

# Incremental Correctness

Oliver Pauffley

October 3, 2021

## Contents

```
Increment(y):  
  if y = 0 then return(1) else  
  if (y mod 2) = 1 then  
  return (2 * Increment(y/2))  
  else return (y + 1)
```

*Solution:*

1. Base case  $n=0$   
Clearly if  $n=0$  then `Increment(0)` returns 1.
2. Assume true for all  $n < y$  prove for  $n = y + 1$   
When  $n$  is even, ie.  $n=2k$  then.

```
Increment(2k)  
2k mod 2 = 0 > return 2k + 1
```

If  $n$  is odd such that  $n = 2m + 1$

$(2m + 1 \bmod 2) = 1$   
then

$$\begin{aligned}
2.\textit{increment}([2m+1]/2) &= 2.\textit{increment}([m+1/2]) \\
&= 2.\textit{increment}(m) \\
&= 2(2m+1) \\
&= 2m+2 = y+1
\end{aligned}
\tag{1}$$