

Lecture III : Lists and Comprehensions.

nats :: [Int]

nats = [1..]

[5..10] :: [Int]

in the
Prelude.

take :: Int → [a] → [a]

take 0 xs = []

take n [] = []

take n (x:xs) = x : take (n-1) xs

< take :: Int → [a] → [a],

[]

x:xs

take n ~~Wrong.~~ x : xs =

take n [x]

[x,y]

[(x:xs)]

~~(x₀, x₁, x₂ ...)~~

x₀ : x₁ : x₂ : xs

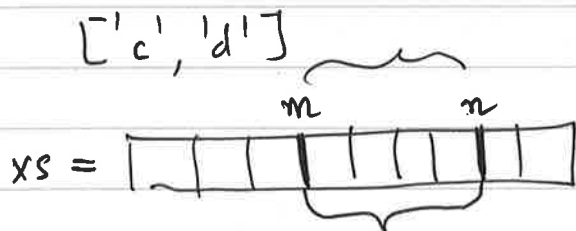
$\text{drop} :: \text{Int} \rightarrow [a] \rightarrow [a]$

$\text{drop } 0 \text{ } xs = xs$

$\text{drop } n \text{ } [] = []$

$\text{drop } n \text{ } (x:xs) = \text{drop } (n-1) \text{ } xs$

$\text{drop } 2 \text{ } ['a', 'b', 'c', 'd']$
 $=$



$\text{drop } m \text{ } (\text{take } n \text{ } xs)$

$=$
 $\text{take } (n-m) \text{ } (\text{drop } m \text{ } xs)$

$\text{alphabet} :: \text{Int} \rightarrow \text{Char}$

$\text{alphabet } 1 = 'a'$

$\text{alphabet } 2 = 'b'$

\vdots

map ~~24~~ ['a', 'b', 'c' ...]

map :: (a → b) → [a] → [b]

[1..26] = [1, 2, 3, 4 ... 26] :: [Int]

alphabet
↓
alphabet
↓
alphabet
↓

['a', 'b', 'c', ... 'z']

map alphabet [1..26]

between :: Int → Int → [Int]

~~between x y = x : between (x+1) y~~

~~between x (x+1) = []~~

between x y

| x > y = []

| otherwise = x : between (x+1) y

~~[x, x+1, ..., y]~~

$\text{Square} :: \text{Int} \rightarrow \text{Int}$

$\text{Square } x = x * x$

map square nats

list comprehension style:

$[\text{square } n \mid n \leftarrow [1..]]$
=

map square nats

$\text{even} :: \text{Int} \rightarrow \text{Bool}$

$\text{map square (filter even nats)}$
=

$[\text{square } n \mid n \leftarrow [1..], \text{even } n]$