Engineering stress: $\sigma = P/A_o$

Engineering strain: $e = (L - L_0)/L_0 = d/L_0$

Effectiveness = Cost + Quality + Flexibility + Rate

Machining (Material Removal)

Price -, Quality ++, Flexibility ++, Rate -

Milling

Turning

Squeezing (Forming)

Price +, Quality ~, Flexibility limited by die shape (dies need to be manufactured), Rate ++

Forging- heat and press into a shape

Stamping- heat and cut into a shape

Rolling- heat and press between rollers to make a sheet

Extruding- heat and press through small hole

Melting

Price -, Quality - (post finishing needed), Flexibility + (good and cheap for large parts. wooden patterns), Rate --

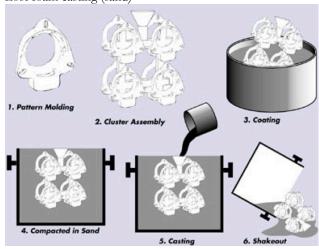
Casting

Disposable mold

Sand casting

- Make polystyrene blank, Surround with sand ,Pour metal into blank, Blank evaporates, sand holds shape
- 2. Solidification time: $t_s = C(V/A)^2$
- 3. Cost: Tooling and equipment cost _, labor cost ^, material utilization _, finishing cost ^
- 4. Quality: ~1mm tolerance, defects in shrinkage, material is inherently poor, rough surface generally.
- 5. Rate: 2-10 weeks. production rate depends on cool time
- 6. Flexibility: High shape complexity limited by pattern

Lost foam casting (sand)



Investment casting

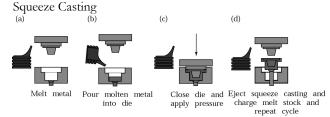
- -Like lost foam but with slurry+stucco to make shell on outside of assembly
- -Advantages: Intricate geometry, close dimensional tolerance, superior surface finish, high melting point alloys
- -Cost: Tooling costs ~, equipment costs _, labor costs ^, material costs _
- -Quality: ~.1mm tolerance, good to excellent surface detail if fine slurry
- -Rate: 5-16 weeks, production depends on cooling
- -Flexibility: Complex possible but at increased costs

Cool: centrifugal casting for metal pipes

Permanent Mold

Die Casting

- -Make mold, inject into mold and release, repeat
- -Advantages: high production rate, closer dimensional tol, superior surface finish, improved mechanical properties, 0.5 million shots die life
- -Solidification time: $t_s = C(V/A)$
- -Cost: Tooling and equipment costs ^, labor costs ~, material utilization ^
- -Quality: 0.02~0.6mm tolerance, good mechanical and microstructure properties due to high pressure, excellent surface detail
- -Rate: 12-20 weeks, production depends on cooling
- -Flexibility: Low- high die modification cost

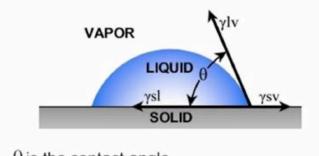


Plastics processing

Cost ~, Quality ++, Flexibility -- (Dies need made), Rate ++ Injection Molding

- Thermosets
- Hold pressure = 150% injection pressure
- Clamping force = projected area * injection pressure
- Gate location: Central for balancing travel, thickest part for balancing cooling rate, hidden for finish, consider weld-line, molecular orientation, size/location to control jetting
- Thermoforming
- -Thermoplastics

Surface Tension



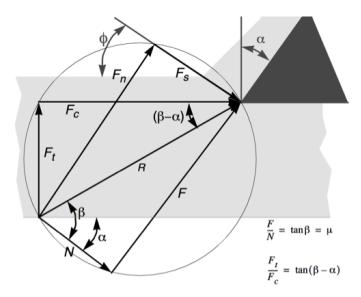
 θ is the contact angle

 γ^{sl} is the solid/liquid interfacial free energy γ^{sv} is the solid surface free energy γ^{lv} is the liquid surface free energy

Young's equation

$$\gamma_{\rm SL} + \gamma_{\rm LG} \cos \theta_{\rm c} = \gamma_{\rm SG}$$

Cutting Forces



MRR * Specific Energy = Power required

Thrust force is $F_t = F_c \tan(\beta - \alpha)$

If $\beta = \alpha$, Thrust goes to zero!

If $\beta \leq \alpha$, thrust is reversed, keeps tool engaged in cut

 $F = F_c \sin(\alpha) + F_t cost(\alpha)$

 $N = F_c \cos(\alpha) - F_t \sin(\alpha)$

 $F_c = R\cos(\beta - \alpha)$

 $F_t = R\sin(\beta - \alpha)$

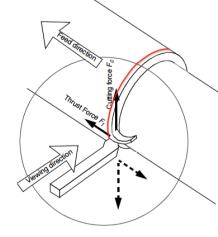
 $F_s = F_c \cos(\Phi) - F_t \sin(\Phi)$

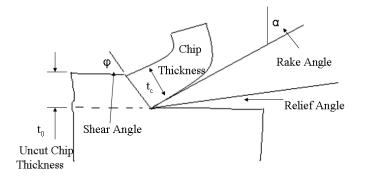
 $F_n = F_c \sin(\Phi) + F_t \cos(\Phi)$

$$\tau = \frac{F_c \cos(\varphi + \beta - \alpha) \sin(\varphi)}{t_0 w \cos(\beta - \alpha)}$$

$$\varphi = 45 + \frac{\alpha}{2} - \frac{\beta}{2}$$

$$\tau = \frac{F_c \cos(\phi + \beta - \alpha)\sin(\phi)}{t_0 w \cos(\beta - \alpha)}$$





Power

How does one design a motor for a cutting operation? We need power. The power in cutting is:

$$F_{c} \cdot V$$

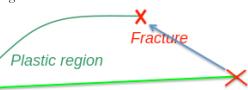
where F_c the horizontal cutting force and V is is the cutting velocity.

The material removal rate, or MRR is $V \cdot w \cdot t_0$. The specific energy of a material is

$$\frac{F_c \cdot V}{V \cdot w \cdot t_0} = \frac{F_c}{w \cdot t_0}$$

Tools

Tool life $V_cT^n=C$ ($V_c = cutting speed, T = tool life$) Hardness vs Toughness:



Equations

$$F = A_o K \ln(\frac{A_o}{A_f})$$

Extrusion force

where K is extr const

Wire drawing force

$$F = Y_{avg} A_f \ln(\frac{A_o}{A_f})$$
Where Y_{avg} is speed of drawing or temperature.

where Y_{avg} is speed of drawing or temperature or lubrication

$$|F_z| = (\pi \cdot R^2) \cdot Y \cdot \left[1 + \left(\frac{2}{3} \cdot \frac{\mu \cdot R}{h}\right)\right]$$

Forging force

Shearing force $F_c=0.7 \text{ UTS} * h * b$

Bending (Springback)

