



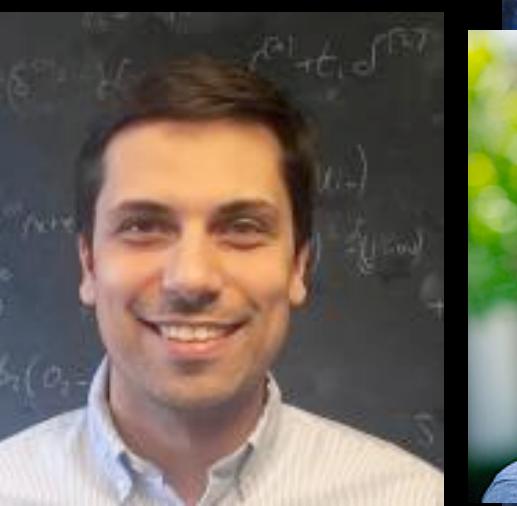
# The Galactic Cosmological Collider

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University of Edinburgh, June 2024

arXiv

[2404.01894](#)  
[2204.01781](#)  
[2201.07238](#)



with **Giovanni Cabass & Misha Ivanov**,  
as well as Marko Simonovic, Kaz Akitsu,  
Stephen Chen & Matias Zaldarriaga



IllustrisTNG

# What do we Want to Know About Inflation?

## Simplest (phenomenological) model

- A **single field** evolving along an almost **flat potential** with **quantum fluctuations**

$$\text{Simplest Lagrangian} \sim \frac{1}{2}(\partial\phi)^2 - V(\phi)$$

**But:**

- What is the **energy scale** of inflation? [Hubble]

$$H \sim 10^{14} \text{GeV} ?$$

$$V(\phi) = ???$$

- What sets the **potential**?

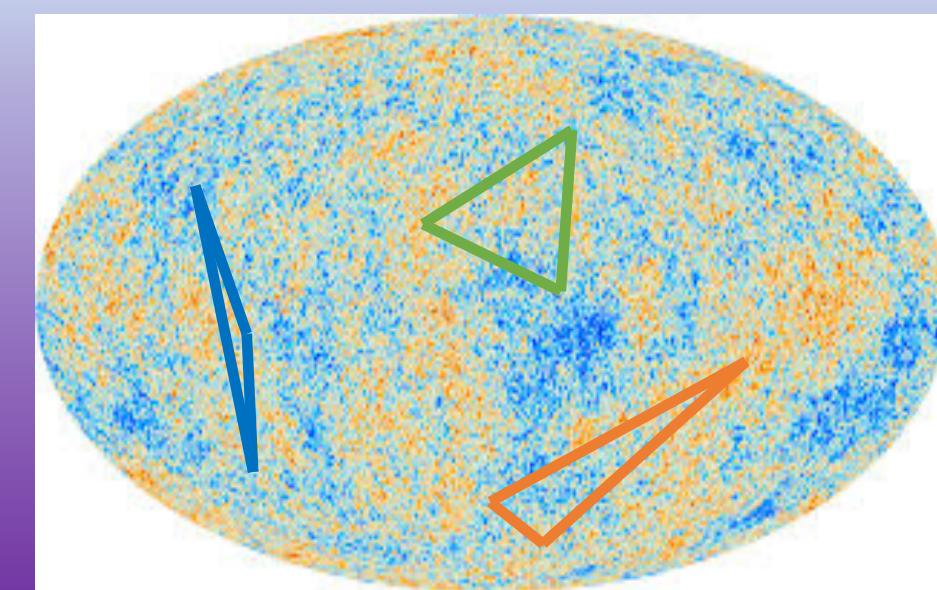
$$\phi \rightarrow \phi, \chi, \psi_\mu, \dots$$

- Were there **other fields** during inflation?

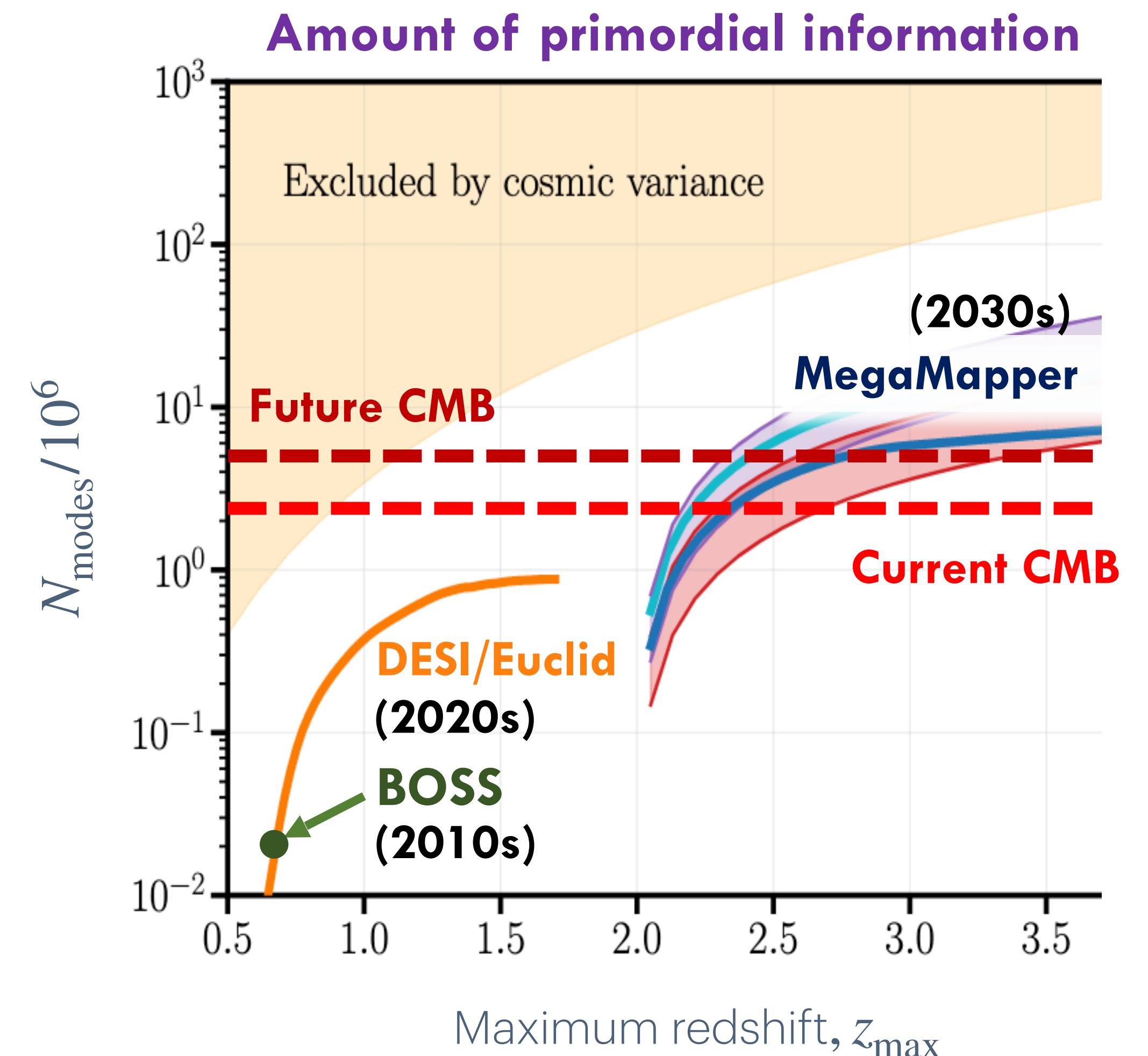
$$\text{Lagrangian} \supset \dot{\phi}^3 + \dots$$

- Did the fields **interact**?

# The Future of Non-Gaussianity



- Future **CMB** experiments will improve by  $\approx 2 \times$ 
    - This is a **two-dimensional** field
    - We're running out of modes to look at!
    - Small-scales are **hard**
  - What about **galaxy surveys**?
    - This is a **three-dimensional** field
    - New surveys will map  $\sim 100 \times$  more galaxies than Stage-III
- [2020s: DESI, Euclid, SPHEREx, LSST, Roman, ...]



# How to Model Inflation

?

*Inflationary Theory*

Encodes **inflation model**

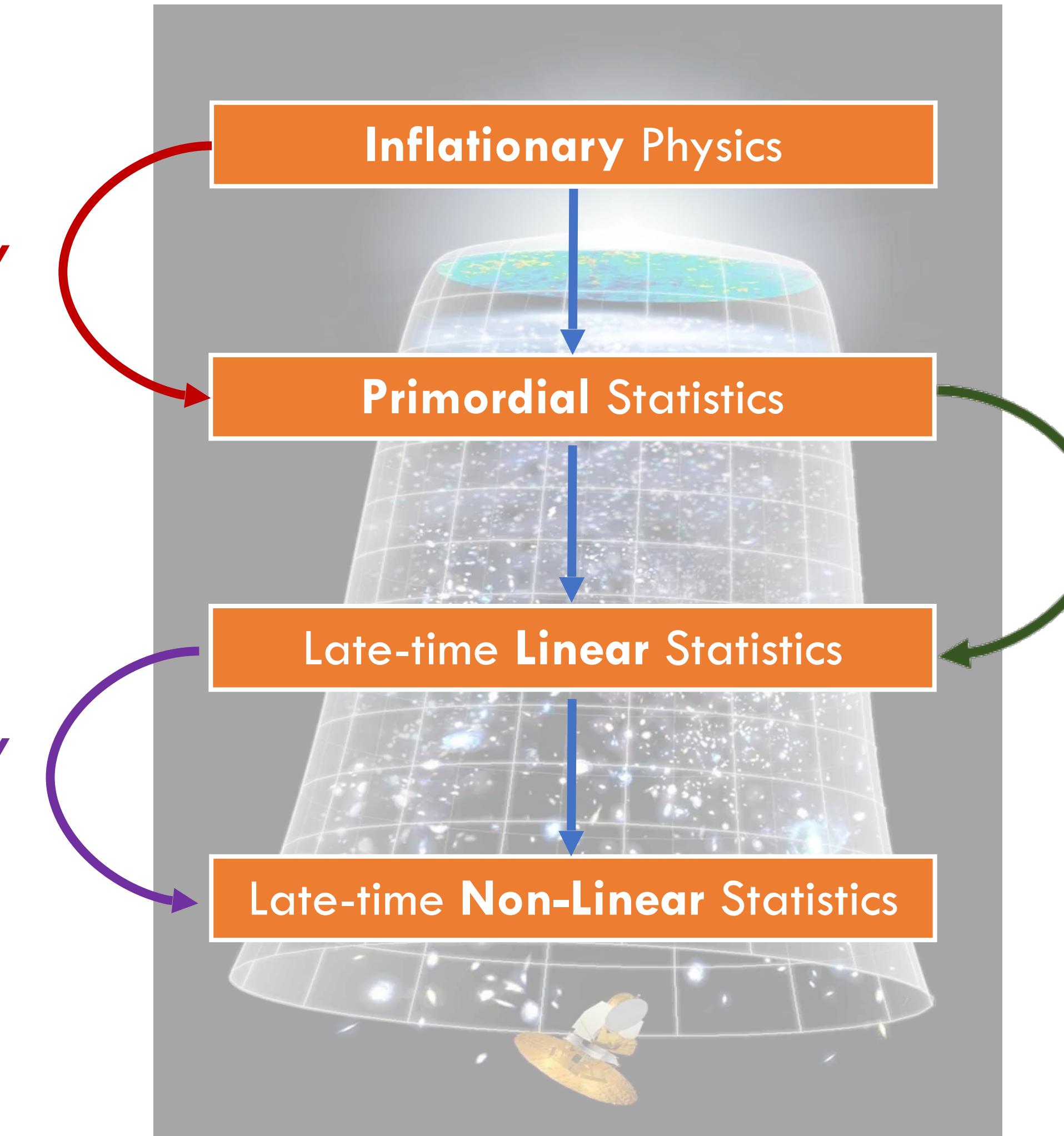
$$P_\zeta, B_\zeta, \dots$$

?

*Perturbation Theory*

Encodes **gravity, hydrodynamics, galaxy formation**

biases, counterterms, etc.



*Linear Theory*

Encodes **expansion history**

$$H_0, \Omega_m, \Omega_b, \Lambda$$



# Step 1: Modeling Inflation

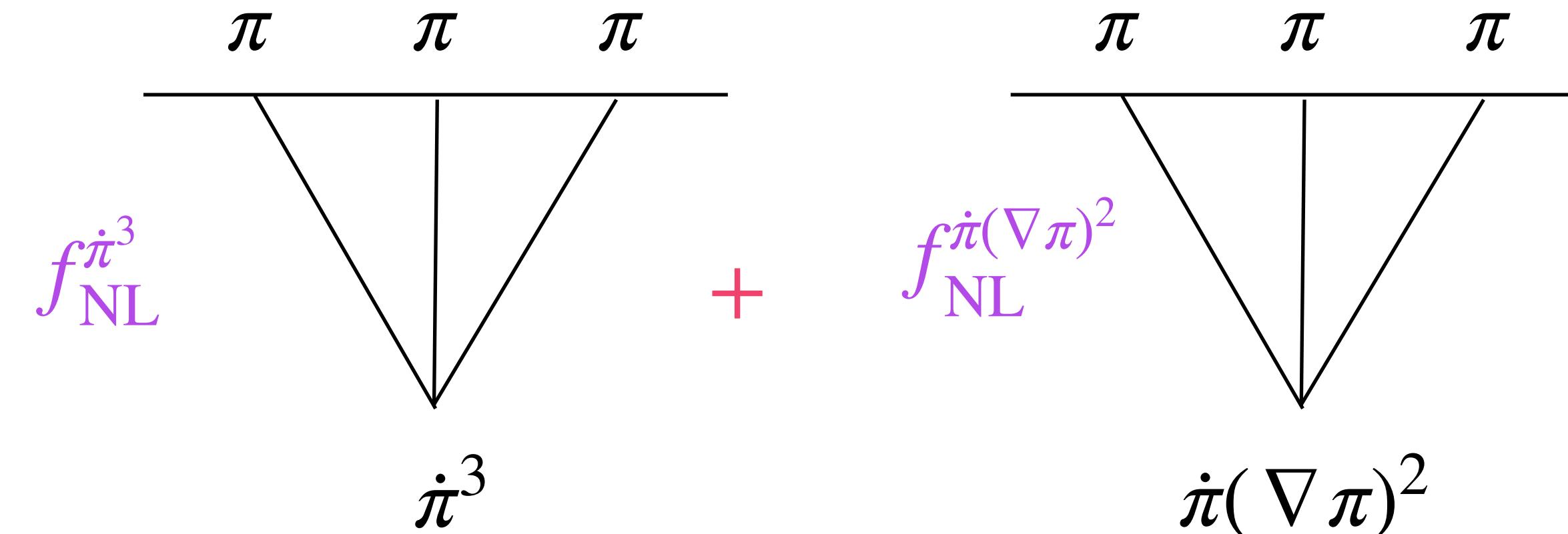
- Write down the most-generic **action** for **single-field inflation** (assuming shift-symmetries)

$$S_{\text{EFT}} = \int d^4x \sqrt{-g} \left[ -\frac{M_P^2 \dot{H}}{c_s^2} \left( \dot{\pi}^2 - c_s^2 \frac{(\nabla \pi)^2}{a^2} \right) + \frac{M_P^2 \dot{H}}{c_s^2} (1 - c_s^2) \left( \frac{\dot{\pi}(\nabla \pi)^2}{a^2} - \left( 1 + \frac{2}{3} \frac{\tilde{c}_3}{c_s^2} \right) \dot{\pi}^3 \right) \right]$$

for **Goldstone mode**  $\pi$  ( $\sim$  inflaton) and **sound-speed**  $c_s$  at  $\mathcal{O}(3)$ .

- This sources two **bispectra**:

Equivalently:  $f_{\text{NL}}^{\text{eq}}$  &  $f_{\text{NL}}^{\text{forth}}$



# Step 1: Modeling Inflation

- We could also consider **multi-field inflation** (still assuming shift-symmetries)

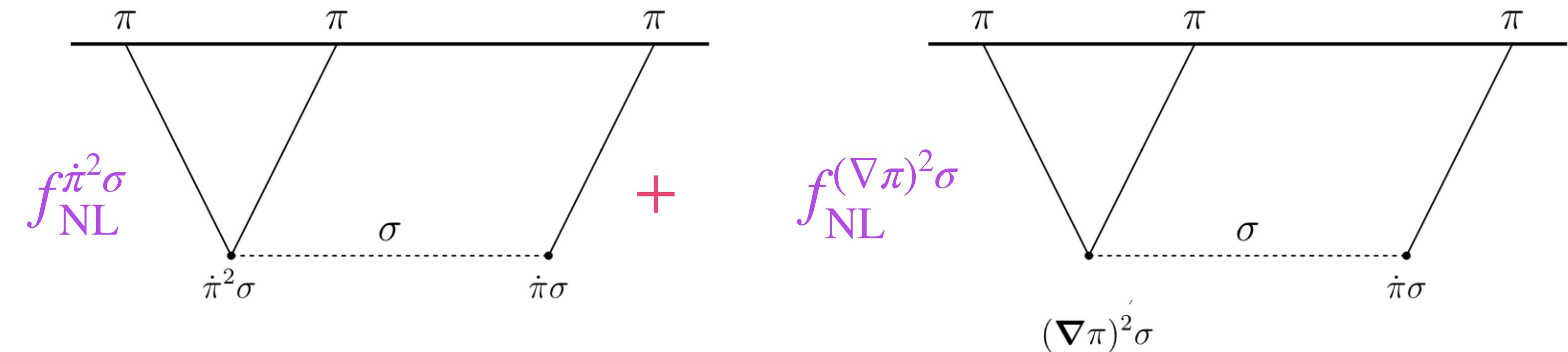
$$S_{\text{EFT}} \supset \int d^4x \sqrt{-g} \left[ A\dot{\pi} + B\dot{\pi}^2 + C \frac{(\nabla\pi)^2}{a^2} \right] \sigma$$

for **scalar-field**  $\sigma$  of **mass**  $m_\sigma$  and **sound-speed**  $c_\sigma$  with coupling constants  $A, B, C$  (at  $\mathcal{O}(3)$ ).

- This sources two more **bispectra**:

If  $m_\sigma \rightarrow 0$ , this is **local**  $f_{\text{NL}}$ !

If  $m_\sigma > 3/2H$ , we get **oscillations**!



# Step 2: Modeling Dark Matter

How does **primordial non-Gaussianity** change the theory model?

1. Induces a **late-time bispectrum**:

$$B_{mmm}(k_1, k_2, k_3) = f_{\text{NL}} T_\zeta(k_1) T_\zeta(k_2) T_\zeta(k_3) B_\zeta(k_1, k_2, k_3)$$

2. Adds new **loop corrections**:

$$P_{mm}(k) \sim \int_{\mathbf{p}_i} \text{kernels}(\mathbf{p}_i, \mathbf{k}) \times \langle \delta_{\text{lin}}(\mathbf{p}_1) \cdots \delta_{\text{lin}}(\mathbf{p}_n) \rangle$$

e.g.,  $P_{mm,12}(k) = 2f_{\text{NL}} \int \frac{d\mathbf{p}}{(2\pi)^3} F_2(\mathbf{p}, \mathbf{k} - \mathbf{p}) B_{111}(\mathbf{p}, \mathbf{k} - \mathbf{p})$



This contains **both**  $P_\zeta$  **and**  $B_\zeta$  terms!

# Step 3: Modeling Galaxies

For galaxies, we have **more effects**:

1. Induces a **late-time bispectrum**:

$$B_{ggg}(k_1, k_2, k_3) = f_{\text{NL}} T_\zeta(k_1) T_\zeta(k_2) T_\zeta(k_3) b_1^3 B_\zeta(k_1, k_2, k_3)$$

2. Adds new **loop corrections**:

$$P_{gg}(k) \sim \int_{\mathbf{p}_i} \text{galaxy kernels}(\mathbf{p}_i, \mathbf{k}) \times \langle \delta_{\text{lin}}(\mathbf{p}_1) \cdots \delta_{\text{lin}}(\mathbf{p}_n) \rangle$$

e.g.,  $P_{gg,12}(k) = 2f_{\text{NL}} b_1 \int \frac{d\mathbf{p}}{(2\pi)^3} K_2(\mathbf{p}, \mathbf{k} - \mathbf{p}) B_{111}(\mathbf{p}, \mathbf{k} - \mathbf{p})$

3. Adds new **bias operators**

$$\delta_g \supset b_\phi \phi + b_{\phi\delta} \phi \delta + \dots \quad (\text{assuming light fields})$$

⇒ scale-dependent bias!

# Step 3: Modeling Galaxies

We also have to be careful of **renormalization!**

- Look at the **UV dependence** of the loop integrals:

$$P_{gg,12}^{\text{UV}}(k) \sim f_{\text{NL}} b_1 \int_{p \gg k} \frac{d\mathbf{p}}{(2\pi)^3} K_2(\mathbf{p}, \mathbf{k} - \mathbf{p}) B_{111}(\mathbf{p}, \mathbf{k} - \mathbf{p})$$

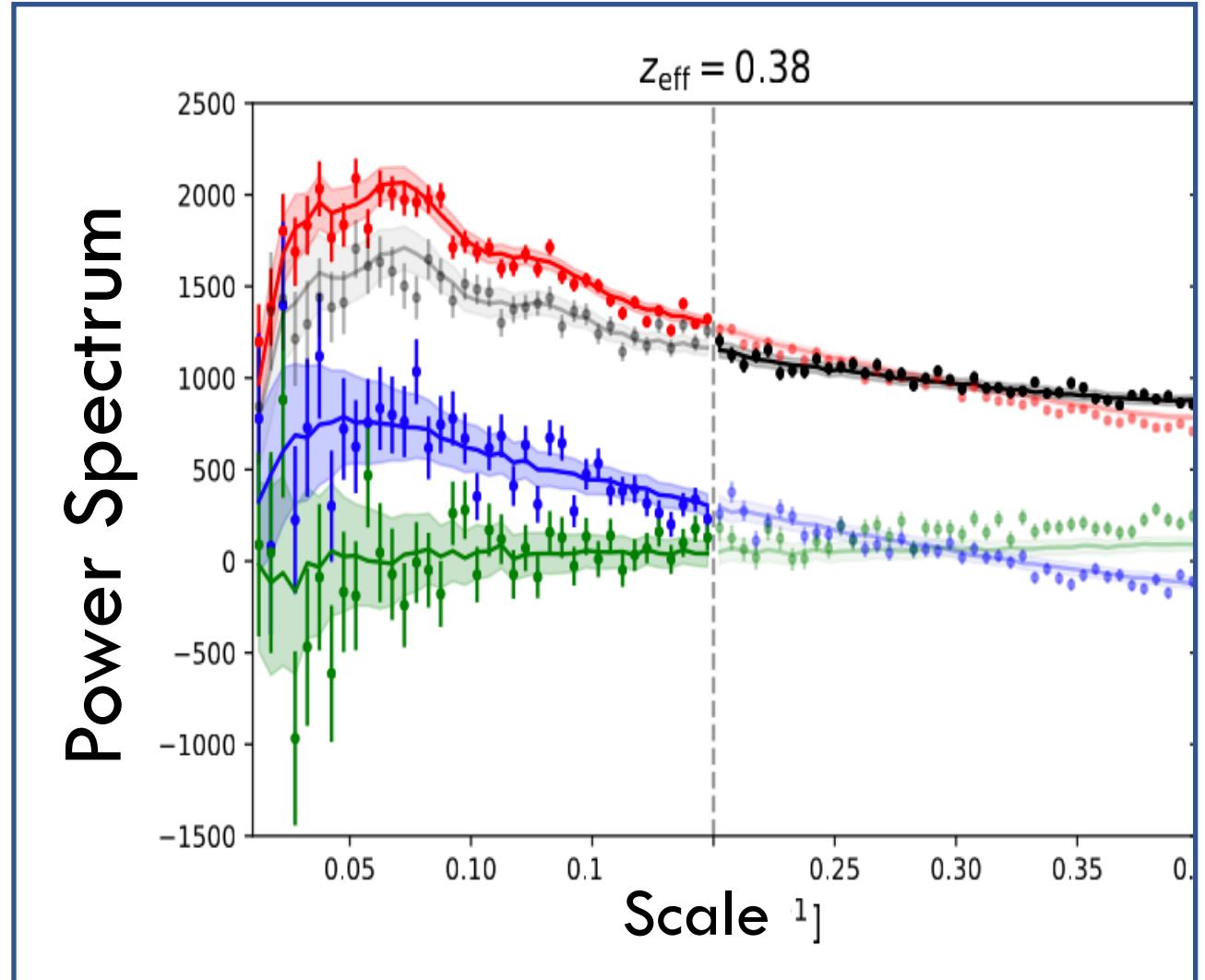
- For **light fields** ( $m_\sigma \ll H$ ):  $P_{gg,12}^{\text{ct}}(k) \sim f_{\text{NL}} k^{-2} P_{\text{lin}}(k)$
- For **massive fields** ( $m_\sigma > 3/2H$ ):  $P_{gg,12}^{\text{ct}}(k) \sim f_{\text{NL}} k^{-1/2} \cos(\mu \log k) P_{\text{lin}}(k)$

This is exactly degenerate with **scale-dependent bias**! (as expected...)

⇒ massive particles lead to **weird** scale-dependent bias!

# Constraining Inflation with BOSS Galaxies

## Statistics



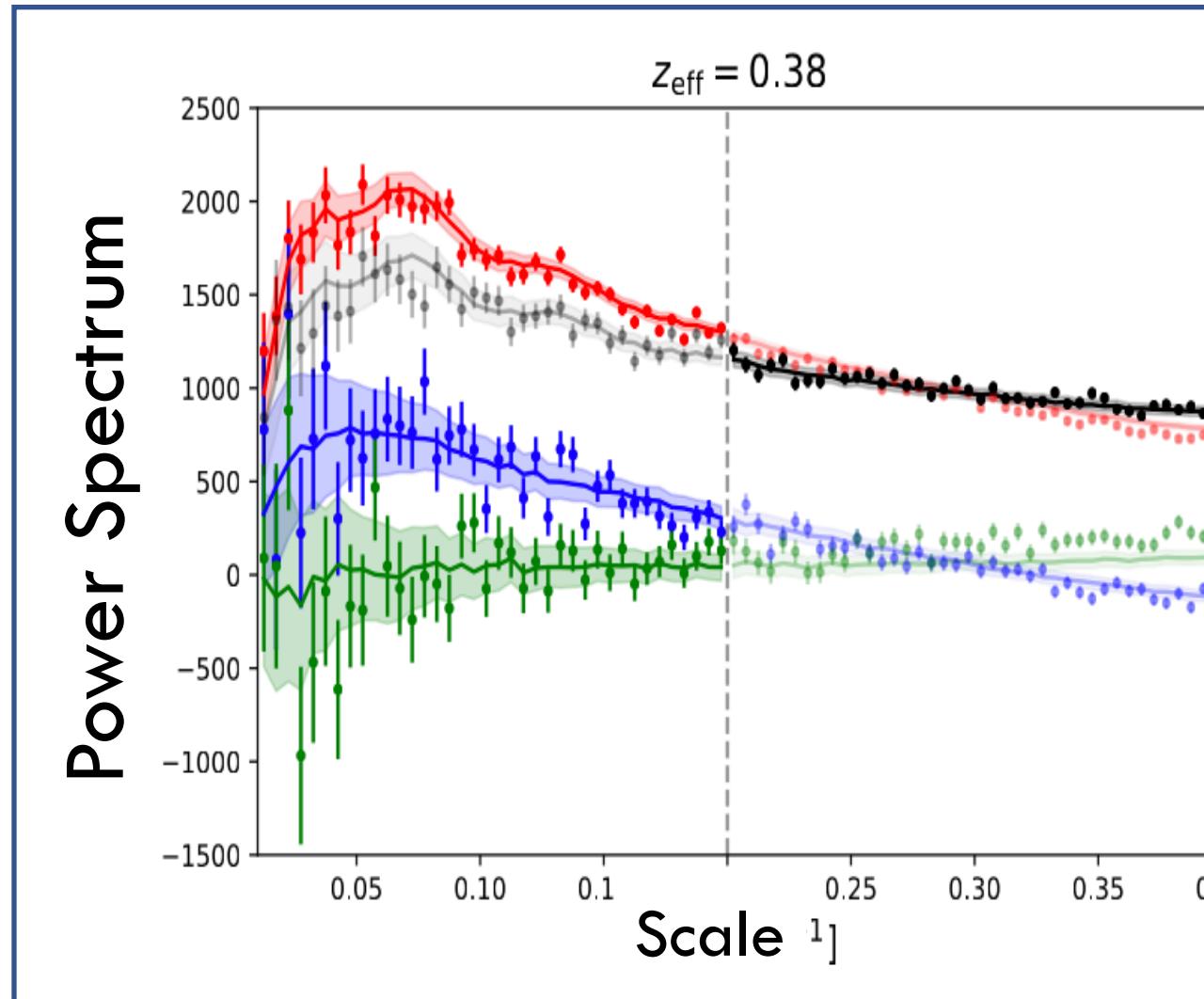
Using (quasi-)minimum-variance  
estimators deconvolving geometry

$$P_\ell(k) + \text{BAO} + P(k_\perp) \\ + B_\ell(k_1, k_2, k_3)$$



# Constraining Inflation with BOSS Galaxies

## Statistics



Using (quasi-)minimum-variance  
estimators deconvolving geometry

Fast loop integrals and  
flexible likelihoods

(  $\sim$  seconds ! )

Gaussian likelihood

$$-2\log L = (\hat{P} - P_{\text{theory}}) C^{-1} (\hat{P} - P_{\text{theory}})$$

$$\begin{aligned} & P_\ell(k) + \text{BAO} + P(k_\perp) \\ & + B_\ell(k_1, k_2, k_3) \end{aligned}$$



## Theory Model

$$\begin{aligned} Z_1(\mathbf{q}_1) &= K_1 + f\mu_1^2, \\ Z_2(\mathbf{q}_1, \mathbf{q}_2) &= K_2(\mathbf{q}_1, \mathbf{q}_2) + f\mu_{12}^2 G_2(\mathbf{q}_1, \mathbf{q}_2) + \frac{f\mu_{12} q_{12}}{2} K_1 \left[ \frac{\mu_1}{q_1} + \frac{\mu_2}{q_2} \right] + \frac{(f\mu_{12} q_{12})^2}{2} \frac{\mu_1 \mu_2}{q_1 q_2}, \\ Z_3(\mathbf{q}_1, \mathbf{q}_2, \mathbf{q}_3) &= K_3(\mathbf{q}_1, \mathbf{q}_2, \mathbf{q}_3) + f\mu_{123}^2 G_3(\mathbf{q}_1, \mathbf{q}_2, \mathbf{q}_3) \\ &+ (f\mu_{123} q_{123}) \left[ \frac{\mu_{12}}{q_{12}} K_1 G_2(\mathbf{q}_1, \mathbf{q}_2) + \frac{\mu_3}{q_3} K_2(\mathbf{q}_1, \mathbf{q}_2) \right] \\ &+ \frac{(f\mu_{123} q_{123})^2}{2} \left[ 2 \frac{\mu_{12} \mu_3}{q_{12} q_3} G_2(\mathbf{q}_1, \mathbf{q}_2) + \frac{\mu_1 \mu_2}{q_1 q_2} K_1 \right] + \frac{(f\mu_{123} q_{123})^3}{6} \frac{\mu_1 \mu_2 \mu_3}{q_1 q_2 q_3}, \\ Z_4(\mathbf{q}_1, \mathbf{q}_2, \mathbf{q}_3, \mathbf{q}_4) &= K_4(\mathbf{q}_1, \mathbf{q}_2, \mathbf{q}_3, \mathbf{q}_4) + f\mu_{1234}^2 G_4(\mathbf{q}_1, \mathbf{q}_2, \mathbf{q}_3, \mathbf{q}_4) \\ &+ (f\mu_{1234} q_{1234}) \left[ \frac{\mu_{123}}{q_{123}} K_1 G_3(\mathbf{q}_1, \mathbf{q}_2, \mathbf{q}_3) + \frac{\mu_4}{q_4} K_3(\mathbf{q}_1, \mathbf{q}_2, \mathbf{q}_3) \right. \\ &\quad \left. + \frac{\mu_{12}}{q_{12}} G_2(\mathbf{q}_1, \mathbf{q}_2) K_2(\mathbf{q}_3, \mathbf{q}_4) \right] \\ &+ \frac{(f\mu_{1234} q_{1234})^2}{2} \left[ 2 \frac{\mu_{123} \mu_4}{q_{123} q_4} G_3(\mathbf{q}_1, \mathbf{q}_2, \mathbf{q}_3) + \frac{\mu_{12} \mu_{34}}{q_{12} q_{34}} G_2(\mathbf{q}_1, \mathbf{q}_2) G_2(\mathbf{q}_3, \mathbf{q}_4) \right. \\ &\quad \left. + 2 \frac{\mu_{12} \mu_3}{q_{12} q_3} K_1 G_2(\mathbf{q}_1, \mathbf{q}_2) + \frac{\mu_1 \mu_2}{q_1 q_2} K_2(\mathbf{q}_3, \mathbf{q}_4) \right] \\ &+ \frac{(f\mu_{1234} q_{1234})^3}{6} \left[ 3 \frac{\mu_{12} \mu_3 \mu_4}{q_{12} q_3 q_4} G_2(\mathbf{q}_1, \mathbf{q}_2) + \frac{\mu_1 \mu_2 \mu_3}{q_1 q_2 q_3} K_1 \right] \\ &+ \frac{(f\mu_{1234} q_{1234})^4}{24} \frac{\mu_1 \mu_2 \mu_3 \mu_4}{q_1 q_2 q_3 q_4}, \end{aligned} \tag{A.3}$$

MCMC

$f_{\text{NL}}$  constraints (and beyond)

GitHub:  
**CLASS-PT**

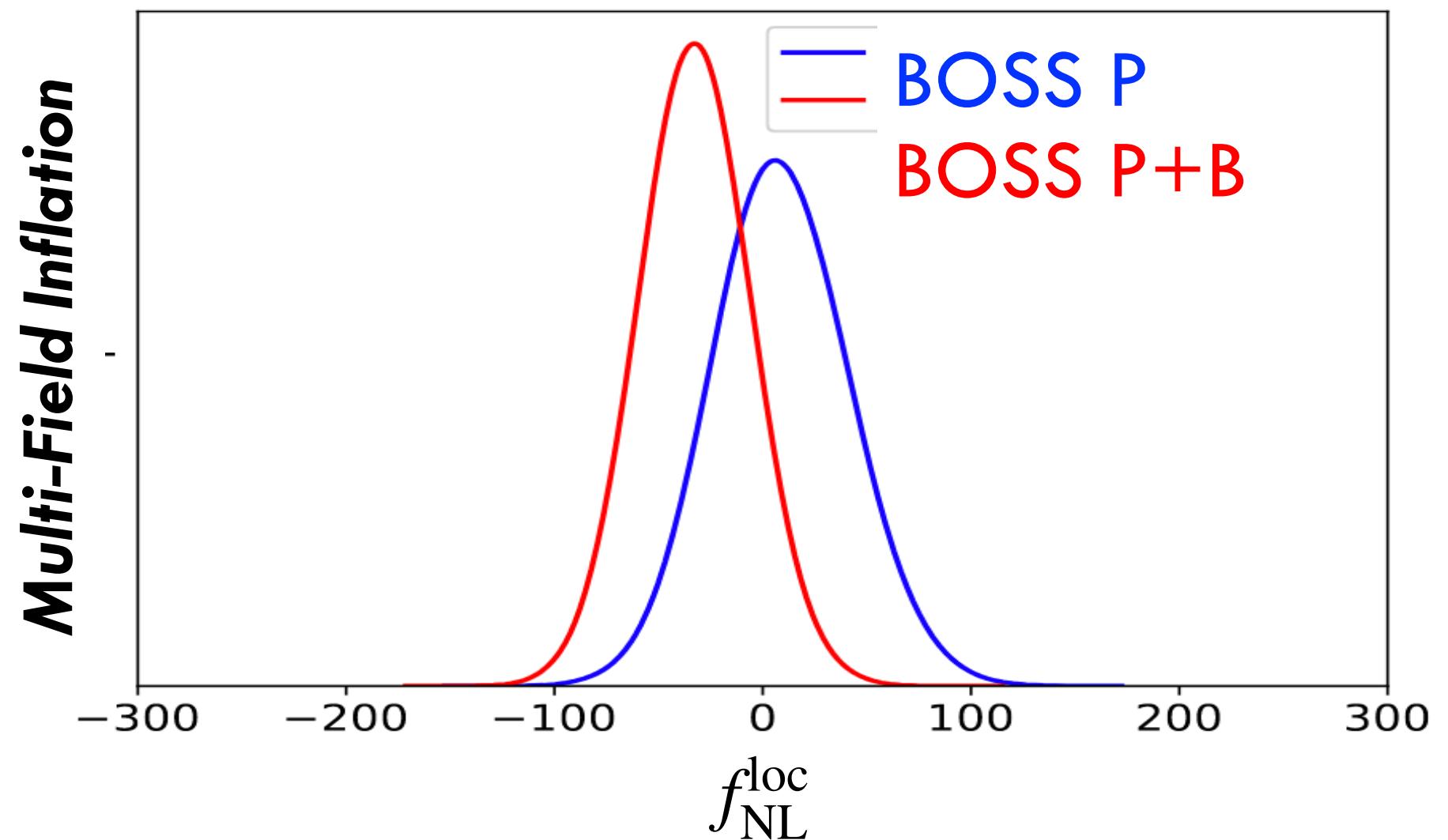
&

**Full-Shape-Likelihoods**

# Some Recent(ish) Results

## 1. Local non-Gaussianity: $f_{\text{NL}}^{\text{loc}}$

- Probes **light particles** ( $m_\sigma \ll H$ ) in **multi-field inflation**
- **Full  $P_g + B_g$  modeling beats power spectrum scale-dependent bias searches by 20%**



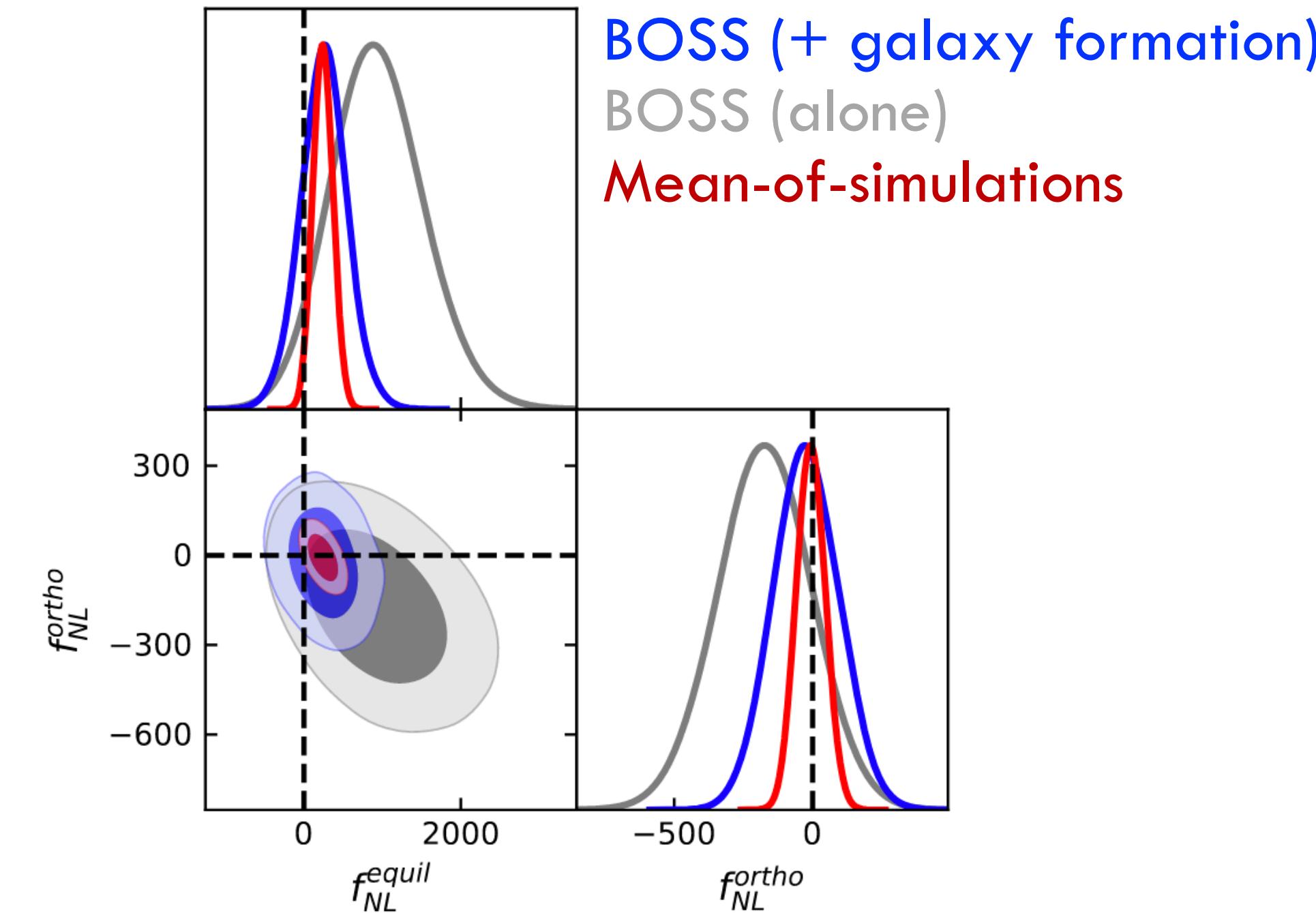
$$f_{\text{NL}}^{\text{loc}} = -33 \pm 28 \quad (9 \pm 34 \text{ w/o } B_g)$$

(CMB:  $\pm 5$ , Target:  $\pm 1$ )

# Some Recent(ish) Results

1. **Local non-Gaussianity:**  $f_{\text{NL}}^{\text{loc}}$
2. **Non-local non-Gaussianity:**  $f_{\text{NL}}^{\text{eq}}, f_{\text{NL}}^{\text{orth}}$

- Probes inflation **interactions** in the **single-field EFT** of inflation:  $10^5 f_{\text{NL}} \sim (H/\Lambda)^2$
- **First** non-CMB analysis
- **Hard:**
  - We need to robustly separate **inflation** from **bias** ( $b_{\mathcal{G}_2}, b_2$ ) [EFTofLSS to the rescue!]
  - **Window functions** are important [use window-deconvolved estimators!]



$$f_{\text{NL}}^{\text{eq}} = 260 \pm 300, f_{\text{NL}}^{\text{orth}} = -23 \pm 120$$

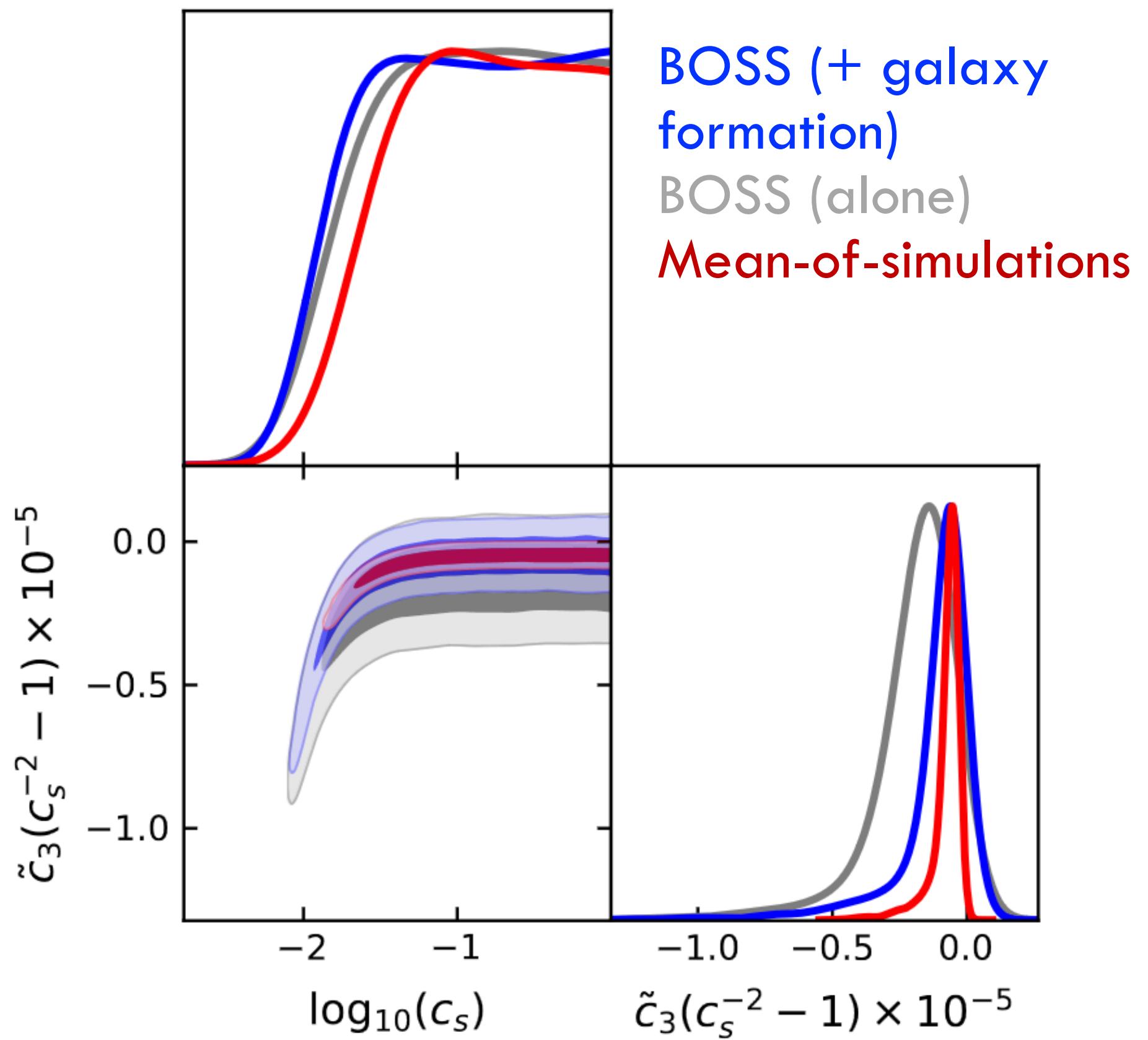
without priors:  $f_{\text{NL}}^{\text{eq}} = 940 \pm 600, f_{\text{NL}}^{\text{orth}} = -170 \pm 170$

(CMB:  $\pm 50, \pm 25$ , Target:  $\pm 1$ )

# Some Recent(ish) Results

1. **Local non-Gaussianity:**  $f_{\text{NL}}^{\text{loc}}$
2. **Non-local non-Gaussianity:**  $f_{\text{NL}}^{\text{eq}}, f_{\text{NL}}^{\text{forth}}$

- We can map these onto the EFT of inflation parameters, directly probing **microphysics!**
- We constrain the inflaton **sound-speed:**  $c_s^2 \geq 0.013$  (95% CL)
- This is greatly improved by priors on **bias parameters**

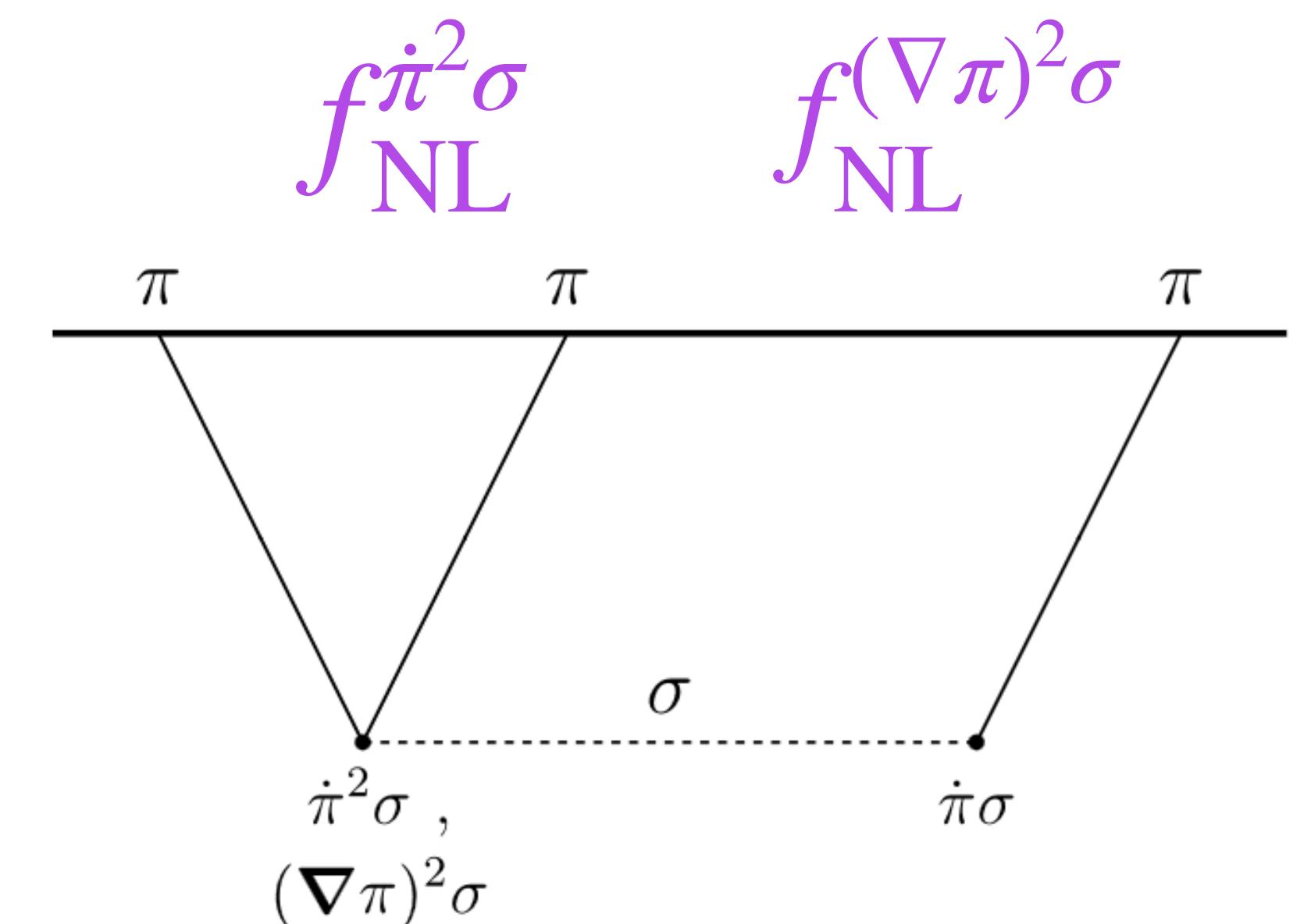


# Some Recent(ish) Results

1. **Local non-Gaussianity:**  $f_{\text{NL}}^{\text{loc}}$
2. **Non-local non-Gaussianity:**  $f_{\text{NL}}^{\text{eq}}, f_{\text{NL}}^{\text{forth}}$
3. **Massive-Particle non-Gaussianity:**  $f_{\text{NL}}(m_\sigma, c_\sigma)$

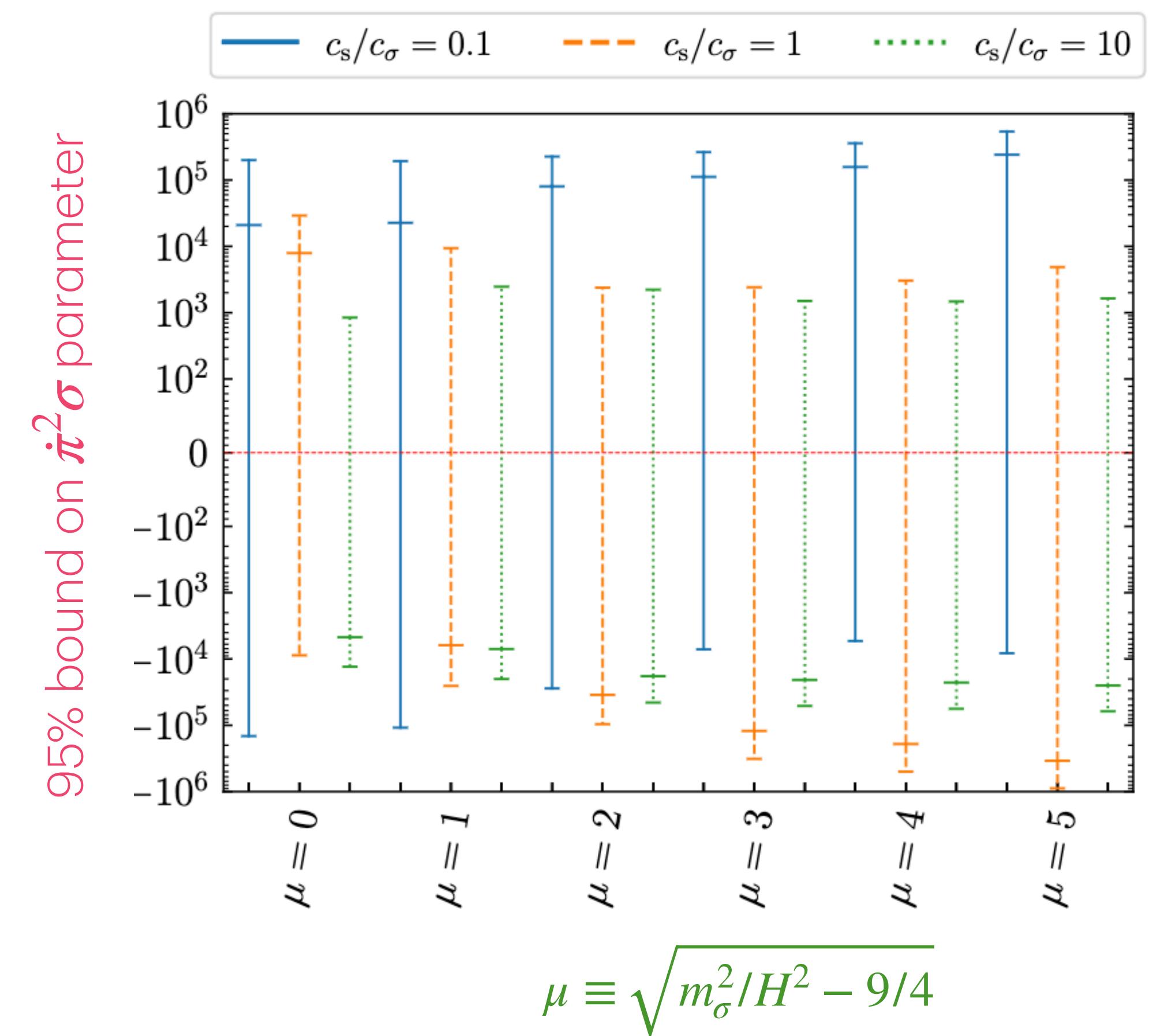
- We can probe multi-field inflation with **massive particles** ( $m_\sigma > 3/2H$ )
- **First** analysis with either CMB or LSS
- This has more interesting phenomenology including **oscillatory features** and varying **speeds**

$$\mathcal{S}(k_1, k_2, k_3) \sim \left(\frac{k_1}{k_3}\right)^{\frac{1}{2}} \cos\left(\mu \ln \frac{c_\sigma k_1}{c_s k_3}\right) \text{ for } k_1 \ll \frac{c_s}{c_\sigma} k_3 \quad + \text{many integrals}$$



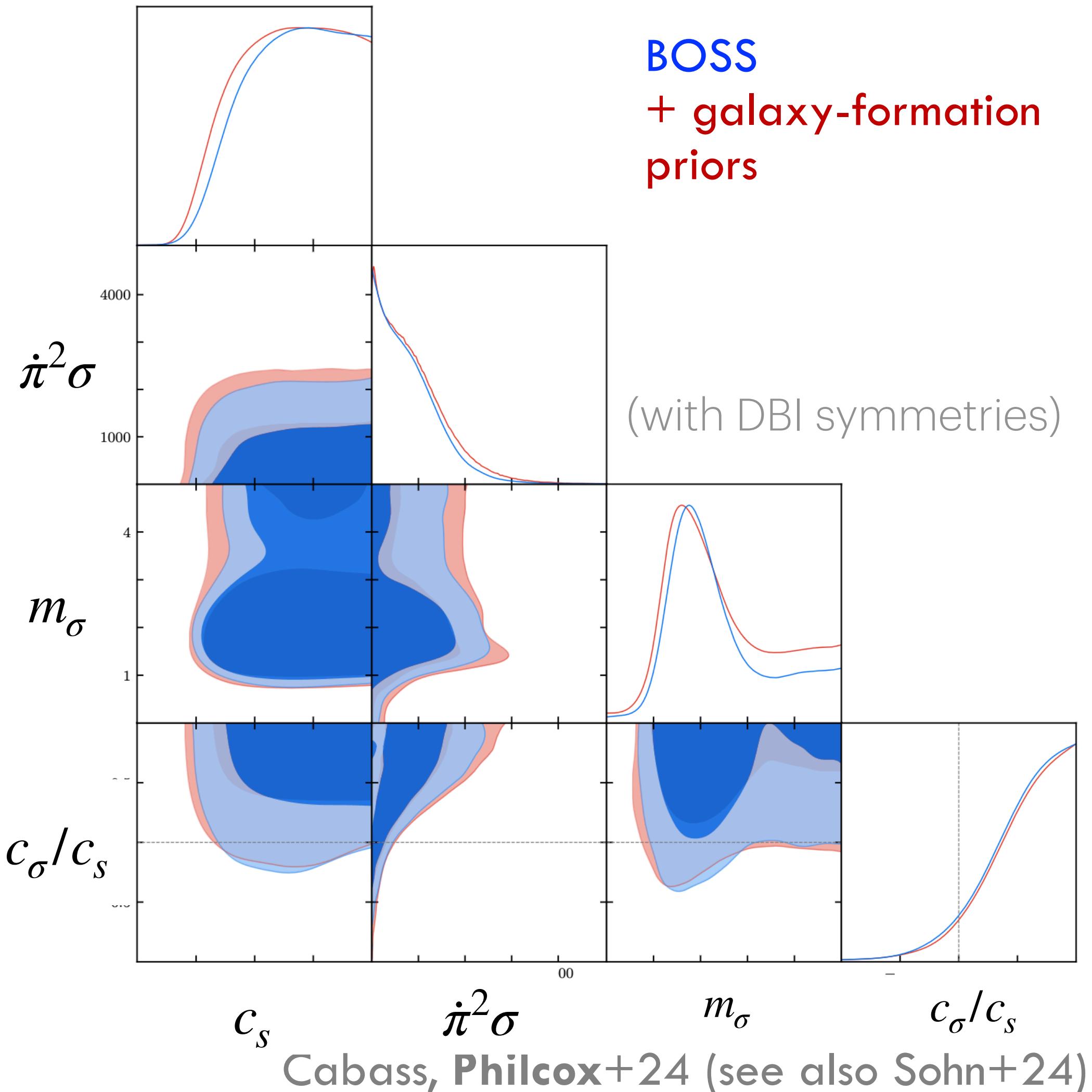
# Some Recent(ish) Results

1. **Local non-Gaussianity:**  $f_{\text{NL}}^{\text{loc}}$
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3. **Massive-Particle non-Gaussianity:**  $f_{\text{NL}}(m_\sigma, c_\sigma)$ 
  - Very massive particles look like **self-interactions**
    - Marginalize over  $f_{\text{NL}}^{\text{eq}}, f_{\text{NL}}^{\text{forth}}$  as well!
  - There are several ways to analyze the data:
    1. Separately analyze each mass and sound-speed



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  - There are several ways to analyze the data:
    1. **Separately** analyze each mass and sound-speed
    2. **Marginalize** over particle mass



# $f_{\text{NL}}$ isn't everything...

Many other things can happen in inflation,  
e.g.:

- **Massive-ish** particles ( $m_\sigma < 3/2H$ )  
*See upcoming paper with Sam Goldstein!*
- Particles with **spin**
- **4-point** interactions
- **Thermal** initial states and **dissipation**
- **Non-perturbative** physics

There's lots to discover in future data!

## Cosmological Collider

Low-energy remnants  
[curvature fluctuations]



High-energy physics  
[particle scattering]



Low-energy remnants  
[curvature fluctuations]

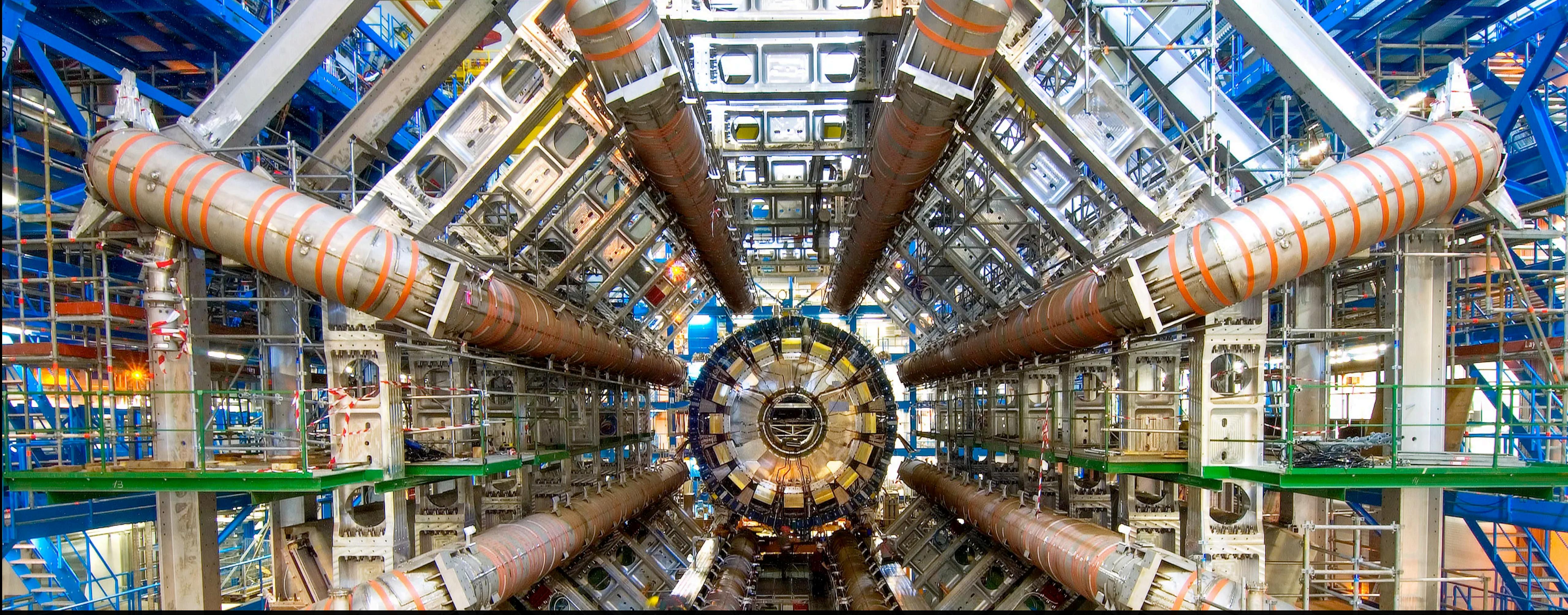


SciTech Daily

# Summary

- We can robustly probe **primordial non-Gaussianity** with LSS
- So far we have constrained:
  - Self-interactions
  - Light fields
  - Massive fields
- There's lots more to do!!





*The Cosmological Collider has been switched on!*

