*. In Proc. 27th Ann. Intl. ACM SIGIR Conf. on Research and Development in Information Retrieval, pages 170-177, 2004.
- [28] D. Metzler and W. B. Croft. *A markov random field model for term dependencies*. In Proc. 28th Ann. Intl. ACM SIGIR Conf. on Research and Development in Information Retrieval, pages 472-479, 2005.
- [30] O. Kurland and L. Lee. *Corpus structure, language models, and ad hoc information retrieval*. In Proc. 27th Ann. Intl. ACM SIGIR Conf. on Research and Development in Information Retrieval, pages 194-201, 2004.
- [31] X. Liu and W. B. Croft. *Cluster-based retrieval using language models*. In Proc. 27th Ann. Intl. ACM SIGIR Conf. on Research and Development in Information Retrieval, pages 186-193, 2004.

## Other Probabilistic Models

- [32] N. Fuhr. *Probabilistic models in information retrieval*. The Computer Journal, 35(3):243-255, 1992.
- [33] G. Amati and C. J. van Rijsbergen. *Probabilistic models of information retrieval based on measuring the divergence from randomness*. ACM Transactions on Information Systems, 20(4):357-389, 2002.
- [34] F. Gey. *Inferring probability of relevance using the method of logistic regression*. In Proc. 17th Ann. Intl. ACM SIGIR Conf. on Research and Development in Information Retrieval, 1994.
- [35] T. Hofmann. *Probabilistic latent semantic indexing*. In Proc. 22nd Ann. Intl. ACM SIGIR Conf. on Research and Development in Information Retrieval, pages 50-57, 1999.
- [36] X. Wei and W. B. Croft. *LDA-based document models for ad-hoc retrieval*. In Proc. 29th Ann. Intl. ACM SIGIR Conf. on Research and Development in Information Retrieval, pages 178-185, 2006.
- [37] Q. Mei, H. Fang, and C. Zhai. *A study of poisson query generation model for information retrieval*. In Proc. 30th Ann. Intl. ACM SIGIR Conf. on Research and Development in Information Retrieval, pages 319-326, New York, NY, USA, 2007. ACM.
- [39] R. Nallapati. *Discriminative models for information retrieval*. In Proc. 27th Ann. Intl. ACM SIGIR Conf. on Research and Development in Information Retrieval, pages 64-71, 2004.
- [40] H. Turtle and W. B. Croft. *Evaluation of an inference network-based retrieval model*. ACM Transactions on Information Systems, 9(3):187-222, 1991.
- [41] C. T. Yu, C. Buckley, K. Lam, and G. Salton. *A generalized term dependence model in information retrieval*. Technical report, Cornell University, 1983.

# References

## Cross-language Retrieval

- [42] A. Berger and J. Lafferty. *Information retrieval as statistical translation*. In Proc. 22nd Ann. Intl. ACM SIGIR Conf. on Research and Development in Information Retrieval, pages 222-229, 1999.
- [43] J. Xu, R. Weischedel, and C. Nguyen. *Evaluating a probabilistic model for cross-lingual information retrieval*. In Proceedings of the Twenty-Fourth Annual International ACM-SIGIR Conference on Research and Development in Information Retrieval, pages 105-110.
- [44] V. Lavrenko, M. Choquette, and W. Croft. *Cross-lingual relevance models*. In Proceedings of the Twenty-Fifth Annual International ACM-SIGIR Conference on Research and Development in Information Retrieval, SIGIR'02, pages 175-182.
- [45] L. A. Ballesteros and W. B. Croft. *Resolving ambiguity for cross-language retrieval*. In Proceedings of the Twenty-First Annual International ACM-SIGIR Conference on Research and Development in Information Retrieval, pages 64-71.
- [46] T. Gollins and M. Sanderson. *Improving cross language information retrieval with triangulated translation*. In Proceedings of the Twenty-Fourth Annual International ACM-SIGIR Conference on Research and Development in Information Retrieval, pages 90-95.
- [47] D. Hiemstra and F. de Jong. *Disambiguation strategies for cross-language information retrieval*. In Proceedings of the Third European Conference on Research and Advanced Technology for Digital Libraries, ECDL'99, pages 274-293.
- [48] P. F. Brown, J. Cocke, S. A. Della Pietra, V. J. Della Pietra, F. Jelinek, J. D. Lafferty, R. L. Mercer, and P. S. Roossin. *A statistical approach to machine translation*. Computational Linguistics, 16(2):79-85, 1990.

# References

## Interaction and Feedback

- [49] C. Buckley and G. Salton. *Optimization of relevance feedback weights*. In Proc. 18th Ann. Intl. ACM SIGIR Conf. on Research and Development in Information Retrieval, pages 351-357, 1995.
- [50] D. Harper and C. J. van Rijsbergen. *An evaluation of feedback in document retrieval using co-occurrence data*. Journal of Documentation, 34(3):189-216, 1978.
- [51] D. J. Harper. *Relevance feedback in document retrieval systems*. PhD thesis, University of Cambridge, UK, February 1980. 4
- [52] T. Joachims, L. Granka, B. Pan, H. Hembrooke, and G. Gay. *Accurately interpreting clickthrough data as implicit feedback*. In Proc. 28th Ann. Intl. ACM SIGIR Conf. on Research and Development in Information Retrieval, pages 154-161, 2005.
- [53] X. Shen and C. Zhai. *Active feedback in ad hoc information retrieval*. In Proc. 28th Ann. Intl. ACM SIGIR Conf. on Research and Development in Information Retrieval, pages 59-66, 2005.
- [54] R. Nallapati, W. Croft, and J. Allan. *Relevant query feedback in statistical language modeling*. In Proceedings of CIKM 2003 conference, pages 560-563, 2003.



# References

## Multimedia Retrieval

- [55] P. Duygulu, K. Barnard, N. Freitas, and D. Forsyth. *Object recognition as machine translation: Learning a lexicon for a fixed image vocabulary*. In Proceedings of the Seventh European Conference on Computer Vision, pages 97-112, 2002.
- [56] J. Jeon, V. Lavrenko, and R. Manmatha. *Automatic image annotation and retrieval using cross-media relevance models*. In In the proceedings of the 26th International ACM SIGIR Conference on Research and Development in Information Retrieval, pages 119-126, Toronto, Canada, August 2003.
- [57] V. Lavrenko, R. Manmatha, and J. Jeon. *A model for learning the semantics of pictures*. In Proceedings of the Seventeenth Annual Conference on Neural Information Processing Systems (NIPS), Vancouver, Canada, December 2003.
- [58] K. Barnard, P. Duygulu, N. Freitas, D. Forsyth, D. Blei, and M. Jordan. *Matching words and pictures*. Journal of Machine Learning Research, 3:1107-1135, 2003.
- [59] C. Carson, M. Thomas, S. Belongie, J. Hellerstein, and J. Malik. *Blobworld: A system for region-based image indexing and retrieval*. In Proceedings of the Third International Conference on Visual Information Systems, pages 509-516, 1999.
- [60] D. Metzler and R. Manmatha. *An inference network approach to image retrieval*. In Proc. 3rd Intl. Conf. on Image and Video Retrieval, pages 42-50, 2004.
- [61] Y. Mori, H. Takahashi, and R. Oka. *Image-to-word transformation based on dividing and vector quantizing images with words*. In Proceedings of the First International Workshop on Multimedia Intelligent Storage and Retrieval Management MISRM'99, 1999.